

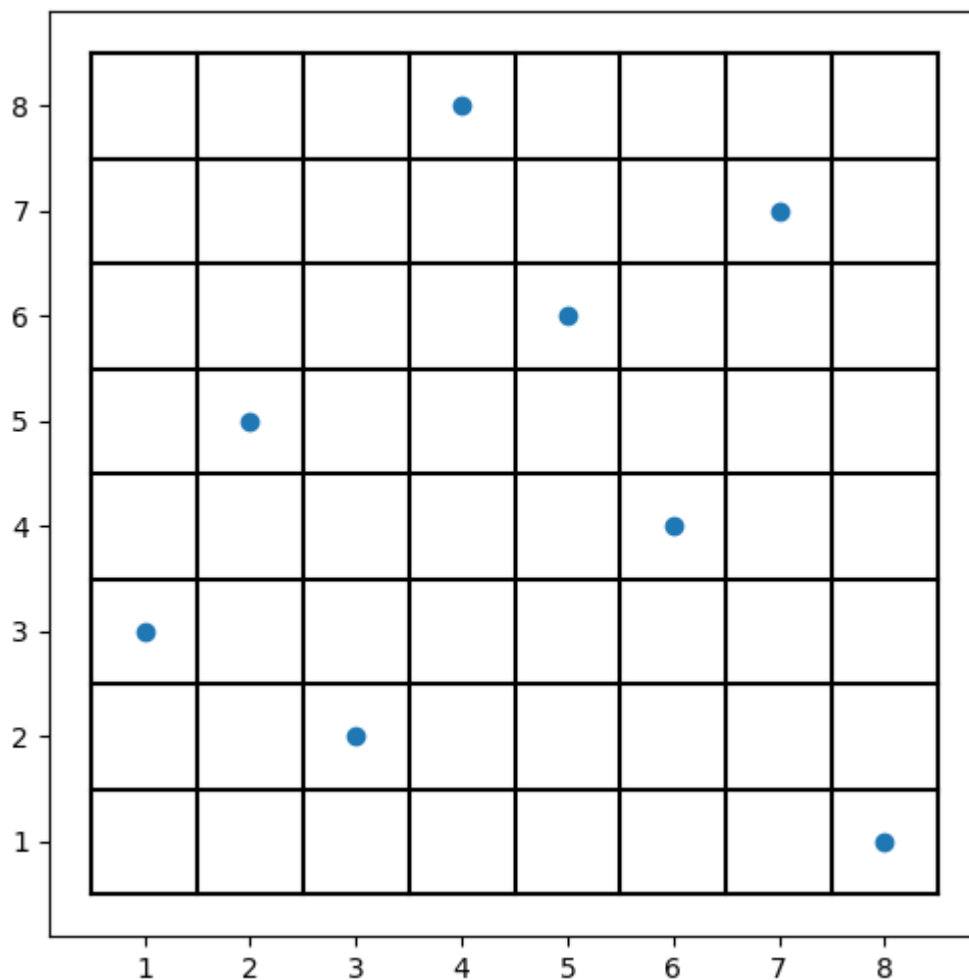
# CS480 Assignment -2

## Genetic Algorithm

Implement a Genetic algorithm to find a solution of the N-queens problem. Use the number of pairwise attacks as the objective function. Repeat the program 100 times for  $N = 8$ ,  $N = 16$ , and  $N = 32$  and show how many times you can find the solutions.

### Output for Queens = 8 Solution 1

Each dot indicates the position of queens on 8X8 chess board for one of the possible results out of 92 distinct solutions which may or may not be found.



## Code Output

C:\Users\Ashish\anaconda3\python.exe

C:\Users\Ashish\PycharmProjects\EightQueen\GeneticAlgorithmEightQueen.py

-----  
Epoch 1

Best Solution: [2, 4, 2, 8, 1, 4, 7, 3, 3]

-----  
Epoch 2

Best Solution: [2, 4, 2, 8, 1, 4, 7, 3, 3]

-----  
Epoch 3

Best Solution: [2, 4, 2, 8, 1, 4, 7, 3, 3]

-----  
Epoch 4

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]

-----  
Epoch 5

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]

-----  
Epoch 6

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]

-----  
Epoch 7

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]

-----  
Epoch 8

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]  
-----

Epoch 9

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]  
-----

Epoch 10

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]  
-----

Epoch 11

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]  
-----

Epoch 12

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]  
-----

Epoch 13

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]  
-----

Epoch 14

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]  
-----

Epoch 15

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]

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Epoch 16

Best Solution: [2, 5, 2, 8, 1, 4, 7, 3, 1]

