# Pattern Recognition CS669

Course Instructor : Dr. Dileep A. D.

## Final Report

Fisher Discriminant Analysis,
Perceptron based classifier
&
Support Vector Machines

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## 1. Problem Description

Classification is the problem of identifying to which of a set of categories (sub-populations) a new observation belongs on the basis of a training set of data containing observations (or instances) whose category membership is known.

#### Data-sets:

- 1. 2 dimensional artificial data
  - (a) Linearly separable dataset used in Assignment1
  - (b) Nonlinearly separable data set used in Assignment1
- 2. 3 class scene image dataset: Consider the 64-dimensional BoVW representation from Assignment-2

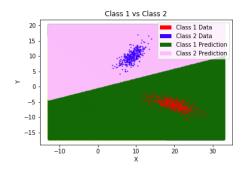
#### Classifiers to be built:

- 1. Apply Fisher linear discriminant analysis (FDA) on Dataset-1 and Dataset-2. Use Bayes classifier using both unomodal Gaussian and GMM
- 2. Perceptron-based classifier on Dataset-1(a).
- 3. SVM-based classifier using (a) linear kernel, (b) polynomial kernel and (c) Gaussian/RBF kernel on Dataset-1 and Dataset-2

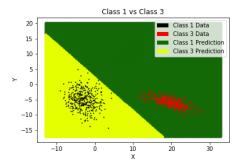
## 2. Results

### 1 Dataset 1(a): Artificial Linearly Separable Data

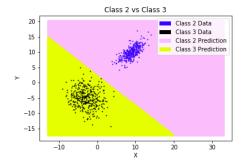
#### 1.1 Perceptron based classification



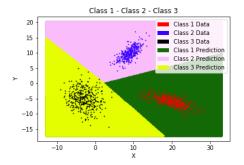
(a) Decision regions and Training data Class 1 and 2



