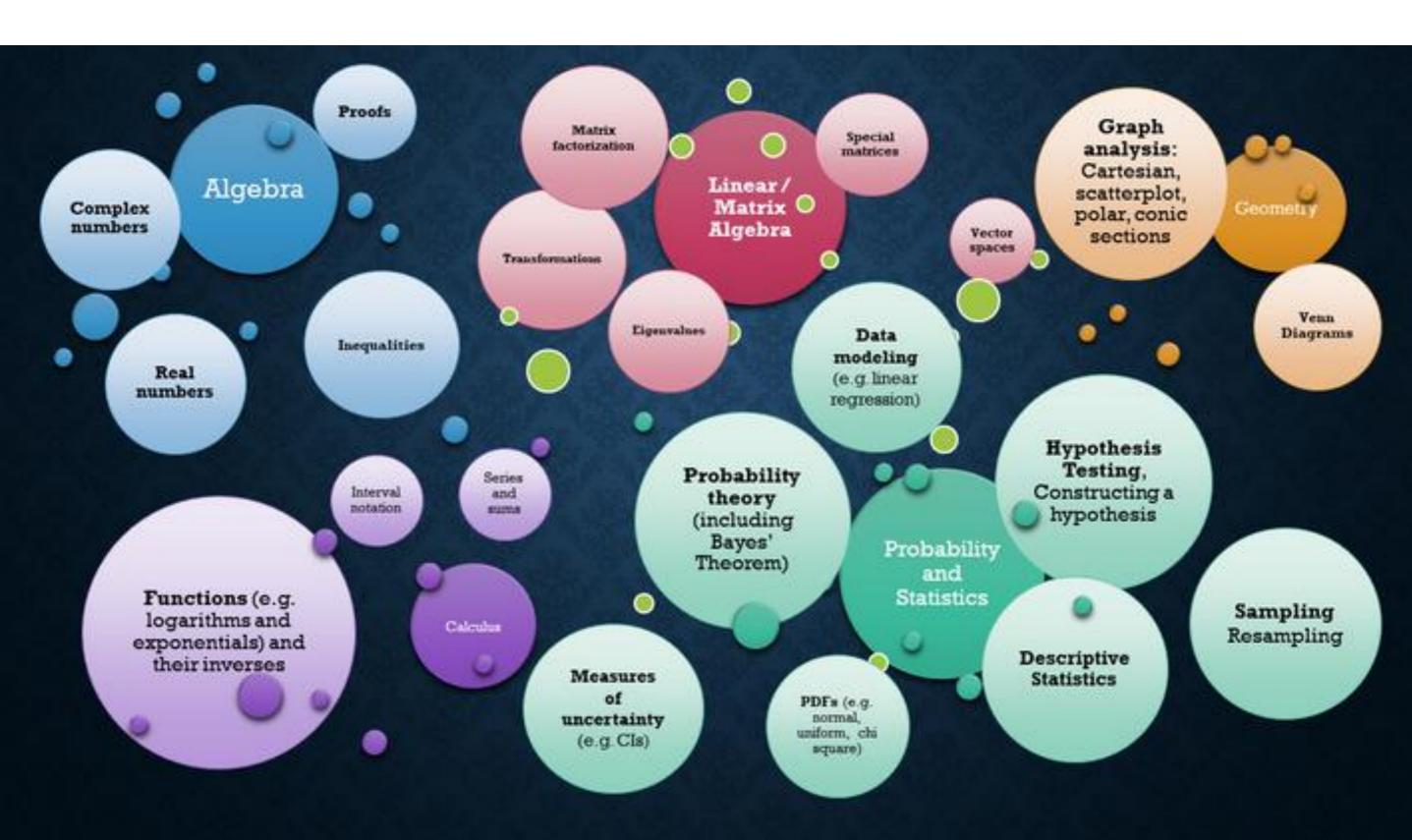
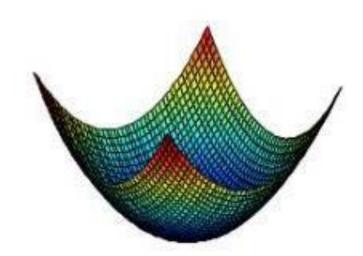


### **Math for Data Science**

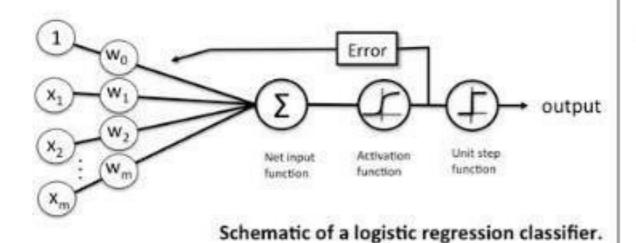


# Deep learning vs Machine learning in One Picture

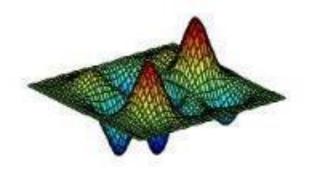
# You



Unique optimum: global/local.

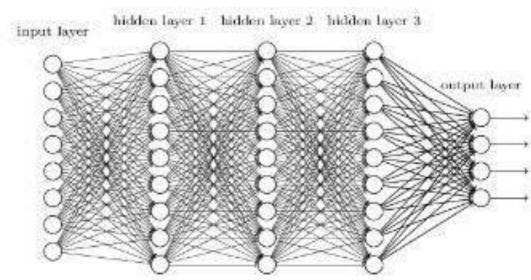


# The guy she tells you not to worry about



- Multiple local optima
- In high dimensions possibly

#### Deep neural network



### Which Software Should I Choose?

# Python

R

SAS

# SQL

Best for:

Availability

Easy to learn?

Advantages

Disadvantages

General programming; Data analysis; Deep learning; Repeated tasks

Free, open source

Yes, especially for software engineers

Easy to deploy; General purpose language; Widely used by corporations

Requires rigorous testing

Statistical analysis; Data analysis; Single passes of data

Free, open source

Steep learning curve; Relatively easier if no prior coding experience

Minimal coding required for statistical models

Very statistics oriented; Not a general-purpose program Statistical analysis; Data analysis

Paid (free for university edition); Closed source

Yes, especially if you already know SQL

Highly reliable, secure and stable

Relatively expensive

Database manipulating, updating, querying; Extracting, wrangling data

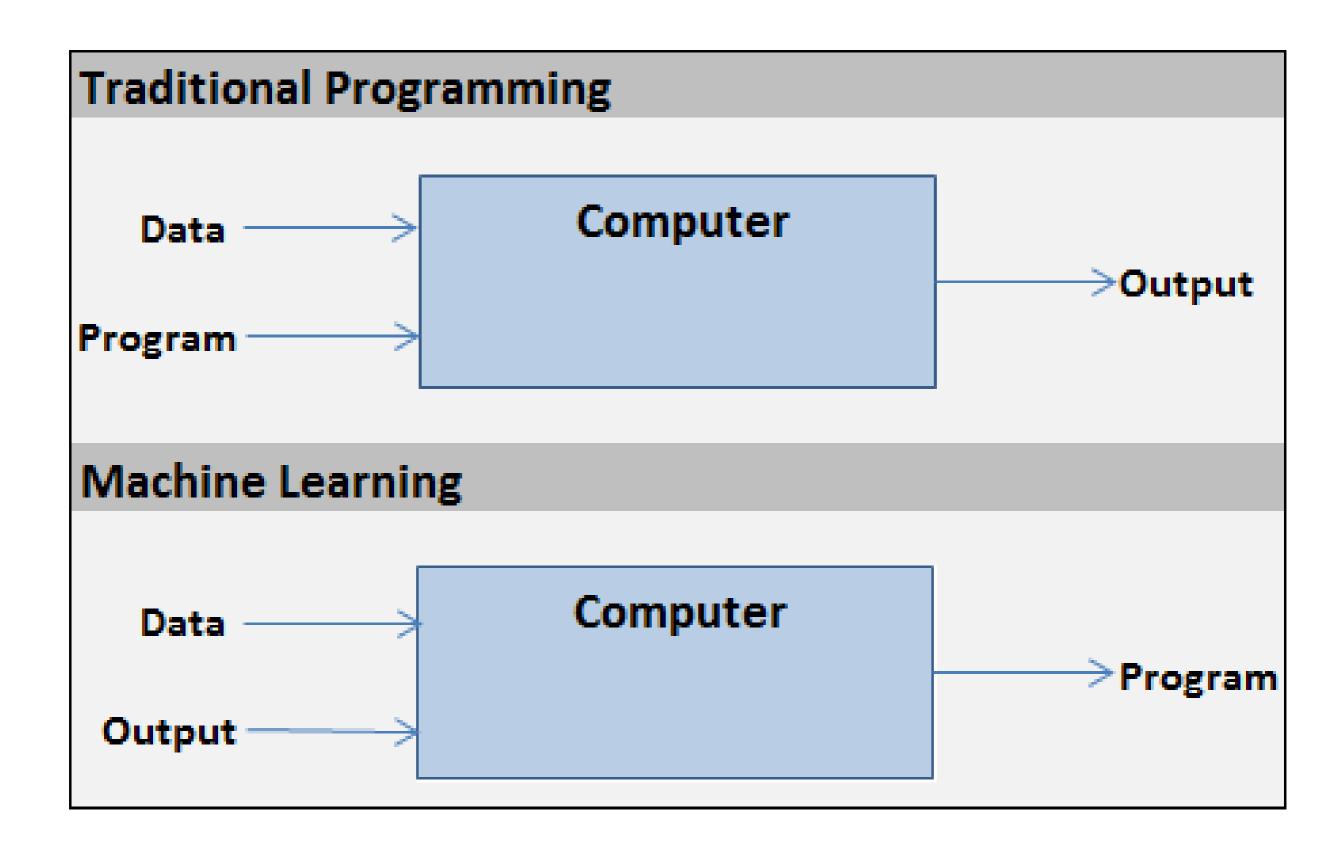
Open and closed source versions available (free and paid)

Relatively easy for basic level; Learning curve for more complex tasks

Very readable

Not general purpose: very specific, limited capability

# **Traditional Programming vs ML in One Picture**



### Prediction:

Predicting Y from X

#### Inference:

Understand relationship between X and Y

Goal

Develop a "best" model (considering all predictors) to predict Y with high accuracy, low error. Estimate an association between and outcome variable and a predictor variable (while adjusting for confounders).

Answers the question

How can I accurately predict new data points? What do the relationships between the variables mean?

Example

What mortality levels does the model predict given a certain income and education level?

Which has the biggest impact on mortality: income or education?

I Want to Predict... Method Subtypes kNN Classification Discrete-valued, Obese **Categorical Outputs Decision Trees** Example: Given eating habits, predict obese or Not not obese. Obese Perception Classifier Linear Regression Regression 00. 100 Real-Valued lbs 220 Outputs Ridge Regression Dolbs lbs Example: Given eating 241 110 lbs habits, predict weight. lbs Lasso Regression

"Null" means that it's a commonly accepted fact that you are working to nullify. Example: the null might be "Data scientists earn an average of \$113,309"

 $H_0$ :  $\mu = 133,309$  $H_1$ :  $\mu < 133,309$ 

The alternative to the null.

For example, you think that data scientists earn a lot less than 100k, and you're going to set out to prove your theory.

The alpha level α is the probability of making the wrong decision when the null hypothesis is true.

Not sure what alpha level to set? 5% is very common.

 $\alpha = 0.05$ 

You may already have the data at hand.

If not, you have four main choices:

- Census
- Sample survey
- Experiment
- Observational survey

Which test statistic you use depends on which test you're running. Choosing the right test is probably the biggest challenge in hypothesis

testing. Four of the most common:

- Z-Statistic
- T-Statistic
- F-Statistic (ANOVA)
- Chi-Square Statistic

The rejection region tells you at what values you should reject the null hypothesis.

> The critical value (the line that separates accept from reject) calculated with statistical tables (or software, based on those tables).

The basic Hypothesis idea is that that your test statistic is going to fall Accept or Reject the Null into one of two areas: accept or reject. In this graph, you would reject the null

hypothesis

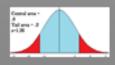
if your test

statistic

the red

area.

falls into



# Type of Distribution

Number of trials, n

Probability, p

With or without replacement?

When to use it?

Example

### Binomial

How many Successes in n trials?

Fixed n

Known p. Probability of Success is constant from trial to trial

With replacement

You know the exact probability of an event happening; you want to find the probability of that event happening k times out of n.

Number of defects in a box of 1,000 factory produced widgets

### Poisson

Good for rare events (large n, small p)

Unknown n (it is a random variable) and potentially infinite.

Unknown p for each trial (but known average p).

With replacement

You know the mean probability of an event and you want to find the probability of n events happening.

Number of innocent people convicted of a crime.

## Hypergeometric

Use for small populations, without replacement

Fixed n

Probability for each trial changes (because of no replacement).

Without replacement

Samples are small compared to the population (n ≥ 5%).

Binomial is easier and provides a good approximation if you have a large population.

30 people (14W, 16M) apply for two jobs. What is the probability both positions are filled by women?

# Normal Distribution

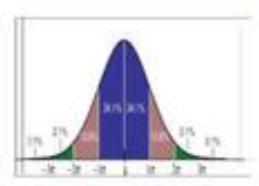
# Student's T-Distribution

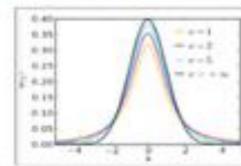
# **Binomial** Distribution

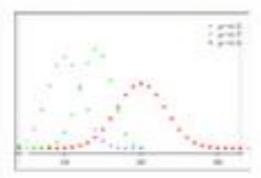
# Poisson Distribution

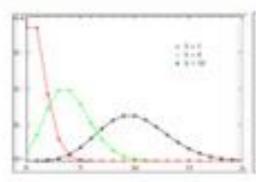
Exponential Distribution

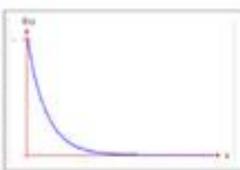
What does it look











Defining Characteristics

Example of When to Use It

Example of DS Application Distinctive Bell Shape

Shorter, fatter than the normal distribution.

Two outcomes: Success/Failure

Various shapes, but valid only for integers on the x-axis.

Models Time Between Events

Modeling natural phenomena (height, weight, IQ, test scores etc.)

When you have small samples or don't know the population variance (o2).

Coin Toss Probability (Heads, Tails)

Gives probability of number of events in a fixed interval.

"How much time will go by before a major hurricane hits the Atlantic Seaboard?"

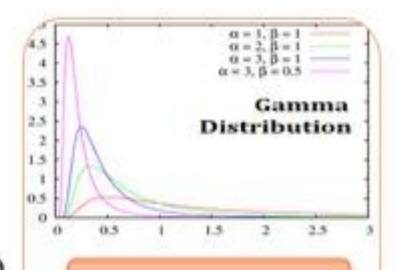
Least squares fitting or propagation of uncertainty.

Unknown o2 is common in real life data, you you'll have to use the Tinstead of the normal in that case.

Anywhere where binary (yes/no, black/white, vote/don't vote) data is used.

Anywhere there is a waiting time between events.

Building continuoustime Markov chains.



**Parameters** 

Rate(β); Shape (α)

Overview

A family that includes the exponential distribution

Common Uses

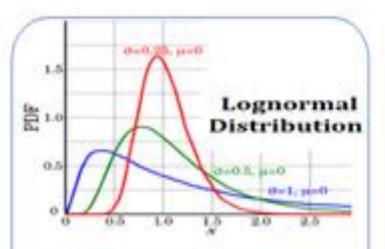
When to Use

Most often used as time to a rth hit in a Poisson process

Event waiting times when the event

process isn't completely random

(Mun, 2008)

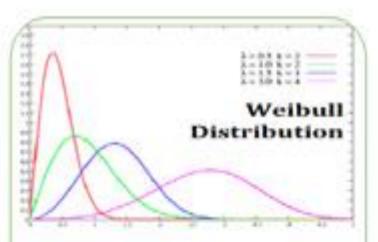


Location ( µ ): Shape (  $\sigma$  )

Exponential (anti-log) of the normal distribution

Model lifetimes in survival analysis /reliability (Bromideh, 2012)

Use when data has small bumps/perturbations that additively affect the result



Location ( µ ); Shape ( y ); Scale ( a )

A natural extension of the exponential distribution

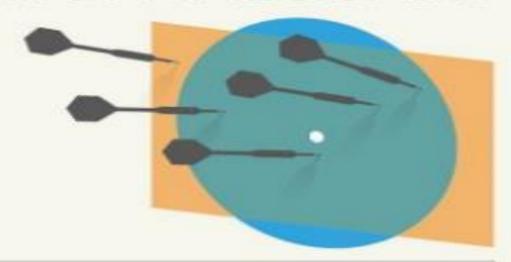
Describe the distribution of lifetime data (Bromideh, 2012) and the time to wait for the next event.

