CSE102 Computer Programming with C

2016-2018 Spring Semester

Dynamic Data Structures

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Largely adapted from J.R. Hanly, E.B. Koffman, F.E. Sevilgen, and others...

Introduction

- Dynamic data structures: expands and contracts as the program executes
 - Decision on space is made during execution
 - Array: decision is made beforehand
 - Partially filled array is possible but still maximum size is decide before compilation
 - Required dynamic memory allocation
 - Allocate space as necessary during execution
- Linked list: linear sequence of nodes
 - Nodes: a structure that points another structure
 - Can be used to form lists, stacks, queues

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Pointers

- Used extensively for dynamic data structures
- Pointer Review:
 - Reference / indirect access

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Comparison of Pointer and Nonpointer Variables nump num Reference **Explanation** Value Direct value of num num Direct value of nump Pointer to location containing 3 nump 3 Indirect value of nump *nump May 2018 CSE102 Lecture 11

Pointers

- Used extensively for dynamic data structures
- Pointer Review:
 - Reference / indirect access
 - Function parameters
 - Output parameter (Ex: long division)
 - · Input parameter

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Pointers as Output Parameters

```
void long division(int dividend, int divisor, int *quotientp,
                         int *remainderp);
        long_division(40, 3, &quot, &rem);
       printf("40 divided by 3 yields quotient %d ", quot);
13.
14.
15.
16.
17.
18.
19.
20.
21.
22.
23.
24.
25.
        printf("and remainder %d\n", rem);
    * Performs long division of two integers, storing quotient
     * in variable pointed to by quotientp and remainder in
     * variable pointed to by remainderp
    void long_division(int dividend, int divisor, int *quotientp,
                         int *remainderp)
        *quotientp = dividend / divisor;
        *remainderp = dividend % divisor:
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```

Pointers

- Used extensively for dynamic data structures
- Pointer Review:
 - Reference / indirect access
 - Function parameters
 - Output parameter (Ex: long division)
 - · Input parameter
 - Representing arrays and strings
 - · Passing as a parameter
 - Pointers to structures
 - File pointers

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Pointers

- Used extensively for dynamic data structures
- · Pointer Review:
 - Reference / indirect access
 - Function parameters
 - Representing arrays and strings
 - Pointers to structures
- · Operations with pointers
 - Indirection
 - Assignment
 - Equality operators (== , !=)
 - Increment, decrement

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Dynamic Memory Allocation

• Pointer declaration does not allocate memory for values.

```
double * nump;
```

• Use function malloc to allocate memory

```
malloc(sizeof(double))
```

- Allocates number of bytes defined by the parameter
- Memory allocated in the heap (not stack)
- Returns a pointer to the block allocated
- Memory allocated by malloc could be used to store any value
- What should be the return type? (type of the pointer)

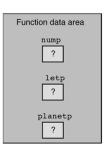
```
void * nump = (double*)malloc(sizeof(double));
```

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Three Pointer-Type Local Variables

```
int *nump;
char *letp;
planet_t *planetp;
```

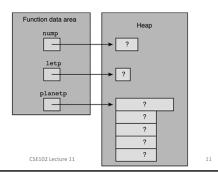


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Dynamic Allocation of Variables

nump = (int *)malloc(sizeof(int));
letp = (char *)malloc(sizeof(char));
planetp = (planet_t *)malloc(sizeof(planet_t));



Assignments to Dynamically Allocated Variables

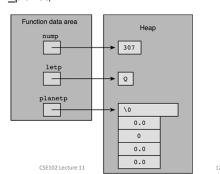
*nump = 307;

*letp = 'Q';

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*planetp = blank_planet;



Components of Dynamically Allocated Structure

Indirection + component selection

