

0.1 Question 1

0.1.1 Part A

Joint distribution is: $P(D)P(S)P(C|D)P(I|C)P(V|C, S, J)P(J|D)P(T|J)$

0.1.2 Part B

0.1.3 Part C

Found this question a bit confusing so I'll explain best I can...

$P(S \perp\!\!\!\perp J) = J \rightarrow V \leftarrow$ (no blocking) $P(S \perp\!\!\!\perp D) = D \rightarrow C \rightarrow V \leftarrow S$ (no blocking) $P(S \perp\!\!\!\perp I) = I \leftarrow C \rightarrow V \leftarrow S$ (no blocking) $P(S \perp\!\!\!\perp C) = C \rightarrow V \leftarrow S$ (no blocking)

For paths $C \rightarrow V \leftarrow S$ and $J \rightarrow V \leftarrow S$ both paths are always unblocked as V is conditioned on.

By conditioning on the variables J, D, I, C , no blocking occurs and hence S is not conditionally independent on J, D, I or C and there is therefore no observation that would lead to no extra information (all would lead to an increase in information).

If you could condition on both C and J , S would become conditionally independent of D but as we are limited to one additional variable, if you condition simply on C or J , there is still a path from D to S via the symmetric route and as such D is not independent.