Use when the exponential doesn't quite fit or when you have steep drop-offs.

# THE GAUSSIAN CORRELATION INEQUALITY

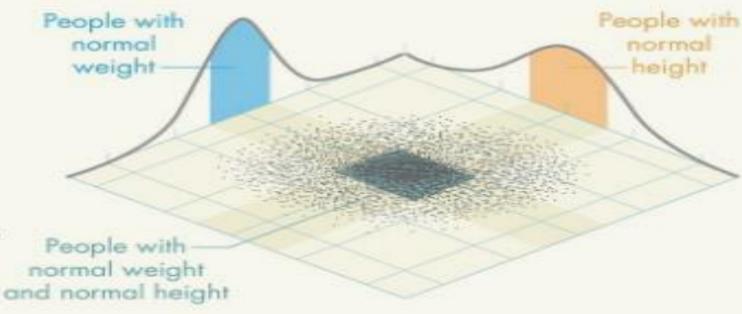
### ... in convex geometry:

Consider any two convex symmetrical shapes in any number of dimensions that are centered on the same point, which forms a target. Darts thrown at the target will land in a bell curve or "Gaussian distribution" of positions. The overlap of the two shapes increases your probability (P) of striking both.



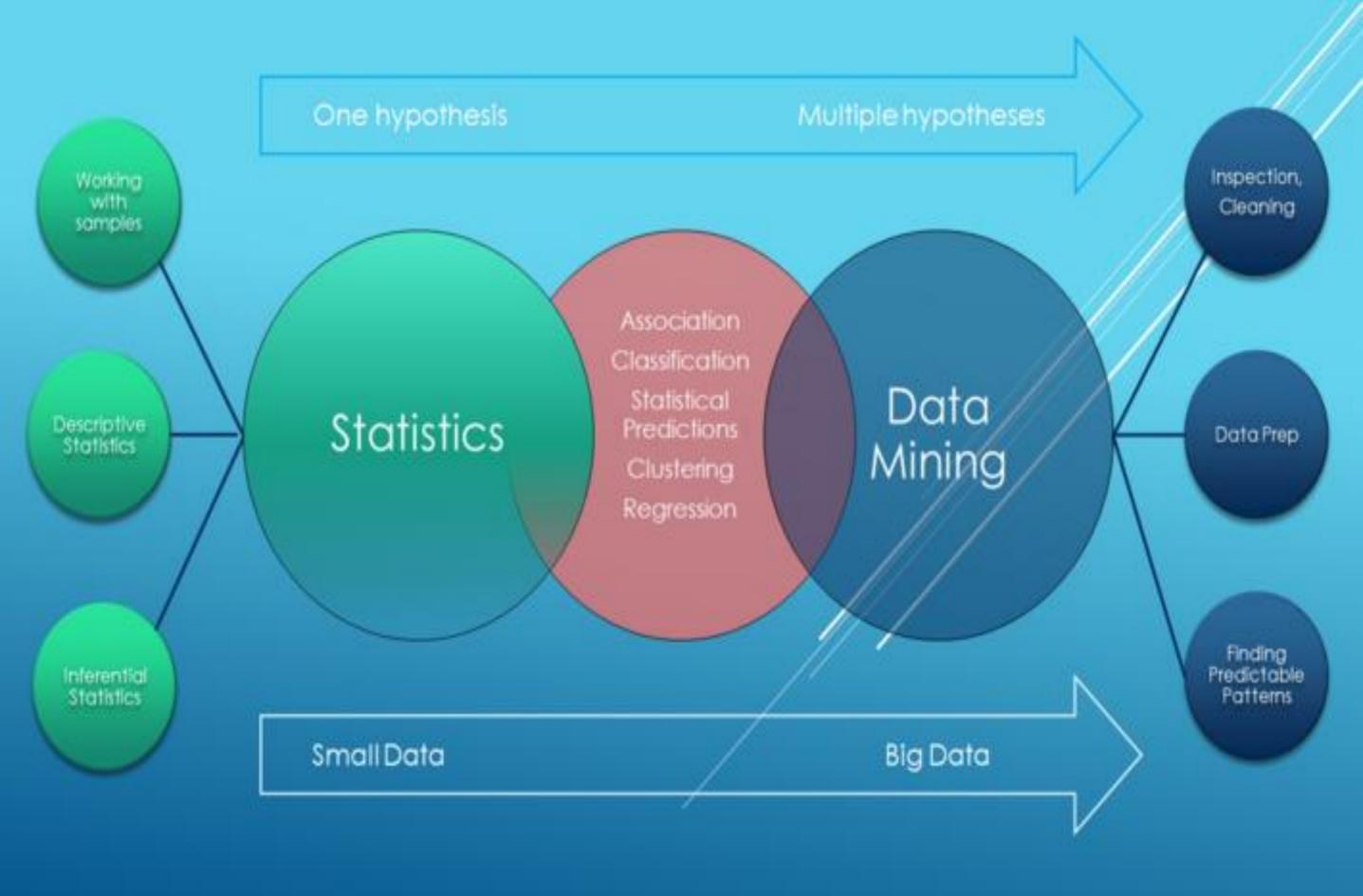
 $P(\frac{\text{Dart lands in both}}{\text{circle} + \text{rectangle}}) \ge P(\frac{\text{Dart lands}}{\text{in circle}}) \times P(\frac{\text{Dart lands}}{\text{in rectangle}})$ 

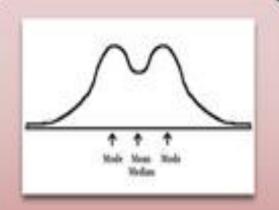
... in multivariate statistics: Consider a sample of people's weights and heights plotted on x-y axes. Because these variables are correlated, the odds that someone's weight and height will both fall within a combined range is greater than or equal to the product of the independent odds of falling in each range. (The general inequality holds for any number of variables.)



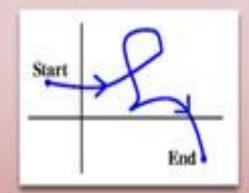
 $\begin{array}{c} \text{Person has both} \\ \text{normal weight} + \text{height} \end{array} \ge \begin{array}{c} \text{Person has} \\ \text{normal weight} \end{array} \times \begin{array}{c} \text{Person has} \\ \text{normal height} \end{array}$ 

	Overview	Process	Subtypes	Examples
Supervised Learning	Majority of algorithms.  Machine is trained  using well-labeled  data; inputs and outputs are matched.	Mapping function takes inputs and matches to outputs, creating a target function.	Classification, Regression	Linear regression, Random forest, SVM.
Unsupervised Learning	Unlabeled data (inputs only) is analyzed. Learning happens without supervision.	Inputs are used to create a model of the data.	Clustering, Association.	PCA, k-Means, Hierarchical clustering.
Semi supervised	Some data is labeled, some not. Goal: better results than labeled data alone. Good for real world data.	Combination of above processes.	All the above.	Self training, Mixture models, Semi-supervised SVM

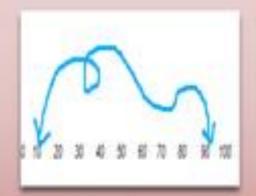




Central Tendency Mean, Median, Mode, Outliers

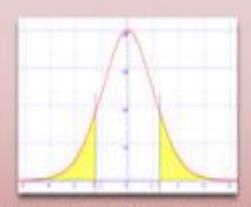


Measures of Spread Range, Standard deviation, Variance, Quartiles



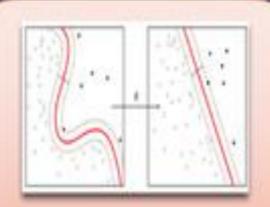
Position of data, percentile rank, percentile range

Percentiles



Probability Distributions: Uniform, normal (Gaussian), Poisson

### Basic Probability and Statistics



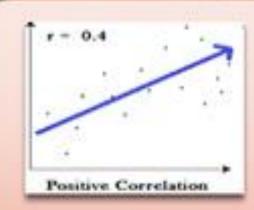
Dimensionality reduction Pruning, PCA



SRS, Reservoir, Undersampling, Oversampling,

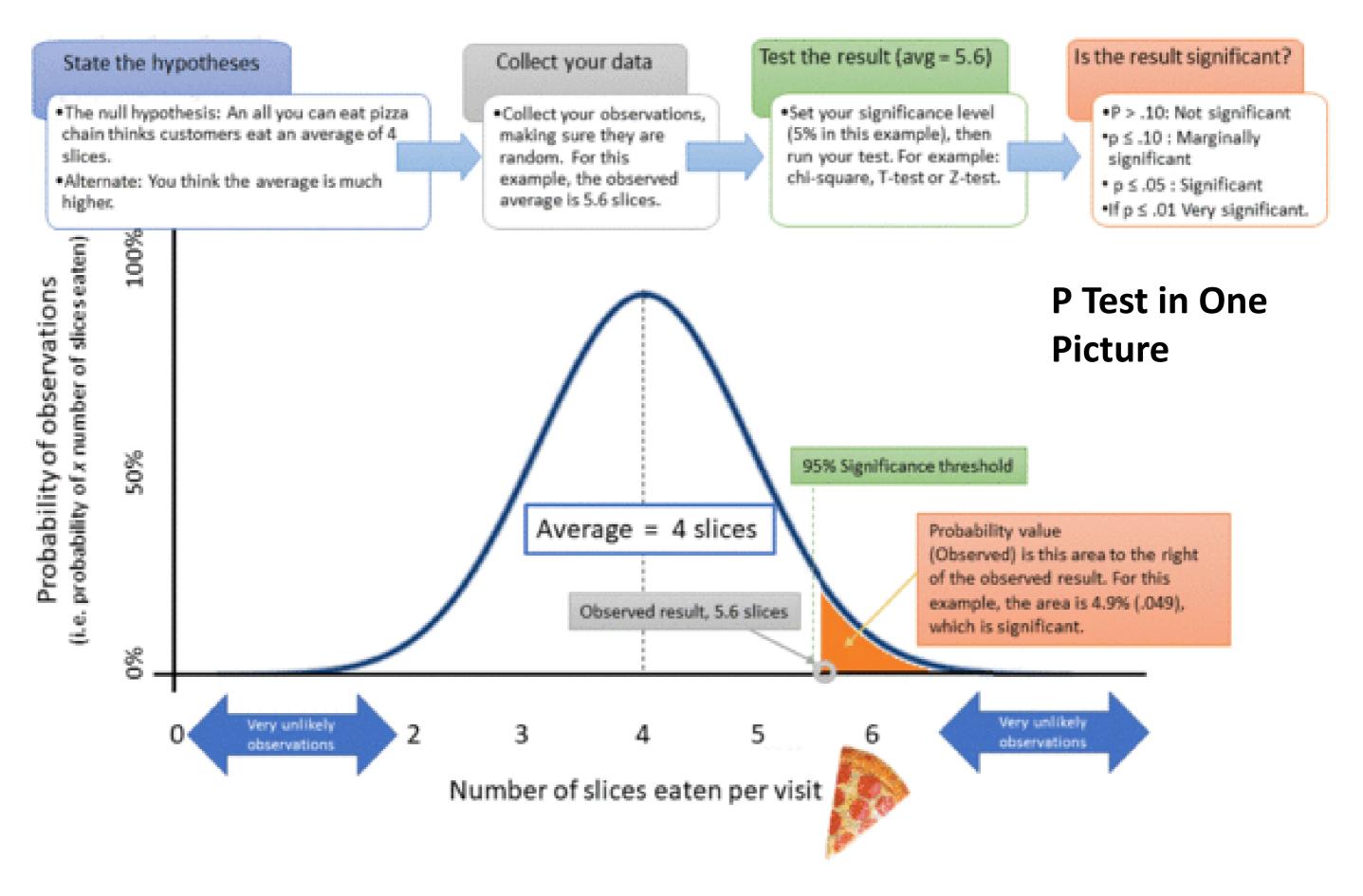
$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

Measuring belief or confidence



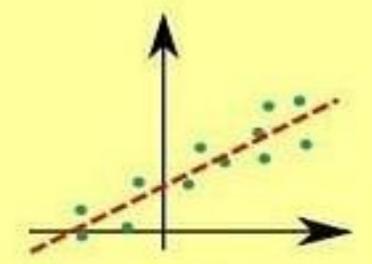
Covariance & correlation How data is related

More Advanced Probability and Statistics



### LINEAR REGRESSION

- Econometric modelling
- Marketing Mix Model
- Customer Lifetime Value



### Continuous ⇒ Continuous

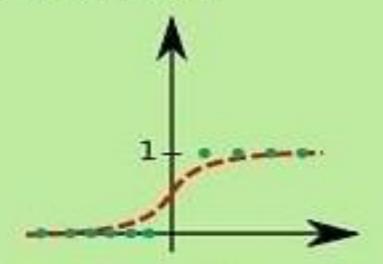
$$y = \alpha_0 + \sum_{i=1}^{N} \alpha_i x_i$$

 $Im(y \sim x1 + x2, data)$ 

1 unit increase in x increases y by α

### LOGISTIC REGRESSION

- Customer Choice Model
- Click-through Rate
- Conversion Rate
- O Credit Scoring



### Continuous ⇒ True/False

$$y = \frac{1}{1 + e^{-z}}$$

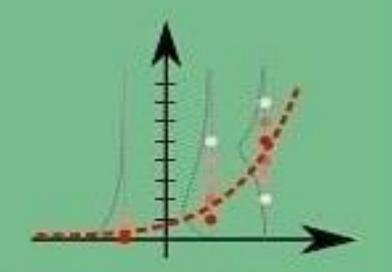
$$z = \alpha_0 + \sum_{i=1}^{N} \alpha_i x_i$$

glm(y ~ x1 + x2, data, family=binomial())

1 unit increase in x increases log odds by α

### POISSON REGRESSION

- Number of orders in lifetime
- Number of visits per user



Continuous ⇒ 0,1,2,...

$$y \sim Poisson(\lambda)$$
$$ln\lambda = \alpha_0 + \sum_{i=1}^{N} \alpha_i x_i$$

glm(y ~ x1 + x2, data, family=poisson())

1 unit increase in x multiplies y by e<sup>α</sup>

# Differences Between Pearson Correlation and Linear Regression

Correlation

Use when...

You want to know if there's an association between two variables.

Results

Strength & direction of relationship (r):

 -1 = perfect negative,

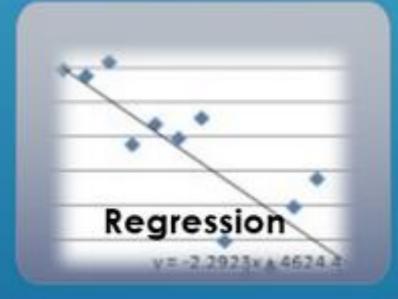
+1. = perfect positive,

0 = no correlation.

Assumptions (Requirements)

Validity: Valid measurements, a good sample, unconfounded comparisons.

Distribution: Linear relationship between the two.



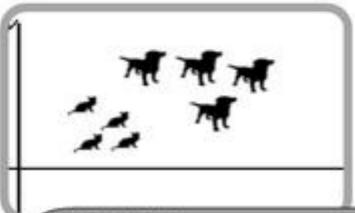
You want to predict how one variable will change with another.