```
(*planetp).name
```

· Indirect component selection

planetp->name

```
    printf("%s\n", planetp->name);
    printf(" Equatorial diameter: %.0f km\n", planetp->diameter);
    printf(" Number of moons: %d\n", planetp->moons);
    printf(" Time to complete one orbit of the sun: %.2f years\n",
    planetp->orbit_time);
    printf(" Time to complete one rotation on axis: %.4f hours\n",
    planetp->rotation_time);
```

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Allocation of Arrays with calloc

- malloc: to allocate single memory block
- calloc: to dynamically create array of elements
 - Elements of any type (built-in or user defined)
- calloc: two arguments
 - Number of elements
 - Size of one element
- Allocates the memory and initializes to zero
- Returns a pointer

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Allocation of Arrays with calloc

```
#include <stdlib.h> /* gives access to calloc */
     int scan_planet(planet_t *plnp);
    main(void)
                     *array of nums;
          planet_t *array_of_planets;
                     str siz, num nums, num planets, i;
          printf("Enter string length and string> ");
           scanf("%d", &str siz);
13.
14.
15.
16.
17.
18.
19.
20.
21.
22.
23.
24.
25.
          string1 = (char *)calloc(str_siz, sizeof (char));
          scanf("%s", string1);
          printf("\nHow many numbers?> ");
          scanf("%d", &num_nums);
           array_of_nums = (int *)calloc(num_nums, sizeof (int));
          array_of_nums[0] = 5;
          for (i = 1; i < num_nums; ++i)
                 array_of_nums[i] = array_of_nums[i - 1] * i;
          printf("\nEnter number of planets and planet data> ");
           scanf("%d", &num planets);
           array_of_planets = (planet_t *)calloc(num_planets,
                                       CSE102 Lecture 15izeof (planet_t));
```

Allocation of Arrays with calloc

```
for (i = 0; i < num planets; ++i)
           scan_planet(&array_of_planets[i]);
                                                                      e n o r m o u s \0
Enter string length and string> 9 enormous
                                                    array_of_nums
How many numbers?> 4
Enter number of planets and planet data> 2
                                                                           10
Earth 12713.5 1 1.0 24.0
                                                                           30
Jupiter 142800.0 4 11.9 9.925
                                                   array_of_planet
                                                                       Earth\0
                                                                        1.27135e+4
                                                                           24.0
                                                                       Jupiter\0
                                                                         1.428e+5
                                                                           11.9
                                                                          9.925
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```

Returning Memory

- free: returns memory cells to heap
 - Allocated by calloc or malloc
 - Returned memory can be allocated later

free(nump);

free(array_of_planets);

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double *xp, *xcopyp; xp = (double *)malloc(sizeof(double)); *xp = 49.5; xcopyp = xp; free(xp); *xcopyp = 52.25; Heap xcopyp xcopyp

Linked Lists

- A sequence of nodes
 - Each node is connected to the following one
 - Like pop beads
 - · A chain can be formed easily
 - Modified easily (remove and insert)





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Reminder on typedef and Struct

• We use:

typedef struct { ... } myType;

Tag namespace

struct myType { ... };

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Reminder on typedef and Struct

```
• We use:
```

myType x;

```
typedef struct { ... } myType;
• Tag namespace
    struct myType { ... };
```

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Reminder on typedef and Struct

```
• We use:
```

```
typedef struct { ... } myType;
```

• Tags — names of structures, unions and enums

```
struct myType { ... };
myType x;
```

· Correct version should be

```
struct myType x;
```

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Reminder on typedef and Struct

• We use:

```
typedef struct { ... } myType;
```

• Tag namespace

```
struct myType { ... };
myType x;
```

Need typedef ...

```
struct myType { ... };
typedef struct myType myType;
```

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Reminder on typedef and Struct

• Or use an abbreviation ...

```
typedef struct myType { ... } myType;
```

• Or declare an anonymous structure and ...

```
typedef struct { ... } myType;
```

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Node Structure

- Structure with pointer components
- Allocate a node as necessary
 - And connect then to form a linked list

```
typedef struct node_s {
    char current[3];
    int volts;
    struct node_s * linkp;
} node_t;
```