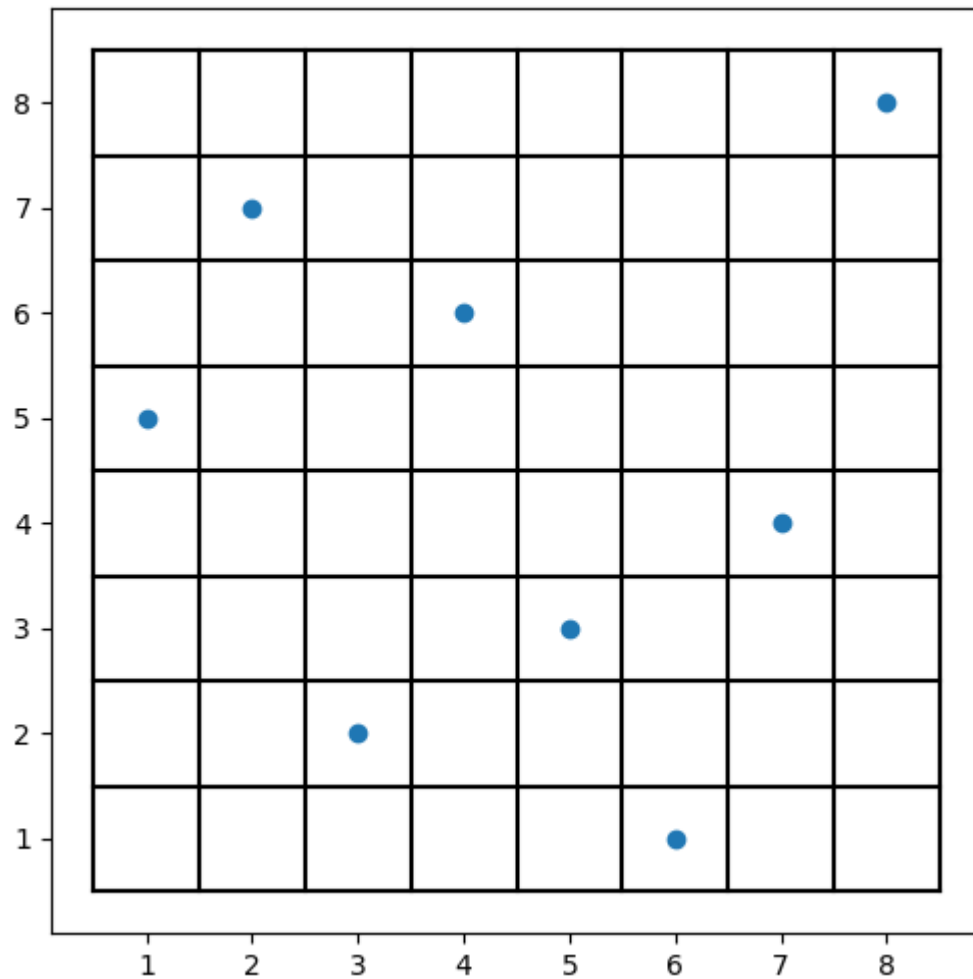
-----

Epoch 17

Solution Found: [3, 5, 2, 8, 6, 4, 7, 1, 0]

**Output for Queens = 8 Solution 2**

Each dot indicates the position of queens



C:\Users\Ashish\anaconda3\python.exe

C:\Users\Ashish\PycharmProjects\EightQueen\GeneticAlgorithmEightQueen.py

-----

Epoch 1

Best Solution: [2, 7, 1, 6, 4, 6, 1, 5, 3]

-----

Epoch 2

Best Solution: [2, 7, 1, 6, 4, 6, 1, 5, 3]

-----

Epoch 3

Best Solution: [2, 7, 1, 6, 3, 1, 4, 8, 2]

---

Epoch 4

Best Solution: [2, 7, 1, 6, 3, 1, 4, 8, 2]

---

Epoch 5

Best Solution: [2, 7, 1, 6, 3, 1, 4, 8, 2]

---

Epoch 6

Best Solution: [2, 7, 1, 6, 3, 1, 4, 8, 2]

---

Epoch 7

Best Solution: [2, 7, 1, 6, 3, 1, 4, 8, 2]

---

Epoch 8

Best Solution: [2, 7, 1, 6, 3, 1, 4, 8, 2]

---

Epoch 9

Best Solution: [2, 7, 2, 6, 3, 1, 4, 8, 1]

---

Epoch 10

Solution Found: [5, 7, 2, 6, 3, 1, 4, 8, 0]

## Output for Queens = 32 Solution 1

Each dot indicates the position of queens

Since the epoch values are very large, I am copying the last few

-----

Epoch 2609

Best Solution: [11, 22, 8, 17, 12, 32, 16, 27, 23, 18, 15, 28, 3, 5, 7, 9, 1, 29, 25, 19, 6, 24, 10, 21, 5, 26, 2, 14, 30, 13, 20, 4, 1]

-----

Epoch 2610

Best Solution: [11, 22, 8, 17, 12, 32, 16, 27, 23, 18, 15, 28, 3, 5, 7, 9, 1, 29, 25, 19, 6, 24, 10, 21, 5, 26, 2, 14, 30, 13, 20, 4, 1]

-----

Epoch 2611

Best Solution: [11, 22, 8, 17, 12, 32, 16, 27, 23, 18, 15, 28, 3, 5, 7, 9, 1, 29, 25, 19, 6, 24, 10, 21, 5, 26, 2, 14, 30, 13, 20, 4, 1]