(c) Decision regions and Training data Class 1 and 3



(b) Decision regions and Training data Class 2 and 3



(d) Decision regions and Training data Class 1, 2, 3

(b) Analysis

Figure 2..1. Perceptron : Linearly Separable Data - Decision Regions

	Class 1	Class 1	Class 3
Class 1	125	0	0
Class 2	0	125	10
Class 3	0	0	125

	Class 1	Class 2	Class 3
Precision	1	1	1
Recall	1	1	1
F-Measure	1	1	1

(a) Confusion Matrix

Accuracy	100%
Precision	1
Recall	1
F-Measure	1

(c) Results

Table 2..1. Confusion Matrix and Analysis

#### 1.2 Support Vector Machines

#### Linear Kernel

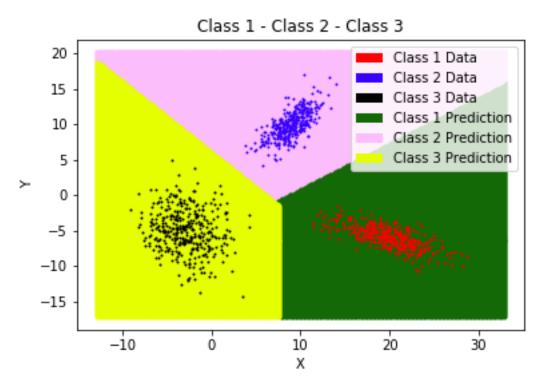


Figure 2..2. SVM : Linearly Separable Data - Decision Regions

	Class 1	Class 1	Class 3
Class 1	125	0	0
Class 2	0	125	10
Class 3	0	0	125

	Class 1	Class 2	Class 3
Precision	1	1	1
Recall	1	1	1
F-Measure	1	1	1

(b) Analysis

(a) Confusion Matrix

Accuracy	100%
Precision	1
Recall	1
F-Measure	1

(c) Results

Table 2..2. Confusion Matrix and Analysis

#### Polynomial Kernel

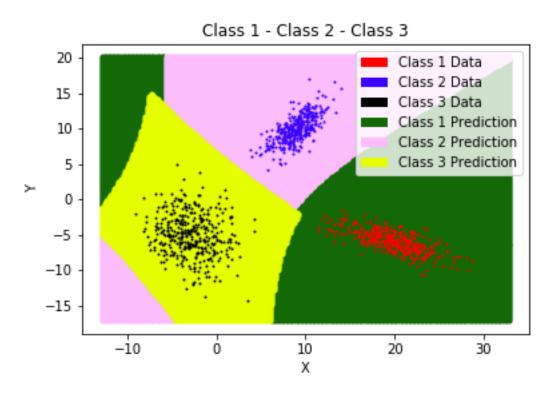


Figure 2..3. SVM : Linearly Separable Data - Decision Regions

	Class 1	Class 1	Class 3
Class 1	125	0	0
Class 2	0	125	10
Class 3	0	0	125

	Class 1	Class 2	Class 3
Precision	1	1	1
Recall	1	1	1
F-Measure	1	1	1

(b) Analysis

(a) Confusion Matrix

Accuracy	100%
Precision	1
Recall	1
F-Measure	1

(c) Results

Table 2..3. Confusion Matrix and Analysis

#### **RBF Kernel**

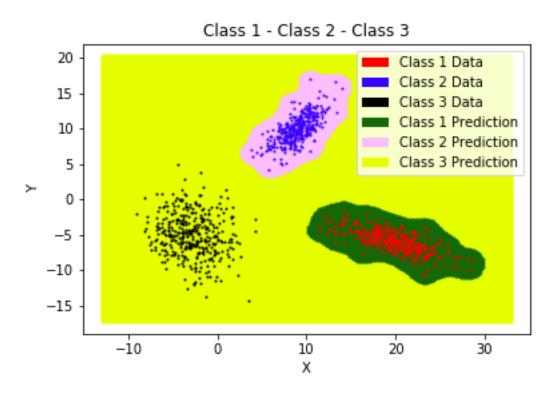


Figure 2..4. SVM : Linearly Separable Data - Decision Regions

	Class 1	Class 1	Class 3
Class 1	125	0	0
Class 2	0	125	10
Class 3	0	0	125

	Class 1	Class 2	Class 3
Precision	1	1	1
Recall	1	1	1
F-Measure	1	1	1

(b) Analysis

(a) Confusion Matrix

Accuracy	100%
Precision	1
Recall	1
F-Measure	1

(c) Results

Table 2..4. Confusion Matrix and Analysis

#### Observations and Inferences

• Perceptron was able to correctly classify all the data

- SVM with a linear kernel gave a linear boundary which was better than that given by the perceptron. The boundaries were centered between the data points of the two corresponding classes.
- Polynomial as well as RBF kernels with SVM gave accurate results with a good approximation.
- 100% accuracy was obtained using both the perceptron as well as SVM with linear, polynomial, RBF kernels

#### Comparisons

For the artificial linearly separable dataset, Bayes classifier with unimodal gaussian distribution, GMM as well as perceptron and SVM based classification gave us a 100% accuracy. hence we can say that linearly separable classes are easy to classify and even simple classifiers can give good results.

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## 2 Dataset 1(b): Artificial Non-Linearly separable dataset