Estimates of parameters for a regression equation:

The B0 and B1 in the linear regression equation Y = B0 + B1 \* X All the above, plus:

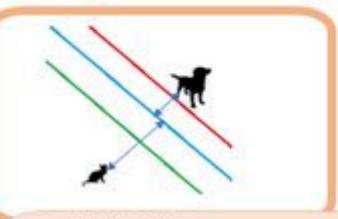
- Quantitative Data
- 2. Outlier Condition
- Independence of Errors
- 4. Homoscedasticity
- Normality of Error Distribution

### **SVM** in One Picture



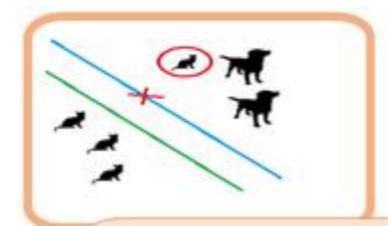
#### 1. Plot the features

- Plot in n-dimensional space (n = number of features). For this example, we have 2 features cats and dogs—so n = 2 (2 dimensional)
- Value of each feature (dogs and cats) = value of coordinate



#### 3a. Consider the Margins.

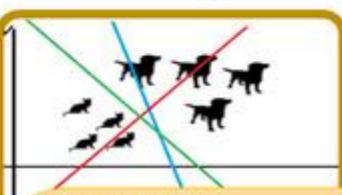
- A margin is the distance between any point and the hyperplane. The points touching this boundary are the Support Vectors (in this simple example, the dog and cat shown are the support vectors).
- Here, the blue line maximizes the distance, so it is the "best".



#### 3b. Look out for Misclassification

- SVM will consider misclassification first.
- If the "best" (blue) results in misclassification, the hyperplane is discarded in favor of one that classifies correctly, but with a less-optimal margin (green).

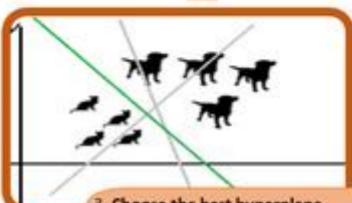




#### 2. Draw the hyperplanes

- The hyperplanes are the possible "best" boundaries to separate features (in this case, cats and dogs).
- Consider all hyperplanes. Here, I plotted 3 for simplicity. In reality, you could have an infinite number of choices!

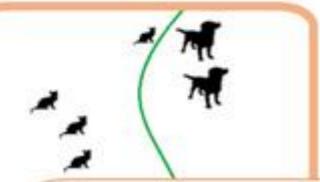




#### 3. Choose the best hyperplane

- In this example, the best hyperplane is the green one, which clearly separates cats and dogs.
- Take into consideration margins, misclassification, and curved/linear possibilities when making your choice.

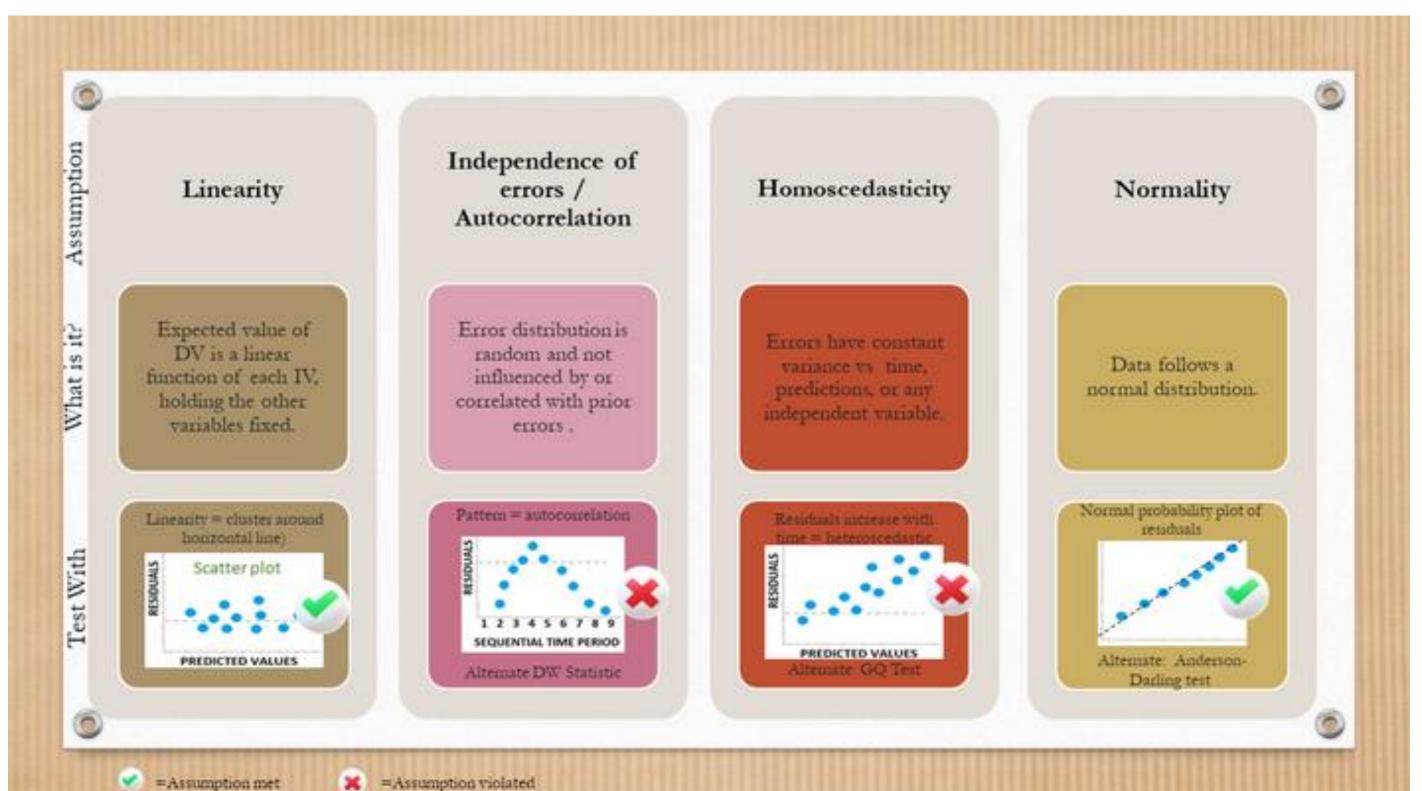




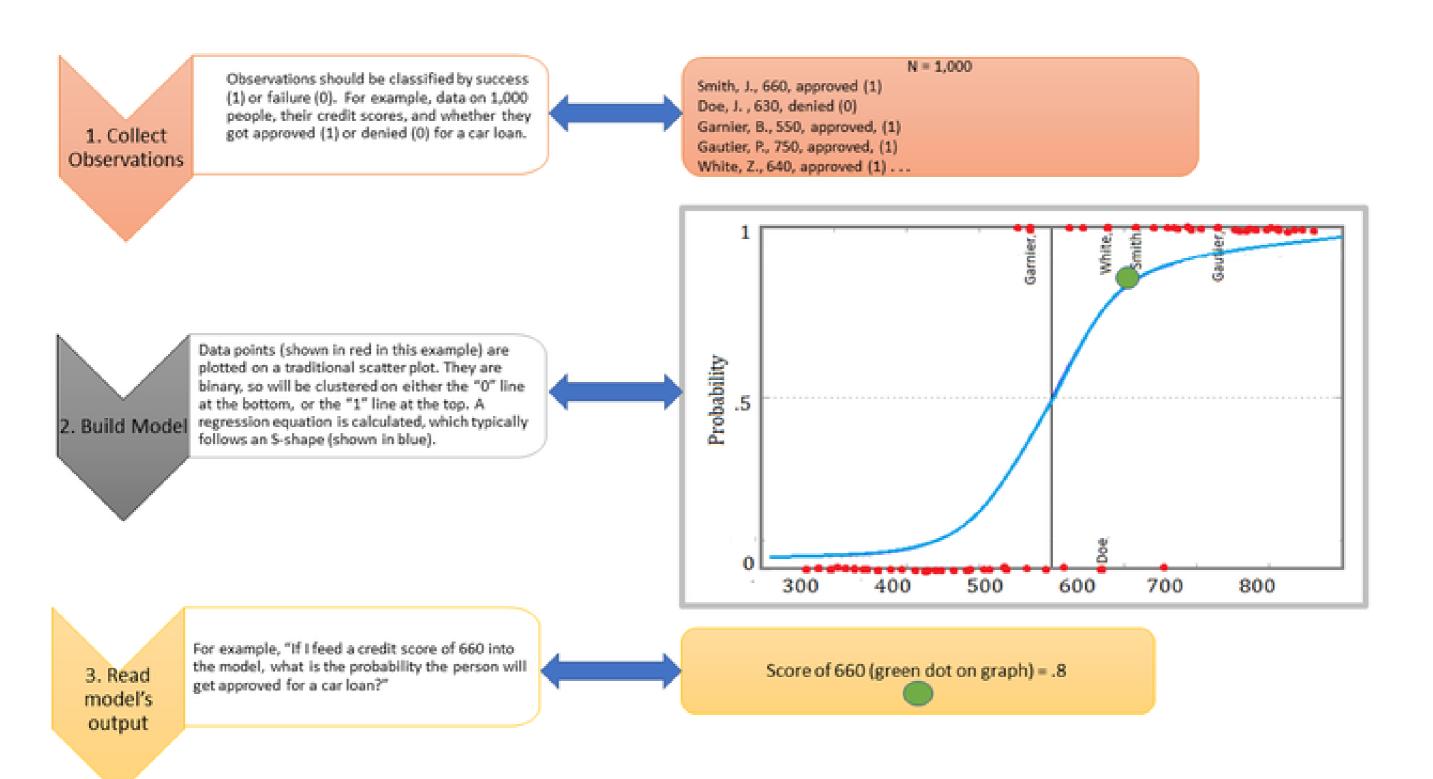
#### 3c. Curved or Linear?

- The best choice might not be a straight line; It may be a curved one.
- SVM considers all possible hyperplanes (straight and curved) before choosing.

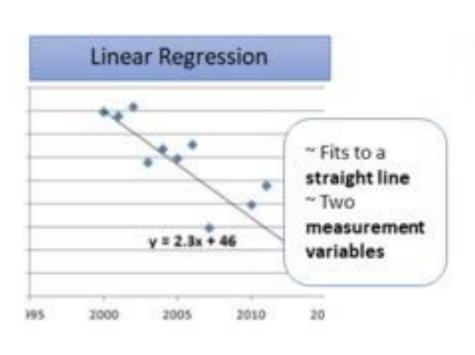
# Assumption of Logistic Regression in One Picture

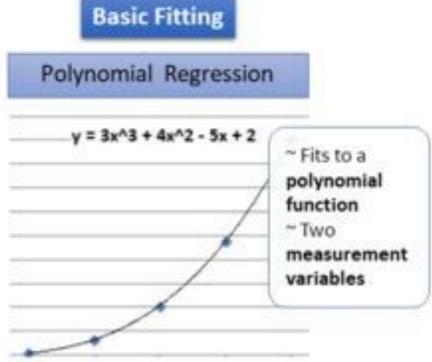


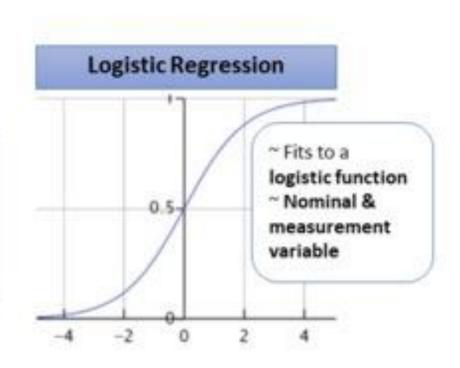
# **Logistic Regression in One Picture**

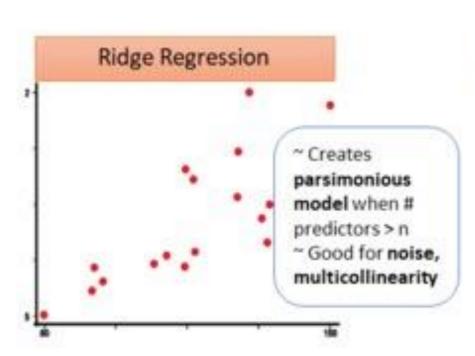


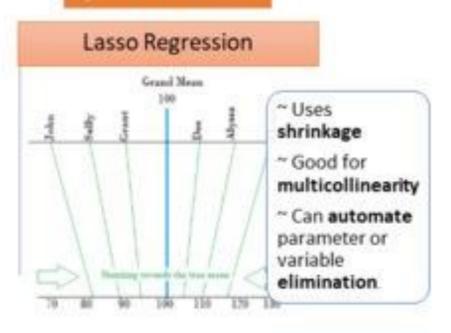
# **Regression Analysis in One Picture**



