And they are:
$$\left\{ H_{1}, 6_{1}^{2} \right\}$$
 $\left\{ H_{2}, 6_{2}^{2} \right\}$

And they are:
$$\{H_1, 67^2\}$$
 as $k=2$ mixfng coeff. / Projection T_K

$$L_{a} = 16$$
 $L_{b} = -56$
 $L_{b}^{2} = 12$
 $L_{b}^{2} = 12$

As k=2, there are two components
$$P(a) = 0.5$$

$$P(b) = 0.5$$

P(x11a)=

$$\frac{\text{E-Step-J}}{P(x;|\mathbf{0})} = \frac{1}{\sqrt{2\pi}G_a^2} \exp\left\{-\frac{(x_i^2 - \mu_a)^2}{2G_o^2}\right\}$$

$$P(xi|b) = \frac{1}{\sqrt{256b^2}} \exp\left\{-\frac{(xi-\mu_b)^2}{26b^2}\right\}$$

$$ai = P(a|xi) = \frac{P(xi|a)P(a)}{P(xi|a)P(a)P(xi|b)P(b)}$$
 $bi = 1-ai$

$$\frac{\chi_{1}' = -67}{P(\chi_{1}|a) = \frac{1}{\sqrt{2\pi} \times 10^{2}}} \exp\left\{-\frac{(-67 - 16)^{2}}{2 \times 100}\right\} = \frac{1}{25} \exp\left\{-\frac{(83)^{2}}{200}\right\}$$

$$= \frac{1}{2} \times 0 = 0$$

$$P(x_1|b) = \frac{1}{\sqrt{2\pi \times 144}} \exp \left\{-\frac{(-67 + 56)^2}{2 \times 144}\right\} = \frac{1}{30} \times 0.65 = 0.021$$

$$a_1 = P(a|x_1) = \frac{0}{0 + 0.5 \times 0.021} = 0$$

$$b_1 = P(b|X_1) = 1 - 0_1 = \frac{1}{2}$$

$$x_2 = -48$$

$$\frac{x^2 = -48}{P(x^2 | a)} = \frac{1}{25} exp \left\{ -\frac{(-48 - 16)^2}{200} \right\} = \frac{1}{25} x^0 = 0$$

$$P(x_2|b) = \frac{1}{30} \exp\left\{-\frac{(-48+56)^2}{288}\right\} = \frac{1}{25} \times 6.80 = 0.026$$

$$a_2 = P(a|x^2) = \frac{0}{0 + 0.5 \times 0.026} = 0$$

$$b2 = 1 - a2 = 1$$

$$PR(x4|a) = \frac{1}{25} exp{-\frac{(\partial-16)^2}{200}} = 0.029$$

$$a_{2} = P(a|x_{2}) = 0.029 \times 0.5 = 1$$

$$0.029 \times 0.5 + 0$$

$$\frac{x_{3}=6}{P(x_{3}|\theta)} = \frac{1}{25} \exp \left\{-\frac{(6-16)^{2}}{200}\right\} = \frac{1}{25} \times 0.6 = 0.024$$

$$p(x_3|b) = \frac{1}{30} \exp \left\{-\frac{(6+56)^2}{280^2}\right\} = \frac{1}{30}x_0 = 0$$

$$Q_3 = P(a|x3) = 0.024 \times 0.5 = 1$$

$$\frac{S = 14}{P(XS|a) = \frac{1}{25}} \exp \left\{-\frac{(14-16)^2}{200}\right\} = \frac{1}{25} \times 0.98 = 0.039$$

$$P(XS1b) = \frac{1}{30} \exp \left\{-\frac{(14+56)^2}{200}\right\} = \frac{1}{30} \times 0 = 0$$

$$b5 = 1 - 1 = 0$$

$$\frac{x_6 = 16}{P(x_6|a)} = \frac{1}{25} \exp\left\{-\frac{(16-16)^2}{200}\right\} = \frac{1}{25}x_1 = 0.04$$

$$P(x_6|b) = \frac{1}{25} \exp\left\{-\frac{(16+56)^2}{200}\right\} = 0$$

$$06 = 1$$

$$06 = 0$$

$$P(x_{7}|a) = \frac{1}{25} exp\{-\frac{(23-16)^{2}}{200}\} = \frac{1}{25} \times 0.78 = 0.031$$

