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Merge Sort Algorithm

In this tutorial, you will learn about merge sort algorithm and its implementation in C, C++, Java and Python.

Merge Sort is one of the most popular [sorting algorithms](#)

(<https://www.programiz.com/dsa/sorting-algorithm>) that is based on the principle of [Divide and Conquer Algorithm](#) (</dsa/divide-and-conquer>).

Here, a problem is divided into multiple sub-problems. Each sub-problem is solved individually. Finally, sub-problems are combined to form the final solution.

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Merge Sort example

Divide and Conquer Strategy

Using the **Divide and Conquer** technique, we divide a problem into subproblems. When the solution to each subproblem is ready, we 'combine' the results from the subproblems to solve the main problem.

Suppose we had to sort an array A . A subproblem would be to sort a sub-section of this array starting at index p and ending at index r , denoted as $A[p..r]$.

Divide

If q is the half-way point between p and r , then we can split the subarray $A[p..r]$ into two arrays $A[p..q]$ and $A[q+1, r]$.

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... and $A[q+1, r]$ for array $A[p..r]$, we combine the results by creating a sorted array $A[p..r]$ from two sorted subarrays $A[p..q]$ and $A[q+1, r]$.

MergeSort Algorithm

The MergeSort function repeatedly divides the array into two halves until we reach a stage where we try to perform MergeSort on a subarray of size 1 i.e. $p == r$.

After that, the merge function comes into play and combines the sorted arrays into larger arrays until the whole array is merged.

```
MergeSort(A, p, r):  
    if p > r  
        return  
    q = (p+r)/2  
    mergeSort(A, p, q)  
    mergeSort(A, q+1, r)  
    merge(A, p, q, r)
```

To sort an entire array, we need to call $\text{MergeSort}(A, 0, \text{length}(A)-1)$.

As shown in the image below, the merge sort algorithm recursively divides the array into halves until we reach the base case of array with 1 element. After that, the merge function picks up the sorted sub-arrays and merges them to gradually sort the entire array.

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$A[0 \dots 1]^*$

$A[0 \dots 1]^*$

$A[0 \dots 1]^*$

Merge sort in action

The merge Step of Merge Sort

Every recursive algorithm is dependent on a base case and the ability to combine the results from base cases. Merge sort is no different. The most important part of the merge sort algorithm is, you guessed it, `merge` step.

The merge step is the solution to the simple problem of merging two sorted lists(arrays) to build one large sorted list(array).

The algorithm maintains three pointers, one for each of the two arrays and one for maintaining the current index of the final sorted array.

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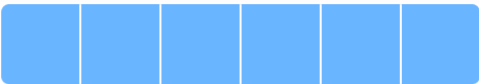
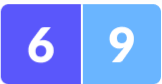


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Merge step

Writing the Code for Merge Algorithm

A noticeable difference between the merging step we described above and the one we use for merge sort is that we only perform the merge function on consecutive sub-arrays.

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1. Create copies of the subarrays `L = A[p..q]` and `M = A[q+1..r]`.

2. Create three pointers `i`, `j` and `k`

a. `i` maintains current index of `L`, starting at 1

b. `j` maintains current index of `M`, starting at 1

c. `k` maintains the current index of `A[p..q]`, starting at `p`.

3. Until we reach the end of either `L` or `M`, pick the larger among the elements from `L` and `M` and place them in the correct position at `A[p..q]`

4. When we run out of elements in either `L` or `M`, pick up the remaining elements and put in `A[p..q]`

In code, this would look like:

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```
for (int j = 0; j < n2; j++)
    M[j] = arr[q + 1 + j];

// Maintain current index of sub-arrays and main array
int i, j, k;
i = 0;
j = 0;
k = p;

// Until we reach either end of either L or M, pick larger among
// elements L and M and place them in the correct position at A[p..r]
while (i < n1 && j < n2) {
    if (L[i] <= M[j]) {
        arr[k] = L[i];
        i++;
    } else {
        arr[k] = M[j];
        j++;
    }
}
```

Merge() Function Explained Step-By-Step

A lot is happening in this function, so let's take an example to see how this would work.

As usual, a picture speaks a thousand words.



Merging two consecutive subarrays of array

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```
int n1 = q - p + 1 = 3 - 0 + 1 = 4;
int n2 = r - q = 5 - 3 = 2;

int L[4], M[2];

for (int i = 0; i < 4; i++)
    L[i] = arr[p + i];
// L[0,1,2,3] = A[0,1,2,3] = [1,5,10,12]

for (int j = 0; j < 2; j++)
    M[j] = arr[q + 1 + j];
// M[0,1] = A[4,5] = [6,9]
```



Create copies of subarrays for merging

Step 2: Maintain current index of sub-arrays and main array

```
int i, j, k;
i = 0;
j = 0;
k = p;
```


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Step 3: Until we reach the end of either L or M, pick larger among elements L and M and place them in the correct position at A[p..r]

```
while (i < n1 && j < n2) {
    if (L[i] <= M[j]) {
        arr[k] = L[i]; i++;
    }
    else {
        arr[k] = M[j];
        j++;
    }
    k++;
}
```

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Comparing individual elements of sorted subarrays until we reach end of one

Step 4: When we run out of elements in either L or M, pick up the remaining elements and put in A[p..r]

```
// We exited the earlier loop because j < n2 doesn't hold
while (i < n1)
{
    arr[k] = L[i];
    i++;
    k++;
}
```

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Copy the remaining elements from the first array to main subarray

```
// We exited the earlier loop because i < n1 doesn't hold
while (j < n2)
{
    arr[k] = M[j];
    j++;
    k++;
}
}
```

Copy remaining elements of second array to main subarray

This step would have been needed if the size of M was greater than L.

At the end of the merge function, the subarray `A[p..r]` is sorted.

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```
# r is the point where the array is divided into two subarrays
r = len(array)//2
L = array[:r]
M = array[r:]

# Sort the two halves
mergeSort(L)
mergeSort(M)

i = j = k = 0

# Until we reach either end of either L or M, pick larger among
# elements L and M and place them in the correct position at A[p..r]
while i < len(L) and j < len(M):
    if L[i] < M[j]:
        array[k] = L[i]
        i += 1
    else:
        array[k] = M[j]
        j += 1
    k += 1
```

Merge Sort Complexity

Time Complexity	
Best	$O(n \cdot \log n)$
Worst	$O(n \cdot \log n)$
Average	$O(n \cdot \log n)$
Space Complexity	
	$O(n)$

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Average Case Complexity: $O(n \log n)$

Space Complexity

The space complexity of merge sort is $O(n)$.

Merge Sort Applications

- Inversion count problem
- External sorting
- E-commerce applications

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