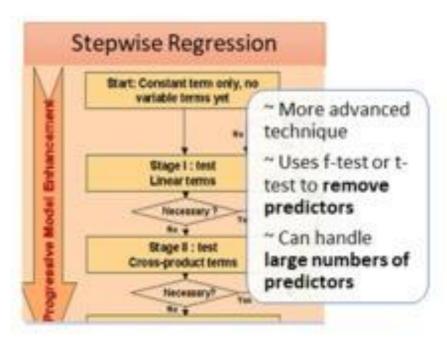






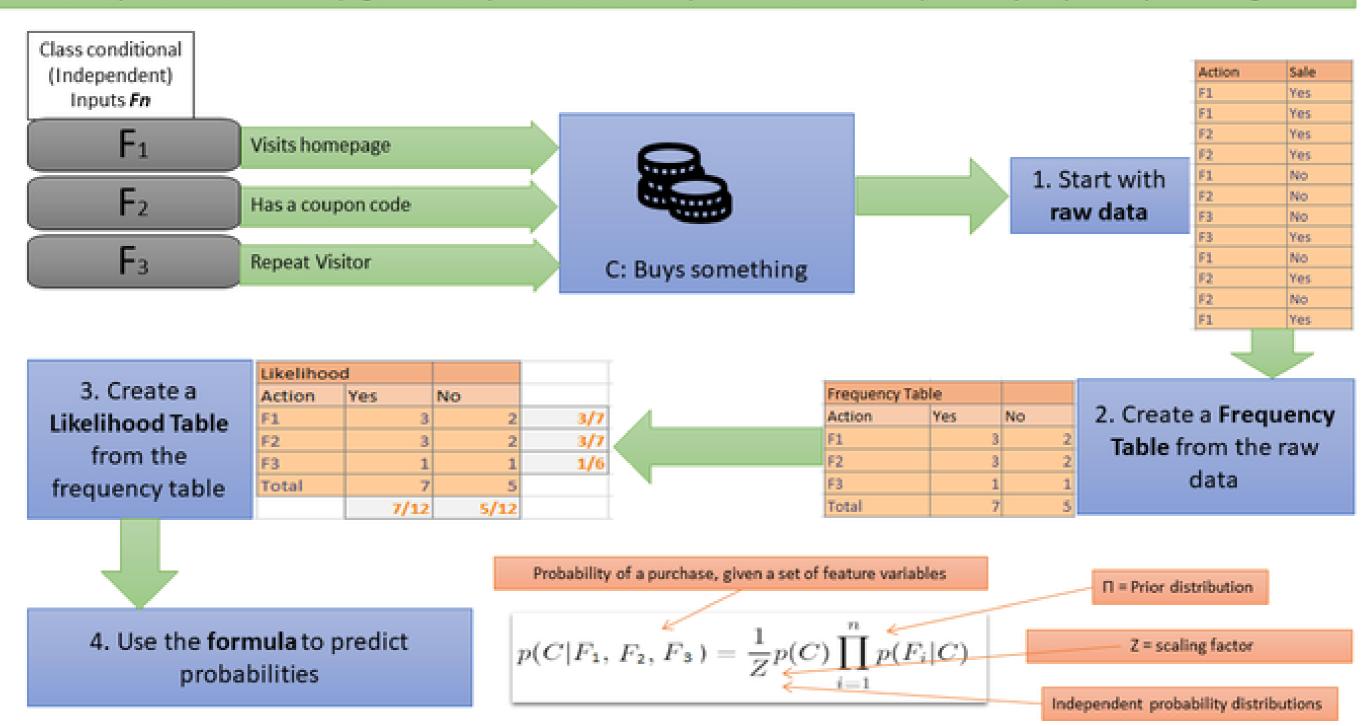


**Special Situations** 

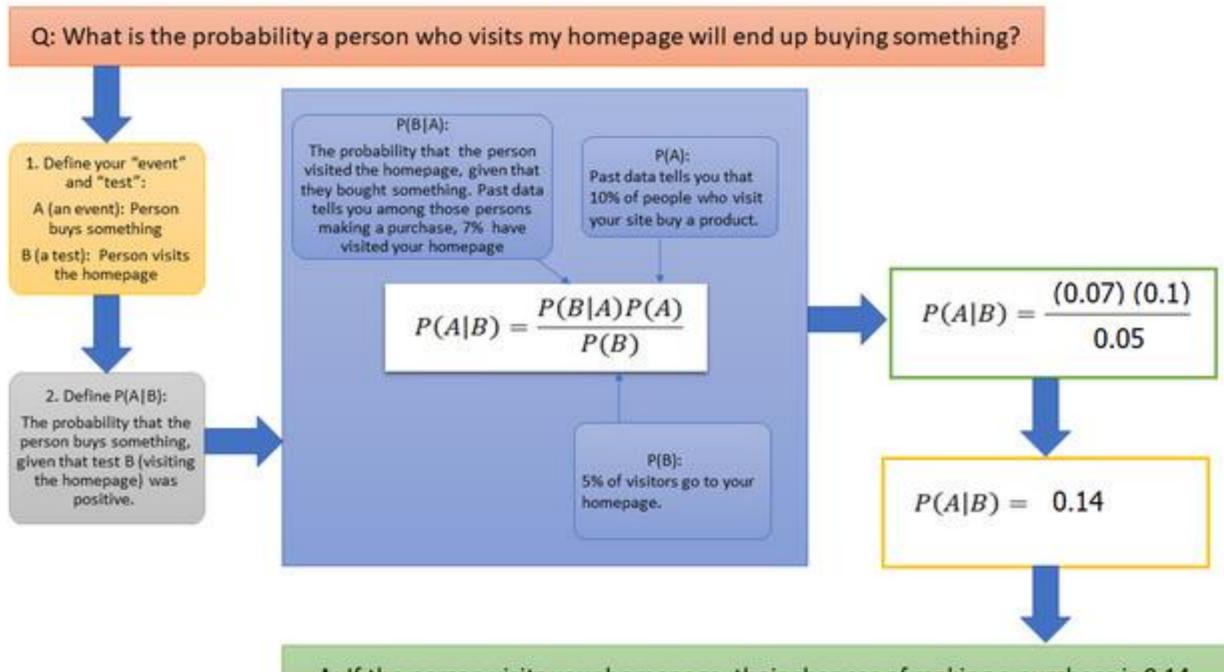


# **Naïve Bayes in One Picture**

Q. If a person visits the homepage, has a coupon code, and is a repeat visitor, what is the probability they will buy something?

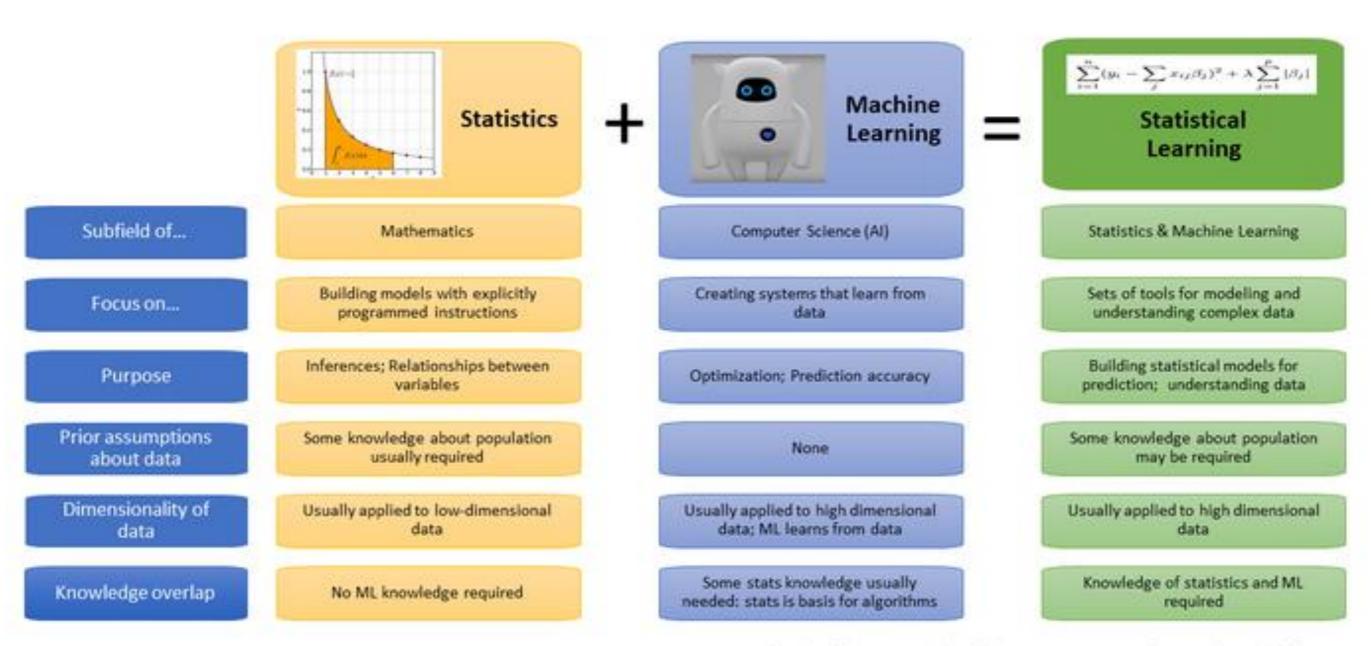


## **Bayes Theorem in One Picture**

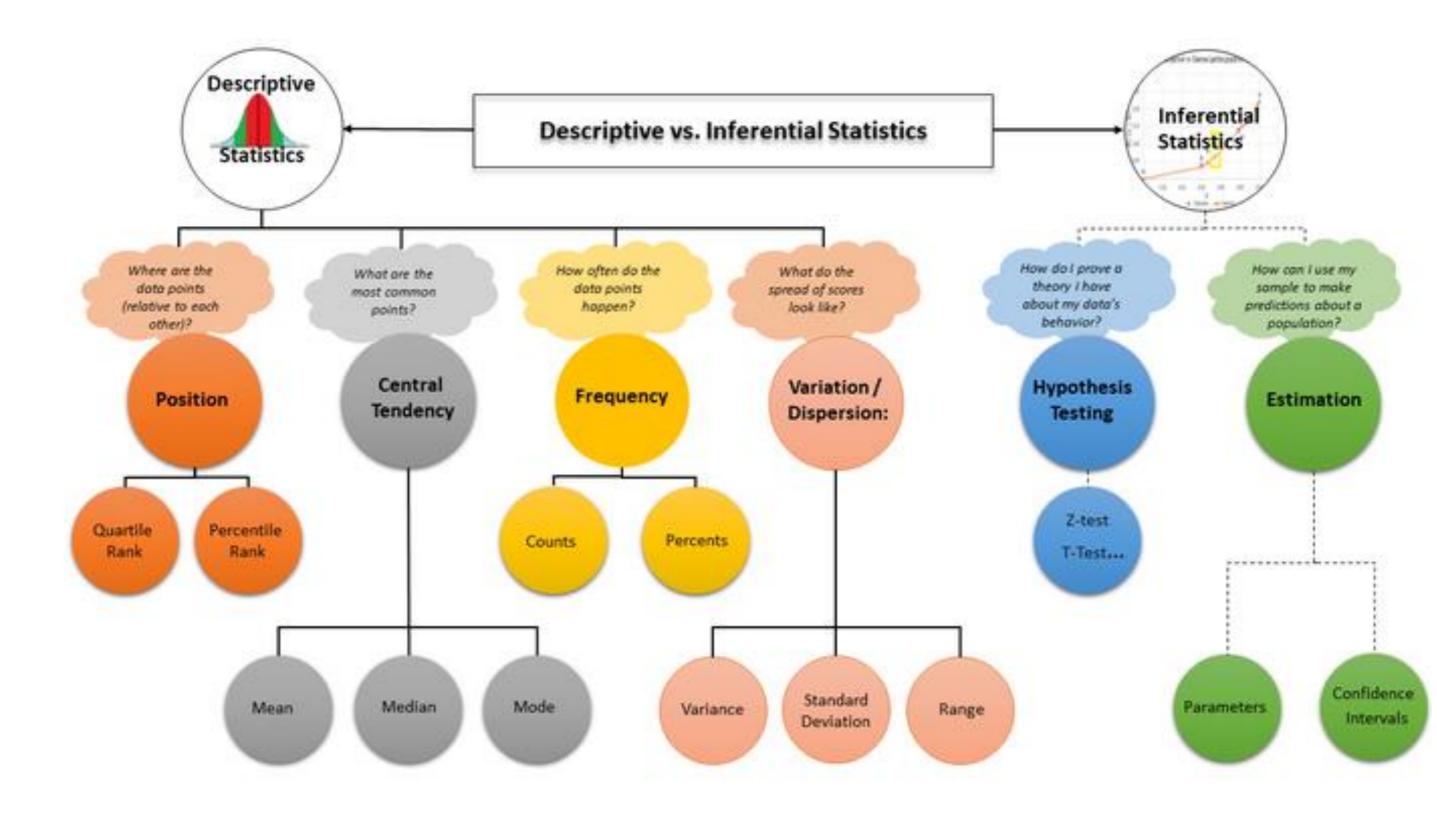


A: If the person visits your homepage, their chances of making a purchase is 0.14 (14%). This is a slight increase from the 10% suggested by past data.

# Statistics and Machine learning In One Picture



Musio image: Akawikipic [CC BY-SA 4.0 (https://creativecommons.org/licenses/by-sa/4.0)]

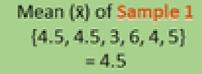


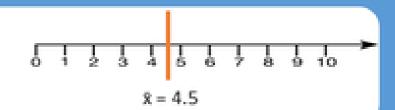
### Standard Deviation vs. Standard Error

### Standard Deviation with One Set of Measurements

#### Step 1: Find the Mean

(What is the Average Value?)





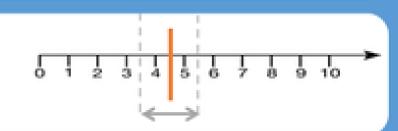
#### Step 2: Find the Standard Deviation

(What does the spread of data look like?)

#### Standard Deviation of Sample 1

= 1

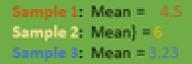
(This tells you the bulk of the scores are one standard deviation either side of the mean)

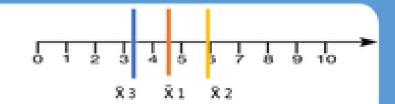


### Standard Error with Multiple Sets of Measurements

#### Step 1:

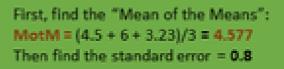
Find the Means for each separate sample

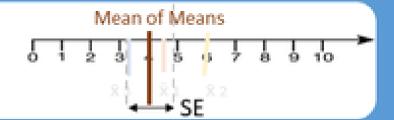




#### Step 2: Find the Standard Error

(aka the Standard Deviation for the average mean)



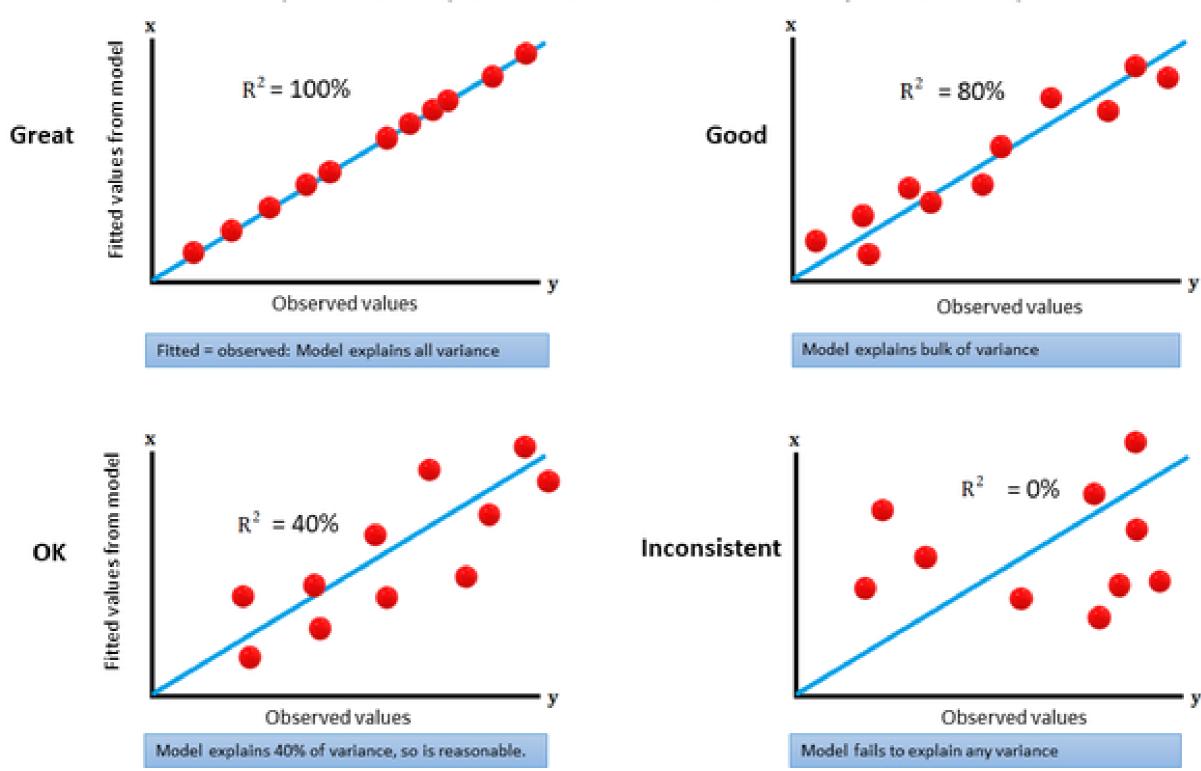


# **Correlation Coefficients in One Picture**

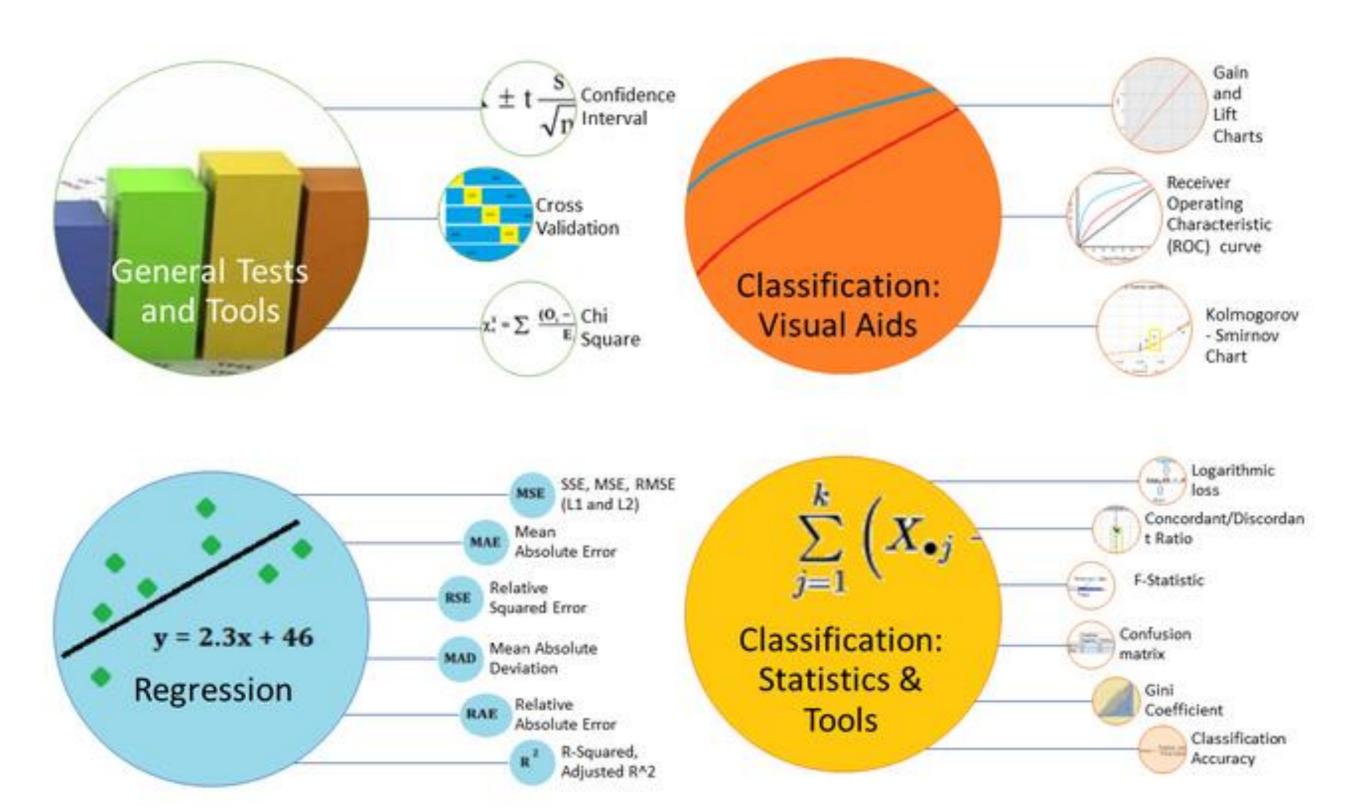
	Pearson's	Spearman's Rank	Kendall's Tau	Gamma	Yule's Q
Relationships evaluated	Linear	Monotonic	Monotonic	Monotonic	Monotonic
Parametric or Non Parametric	Parametric	Non Parametric	Non Parametric	Non Parametric	Non Parametric
Input variables	Continuous	Continuous, ordinal, or ratio	Ordinal	Ordinal	Ordinal (2x2)
Advantages	Easy to use and understand Widely available	Normal distribution not required Widely available	Insensitive to errors  More accurate p-value for smaller samples than Spearman's	Good for tied ranks  Not affected much by outliers	Simplified version of Gamma for 2x2 table
1/2					