 $P(x_{7}|b) = \frac{1}{30} exp\{-\frac{(23+56)^{2}}{288}\} = \frac{1}{30} \times 0 = 0$

$$\frac{x8 = 24}{P(x8/0)} = \frac{1}{25} \exp\left\{-\frac{(24-16)^2}{200}\right\} = \frac{1}{25} \times 0.72 = 0.029$$

$$P(x0|b) = \frac{1}{25} \exp\left\{-\frac{(24+56)^2}{280}\right\} = \frac{1}{30}x0 = 0$$

$$08 = 1$$

$$b8 = 0$$

$$Q_1 = Q_2 = Q_3$$

 $Q_3 = Q_4 = Q_5 = Q_6 = Q_7 = Q_8 = 1$

$$b_1 = b_2 = 1$$

 $b_3 = b_4 = b_5 = b_6 = b_7 = b_8 = 0$

$$y_a = \frac{a_1 x_1 + a_2 x_2 - \dots - a_8 x_8}{a_1 + a_2 - \dots - a_8}$$

$$= \frac{0+0+6+8+14+16+23+24}{6} = \frac{15.166}{1}$$

$$6a^{2} = 0, (\mu_{q} - \chi_{1})^{2} + 0_{2}(\mu_{q} - \chi_{2})^{2} + - +\alpha_{8}(\mu_{q} - \chi_{8})^{2}$$

$$\alpha_{1} + \alpha_{2} - - +\alpha_{8}$$

Estable with the first of the first of the standing

Maria Caracter Commence

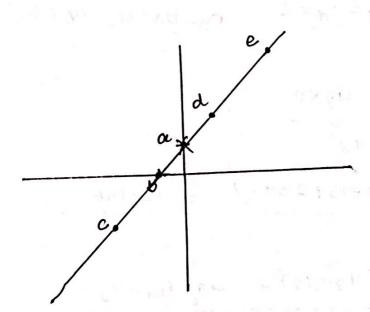
$$M_{b} = \frac{b_{1}x_{1}+b_{2}x_{2}+--b_{8}x_{8}}{b_{1}+b_{2}+--b_{8}}$$

$$= \frac{-67 - 48}{2} = -57.5$$

$$\sqrt[6]{b^2} = \frac{90.25 + 90.25}{2} = \frac{90.25}{2}$$

2) Principle Component Analysis

 $\frac{a}{2}$ dataset: {(0,1), (-1,0), (-3,-2), (1,2), (3,4)}



Hean =
$$\left(\frac{0+(1)\cdot3+1+3}{5}, \frac{1+0-2+2+4}{5}\right)$$

= $\left(0,1\right) = 0$

Recenter 7

$$X_c \leftarrow x - \overline{x}$$

$$a' = (0,0), b' = (+,+), c' = (-3,-3), d' = (3,3)$$

Posnciple Component 17

$$= \frac{1}{\sqrt{1^2+1^2}} (1,1) \Rightarrow (\frac{1}{12},\frac{1}{12})$$

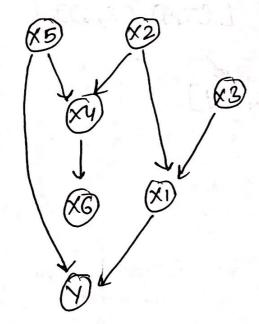
Pranciple Comparent 27 (orthogonal to PC 1)
= \frac{1}{12+12}(-1,1) => (-\frac{1}{12}, \frac{1}{12}) \sigma \left(\frac{1}{12}, -\frac{1}{12} \right)

2.2) Reconstruction From 7

国mxn

for m example of a m-dimensional dataset, we can compute m principle comparents and if we are going to use all m fir seconstruction of the data set them, the seconstruction error will be giro as we all selecting all possible n-dimension for the recurstruction.