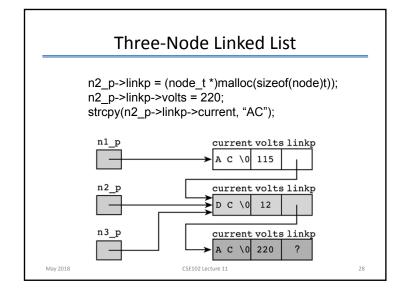
Use a structure tag

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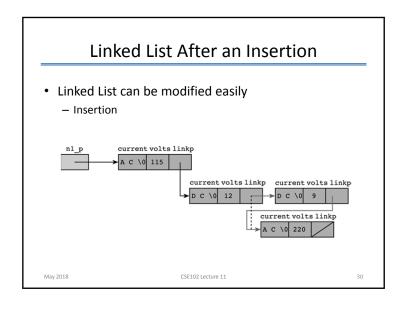
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Linking Two Nodes n1_p->linkp = n2_p; current volts linkp n2_p current volts linkp D C \ 0 12 ?

Multiple Pointers to the Same Structure node_t *n1_p, *n2_p, *n3_p; n1_p = (node_t *)malloc(sizeof(node_t)); n1_p->volts = 115; n2_p = (node_t *)malloc(sizeof(node_t)); n2 p->volts = 12; $n3_p = n2_p;$ n1_p current volts linkp 115 n2_p current volts linkp 12 n3_p May 2018 CSE102 Lecture 11



Three-Element Linked List • List head • End of list indicator • Empty list **Current volts linkp** **CSEIQ2 Lecture 11** **Description** **Comparison** **Comparison



Linked List After a Deletion • Linked List can be modified easily — Insertion — Deletion • Deletion May 2018 CSE102 Lecture 11 31

Linked List Operations

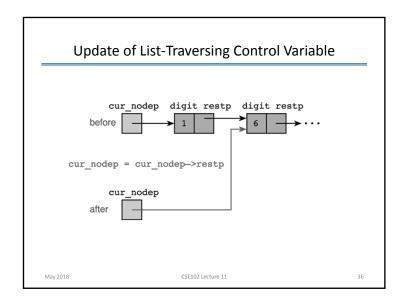
• Assume following declaration

- Traversing a list
 - Process each node in sequence
 - Start with the list head and follow list pointers
- Operations should take list head as a parameter

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1. /* 2. * Displays the list pointed to by headp 3. */ 4. void 5. print_list(list_node_t *headp) 6. { May 2018 CSE102 Lecture 11 33

Recursive and Iterative List Printing • Tail recursion: recursive call is at the last step - Easy to convert it to recursion /* Displays the list pointed to by headp */ print_list(list_node_t *headp) { list_node_t *cur_nodep; if (headp == NULL) {/* simple case */ printf("\n"); for (cur_nodep = headp; /* start at } else { beginning ' /* recursive step */ printf("%d", headp->digit); cur_nodep != NULL; /* not at print list(headp->restp); end yet cur_nodep = cur_nodep->restp) printf("%d", cur_nodep->digit); printf("\n"); May 2018 CSE102 Lecture 11



Recursive Function get_list

```
1. #include <stdlib.h> /* gives access to malloc */
2. #define SENT -1
3. /*
4. * Forms a linked list of an input list of integers
5. * terminated by SENT
6. */
7. list_node_t *
8. get_list(void)
9. {

May 2018 CSE102 Lecture 11 37
```