# **R-Square metrics in One Picture**

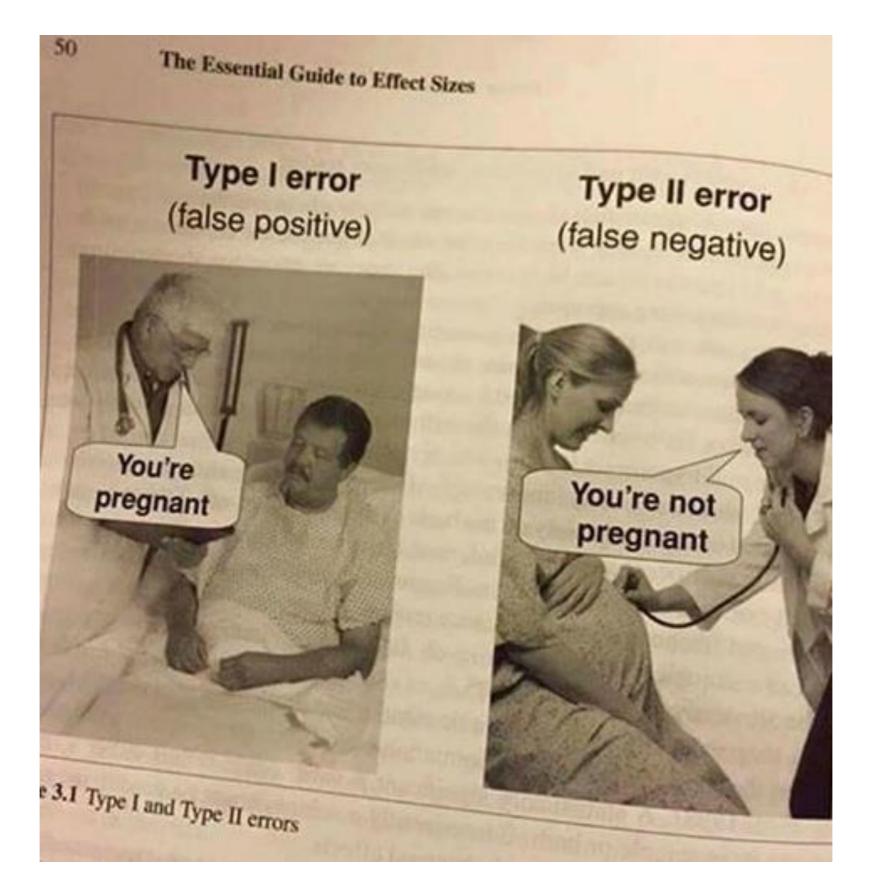
Comparison of R-Squared for Different Linear Models (Same Data Set)



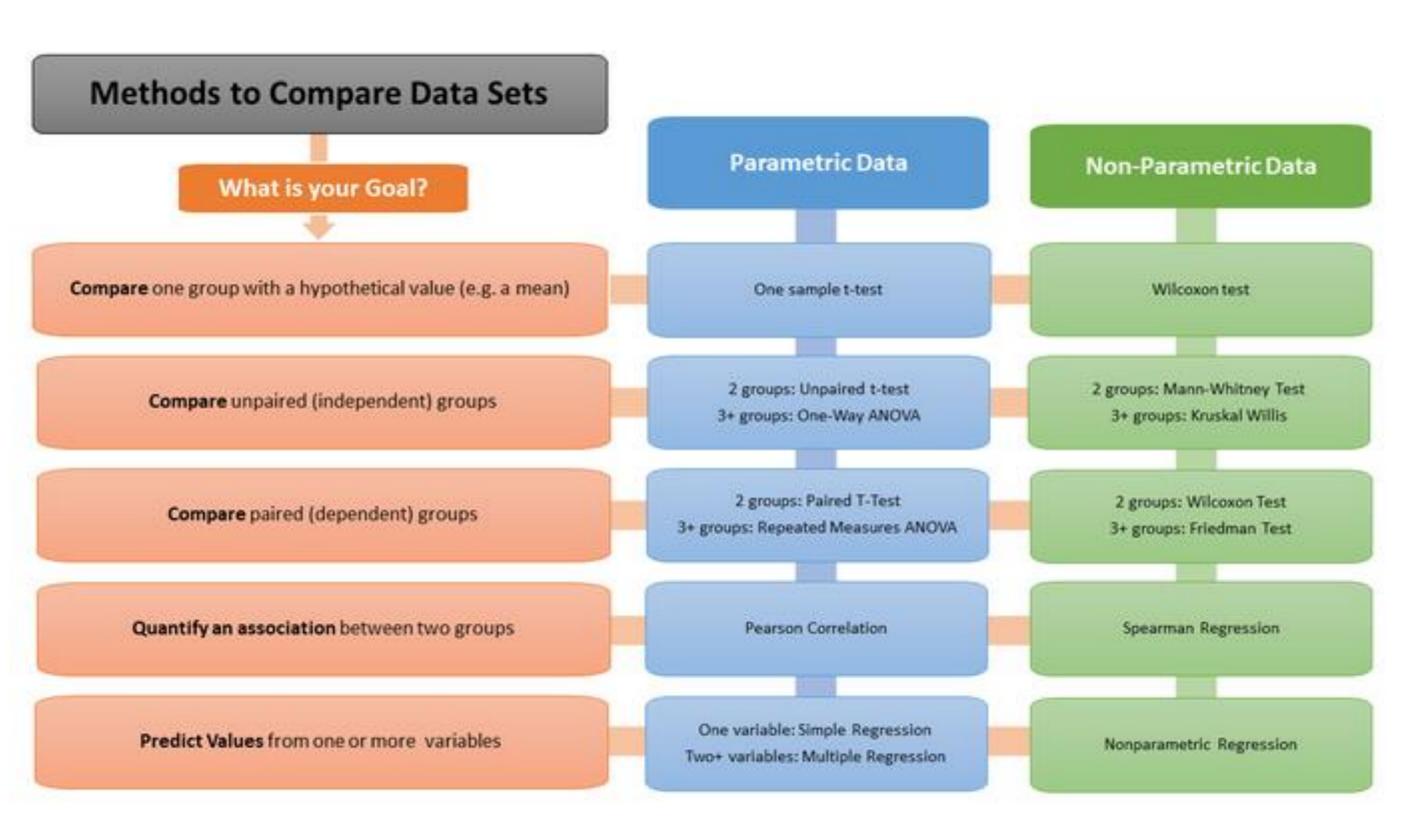
### **Evaluation metrics in One Picture**