-----

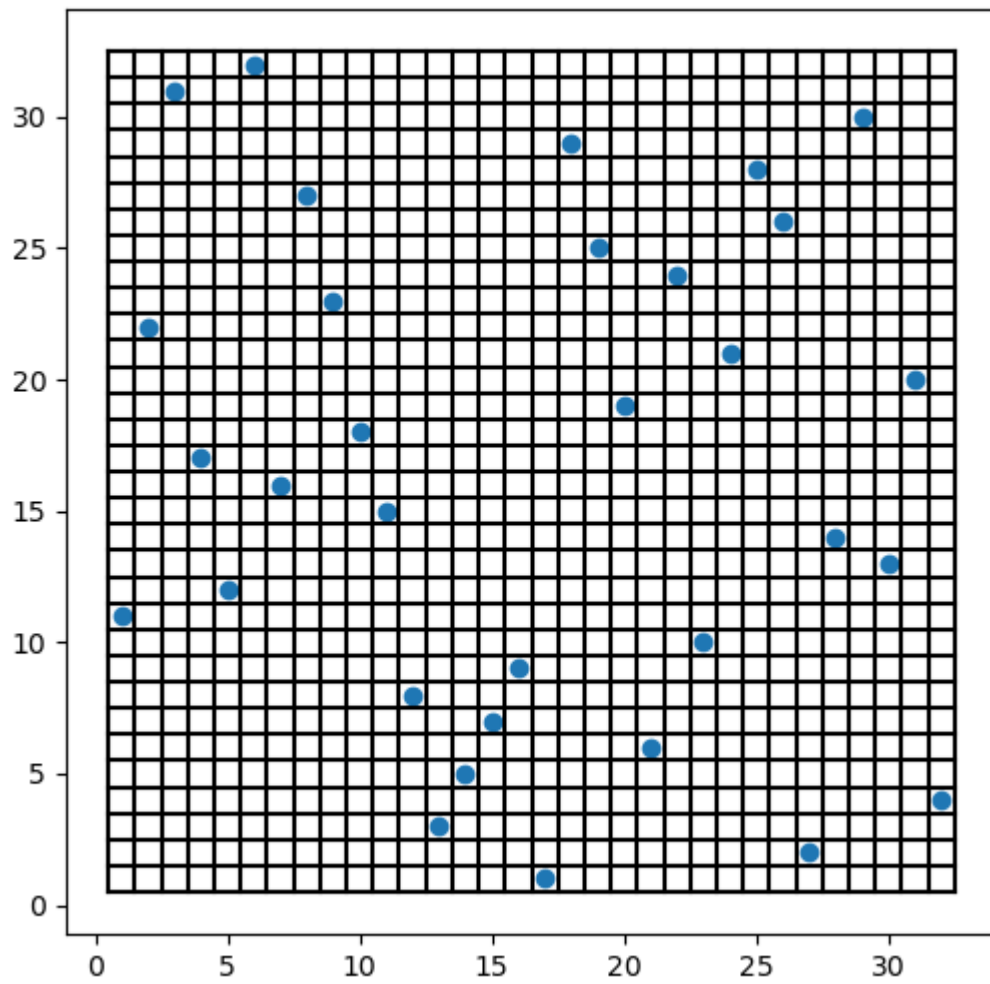
Epoch 2612

Best Solution: [11, 22, 8, 17, 12, 32, 16, 27, 23, 18, 15, 28, 3, 5, 7, 9, 1, 29, 25, 19, 6, 24, 10, 21, 5, 26, 2, 14, 30, 13, 20, 4, 1]

-----

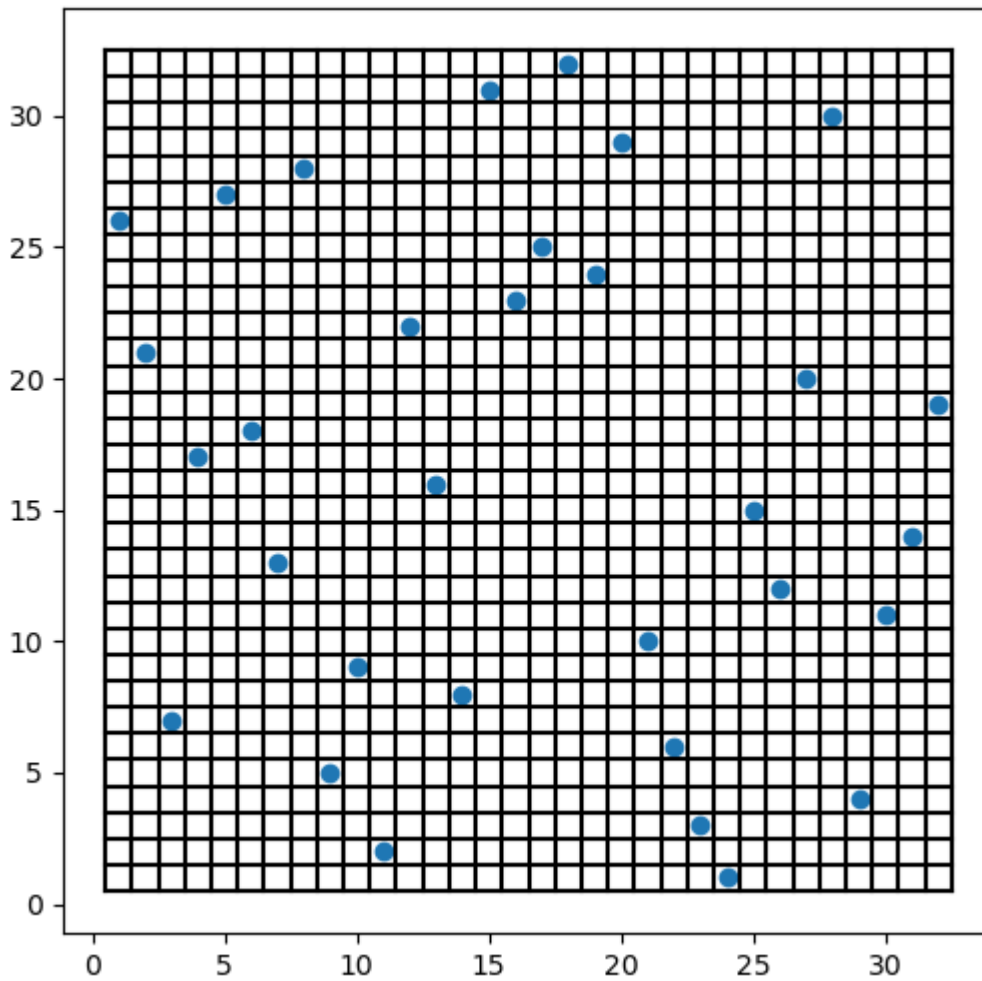
Epoch 2613

Solution Found: [11, 22, 31, 17, 12, 32, 16, 27, 23, 18, 15, 8, 3, 5, 7, 9, 1, 29, 25, 19, 6, 24, 10, 21, 28, 26, 2, 14, 30, 13, 20, 4, 0]



**Output for Queens = 32 Solution 2**





Since the epoch values are very large, I am copying the last few

Epoch 735

Best Solution: [26, 21, 7, 4, 6, 29, 13, 28, 5, 9, 2, 22, 16, 8, 31, 23, 25, 32, 24, 17, 10, 6, 3, 1, 15, 12, 20, 30, 27, 11, 14, 19, 1]

-----

Epoch 736

Best Solution: [26, 21, 7, 4, 6, 29, 13, 28, 5, 9, 2, 22, 16, 8, 31, 23, 25, 32, 24, 17, 10, 6, 3, 1, 15, 12, 20, 30, 27, 11, 14, 19, 1]

-----

Epoch 737

Best Solution: [26, 21, 7, 4, 6, 29, 13, 28, 5, 9, 2, 22, 16, 8, 31, 23, 25, 32, 24, 17, 10, 6, 3, 1, 15, 12, 20, 30, 27, 11, 14, 19, 1]

-----

Epoch 738

Best Solution: [26, 21, 7, 4, 6, 29, 13, 28, 5, 9, 2, 22, 16, 8, 31, 23, 25, 32, 24, 17, 10, 6, 3, 1, 15, 12, 20, 30, 27, 11, 14, 19, 1]

