

1a. See Attached Graph

1b. See Attached Graph

There is no decision boundary that satisfies the conditions of 1bii

1c. $D_{KL}[pw1(x), pw2(x)] = 0.419$

$D_{KL}[pw2(x), pw1(x)] = 0.0105$

2a. Information of $\Delta = 1.78$

Information of "orange" = 2

2b. $H_a = 1.75$

$H_b = 2.37$

2c. The maximum entropy, which would occur when all of the events are equally likely, are $H_{a_max} = 2$ and $H_{b_max} = 2.585$. Since $H_{a_max} > H_a$ and $H_{b_max} > H_b$ neither $P_a(\cdot)$ nor $P_b(\cdot)$ are maximum entropy distributions.

2d. $P = 6.5104e-04$

2e. $P = 0.0052$

3a. Under these circumstances the system is non-ergodic. This is due to the fact that A is a random variable, therefore for every repetition of the experiment the amplitude may vary.

3b. $X(t)$ is not stationary in any case as its statistics are time dependent due to the time dependent exponential term.

3c. $X(t)$ is neither quasi-stationary nor quasi-ergodic as there are no known models that can be used to transform this system into a stationary system or an ergodic system.

3d. Under these circumstances the system would be mean-ergodic since its initial conditions are stable and its mean is independent of time.

3e. $X(t)$ is not wide sense stationary as its statistics (specifically mean and standard deviation) are time dependent due to the time dependent exponential term.

3f. No, this will not be a random process as we know the outcome of the system at every point.