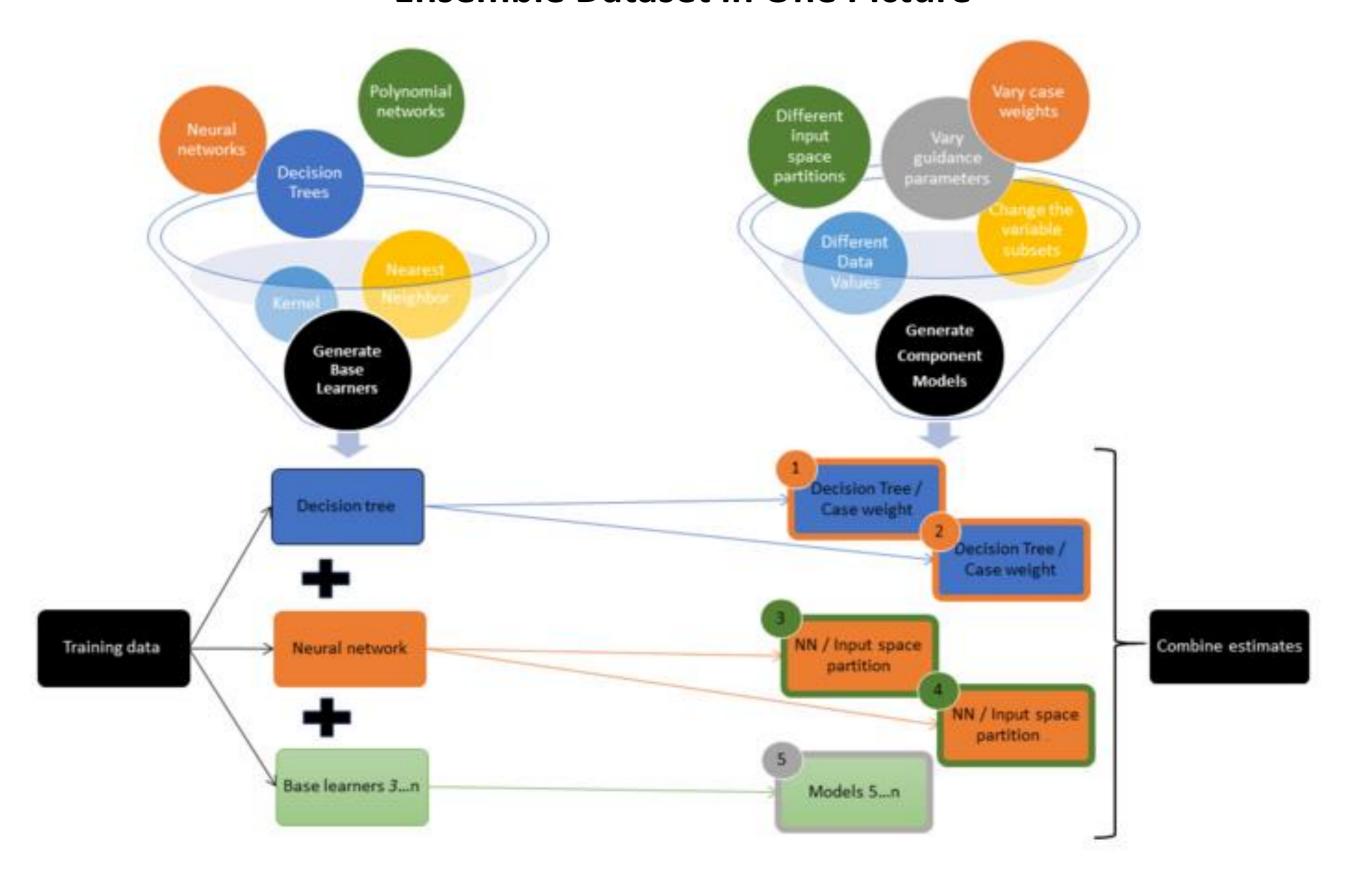
# Type-I and Type-II in One Picture



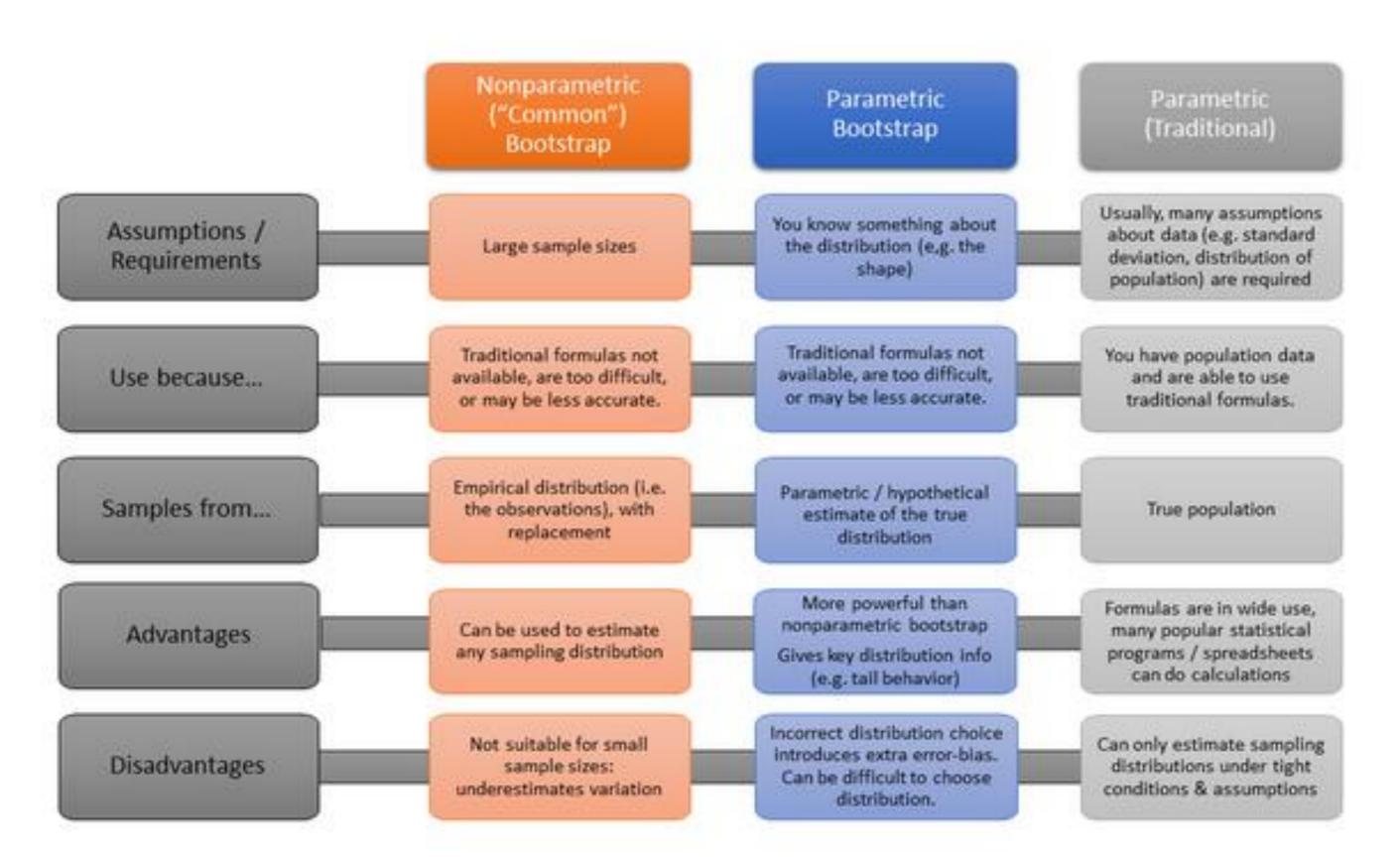
## **Comparing Dataset in One Picture**



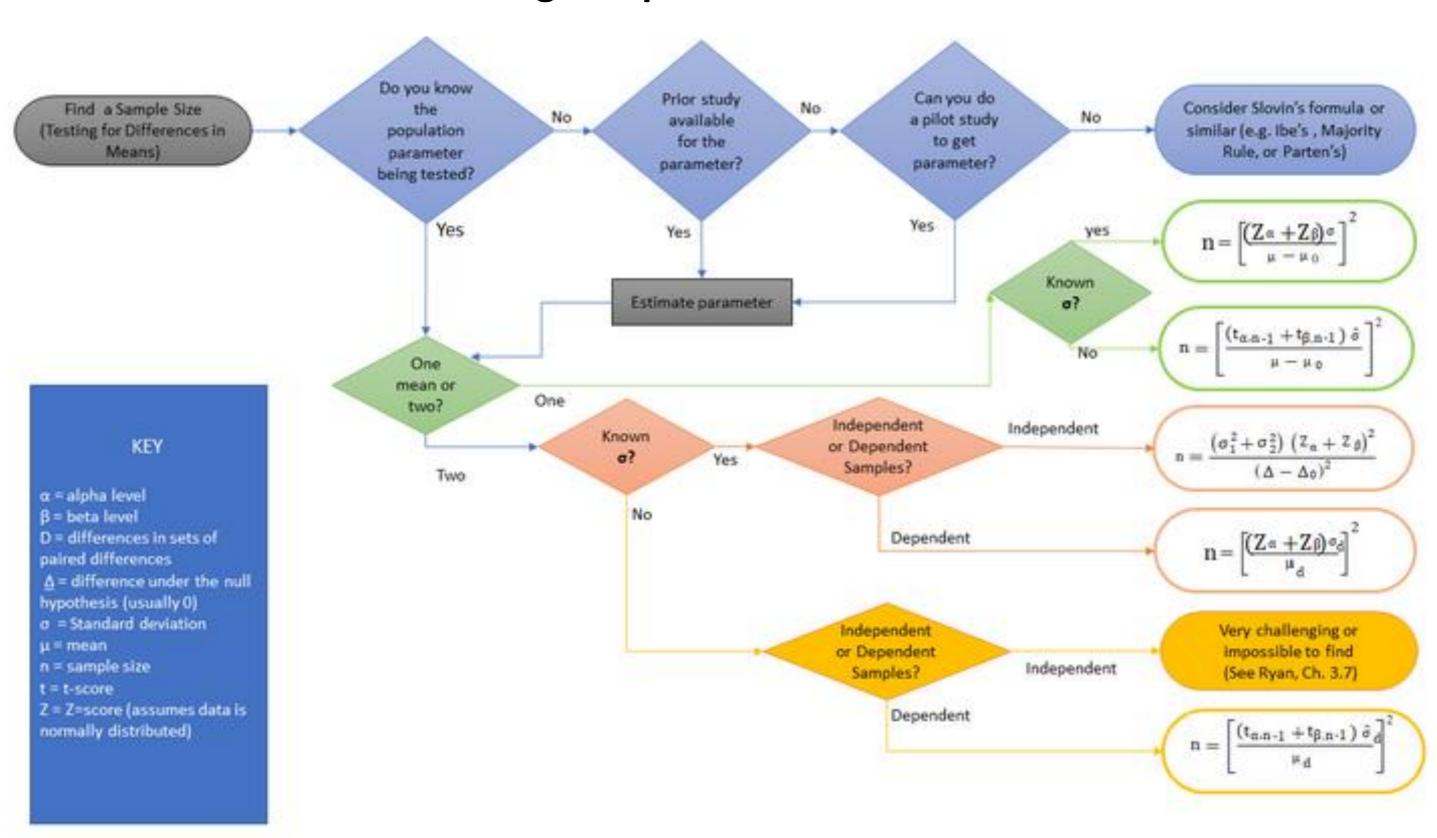
### **Ensemble Dataset in One Picture**



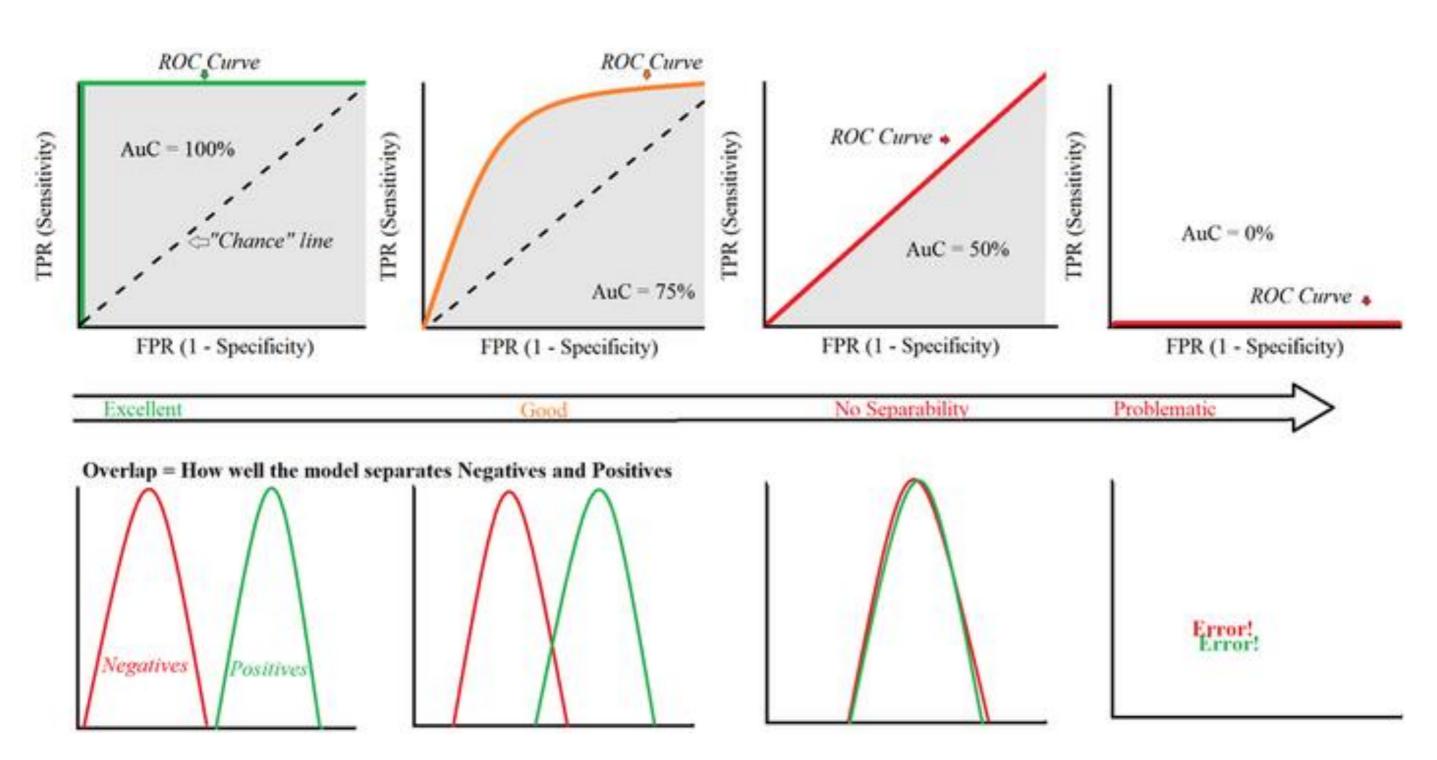
### Parametric and Non-Parametric in One Picture



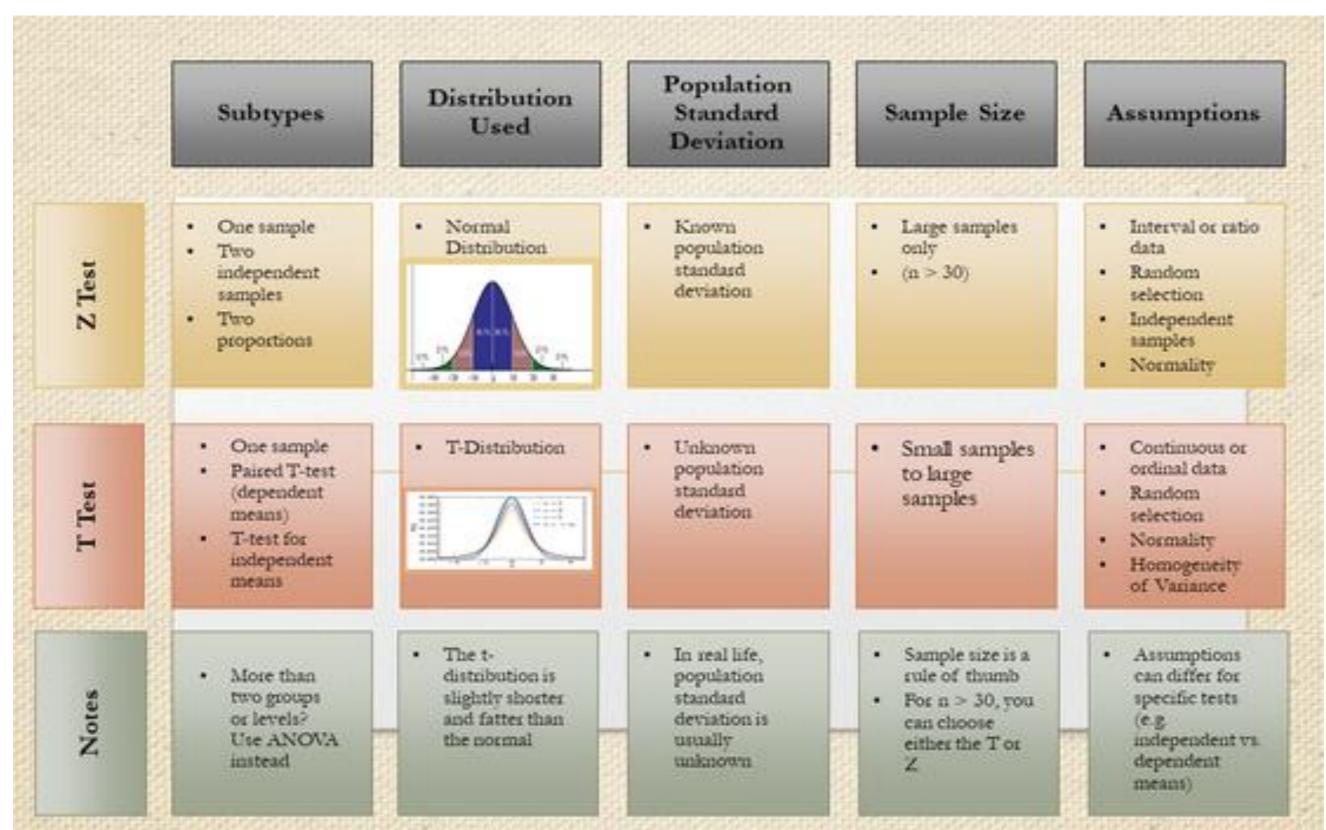
# **Determining Sample Size in One Picture**



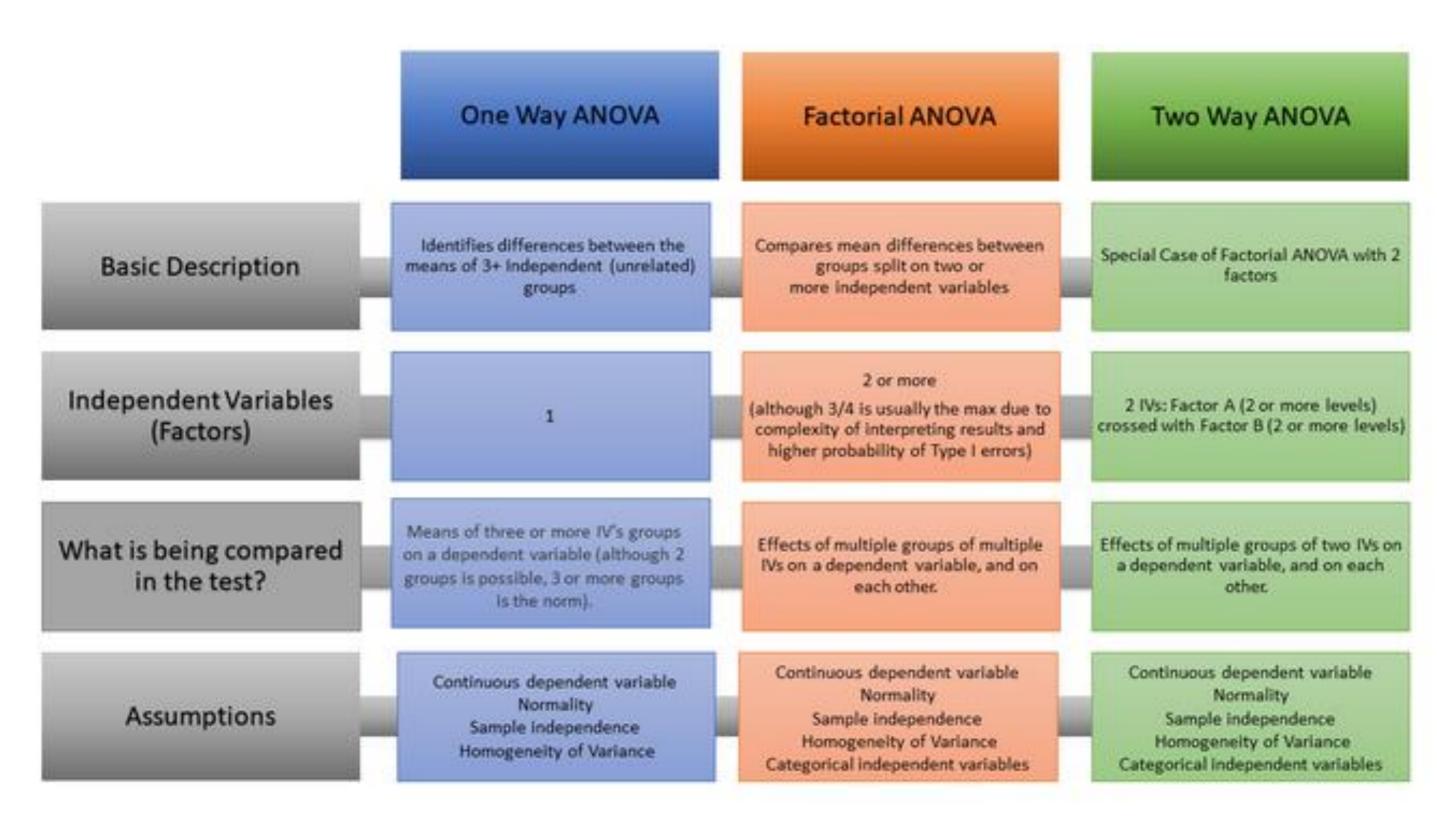
### **ROC CURVE in One Picture**



### **Z-test and T-test in One Picture**



#### **Anova in One Picture**

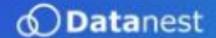


## **Predictive Analytics in One Picture**

Technique	Purpose	Advantages / Disadvantages	What questions can be answered?	
Decision Trees	Predict future classes of data.	Advantages: Easy to implement and understand.  Disadvantage: Can be overly simplistic for many problems.	"Which one" (i.e. one discrete variable) or answers to Yes/No questions.	
Neural Networks	Cluster and classify by recognizing patterns in data.	Advantage: Outperforms most ML algorithms.  Disadvantages: Tough to implement; requires parallel processor.	Pretty much any question (as long as there's sufficient data and some kind of correlation/causation)	
Regression (Linear and Logistic)	Estimates relationships between variables, uses those to predict future outcomes.	Advantage: Results are easy to understand.  Disadvantage: Limited to linear/logistic data.	How much or how many of a certain target variable?	
Time Series	Forecasts continuous variables over time.	Advantage: Easy to understand results.  Disadvantage: Limited to time-dependent data.	What is the result going to be at a future data?	
Clustering (K-means)	Organization of data into similar groups.	Advantage: Easy to implement. Disadvantage: Can be hard to predict "k", the number of clusters.	What kinds of patterns are in the data?	
Factor Analysis	Find explanations for outcomes / correlations.	Advantage: Reduction of data to concise "picture".  Disadvantage: Factors can be hard to interpret; Information can be lost.	What are the explanations for the themes in the data?	