#### 2.1 Support Vector Machines

Linear Kernel

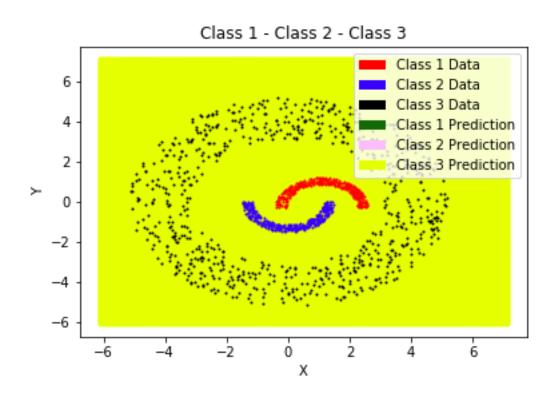


Figure 2..5. SVM Linear Kernel : Non-Linearly Separable Data - Decision Regions

	Class 1	Class 1	Class 3
Class 1	0	0	125
Class 2	0	0	125
Class 3	0	0	250

	Class 1	Class 2	Class 3
Precision	0	0	1
Recall	0	0	0.5
F-Measure	0	0	0.66

(b) Analysis

(a) Confusion Matrix

Accuracy	50%
Precision	0.33
Recall	0.166
F-Measure	0.22

(c) Results

Table 2..5. Confusion Matrix and Analysis

#### Polynomial Kernel

#### Degree = 2



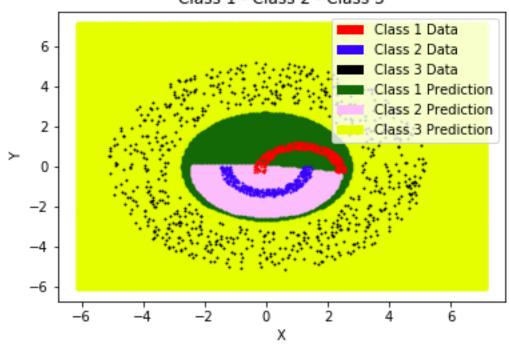


Figure 2..6. SVM Polynomial Kernel, Degree = 2: Non-Linearly Separable Data - Decision Regions

	Class 1	Class 1	Class 3
Class 1	116	9	0
Class 2	9	116	10
Class 3	0	0	250

	Class 1	Class 2	Class 3
Precision	0.928	0.928	1
Recall	0.928	0.928	1
F-Measure	0.928	0.928	

(b) Analysis

(a) Confusion Matrix

Accuracy	96.4%
Precision	0.952
Recall	0.952
F-Measure	0.952

(c) Results

Table 2..6. Confusion Matrix and Analysis

Degree = 3

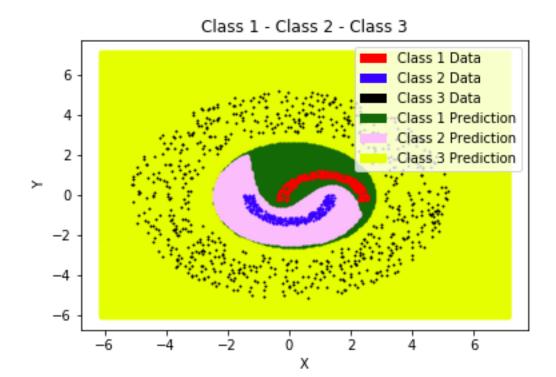


Figure 2..7. SVM Polynomial Kernel, Degree = 2: Non-Linearly Separable Data - Decision Regions

	Class 1	Class 1	Class 3
Class 1	125	0	0
Class 2	0	125	10
Class 3	0	0	250

	Class 1	Class 2	Class 3
Precision	1	1	1
Recall	1	1	1
F-Measure	1	1	1

(b) Analysis

(a) Confusion Matrix

Accuracy	100%
Precision	1
Recall	1
F-Measure	1

(c) Results

Table 2..7. Confusion Matrix and Analysis

#### RBF Kernel

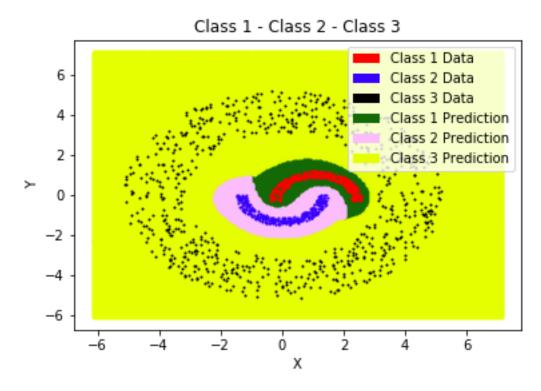


Figure 2..8. SVM RBF Kernel : Non-Linearly Separable Data - Decision Regions

	Class 1	Class 1	Class 3
Class 1	125	0	0
Class 2	0	125	10
Class 3	0	0	250

	Class 1	Class 2	Class 3
Precision	1	1	1
Recall	1	1	1
F-Measure	1	1	1

(b) Analysis

(a) Confusion Matrix

Accuracy	100%
Precision	1
Recall	1
F-Measure	1

(c) Results

Table 2..8. Confusion Matrix and Analysis

#### Comparisons

With unimodal gaussian distribution we achieved a maximum accuracy of 96%. Using Gaussiam Mixture Model based density estimation we were able to achieve 100%

Accuracy of 100% was also achieved using SVM with a polynomial kernel of degree of 2 as well as with the RBF kernel.

