# Model Evaluation Cross Validation, underfitting vs overfitting, learning curves



# SUBSCRIBERS **YouTube**





#### Majaa Matrix from now onwards...





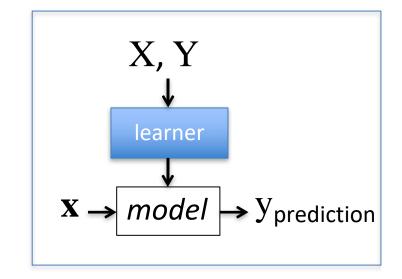
#### Stages of Machine Learning

**Given:** labeled training data  $X, Y = \{hx_i, y_i\}_{i=1}^n$ 

• Assumes each  $\mathbf{x}_i \leftarrow D(X)$  with  $y_i = f_{target}(\mathbf{x}_i)$ 

#### Train the model:

 $model \leftarrow classifier.train(X, Y)$ 



#### Apply the model to new data:

• Given: new unlabeled instance  $\mathbf{x} \leftarrow D(X)$  $y_{\text{prediction}} \leftarrow model.predict(\mathbf{x})$ 

#### Metrics

Regression	Classification
<ul> <li>Mean Absolute Error (MAE)</li> <li>Root Mean Squared Error (RMSE)</li> <li>R-Squared and Adjusted R-Squared</li> </ul>	<ul> <li>Recall</li> <li>Precision</li> <li>F1-Score</li> <li>Accuracy</li> <li>Area Under the Curve (AUC)</li> </ul>

#### **Training Data and Test Data**

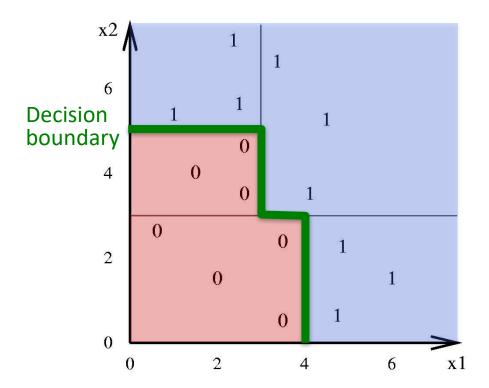
- Training data: data used to build the model
- Test data: new data, not used in the training process

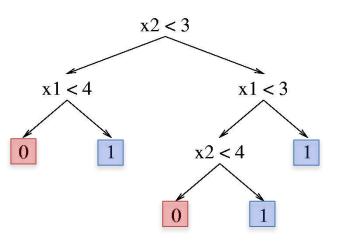
- Training performance is often a poor indicator of generalization performance
  - Generalization is what we <u>really</u> care about in ML
  - Easy to overfit the training data
  - Performance on test data is a good indicator of generalization performance
  - i.e., test accuracy is more important than training accuracy



#### Decision Tree – Decision Boundary

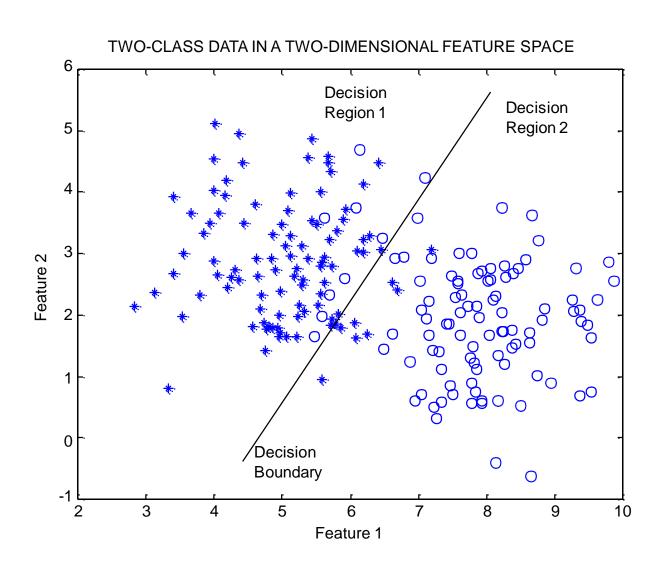
- Decision trees divide the feature space into axisparallel (hyper-)rectangles
- Each rectangular region is labeled with one label
  - or a probability distribution over labels