3) Graphical Model 7



P(Y, X1, X2, X3, X4, X5, X6)

= P(Y(X5,X1), P(X1)X2,X3), P(X2), P(X3), P(X4) X2,X5). P(X5), P(X6)X4)

1 K-Means 7

41

a	b	C	d
3	7 -	9	5
3	9	7	3

Given 7 cluster-1 ⇒ a, c cluster-2 ⇒ b, d

Devation - 17

Clusters = [[(3,3), (9,7)], [(7,9), (5,3)]]

Recenta-skp Centroid = [(6.5)], [(6.6)]

Phrahion-2-

classify Step-

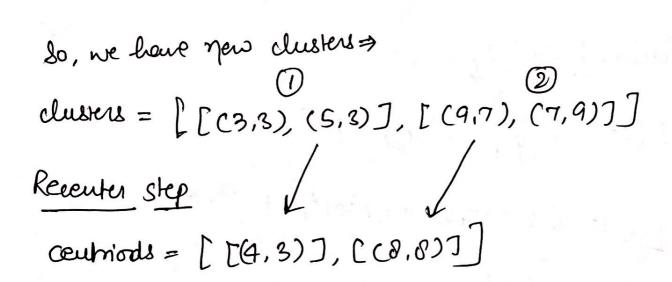
de'stauce from distauce from Centroid 1

a (3,3) MM (\sqrt{13} \sqrt{13} \sqrt{18})

b (9,7) MM (\sqrt{15} \sqrt{10} \sqrt{10})

c (7,9) MM (\sqrt{17} \sqrt{10} \sqrt{10})

d (5,3) MM (\sqrt{5} \sqrt{10} \sqrt{10})



Eteration 3 7 Classify Step >>

	U	distance from	distance form
		distance from Ceathood 1	centroid 2
a	(3.3)	MAM (VI	5/2)
b	(9,7)	mm (\191	V2 L)
C	(7,9)	MM (J45	52 ~)
d	(5,3)	mmc JI	V34)

The clusters \mathcal{D} clusters = [[(3,3),(5,3)],[(9,7),(7,9)]]Recent step [(4,3)],[(8,8)]

Since you clusters and you controls intention 3 are equal to Iteration 2, we can say that it has cornered and above clusters will be the final clusters:

4.2) Potential functo

F(M,C)= = 11 McGj-xj112

 $= \left[(1^{2}+0) + (1^{2}+0) + (1^{2}+1^{2}) + (1^{2}+1^{2}) \right]$

= [1+1+2+2]

4.3) K- Means Implementation 7

Bendo Code 7

Step-1 > froces the dataset, ignere the 1st & last column as
It is not needed for clusterizg.

Step 2 >> Randonly pick the K-centroids

Step-3 => Non perform the classify & sententer step untill et is unverged. r.e.

classify step - Assign each of the example I data point to its nearest controid based on ecludian distance. i-e.

Recenter step - Now eyee each data point is assigned to some cluster, find the new centroid for each cluster which is yothing but the average of all points meide that cluster. I'e.

