

Job Fair 2023 DSA Data Structures Algorithms Array Strings Linked List Stack Queue Tree

### Graph Coloring | Set 1 (Introduction and Applications)

Read Discuss Courses Practice Video

<u>Graph coloring</u> problem is to assign colors to certain elements of a graph subject to certain constraints.

**Vertex coloring** is the most common graph coloring problem. The problem is, given m colors, find a way of coloring the vertices of a graph such that no two adjacent vertices are colored using same color. The other graph coloring problems like *Edge Coloring* (No vertex is incident to two edges of same color) and *Face Coloring* (Geographical Map Coloring) can be transformed into vertex coloring.

### Algorithm for graph coloring

```
Algorithm GRAPH COLORING(G, COLOR, i)

Description: Solve the graph coloring problem using backtracking 
//Input: Graph G with n vertices, list of colors, initial vertex i 
COLOR(1...n] is the array of n different colors

//Output: Colored graph with minimum color 
if CHECK_VERTEX(i)==1 then 
if i == N then

print COLOR[1...n] 
else 
j <- 1 
while (S<=M) do 
COLOR(i+1) <- j 
j +j <- 1
```

We use cookies to ensure you have the best browsing experience on our website. By using our site, you acknowledge that you have read and understood our <u>Cookie Policy</u> & <u>Privacy Policy</u>

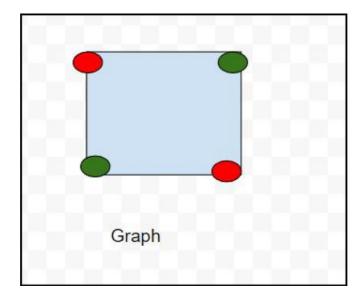
Got It!

end

end

```
Function CHECK_VERTEX(i)
for j <- 1to i -1 do
if Adjacent(i,j) then
if COLOR(i)==COLOR(j) then
return 0
end
end
end
return 1</pre>
```

**Chromatic Number:** The smallest number of colors needed to color a graph G is called its chromatic number. For example, the following can be colored minimum 2 colors.



Chromatic number of this graph is 2 because in this above diagram we can use to color red and green .

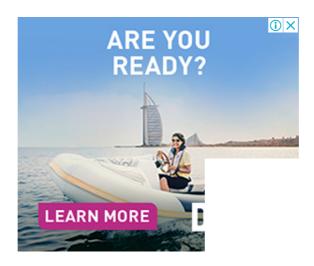
so chromatic number of this graph is 2 and is denoted x(G), means x(G)=2.

Chromatic number define as the least no of colors needed for coloring the graph .

and types of chromatic number are:

- 1) Cycle graph
- 2) planar graphs
- 3) Complete graphs
- 4) Bipartite Graphs:
- 5) Trees

The problem to find chromatic number of a given graph is NP Complete.



The chromatic number is denoted by X(G). Finding the chromatic number for the graph is NP-complete problem. Graph coloring problem is both, a decision problem as well as an optimization problem. A decision problem is stated as, "With given M colors and graph G, whether a such color scheme is possible or not?".

The optimization problem is stated as, "Given M colors and graph G, find the minimum number of colors required for graph coloring." Graph coloring problem is a very interesting problem of graph theory and it has many diverse applications.

### **Applications of Graph Coloring:**

The graph coloring problem has huge number of applications.

1) Making Schedule or Time Table: Suppose we want to make am exam schedule for a

do we schedule the exam so that no two exams with a common student are scheduled at same time? How many minimum time slots are needed to schedule all exams? This problem can be represented as a graph where every vertex is a subject and an edge between two vertices mean there is a common student. So this is a graph coloring problem where minimum number of time slots is equal to the chromatic number of the graph.