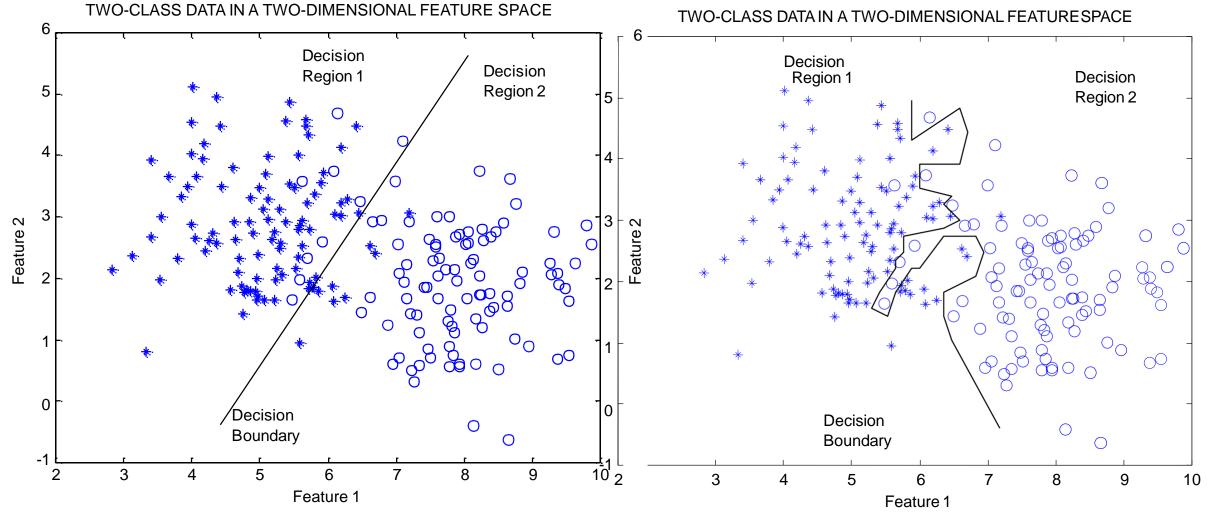
#### Simple Decision Boundary



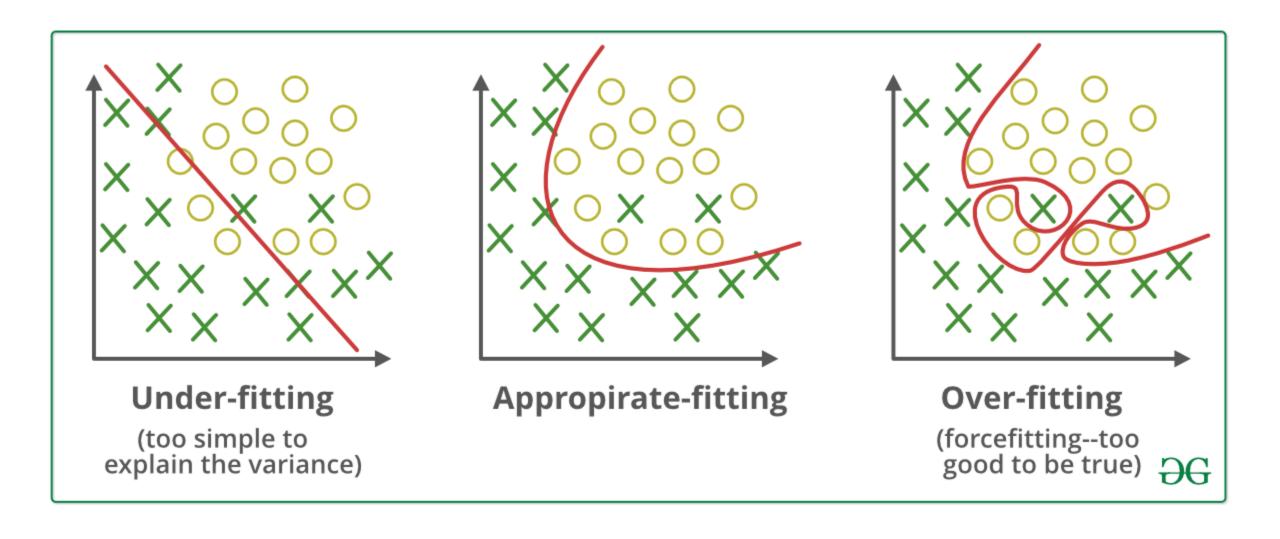
#### More Complex Decision