Ur ← ay m²n ≤ 11 H-xj 112 j:ccj)=i

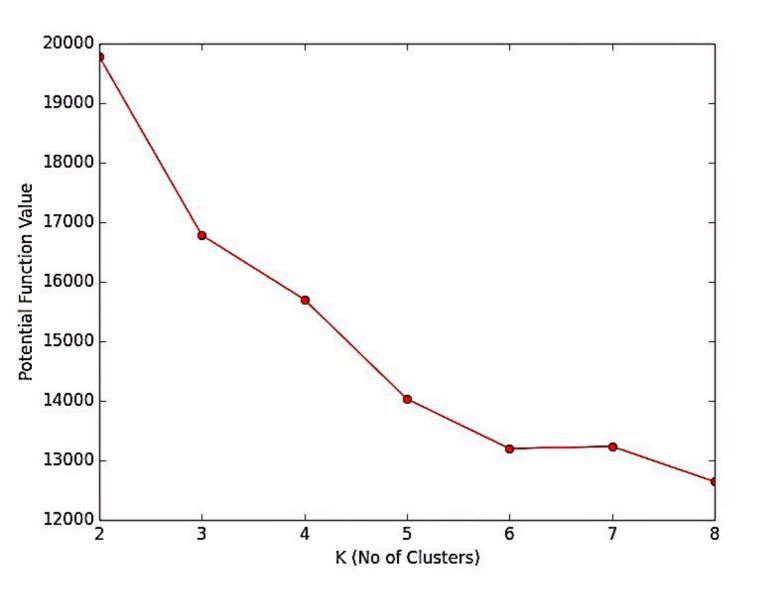
teep penfoming the classfy & secenter step until it is converged.

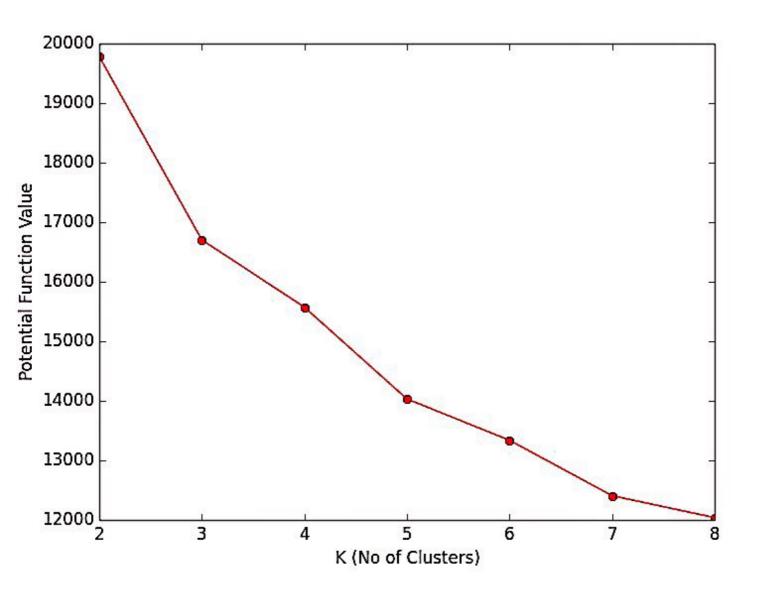
Step-4 find the potential function i.e.