Recursive Function get_list

```
1. #include <stdlib.h> /* gives access to malloc */
2. #define SENT -1
3. /*
4. * Forms a linked list of an input list of integers
5. * terminated by SENT
6. */
7. list_node t*
8. get_list(void)
9. {
10. int data;
11. list_node_t *ansp;
12.
13. scanf("%d", &data);
14. if (data == SENT) {
    ansp = NULL;
15. } else {
    ansp = NULL;
17. ansp->digit = data;
19. ansp->restp = get_list();
19. }
20. }
21. return (ansp);
22. return (ansp);
23. }

Response of the first contents of the contents
```

```
* Forms a linked list of an input list of integers terminated by SENT
get_list(void)
     restp component is unfilled
                             /* pointer to newly allocated node
      /* Builds first node, if there is one */
      scanf("%d", &data);
if (data == SENT) {
            ansp = NULL;
      } else {
            ansp = (list_node_t *)malloc(sizeof (list_node_t));
ansp->digit = data;
to_fillp = ansp;
            /\star Continues building list by creating a node on each
               iteration and storing its pointer in the restp component of the
               node accessed through to_fillp */
            for (scanf("%d", &data);
                  data != SENT;
                  scanf("%d", &data)) {
                newp = (list_node_t *)malloc(sizeof (list_node_t));
newp->digit = data;
                to_fillp->restp = newp;
to_fillp = newp;
            /* Stores NULL in final node's restp component */
            to_fillp->restp = NULL;
      return (ansp);
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```

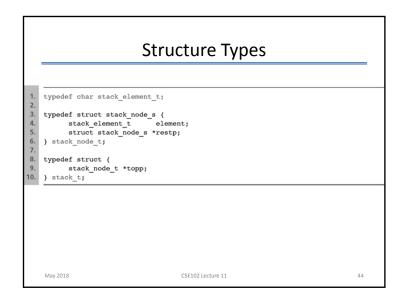
Function search

```
1. /*
2. * Searches a list for a specified target value. Returns a pointer to
3. * the first node containing target if found. Otherwise returns NULL.
4. */
5. list_node_t *
6. search(list_node_t *headp, /* input - pointer to head of list */
7. int target) /* input - value to search for */
8. {

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```


Stack May 2018 CSE102 Lecture 11 42

Linked List Representation of Stacks • Stack can be implemented using array • Stack = LIFO List — Linked list can be used Stack of three characters Stack after insertion (push) of '/' Stack after insertion (push) of '/'



Stack Manipulation with push and pop 1. /* 2. * Creates and manipulates a stack of characters 3. */ 4. *include <stdio.h> 6. *include <stdlib.h> 7. 8. /* Include typedefs from Fig. 14.24 */ 9. void push(stack_t *sp, stack_element_t c); stack_element_t pop(stack_t *sp); (continued) May 2018 CSE102 Lecture 11 45

```
Stack Manipulation with push and pop
    #include <stdio.h>
     #include <stdlib.h>
    /* Include typedefs from Fig. 14.24 */
9. vo
10. st
11. in
12. ma
13. {
14.
15.
16.
17.
20.
21.
22.
23.
24.
25.
26.
27.
28.
29.
30.
     void push(stack_t *sp, stack_element_t c);
    stack_element_t pop(stack_t *sp);
int
     main(void)
           stack_t s = {NULL}; /* stack of characters - initially empty */
          /* Builds first stack of Fig. 14.23
          push(&s, '2');
           push(&s, '+');
           push(&s, 'C');
           /* Completes second stack of Fig. 14.23 */
           push(&s, '/');
           /* Empties stack element by element
           printf("\nEmptying stack: \n");
           while (s.topp != NULL) {
                 printf("%c\n", pop(&s));
           return (0);
                                      CSE102 Lecture 11
```

```
* The value in c is placed on top of the stack accessed through sp
35. * P
36. */
37. void
     * Pre: the stack is defined
                      *sp, /* input/output - stack
    push(stack t
         stack_element_t c) /* input
                                             - element to add */
          stack node t *newp; /* pointer to new stack node */
          /* Creates and defines new node
          newp = (stack_node_t *)malloc(sizeof (stack_node_t));
          newp->element = c;
          newp->restp = sp->topp;
          /* Sets stack pointer to point to new node
           sp->topp = newp;
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```

