NCERT QUESTIONS WITH SOLUTIONS

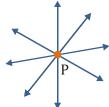
EXERCISE: 5.1

- **1.** Which of the following statements are true and which are false? Give reasons for your answers.
 - (i) Only one line can pass through a single point.
 - (ii) There are an infinite number of lines which pass through two distinct points.
 - (iii) A terminated line can be produced indefinitely on both the sides.
 - (iv) If two circles are equal, then their radii are equal.
 - (v) In Fig., if AB = PQ and PQ = XY, then AB = XY.



Sol. (i) False, because infinitely many lines can pass through a single point.

This is self evident and can be seen visually by the student as follows:



(ii) False, because the given statement contradicts the postulate I of the Euclid that assures that there is a unique line that passes through two distinct points.



Through two points P and Q, a unique line can be drawn.

(iii) True,

Evidence: According to Euclid's postulate 2; a terminated line can be produced indefinitely.



(iv) True,

Evidence: According to the axiom 4 of Euclid; that "the things which coincide with one another are equal to one another". If we superimpose the region bounded by one circle on the other, then they coincide. So, their centres and boundaries coincide. Therefore, their radii will coincide.

- (v) True,
 Evidence: Euclid's axiom 1 states that
 the things which are equal to the
 same thing are equal to one another.
- 2. Give a definition for each of the following terms. Are there other terms that need to be defined first? What are they and how might you define them?
 - (i) parallel lines
 - (ii) perpendicular lines
 - (iii) line segment
 - (iv) radius of a circle
 - (v) square
- Sol. (i) Parallel lines: Parallel straight lines are straight lines which, being in the same plane and being produced indefinitely in both directions, do not meet one another in either direction.

 Other term involved is the "plane".

 We keep the Plane as undefined term.

 The only thing is that we can represent it intuitively or explain it with the help of physical model.

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- (ii) Perpendicular lines: When a straight line set up on a straight line makes the adjacent angles equal to one another, each of equal angle is right and the straight line standing on the other is called a perpendicular to that on which it stands. The other terms that need to be defined first is (1) Angle (2) Adjacent angles (3) Right angle. Let us define these.
- (1) Angle: A plane angle is the inclination to one another of two lines in a plane which meet one another and do not lie in a straight line.
- (2) Adjacent angles: The two angles with the same vertex, one arm common and other arms lying on the opposite sides of the common arm are called adjacent angles.
- (3) Right angle: An angle equal to one quarter of a complete angle is called a right angle.
 - extends indefinitely in both directions gives a line.
 Other term involved is line. We keep the line as undefined term. The only thing is that we can represent it intuitively or explain it with the help of physical model.

(iii) Line segment: A line segment which

- (iv) Radius of a circle: A line segment joining the centre to any point on the circle is called the radius of the circle.Other terms that need to be defined first are:
- (1) Circle (2) Centre. Let us define these:
- (1) Circle: A circle is a closed curve on a plane, all points on which are at the same distance from a fixed point which is centre.

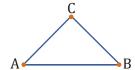
- (2) Centre of circle: The fixed point from which all the points on a circle are equidistant is called its centre.
 - (v) Square: Of quadrilateral figures, a square is that which is both equilateral and right-angled. Other terms that need to be defined first are
 - (1) equilateral
 - (2) right angle. Let us define these.
- (1) Equilateral : A figure having all its sides equal is called an equilateral.
- (2) Right angle: An angle equal to one quarter of a complete angle is called a right angle.
- **3.** Consider two 'postulates' given below :
 - (i) Given any two distinct points A and B, there exists a third point C which is in between A and B.
 - (ii) There exist at least three points that are not on the same line.Do these postulates contain any undefined terms? Are these postulates consistent? Do they follow from Euclid's postulates? Explain.
- **Sol.** There are several undefined terms which are to be listed by a student. These two postulates (i) and (ii) are consistent because they deal with two different situations.

Postulate (i) states that given two points A and B, there is a point C lying on the line in between them.