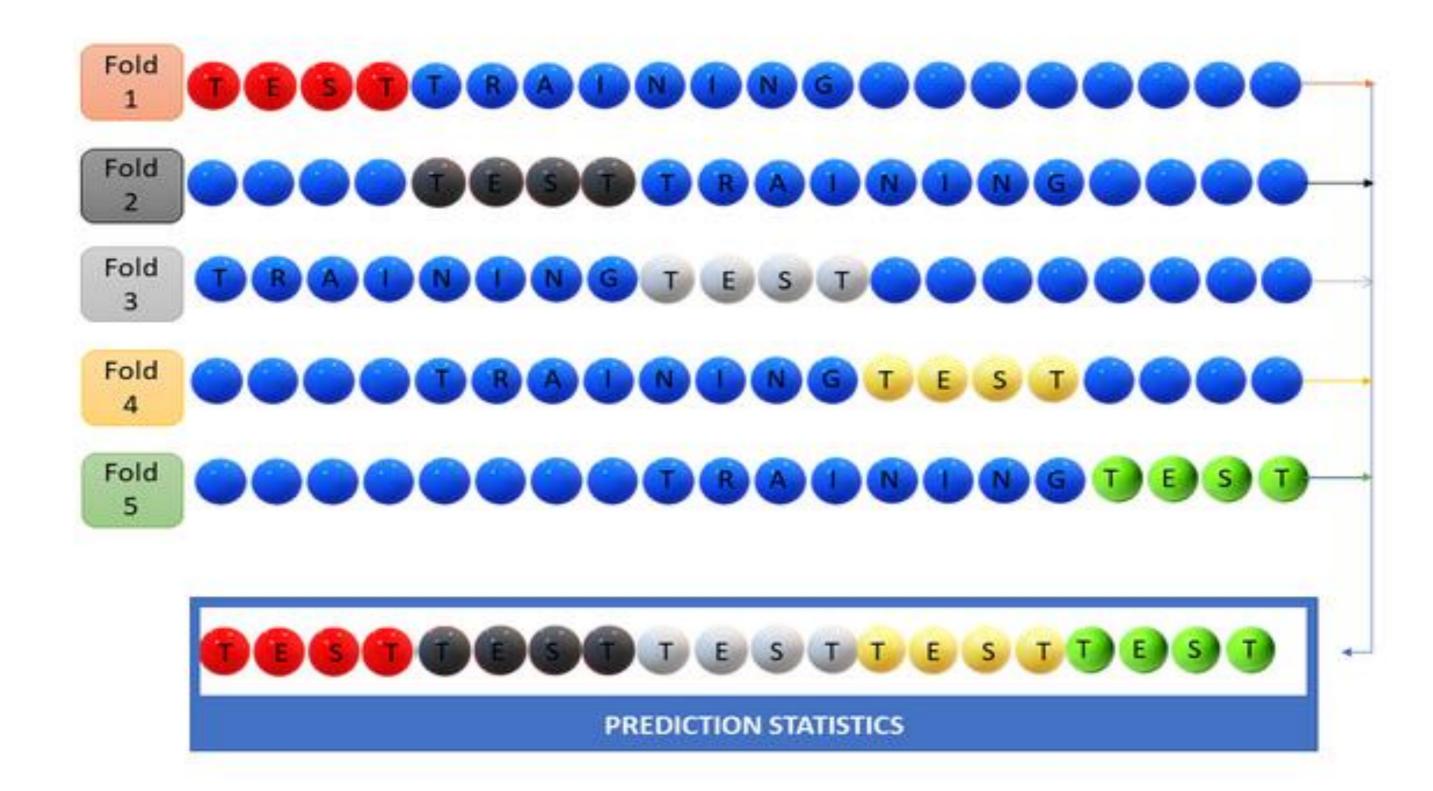
#### **Time Series Method in One Picture**

#### **List of Time Series Method**

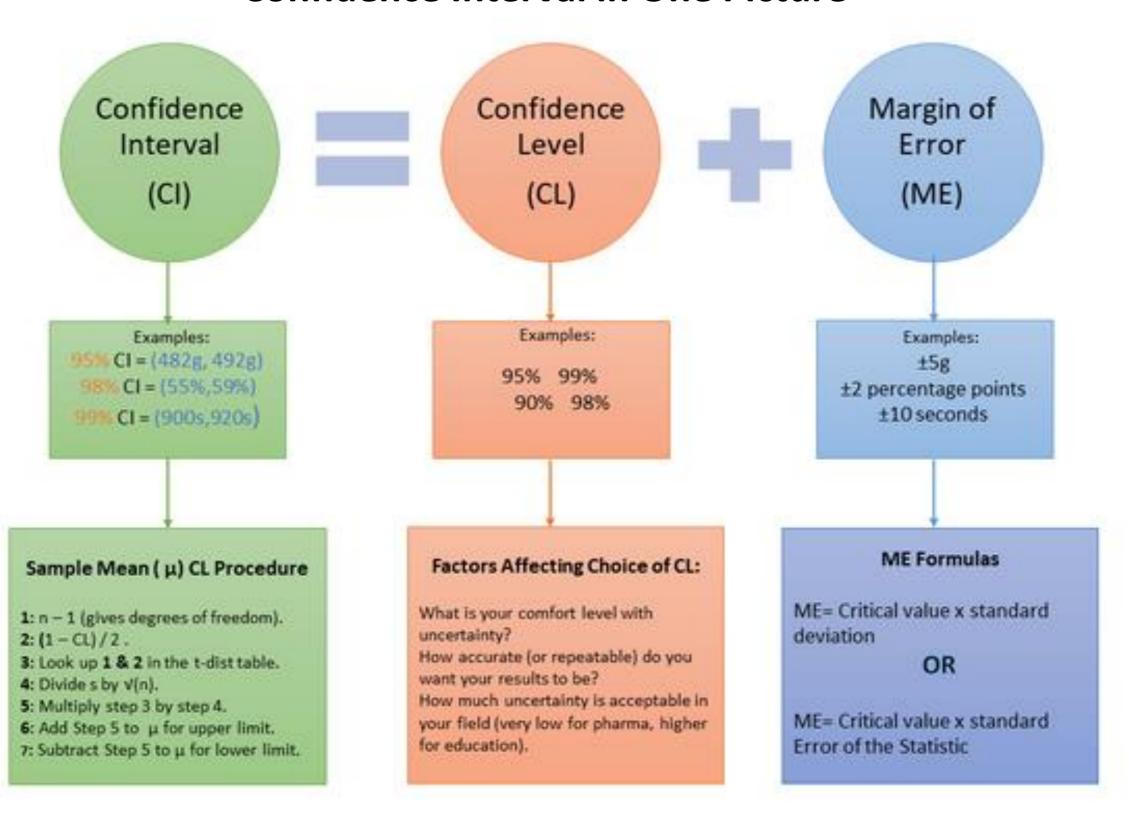


- 1. Autoregression (AR)
- Moving Average (MA)
- Autoregressive Moving Average (ARMA)
- Autoregressive Integrated Moving Average (ARIMA)
- Seasonal Autoregressive Integrated Moving-Average (SARIMA)
- Seasonal Autoregressive Integrated Moving-Average with Exogenous Regressors (SARIMAX)
- Vector Autoregression (VAR)
- 8. Vector Autoregression Moving-Average (VARMA)
- 9. Vector Autoregression Moving-Average with Exogenous Regressors (VARMAX)
- Simple Exponential Smoothing (SES)
- Holt Winter's Exponential Smoothing (HWES)
- 12. Prophet
- Naive method
- 14. LSTM (Long Short Term Memory)
- 15. STAR (Space Time Autoregressive)
- GSTAR (Generalized Space Time Autoregressive)
- LSTAR (Logistic Smooth Transition Autoregressive)
- 18. Transfer Function
- Intervention Method
- 20. Recurrent Neural Network
- Fuzzy Neural Network

#### **Cross Validation in One Picture**



### **Confidence Interval in One Picture**



## **Unsupervised Learning in One Picture**



Type

Overview of process

Disadvantages

Advantages

Works well for

Clustering

Nonhierarchical method that finds mutually exclusive spherical clusters based on distance.

- Requires known "k" clusters; Can be difficult to choose.
- Initial cluster choices and order of data strongly affect results.
- Can be difficult to reproduce results due to random initial "centroid" choice.
- · Easy to implement.
- · Fast (for small k).
- · Clusters can be recalibrated.

Big data; Hyper spherical (e.g. 3D sphere).

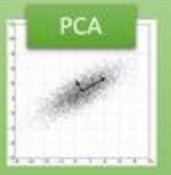


Clustering

Repeatedly links pairs of clusters until every data object is included.

- Initial seeds, data order have strong effect.
- Merges cannot be undone.
- No statistical / theoretical foundation for results.
- Sensitive to outliers.
- Easy to implement.
- Dendogram makes for easy visualization of "k".
- Results easily reproducible.

Small to medium data. Performance and execution time increase dramatically for large data sets.



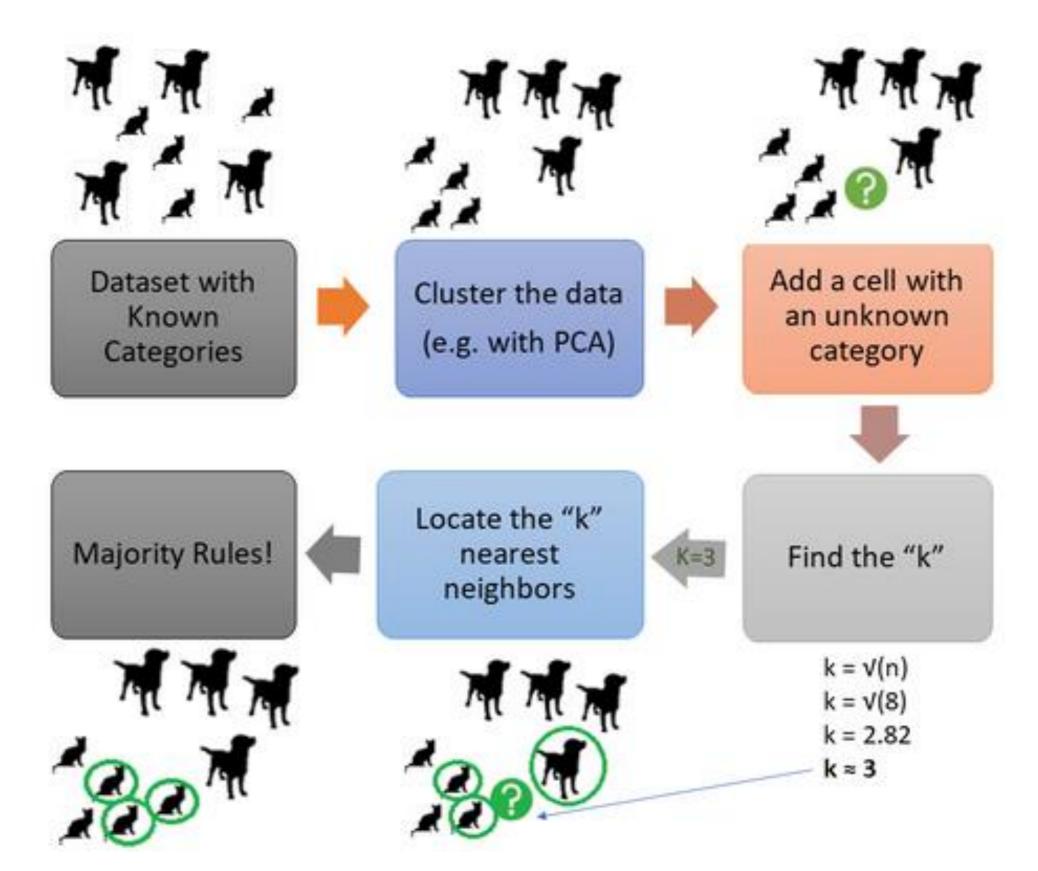
Dimension Reduction

Transforms high dimensional data into low dimensional data using orthogonal transformations.

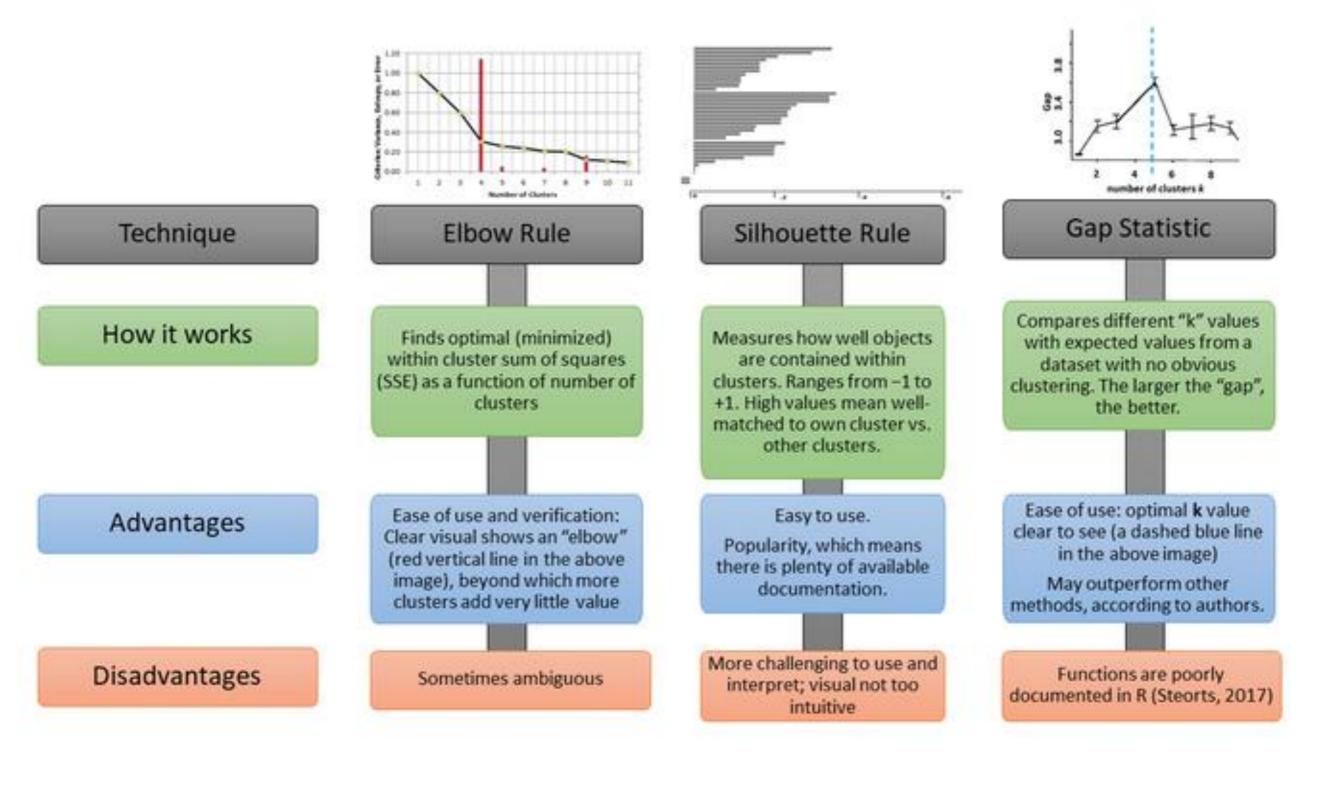
- Principal components (a linear combination of the original features) can be challenging to interpret and read, compared to the original features.
- Data must be standardized beforehand.
- · Good visualization tool.
- Reduces irrelevant or redundant features.
- Reduces overfitting (by reducing features).

Extracting important features (components) from big data.