Boundary



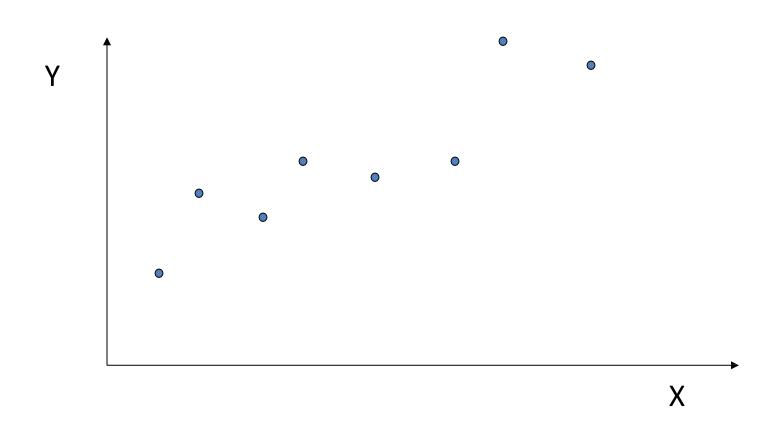




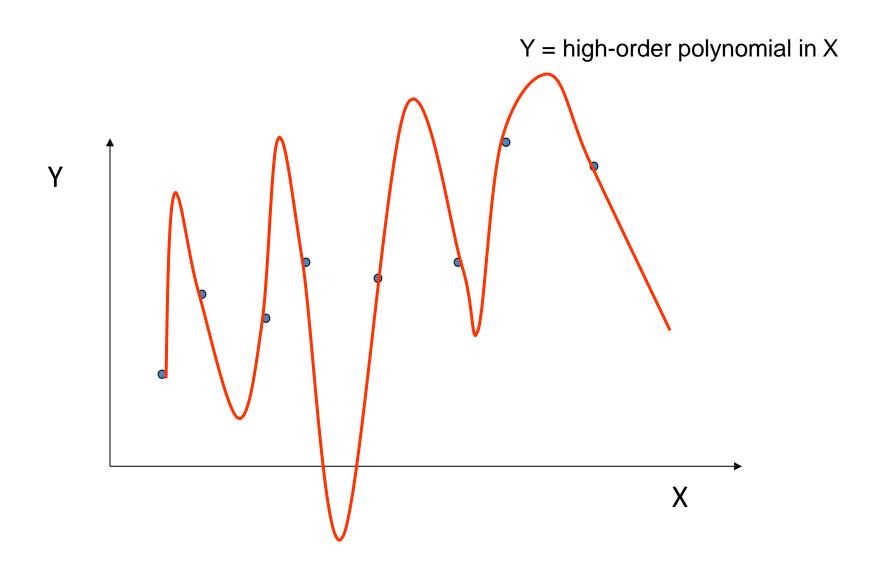
### Underfitting vs Overfitting