- 2) <u>Mobile Radio Frequency Assignment:</u> When frequencies are assigned to towers, frequencies assigned to all towers at the same location must be different. How to assign frequencies with this constraint? What is the minimum number of frequencies needed? This problem is also an instance of graph coloring problem where every tower represents a vertex and an edge between two towers represents that they are in range of each other.
- *3) Sudoku:* Sudoku is also a variation of Graph coloring problem where every cell represents a vertex. There is an edge between two vertices if they are in same row or same column or same block.
- 4) <u>Register Allocation</u>: In compiler optimization, register allocation is the process of assigning a large number of target program variables onto a small number of CPU registers. This problem is also a graph coloring problem.
- *5) Bipartite Graphs:* We can check if a graph is Bipartite or not by coloring the graph using two colors. If a given graph is 2-colorable, then it is Bipartite, otherwise not. See this for more details.
- *6) Map Coloring:* Geographical maps of countries or states where no two adjacent cities cannot be assigned same color. Four colors are sufficient to color any map (See <u>Four Color Theorem</u>)

**There can be many more applications:** For example the below reference video lecture has a case study at 1:18.

Akamai runs a network of thousands of servers and the servers are used to distribute content on Internet. They install a new software or update existing softwares pretty much every week. The update cannot be deployed on every server at the same time, because the server may have to be taken down for the install. Also, the update should not be done one at a time, because it will take a lot of time. There are sets of servers that cannot be taken down together, because they have certain critical functions. This is a typical scheduling application of graph coloring problem. It turned out that 8 colors were good enough to color the graph of 75000 nodes. So they could install updates in 8 passes.

### References:

### Lec 6 | MIT 6.042J Mathematics for Computer Science, Fall 2010 | Video Lecture

Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above

Last Updated : 22 Feb, 2023

### Similar Reads

Java Program to Find Independent Sets in a Graph using Graph Coloring 1. 2. Java Program to Find Independent Sets in a Graph By Graph Coloring Graph Coloring | Set 2 (Greedy Algorithm) 3. Mathematics | Planar Graphs and Graph Coloring 4. 5. Coloring a Cycle Graph Java Program to Use Color Interchange Method to Perform Vertex Coloring of Graph 6. Edge Coloring of a Graph 7. DSatur Algorithm for Graph Coloring 8. 3-coloring is NP Complete 9.

### Related Tutorials

10. m Coloring Problem

- 1. Learn Data Structures with Javascript | DSA Tutorial
- 2. Introduction to Max-Heap Data Structure and Algorithm Tutorials
- 3. Introduction to Set Data Structure and Algorithm Tutorials
- 4. Introduction to Map Data Structure and Algorithm Tutorials

Previous

### **Article Contributed By:**



### Vote for difficulty

Current difficulty: Medium

Easy

Normal

Medium

Hard

Expert

Improved By: ashrith2o, laxmishinde5t82, rathoadavinash

Article Tags: Graph Coloring, DSA, Graph

Practice Tags: Graph

Improve Article

Report Issue



A-143, 9th Floor, Sovereign Corporate Tower, Sector-136, Noida, Uttar Pradesh -201305

feedback@geeksforgeeks.org

Company Explore

About Us Job Fair For Students

Careers POTD: Revamped

In Media Python Backend LIVE

Contact Us Android App Development

Terms and Conditions DevOps LIVE

Privacy Policy DSA in JavaScript

Copyright Policy

Languages	Data Structures
Python	Array
Java	String
C++	Linked List
GoLang	Stack
SQL	Queue
R Language	Tree

### Algorithms

Android Tutorial

## Sorting HTML Searching CSS Greedy JavaScript

Dynamic Programming

Pattern Searching

ReactJS

Recursion

AngularJS

Backtracking

NodeJS

### **Data Science & ML**

# Data Science With Python Data Science For Beginner Machine Learning Tutorial Preparation for SDE Company Interview Corner Experienced Interview Pandas Tutorial NumPy Tutorial NLP Tutorial Company Preparation Preparation for SDE Company Interview Corner Experienced Interview Competitive Programming Aptitude

### **Python**

Python Tutorial	CBSE Notes for Class 8
Python Programming Examples	CBSE Notes for Class 9
Django Tutorial	CBSE Notes for Class 10
Python Projects	CBSE Notes for Class 11
Python Tkinter	CBSE Notes for Class 12
OpenCV Python Tutorial	English Grammar

### UPSC/SSC/BANKING

### Write & Farn

**GfG School** 

Graph

**Web Development** 

**Interview Corner** 

SBI PO Syllabus Improve an Article

IBPS PO Syllabus Pick Topics to Write

UPSC Ethics Notes Write Interview Experience

UPSC Economics Notes Internships

UPSC History Notes Video Internship

@geeksforgeeks, Some rights reserved