#### 3 Dataset 2 : Scene Image Dataset

#### 3.1 Classification using GMM on Color Histograms

	C = 1	C = 2	C = 4	C = 8	C = 16	C = 32
Accuracy	46.0%	24.66%	40.0%	45.33%	40.66%	47.99%
mean precision	0.5146	0.2368	0.3852	0.4769	0.4103	0.4908
mean recall	0.46	0.2466	0.4155	0.4533	0.4066	0.4799
mean F-Measure	0.4419	0.2237	0.3878	0.4397	0.4061	0.4779

Table 2..9. GMM Results for Color Histograms

#### 3.2 Classification using GMM on BOVW representation

	C = 1	C = 2	C = 4	C = 8	C = 16	C = 32
Accuracy	34.67	46.0	45.33	54.67	46.67	38.0
mean precision	0.3522	0.4706	0.4578	0.5498	0.4899	0.3731
mean recall	0.3467	0.46	0.4533	0.5467	0.4667	0.38
mean F-Measure	0.3014	0.4531	0.4326	0.5474	0.4616	0.3582

Table 2..10. GMM Results for BOVW

#### 3.3 Principal Component Analysis

Variation of Accuracy with L and number of GMM components

	C = 1	C=2	C = 4	C = 8
L=2	34.67%	34.67%	34.0%	37.33%
L = 5	29.33%	43.33%	36.0%	40.67%
L = 10	30.67%	42.0%	34.67%	39.33%
L = 15	34.0%	44.67%	42.0%	43.33%
L = 21	30.67%	32.67%	45.33%	45.33%

Table 2..11. Variation of Accuracy with L and C

We observe that in general that accuracy increases with increase in L and the number of GMM components although there are a few spikes in occasionally.

#### 3.4 Support Vector Machines

#### Linear Kernel

	Bayou	Chalet	Creek
Bayou	21	13	16
Chalet	19	21	10
Creek	20	8	22

	Bayou	Chalet	Creek
Precision	0.42	0.42	0.44
Recall	10.35	0.5	0.458
F-Measure	0.381	0.456	0.448

(a) Confusion Matrix

(b) Analysis

Accuracy	42.66%
Precision	42.6 6
Recall	43.61
F-Measure	42.91

(c) Results

Table 2..12. Confusion Matrix and Analysis

#### Polynomial Kernel

Degree = 2

	Bayou	Chalet	Creek
Bayou	30	10	10
Chalet	20	21	9
Creek	16	18	16

	Bayou	Chalet	Creek
Precision	0.6	0.42	0.32
Recall	0.45	0.42	0.45
F-Measure	0.51	0.42	0.37

(a) Confusion Matrix

(b) Analysis

Accuracy	44.6%
Precision	0.446
Recall	0.446
F-Measure	0.439

(c) Results

Table 2..13. Confusion Matrix and Analysis

Degree = 3

	Bayou	Chalet	Creek
Bayou	31	11	8
Chalet	29	24	7
Creek	14	18	18

	Bayou	Chalet	Creek
Precision	0.62	0.48	0.36
Recall	0.48	0.45	0.54
F-Measure	0.54	0.46	0.43

#### (a) Confusion Matrix

(b) Analysis

Accuracy	48.6%
Precision	0.486
Recall	0.494
F-Measure	0.481

(c) Results

Table 2..14. Confusion Matrix and Analysis

#### **RBF Kernel**

	Bayou	Chalet	Creek
Bayou	46	4	0
Chalet	42	7	1
Creek	46	4	0

	Bayou	Chalet	Creek
Precision	0.92	0.14	0
Recall	0.34	0.46	0
F-Measure	0.5	0.21	nan

(b) Analysis

(a) Confusion Matrix

Accuracy 0.35%
Precision 0.35
Recall 0.26
F-Measure nan

(c) Results

Table 2..15. Confusion Matrix and Analysis

#### Comparisons

The best accuarcy was obtained using a GMM based desnity estimation. Accuracy using a PCA based dimensionality reduction also gave us comparable results but not better.

SVM with a degree 3 polynomial kernel gave an accuracy of 48% which is comparable to the one obtained with GMM based density estimation.

## 3. Conclusion & Inferences

- Even a single perceptron was able to efficiently classify multiple linearly separable classes.
- SVM gave a better decision boundary in in comparison to a single perceptron.
- SVM with a polynomial or RBF kernel is in general more effective than that using a linear kernel for non linearly separable data.
- Increasing the degree of the polynomial kernel in SVM increases accuracy to some extent.
- For the scene image dataset, SVM was not much effective than the previously used PCA and GMM combinations.
- For scene image dataset, accuracy was observed to increase with increase in the degree of the polynomial kernel.

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