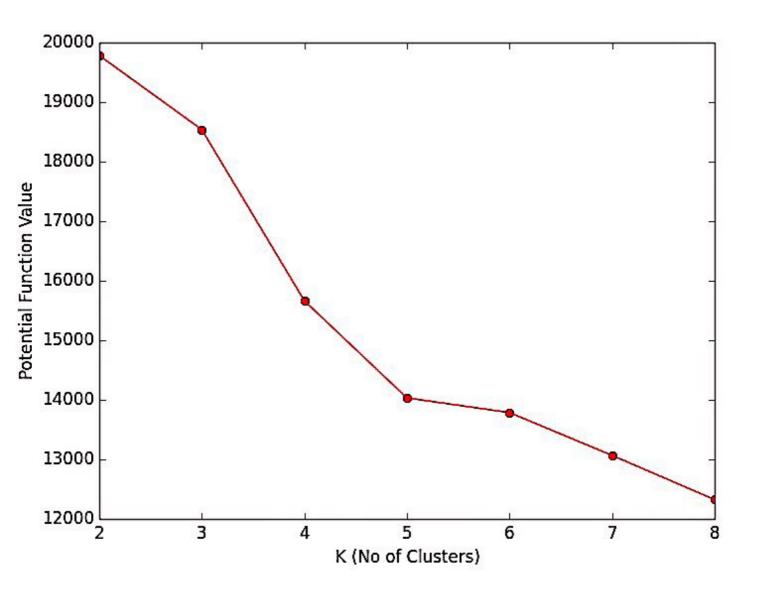
F(M,C) = \$\frac{7}{57} \land \l

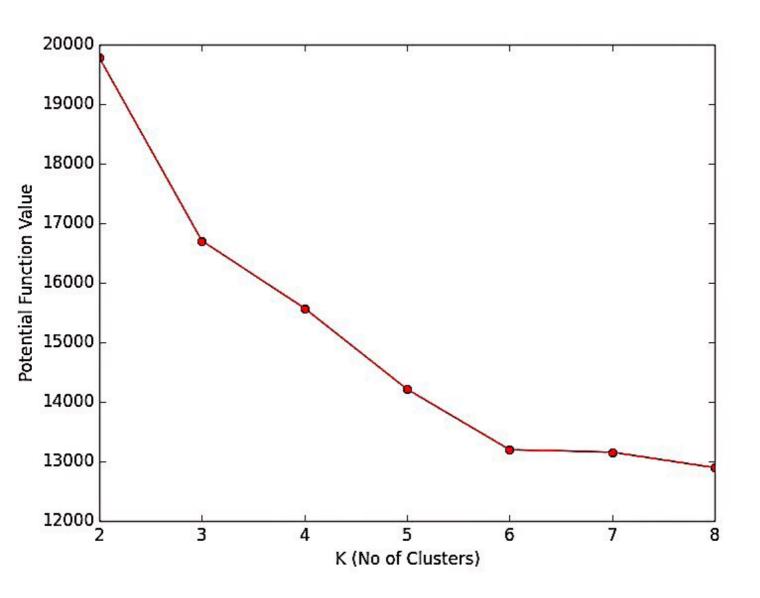
fine the L(K) VK plot on next page.

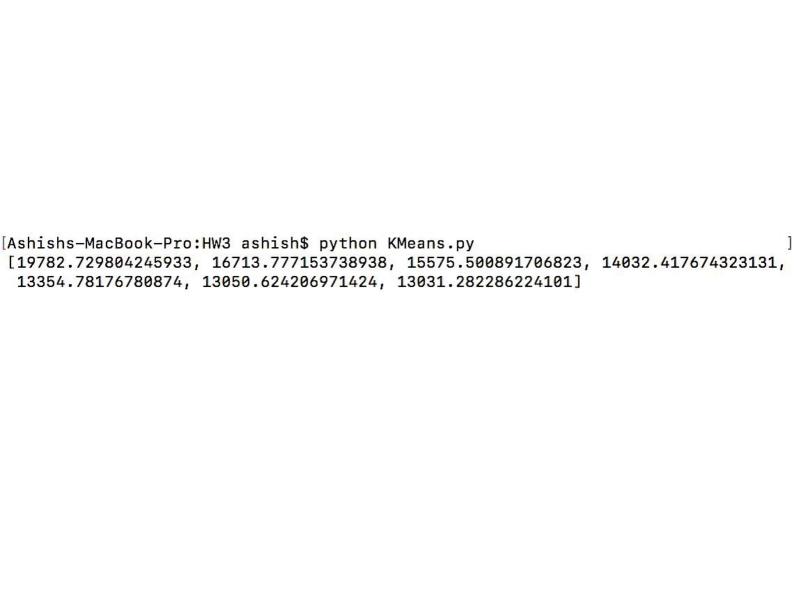
We will use the "elbow" yethord for picking the pphimal ralue of K. And based on the graph plot on yest page, she will be choosing k=6 as our optimal value as peu potential funds value decreases absorptly at k=6 & stabilizes after that. We won't be choosing the minimum k value with min, potential functs. This k can charge but we will always follow the elbow rule to determine it.











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