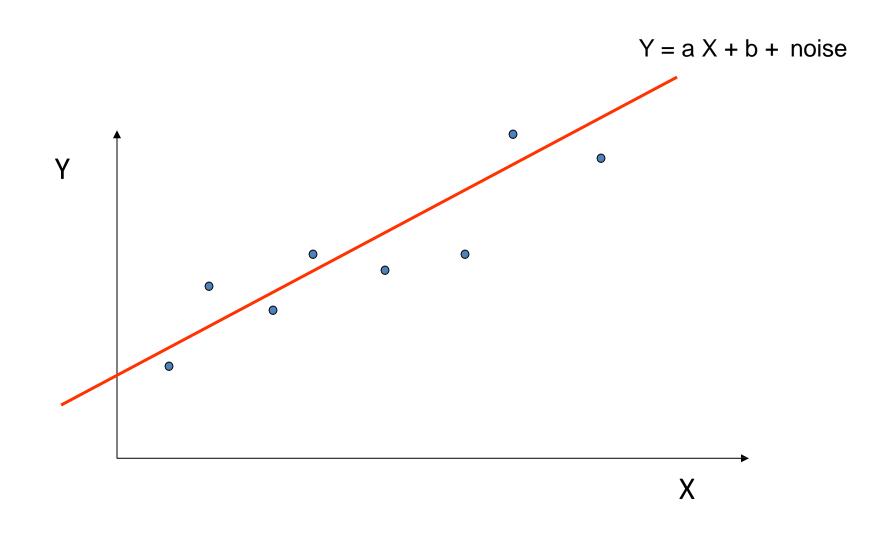
#### Fitting a Regression Model



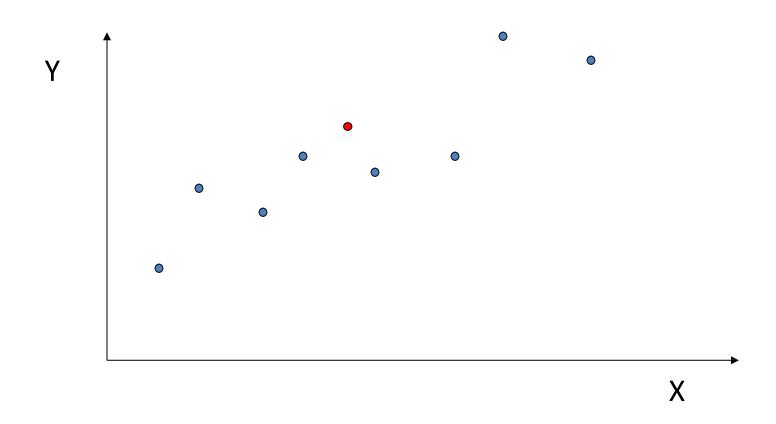
## A Complex Model