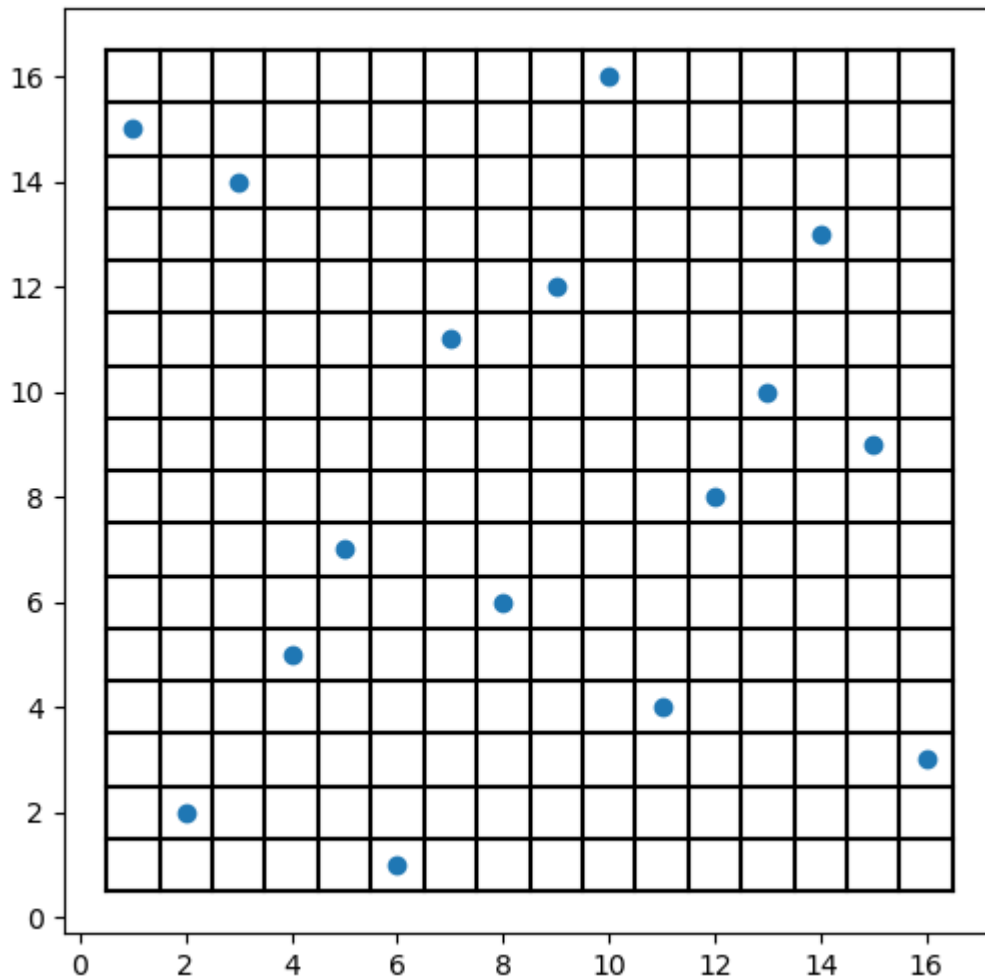
-----

Epoch 739

Solution Found: [26, 21, 7, 17, 27, 18, 13, 28, 5, 9, 2, 22, 16, 8, 31, 23, 25, 32, 24, 29, 10, 6, 3, 1, 15, 12, 20, 30, 4, 11, 14, 19, 0]

### **Output for Queens = 16 Solution 1**

Each dot indicates the position of queens



Since the epoch values are very large, I am copying the last few

Epoch 96

Best Solution: [15, 2, 10, 5, 7, 1, 11, 6, 14, 16, 4, 8, 4, 13, 9, 3, 1]

-----

Epoch 97

Best Solution: [15, 2, 10, 5, 7, 1, 11, 6, 14, 16, 4, 8, 4, 13, 9, 3, 1]

-----

Epoch 98

Best Solution: [15, 2, 10, 5, 7, 1, 11, 6, 14, 16, 4, 8, 4, 13, 9, 3, 1]

-----

Epoch 99

Best Solution: [15, 2, 10, 5, 7, 1, 11, 6, 14, 16, 4, 8, 4, 13, 9, 3, 1]

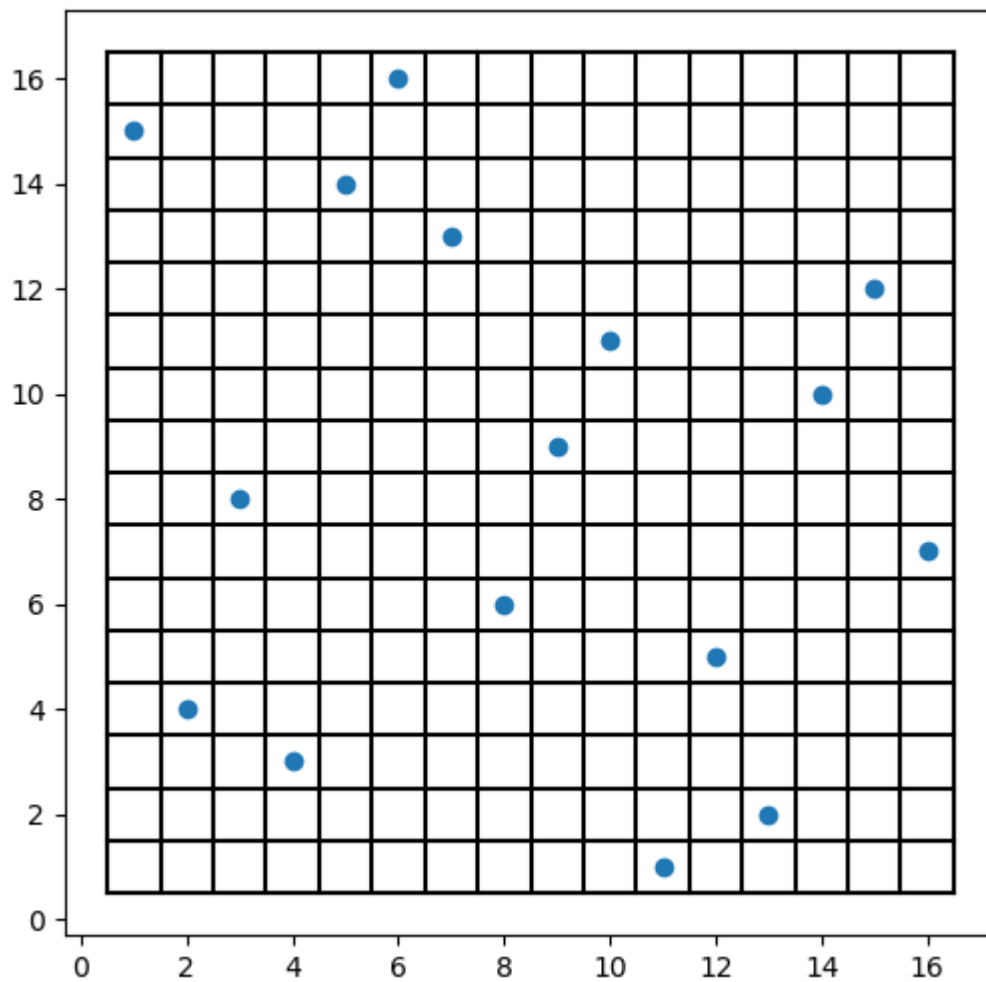
-----

Epoch 100

Solution Found: [15, 2, 14, 5, 7, 1, 11, 6, 12, 16, 4, 8, 10, 13, 9, 3, 0]