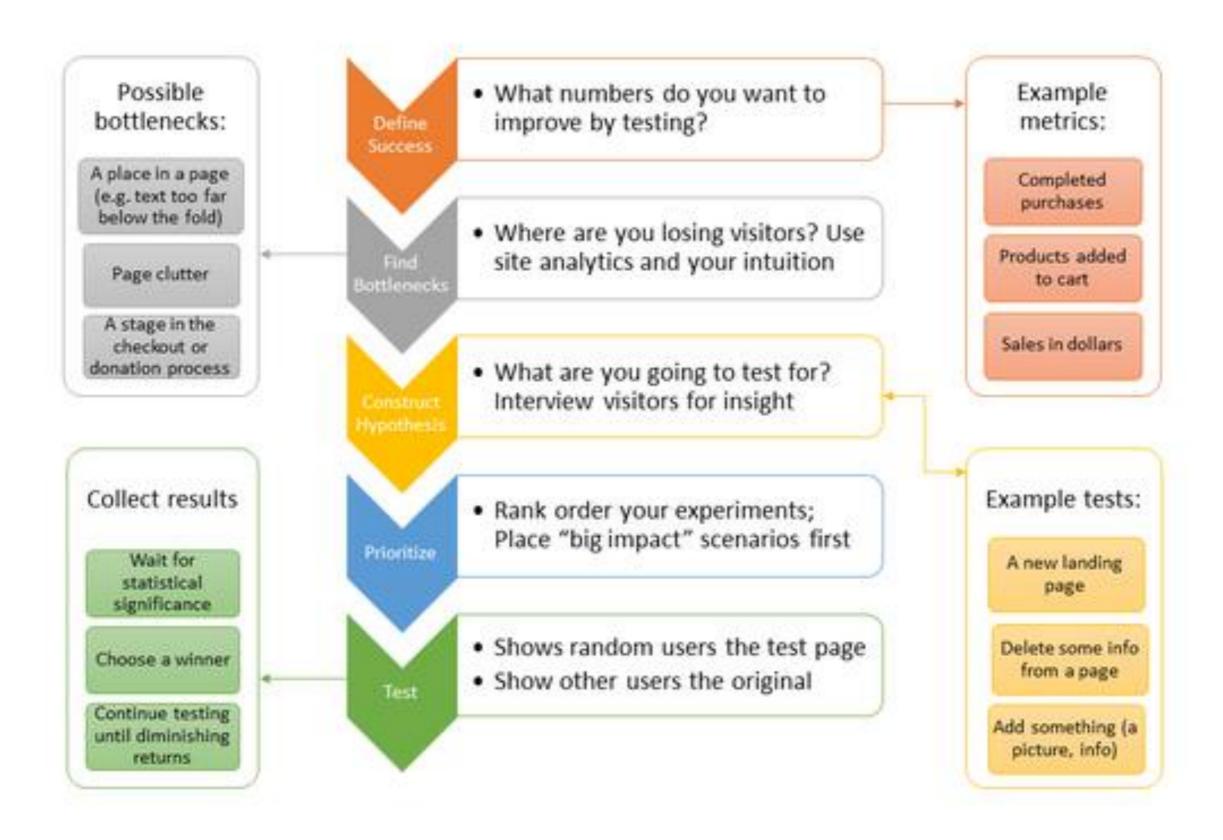
## **KNN** in One Picture



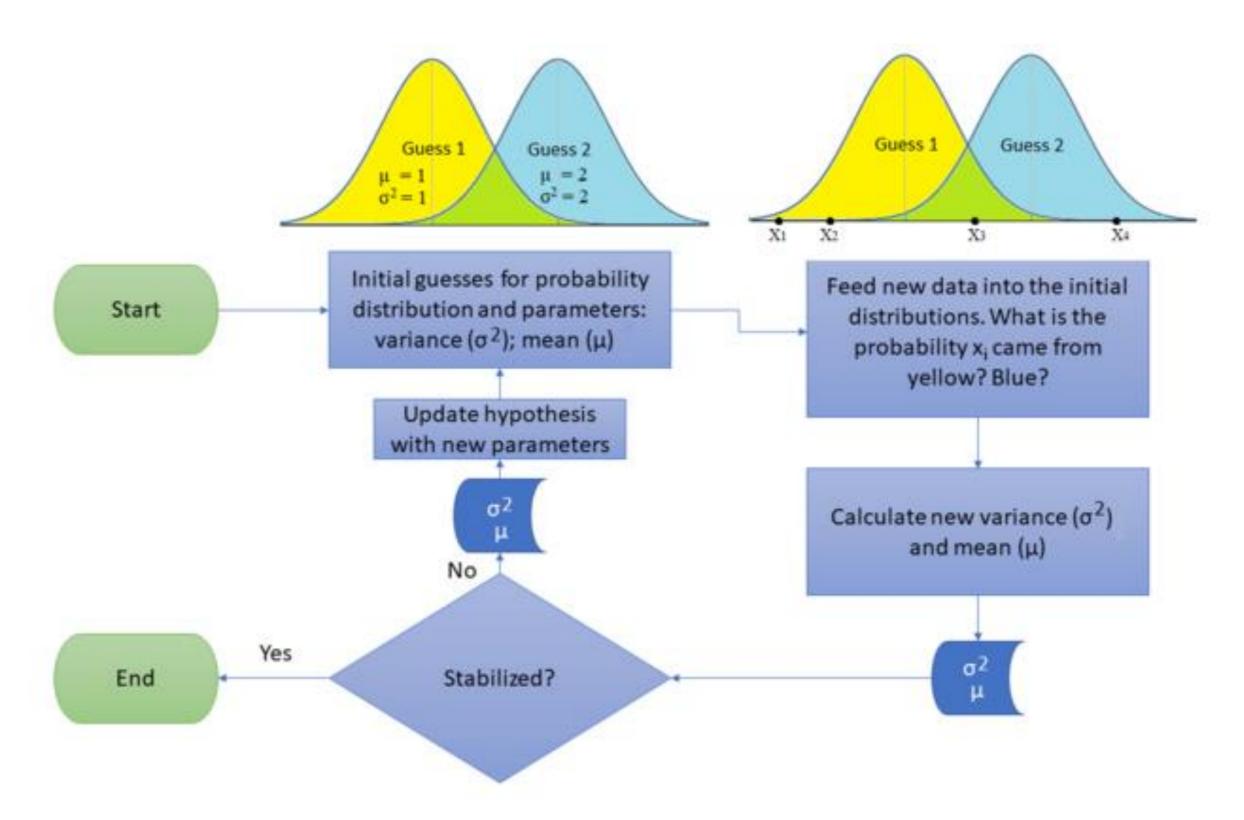
## Number of Clusters Selection Method in One Picture



## **AB Testing in One Picture**



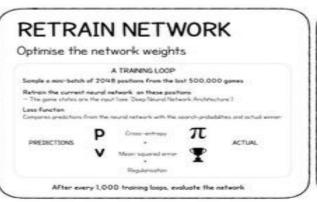
## **EM Algorithm in One Picture**

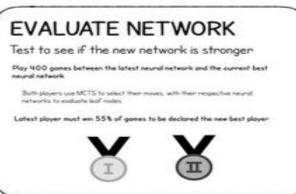


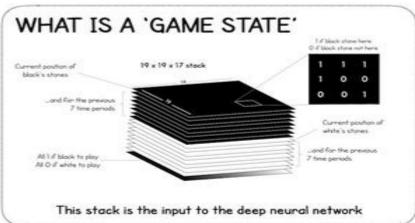
## ALPHAGO ZERO CHEAT SHEET

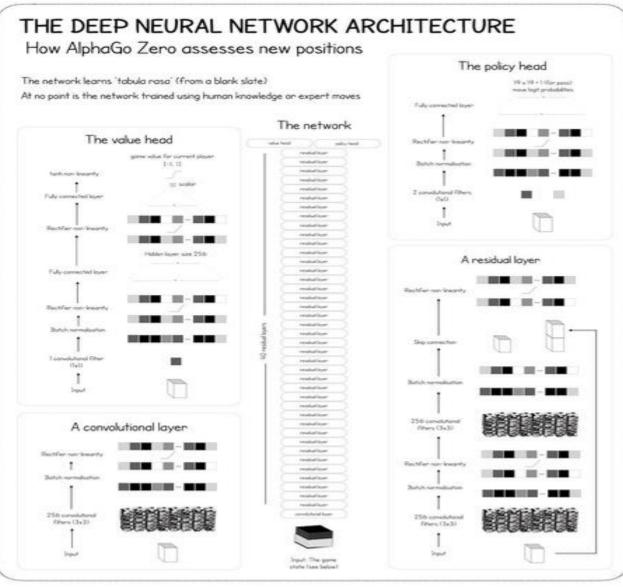
The training pipeline for AlphaGo Zero consists of three stages, executed in parallel

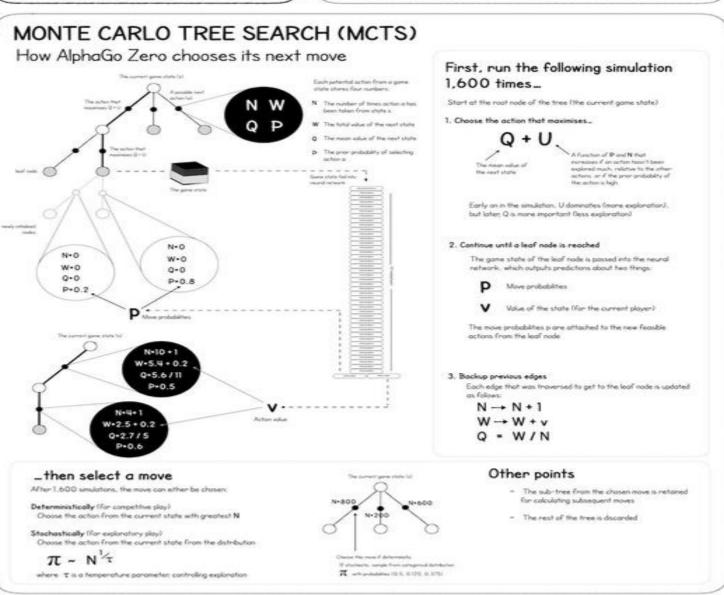


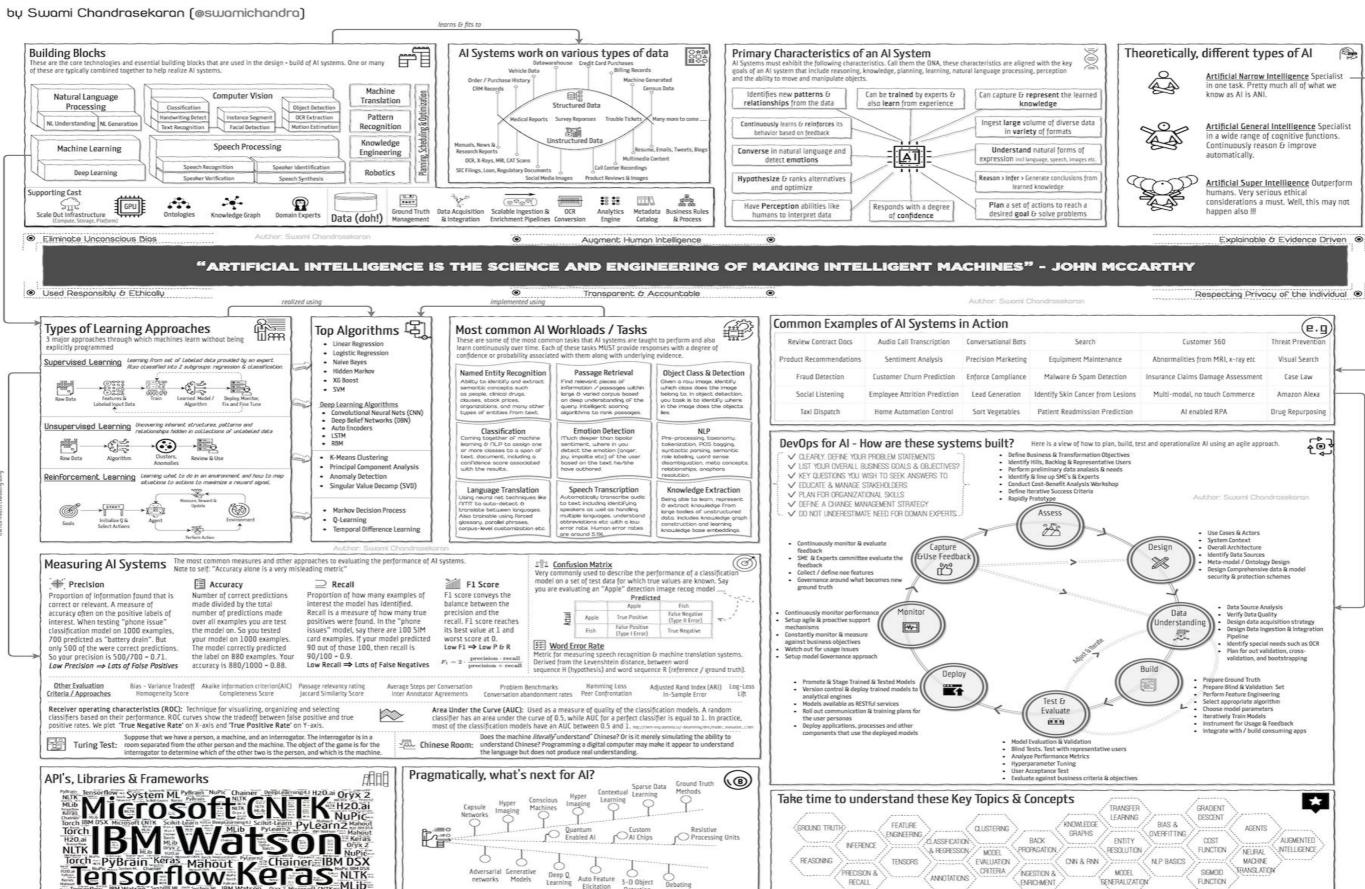












# Number Representation Systems in One Picture

	Logistic Map (p = 1)	Logistic Map (p = 0.5)	Nested Square Root	Base b (b > 1, integer)	Base b (b >1, not an integer)	Continued Fraction
Support domain for $x = x(1)$ , $x(n)$ and $g(x)$	[0, 1]	[0, 1]	[1, 2]	[0, 1]	[0, 1]	[0, 1]
Support domain for digits a(n)	{0, 1}	{0, 1}	{0, 1, 2}	$\{0,1,\cdots,b-1\}$	$\{0,1,\cdots,\lfloor b\rfloor\}$	1, 2, 3,
g(x) [ $x(n+1) = g(x(n))$ ]	4x(1-x)	$\sqrt{4x(1-x)}$	$x^2 - \lfloor x^2 \rfloor + 1$	$bx - \lfloor bx \rfloor$	$bx - \lfloor bx \rfloor$	$1/x - \lfloor 1/x \rfloor$
h(x) $[a(n) = h(x(n))]$	$\lfloor 2x \rfloor$	$\lfloor 2x \rfloor$	$\lfloor x^2 \rfloor - 1$	$\lfloor bx \rfloor$	$\lfloor bx \rfloor$	$\lfloor 1/x \rfloor$
$x = f(\{a(n)\})$	Unknown	Unknown	$\sqrt{a(1)+\sqrt{a(2)+\cdots}}$	$\sum_{k=1}^{\infty} \frac{a(k)}{b^k}$	$\sum_{k=1}^{\infty} \frac{a(k)}{b^k}$	$\frac{1}{a(1) + \frac{1}{a(2) + \cdots}}$
Digits distribution $P(a(n) = k)$	Uniform on {0, 1}		$r(k+2)-r(k+1)$ $r(k)=\sqrt{5\sqrt{k}-1}$	Uniform on {0, 1, , b - 1)	Non uniform	$\log_2\left(rac{(k+1)^2}{k(k+2)} ight)$
Equilibrium distribution $P(x(n) < y)$	$\frac{1}{\pi} \int_0^y \frac{1}{\sqrt{x(1-x)}} dx$	$1-\sqrt{1-y}$	$-2+\sqrt{5y-1}$	Uniform on [0, 1]	Non uniform	$\frac{\log(1+y)}{\log 2}$
Correlation between x(n+1) and x(n)	0	-1/2	Non zero	1/b	Non zero	Nonzero
Correlation between a(n+1) and a(n)	0	-1/4	Non zero (but close)	0	Non zero	E[a(n)] is infinite

The equilibrium distribution is the one satisfying P(X < y) = P(g(X) < y). The statistical properties listed here, are valid for almost all seeds x, except for a set of seeds of measure 0 (depending on the system), known as bad seeds. This document was produced by www.datasciencecentral.com.