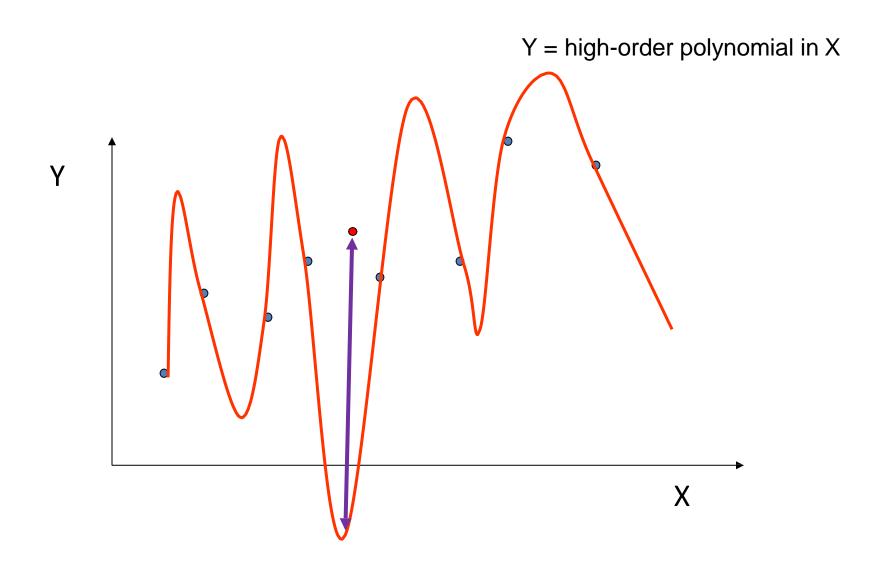
## The True (simpler) Model



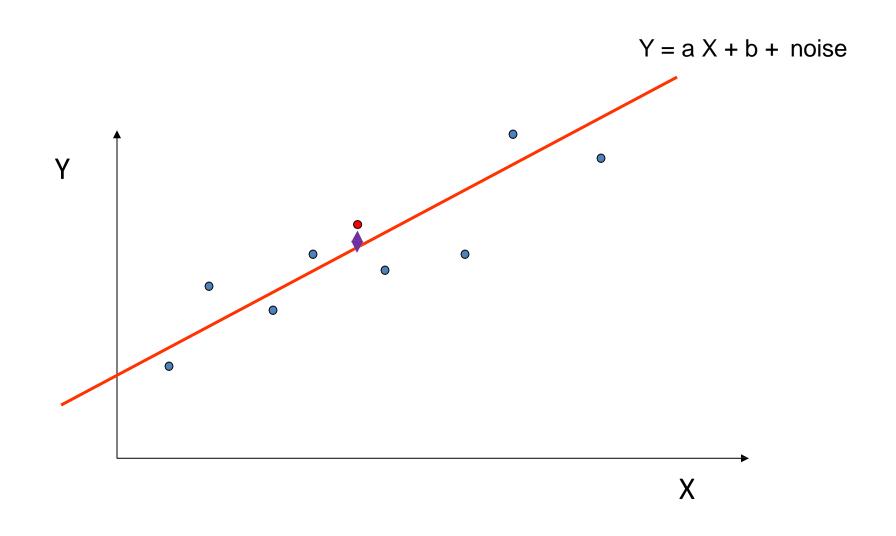
#### Example: The Overfitting Phenomenon