### **Output for Queens = 16 Solution 2**

Each dot indicates the position of queens



Since the epoch values are very large, I am copying the last few

Epoch 202

Best Solution: [15, 4, 8, 3, 14, 16, 13, 6, 1, 11, 15, 5, 2, 10, 12, 7, 1]

-----

Epoch 203

Best Solution: [15, 4, 8, 3, 14, 16, 13, 6, 1, 11, 15, 5, 2, 10, 12, 7, 1]

-----

Epoch 204

Best Solution: [15, 4, 8, 3, 14, 16, 13, 6, 1, 11, 15, 5, 2, 10, 12, 7, 1]

-----

Epoch 205

Solution Found: [15, 4, 8, 3, 14, 16, 13, 6, 9, 11, 1, 5, 2, 10, 12, 7, 0]

```
import random
import matplotlib.pyplot as plt
import matplotlib
matplotlib.use('TkAgg')
```

```
n = 16 # Number of Queens
p = 100 # Number of Population
```

```
current_generation = [] # Current Generation
new_generation = [] # New Generation
```

```
def RandomPopulationGeneration(num_rows, num_queens):
```

```
    """
    :param num_rows: Rows of the board.
    :param num_queens: Number of queens for the problem.
    :return: List of the random board generated.
    """
```

```
    list_of_generation = []
    for i in range(num_rows):
        gene = []
        for j in range(num_queens):
            gene.append(random.randint(1, n))
        gene.append(0)
        list_of_generation.append(gene)
    return list_of_generation
```

```
def FitnessSurvival(population):
```

```
    """
    :param population: List of the population of the board generated.
    :return: Best fitting population after swap is made.
    """
```

```
    i = 0
    attacking = 0
    while i < len(population):
        j = 0
        attacking = 0
        while j < n:
            l = j + 1

            while l < n:
                if population[i][j] == population[i][l]:
                    attacking += 1
                if abs(j - l) == abs(population[i][j] - population[i][l]):
                    attacking += 1
                l += 1
            j += 1
        population[i][len(population[j]) - 1] = attacking
        i += 1

    for i in range(len(population)):
        minimum = i
        for j in range(i, len(population)):
            if population[j][n] < population[minimum][n]:
                minimum = j

        temp = population[i]
        population[i] = population[minimum]
        population[minimum] = temp
    return population
```

```
def CrossOver(list_of_generation):
```

```
    """
```

```
:param list_of_generation: List of the generations for crossover
:return: Completed cross over list
"""
```

```
for i in range(0, len(list_of_generation), 2):
    z = 0
    new_child1 = []
    new_child2 = []
    while z < n:
        if (z < n // 2):
            new_child1.append(list_of_generation[i][z])
            new_child2.append(list_of_generation[i + 1][z])
        else:
            new_child1.append(list_of_generation[i + 1][z])
            new_child2.append(list_of_generation[i][z])
        z += 1
    new_child1.append(0)
    new_child2.append(0)
    list_of_generation.append(new_child1)
    list_of_generation.append(new_child2)
return list_of_generation
```

```
def Mutation(list_of_generation):
    """
```

```
:param list_of_generation: List for mutation function
:return: Lis of mutated population.
"""
```

```
list_of_mutation = []
i = 0
while i < p // 2:
    new_rand = random.randint(p // 2, p - 1)
    if new_rand not in list_of_mutation:
        list_of_mutation.append(new_rand)
        list_of_generation[new_rand][random.randint(0, n - 1)] = random.randint(1, n - 1)
        i += 1
return list_of_generation
```

```
def ShowResults(response):
    """
```

```
:param response: Plot the queens position using matplotliblib
:return: Show plot.
"""
```

```
l = len(response)
plt.figure(figsize=(6, 6))
plt.scatter([x + 1 for x in range(1 - 1)], response[:1 - 1])
for i in range(1):
    plt.plot([0.5, 1 - 0.5], [i + 0.5, i + 0.5], color="k")
    plt.plot([i + 0.5, i + 0.5], [0.5, 1 - 0.5], color="k")
plt.show()
```

```
# Call the driver program.
```

```
current_generation = RandomPopulationGeneration(p, n)
current_generation = FitnessSurvival(current_generation)
epoch = 1
```

```
while True:
    print("-----")
    print("Epoch ", epoch)
    current_generation = current_generation[0:p // 2]
    new_generation = CrossOver(current_generation)
    new_generation = Mutation(new_generation)
    current_generation = new_generation
    current_generation = FitnessSurvival(current_generation)
    if current_generation[0][n] == 0:
```