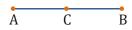


Postulate (ii) states that for given two points A and B, we can take point C not lying on the line through A and B.



Hence, we observe that the postulates do not follow from Euclid's postulates, however they follow from Axiom 1.

- **4.** If a point C lies between two points A and B such that AC = BC, then prove that AC = $\frac{1}{2}$ AB. Explain by drawing the figure.
- **Sol.** Given that C lies between A and B



And AC = BC So, AC + AC = BC + AC

[: according to Euclid's Axiom-2, if equals are added to equals, the wholes are equal]

i.e.,
$$2AC = AB$$

[BC + AC coincides with AB]

Therefore, AC =
$$\frac{1}{2}$$
 AB

- 5. In Question 4, point C is called a mid-point of line segment AB. Prove that every line segment has one and only one mid-point.
- **Sol.** Let C and D be the two mid-points of line segment AB.

So, according to Euclid's axiom (4) when line is folded about point C we observe that part BC superimposes over the part AC. It implies that

$$AC = BC \qquad ... (1)$$

Similarly, D is the midpoint of AB implies

that
$$AD = BD$$
 ... (2)

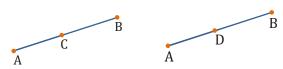
we have, AB = AB

or
$$AC + BC = AD + BD$$

or
$$AC + AC = AD + AD$$
 [Using (1) and (2)]

or
$$2AC = 2AD$$

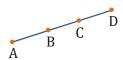
or
$$AC = AD$$
 ... (3)



When we superimpose AD over AC and BD over BC we find that D exactly lies over C. It implies that D and C are not two different points but the same.

Hence, we conclude that mid-point of a line segment is unique.

6. In Fig., if AC = BD, then prove that AB = CD.



Sol. Given that
$$AC = BD$$
 ... (1)

$$AC = AB + BC$$

$$BD = BC + CD$$

(point C lies between B and D) ... (3)

Substituting (2) and (3) in (1), we get

$$AB + BC = BC + CD$$

Subtracting BC from both sides, we get

$$AB + BC - BC = BC + CD - BC$$

So,
$$AB = CD$$

(: if equals are subtracted from equals,

the remaining are equal)

- 7. Why is axiom 5, in the list of Euclid's axioms, considered a 'universal truth'? (Note that the question is not about the fifth postulate.)
- **Sol.** Euclid's Axiom 5 states that "The whole is greater than the part."

Since, this is true for anything in any part of the world.

So, this is a universal truth.

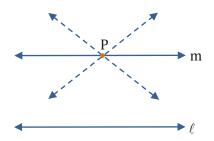
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- **1.** How would you rewrite Euclid's fifth postulate so that it would be easier to understand?
- Sol. There are several easy equivalent versions of Euclid's fifth postulate.

 Playfair's axiom is one of the other equivalent versions of Euclid's fifth postulate which is easily understandable.

 According to it,

For every line ℓ and for every point P not lying on ℓ , there exists a unique line m passing through point P and is parallel to ℓ . Clearly, if all lines passing through the point P, only line m is parallel to line ℓ .



Other equivalent versions of Euclid's fifth postulate are as follows:

According to Poseidonios; If two lines never meet no matter how much they are produced; then they are equidistant. (100 B.C.)

According to Proclus; The distance between a pair of parallel infinite straight lines (may fluctuate but) remain less than a certain fixed distance (5th century).

According to Clauvius; all the points equidistant from a given straight line, on a given side of it, constitute a straight line (1574).

- **2.** Does Euclid's fifth postulate imply the existence of parallel lines? Explain.
- **Sol.** Yes. Euclid's fifth postulate is valid for parallelism of lines because if a straight line ℓ falls on two straight lines m and n such that sum of the interior angles on one side of ℓ is two right angles, then by Euclid's fifth postulate the line will not meet on this side of ℓ . Next, you know that the sum of the interior angles on the other side of line ℓ will also be two right angles.

Therefore, they will not meet on the other side also. So, the lines m and n never meet and are therefore, parallel.