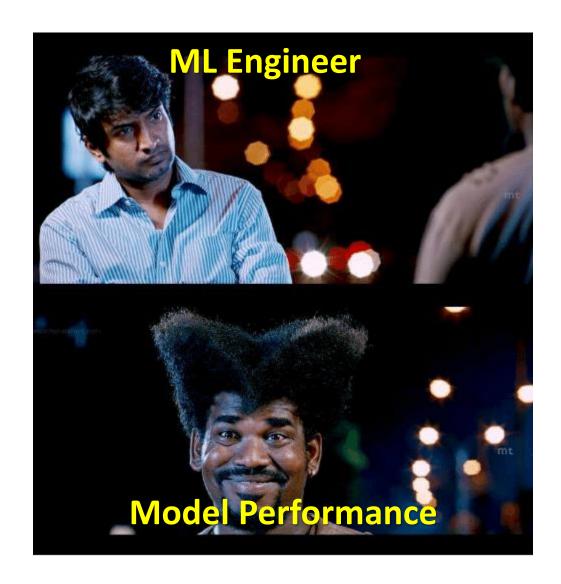
### A Complex Model



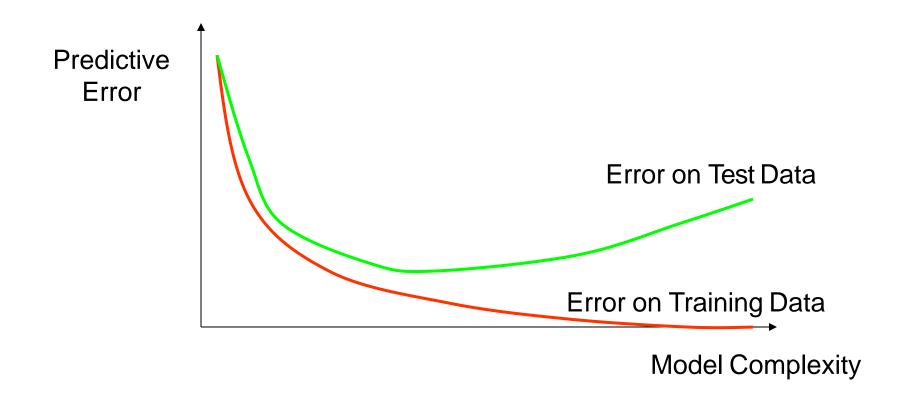
## The True (simpler) Model



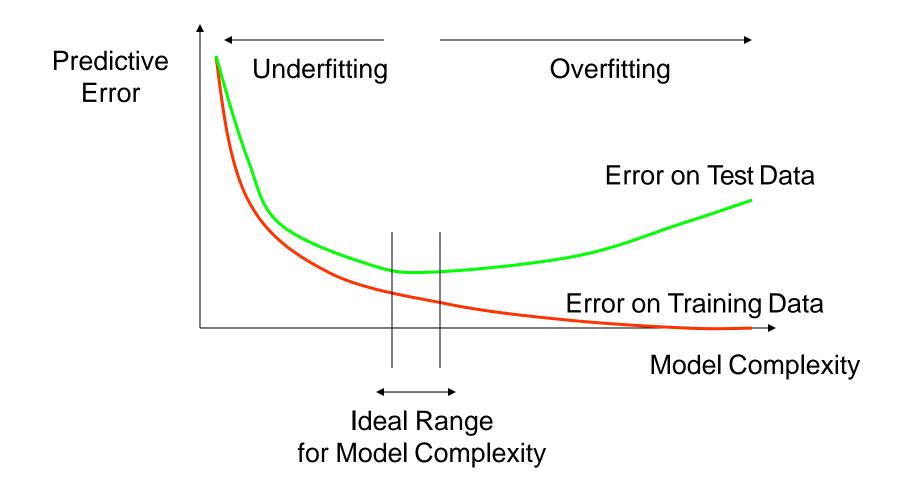
#### When underfitting and overfitting happens?



#### **How Overfitting Affects Prediction**



#### **How Overfitting Affects Prediction**



#### **Comparing Classifiers**

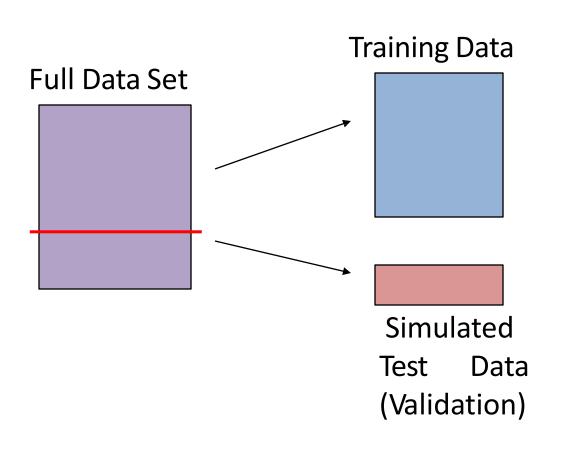
Say we have two classifiers, C1 and C2, and want to choose the best one to use for future predictions

Can we use training accuracy to choose between them?

- No!
  - e.g., C1 = pruned decision tree, C2 = 1-NN training\_accuracy(1-NN) = 100%, but may not be best

Instead, choose based on test accuracy...