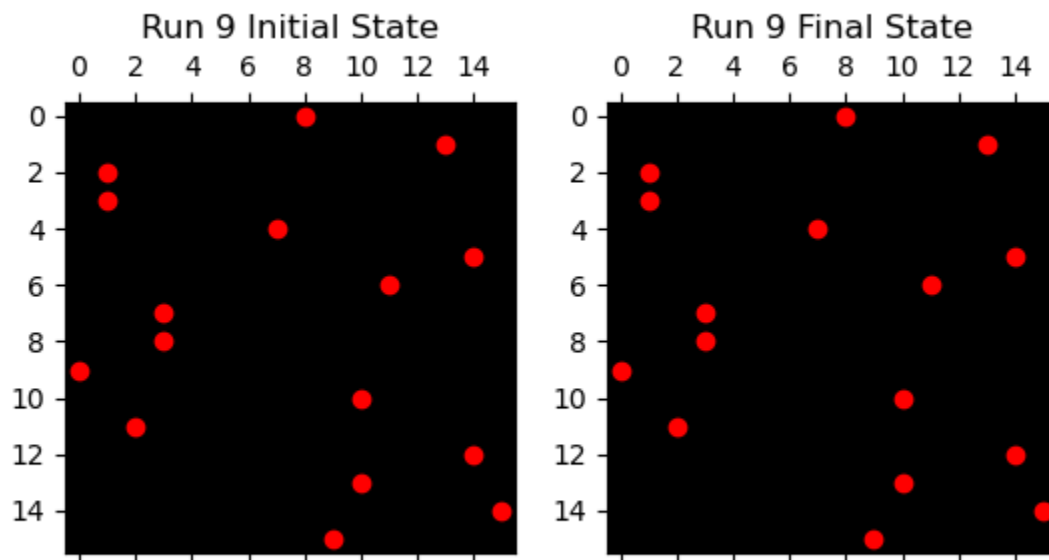
```
    print("Solution Found: ", current_generation[0])
    ShowResults(current_generation[0])
    break
else:
    print("Best Solution: ", current_generation[0])
epoch += 1
```

# CS480 Assignment -2

## Hill Climbing

Implement a Hill Climbing Search algorithm to find a solution of the N-queens problem from a random given position. Use the number of pairwise attacks as the objective function. Repeat the program 100 times for  $N = 8$ ,  $N = 16$ , and  $N = 32$  and show how many times you can find the solutions. Plot the initial state and the final state (not necessary the solution) of the first 10 times.

**Number of Queens = 16, output for first run**



C:\Users\Ashish\anaconda3\python.exe

C:\Users\Ashish\PycharmProjects\EightQueen\HillClimbingAlgorightmEightQueen.py

Run 1: Initial Attacks = 18, Final Attacks = 5

Run 2: Initial Attacks = 36, Final Attacks = 5

Run 3: Initial Attacks = 16, Final Attacks = 4

Run 4: Initial Attacks = 15, Final Attacks = 3

Run 5: Initial Attacks = 14, Final Attacks = 5

Run 6: Initial Attacks = 22, Final Attacks = 3

Run 7: Initial Attacks = 21, Final Attacks = 5

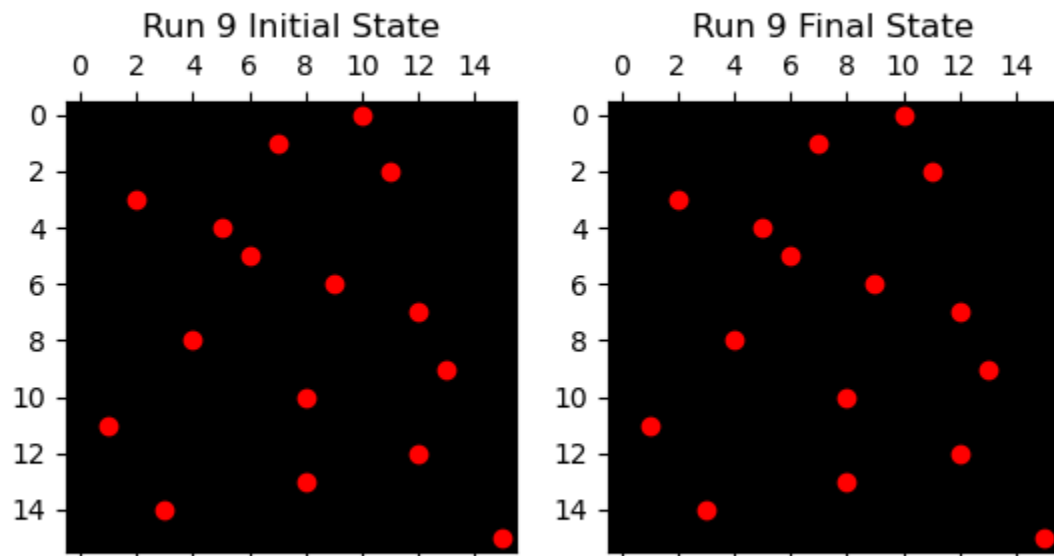
Run 8: Initial Attacks = 11, Final Attacks = 4

Run 9: Initial Attacks = 16, Final Attacks = 6

Run 10: Initial Attacks = 15, Final Attacks = 4

Total solutions found for N = 16: 0 out of 100 runs

**Number of Queens = 16, output for second run**



Run 1: Initial Attacks = 14, Final Attacks = 6

Run 2: Initial Attacks = 12, Final Attacks = 5

Run 3: Initial Attacks = 16, Final Attacks = 5

Run 4: Initial Attacks = 25, Final Attacks = 6

Run 5: Initial Attacks = 15, Final Attacks = 6

Run 6: Initial Attacks = 12, Final Attacks = 5

Run 7: Initial Attacks = 14, Final Attacks = 4

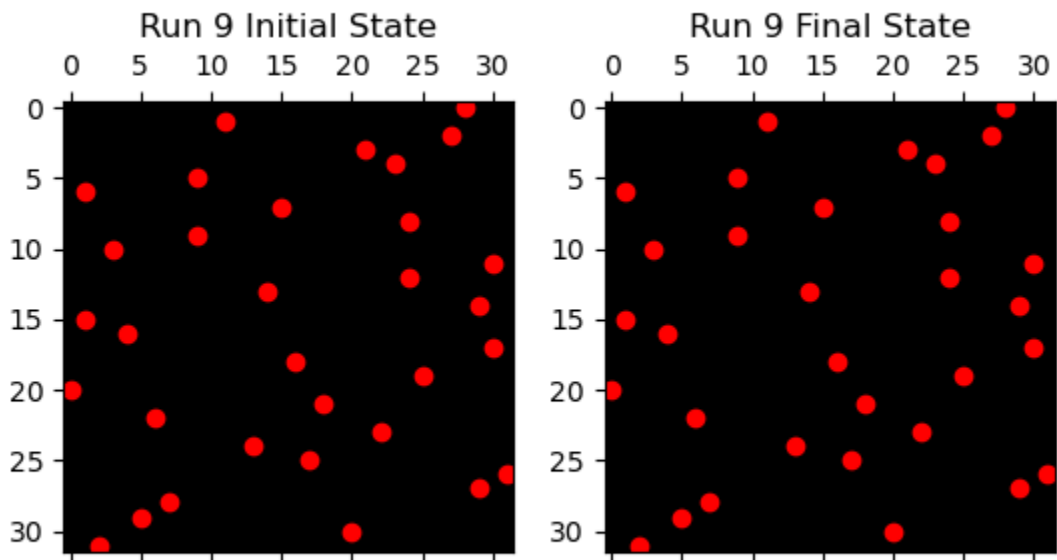
Run 8: Initial Attacks = 17, Final Attacks = 5