#### **Training and Test Data**



#### Idea:

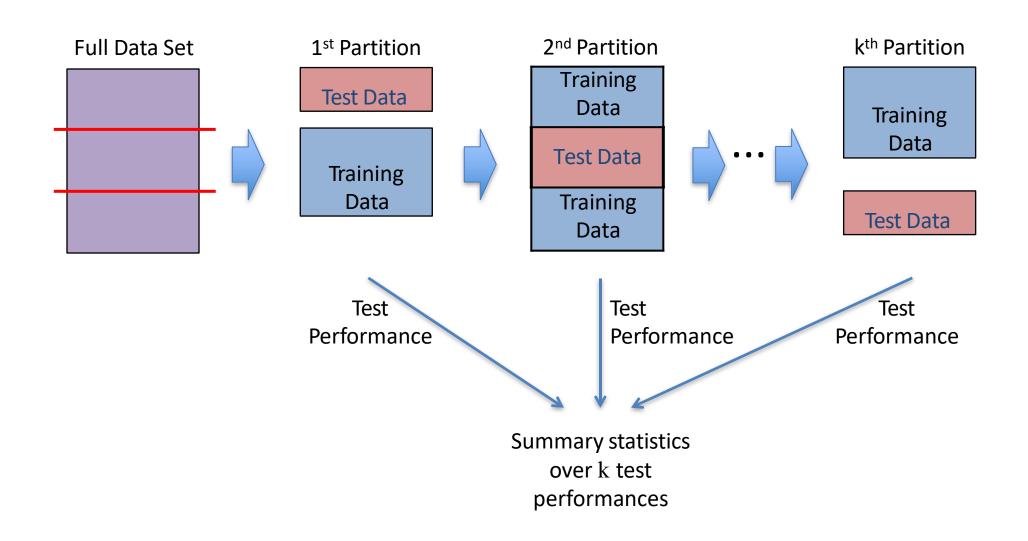
Train each model on the "training data"...

...and then test each model's accuracy on the "test" data

#### k-Fold Cross-Validation

- Why just choose one particular "split" of the data?
  - In principle, we should do this multiple times since performance may be different for each split
- k-Fold Cross-Validation (e.g., k=10)
  - randomly partition full data set of n instances into  $\underline{k}$  disjoint subsets (each roughly of size n/k)
  - Choose each fold in turn as the test set; train model on the other folds and evaluate
  - Compute statistics over k test performances, or choose best of the k models
  - Can also do "leave-one-out CV" where k = n

## Example 3-Fold CV



#### More on Cross-Validation

- Cross-validation generates an approximate estimate of how well the classifier will do on "unseen" data
  - As k → n, the model becomes more accurate (more training data)
  - ...but, CV becomes more computationally expensive
  - Choosing k < n is a compromise
- Averaging over different partitions is more robust than just a single train/validate partition of the data

#### **Learning Curve**

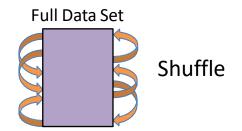
• Line plot of learning (y-axis) over experience (x-axis).

#### Time for Terms

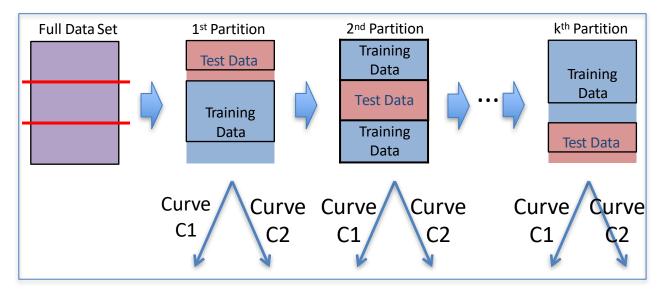
- Train Learning Curve: Learning curve calculated from the training dataset that gives an idea of how well the model is learning.
- Validation Learning Curve: Learning curve calculated from a hold-out validation dataset that gives an idea of how well the model is generalizing.
- Optimization Learning Curves: Learning curves calculated on the metric by which the parameters of the model are being optimized, e.g. loss.
- **Performance Learning Curves**: Learning curves calculated on the metric by which the model will be evaluated and selected, e.g. accuracy.