Run 9: Initial Attacks = 13, Final Attacks = 5

Run 10: Initial Attacks = 13, Final Attacks = 5

Total solutions found for N = 16: 0 out of 100 runs

**Number of Queens = 32, output for first run**



Run 1: Initial Attacks = 36, Final Attacks = 12

Run 2: Initial Attacks = 33, Final Attacks = 13

Run 3: Initial Attacks = 41, Final Attacks = 15

Run 4: Initial Attacks = 32, Final Attacks = 13

Run 5: Initial Attacks = 31, Final Attacks = 9

Run 6: Initial Attacks = 36, Final Attacks = 18

Run 7: Initial Attacks = 35, Final Attacks = 11

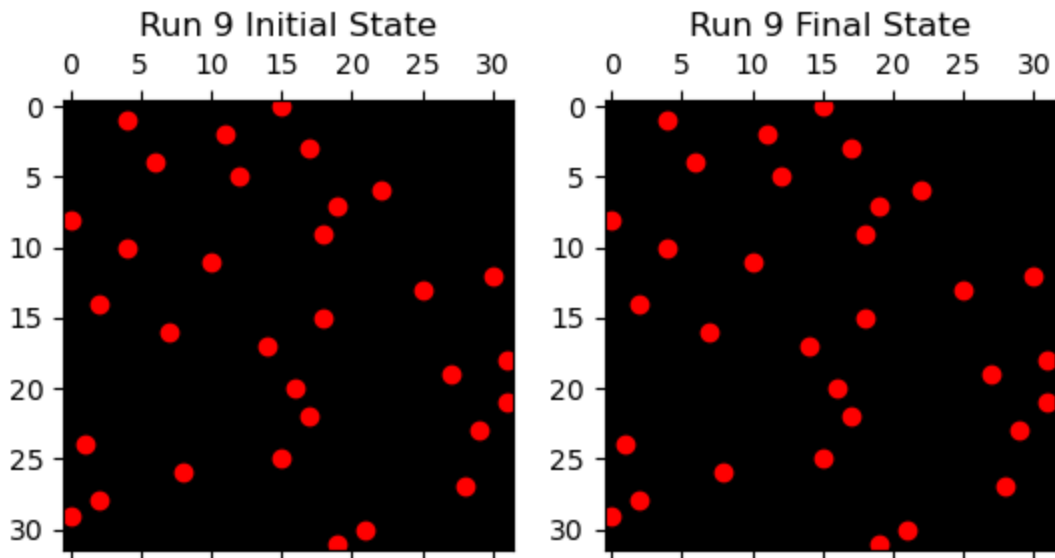
Run 8: Initial Attacks = 37, Final Attacks = 12

Run 9: Initial Attacks = 35, Final Attacks = 10

Run 10: Initial Attacks = 29, Final Attacks = 14

Total solutions found for  $N = 32$ : 0 out of 100 runs

**Number of Queens = 32, output for second run**



Run 1: Initial Attacks = 37, Final Attacks = 16

Run 2: Initial Attacks = 36, Final Attacks = 11

Run 3: Initial Attacks = 36, Final Attacks = 13

Run 4: Initial Attacks = 34, Final Attacks = 15

Run 5: Initial Attacks = 33, Final Attacks = 10

Run 6: Initial Attacks = 32, Final Attacks = 12

Run 7: Initial Attacks = 35, Final Attacks = 13

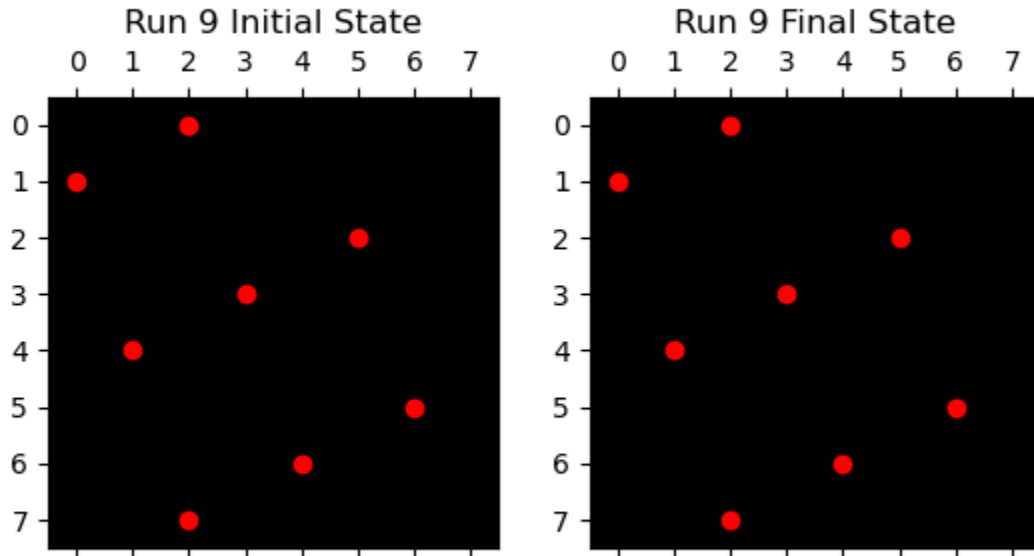
Run 8: Initial Attacks = 38, Final Attacks = 13

Run 9: Initial Attacks = 31, Final Attacks = 14

Run 10: Initial Attacks = 28, Final Attacks = 15

Total solutions found for  $N = 32$ : 0 out of 100 runs

**Number of Queens = 8, output for first run**



Run 1: Initial Attacks = 11, Final Attacks = 2

Run 2: Initial Attacks = 6, Final Attacks = 1

Run 3: Initial Attacks = 4, Final Attacks = 1

Run 4: Initial Attacks = 7, Final Attacks = 1

Run 5: Initial Attacks = 11, Final Attacks = 1

Run 6: Initial Attacks = 11, Final Attacks = 2

Run 7: Initial Attacks = 11, Final Attacks = 2

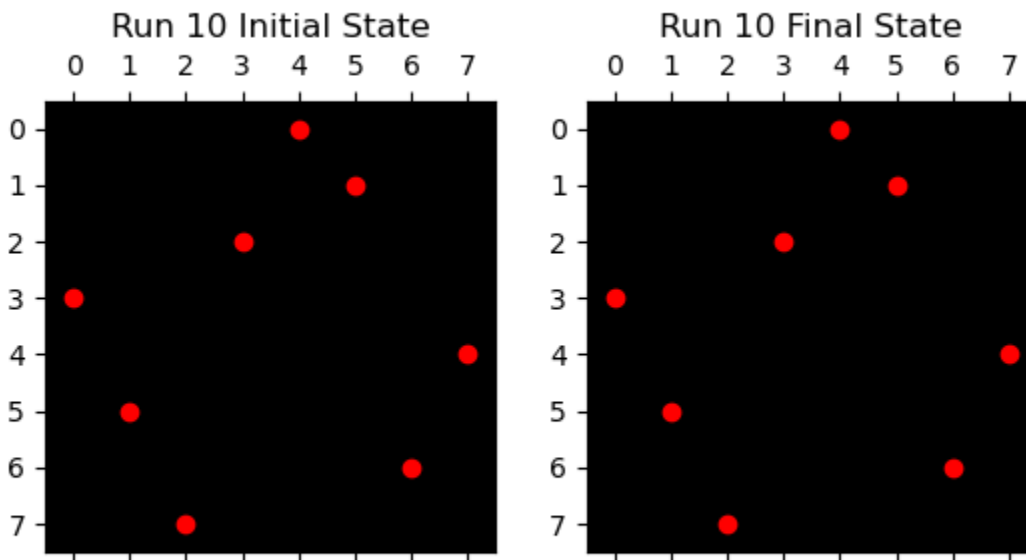
Run 8: Initial Attacks = 9, Final Attacks = 4

Run 9: Initial Attacks = 10, Final Attacks = 1

Run 10: Initial Attacks = 10, Final Attacks = 1

Total solutions found for N = 8: 7 out of 100 runs

**Number of Queens = 8, output for second run**



Run 1: Initial Attacks = 7, Final Attacks = 1

Run 2: Initial Attacks = 9, Final Attacks = 1

Run 3: Initial Attacks = 4, Final Attacks = 0

Run 4: Initial Attacks = 6, Final Attacks = 1

Run 5: Initial Attacks = 8, Final Attacks = 2

Run 6: Initial Attacks = 14, Final Attacks = 1

Run 7: Initial Attacks = 7, Final Attacks = 1

Run 8: Initial Attacks = 6, Final Attacks = 2

Run 9: Initial Attacks = 7, Final Attacks = 2



Run 10: Initial Attacks = 6, Final Attacks = 2

Total solutions found for  $N = 8$ : 5 out of 100 runs

```
import random
import numpy as np
import matplotlib.pyplot as plt
```

```
def GenerateRandomBoard(n):
    """
    :param n: Number queens for board
    :return: List of the random boards.
    """
    return [random.randint(0, n - 1) for _ in range(n)]
```

```
def ShowBoard(board, title1, title2):
    """
    :param board: Board with Queens
    :param title1: Initial State Plot
    :param title2: Final State Plot
    :return:
    """
    n = len(board)
    fig, (ax1, ax2) = plt.subplots(1, 2)

    # Plot initial state
    ax1.matshow(np.zeros((n, n)), cmap='gray')
    for i in range(n):
        ax1.plot(board[i], i, 'ro')
    ax1.set_title(title1)

    # Plot final state
    ax2.matshow(np.zeros((n, n)), cmap='gray')
    for i in range(n):
        ax2.plot(board[i], i, 'ro')
    ax2.set_title(title2)

    plt.show()
```

```
def GetQueenAttackCounts(board):
    """
    :param board: Any board state
    :return: Number of attacking queens
    """
    n = len(board)
    attacks = 0
    for i in range(n):
        for j in range(i + 1, n):
            if board[i] == board[j] or abs(board[i] - board[j]) == abs(j - i):
                attacks += 1
    return attacks
```

```
def HillClimbingAlgorithm(n, max_iterations=100):
    """
    :param n: Number of queens
    :param max_iterations: Number of times before the Algorithm ends
    :return:
    """
    solutions_found = 0

    for i in range(1, 101): # Repeat the program 100 times
        board = GenerateRandomBoard(n)
        initial_attacks = GetQueenAttackCounts(board)
        current_attacks = initial_attacks
        iterations = 0
```

```

while current_attacks > 0 and iterations < max_iterations:
    neighbor = list(board)
    row = random.randint(0, n - 1)
    col = random.randint(0, n - 1)
    neighbor[row] = col
    neighbor_attacks = GetQueenAttackCounts(neighbor)

    if neighbor_attacks < current_attacks:
        board = neighbor
        current_attacks = neighbor_attacks

    iterations += 1

if current_attacks == 0:
    solutions_found += 1

if i <= 10: # Plot initial and final states for the first 10 runs
    print(f"Run {i}: Initial Attacks = {initial_attacks}, Final Attacks = {current_attacks}")
    ShowBoard(board, f"Run {i} Initial State", f"Run {i} Final State")

return solutions_found

def main():
    """
    :return: Driver method.
    """
    N = 8
    solutions = HillClimbingAlgorithm(N)
    print(f"Total solutions found for N = {N}: {solutions} out of 100 runs")

if __name__ == "__main__":
    main()

```

How to execute the code.

Genetic Algorithm.

Change the parameter  $n = 8, 12, 32$  (number of queens)

```
Cd ~\EightQueen\GeneticAlgorithmEightQueen.py python3 GeneticAlgorithmEightQueen.py
```

Hill Climbing

Change the parameter  $n = 8, 12, 32$  (number of queens)

```
cd ~\EightQueen\HillClimbingAlgorightmEightQueen.py python3  
HillClimbingAlgorightmEightQueen.py
```