#### **Building Learning Curves**

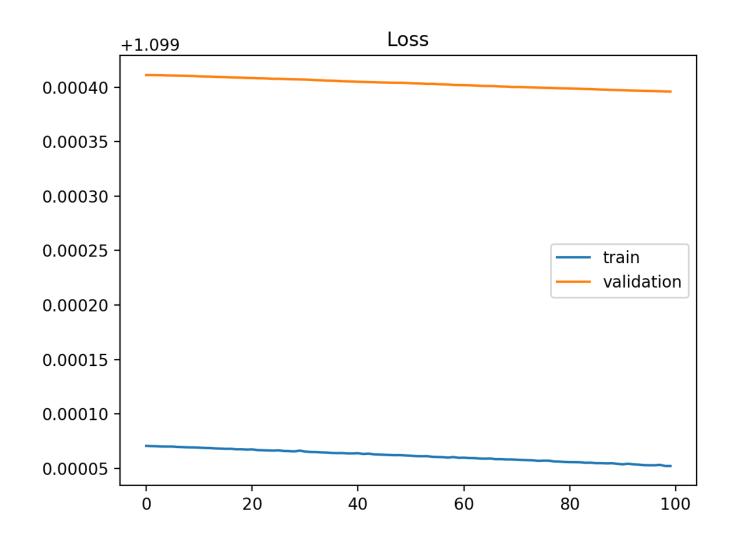
a.) Randomize
Data Set



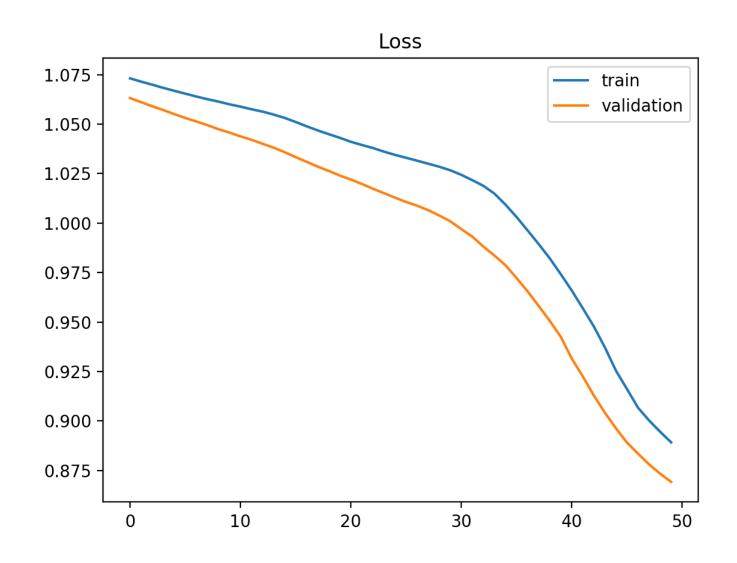
b.) Perform k-fold CV



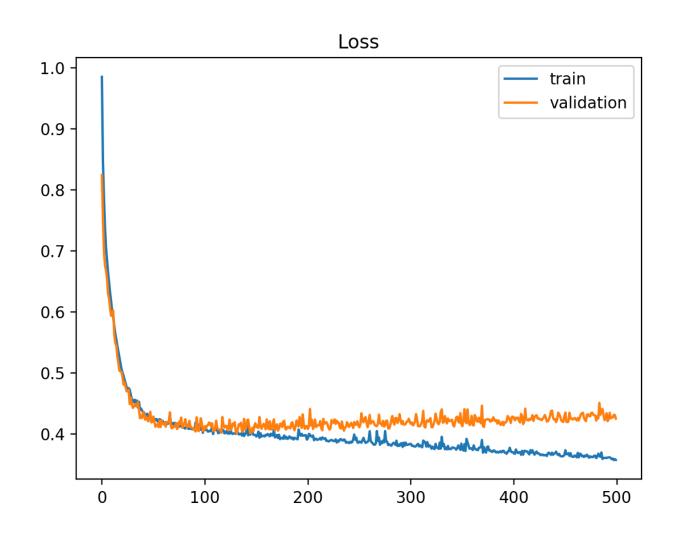
# Example of Training Learning Curve Showing An Underfit Model That Does Not Have Sufficient Capacity



# Example of Training Learning Curve Showing an Underfit Model That Requires Further Training



# Example of Train and Validation Learning Curves Showing an Overfit Model



# Example of Train and Validation Learning Curves Showing a Good Fit