```
* Removes and frees top node of stack, returning character value
* stored there.
* Pre: the stack is not empty
stack element t
pop(stack_t *sp) /* input/output - stack */
      stack_node_t *to_freep; /* pointer to node removed */
     stack_element_t ans;
                               /* value at top of stack */
                                   /* saves pointer to node being deleted
     to_freep = sp->topp;
                                   /* retrieves value to return
      ans = to_freep->element;
     sp->topp = to_freep->restp;
                                  /* deletes top node
     free(to_freep);
                                   /* deallocates space
      return (ans);
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```

Queue

- Queue = FIFO List
- EX: Model a line of customers waiting at a checkout counter
- Need to keep both ends of a queue
 - Front and rear

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A Queue of Passengers Brown Watson Carson F(irstClass) q.frontp q.rearp q.size 3

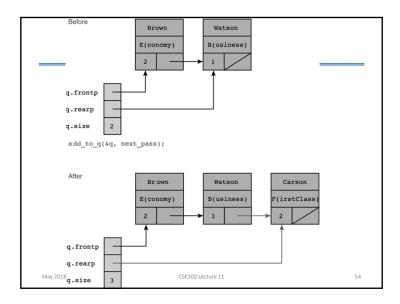
Structure Types

```
* Creates and manipulates a queue of passengers.
   int scan_passenger(queue_element_t *passp);
  void print_passenger(queue_element_t pass);
  void add_to_q(queue_t *qp, queue_element_t ele);
  queue_element_t remove_from_q(queue_t *qp);

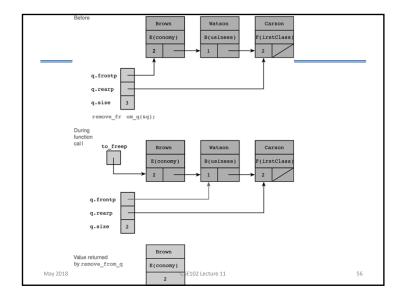
    void display_q(queue_t q);

  int
  main(void)
         queue_t pass_q = {NULL, NULL, 0}; /* passenger queue - initialized to
                                             empty state */
         queue element t next pass, fst pass;
         char choice; /* user's request */
         /* Processes requests */
            printf("Enter A(dd), R(emove), D(isplay), or Q(uit)> ");
             scanf(" %c", &choice);
            switch (toupper(choice)) {
            case 'A':
                  printf("Enter passenger data> ");
                  scan_passenger(&next_pass);
                  add_to_q(&pass_q, next_pass);
                                                                              52
```

```
case 'R':
               if (pass_q.size > 0) {
                     fst_pass = remove_from_q(&pass_q);
                     printf("Passenger removed from queue: \n");
                     print_passenger(fst_pass);
               } else {
                     printf("Queue empty - noone to delete\n");
               break;
         case 'D':
               if (pass_q.size > 0)
                     display_q(pass_q);
                     printf("Queue is empty\n");
               break;
         case 'Q':
               printf("Leaving passenger queue program with %d n",
                      pass_q.size);
               printf("passengers in the queue\n");
         default:
               printf("Invalid choice -- try again\n");
     } while (toupper(choice) != 'Q');
May 2018return (0);
                                CSE102 Lecture 11
                                                                          53
```



```
* Adds ele at the end of queue accessed through qp
* Pre: queue is not empty
*/
void
                       *qp, /* input/output - queue */
add_to_q(queue_t
        queue_element_t ele) /* input - element to add */
                                        /* adds to empty queue
     if (qp->size == 0) {
           qp->rearp = (queue_node_t *)malloc(sizeof (queue_node_t));
           qp->frontp = qp->rearp;
                                        /* adds to nonempty queue
     } else {
           qp->rearp->restp =
                 (queue_node_t *)malloc(sizeof (queue_node_t));
           qp->rearp = qp->rearp->restp;
     qp->rearp->element = ele;
                                        /* defines newly added node
                                                                             */
     qp->rearp->restp = NULL;
     ++(qp->size);
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                                                                          55
```



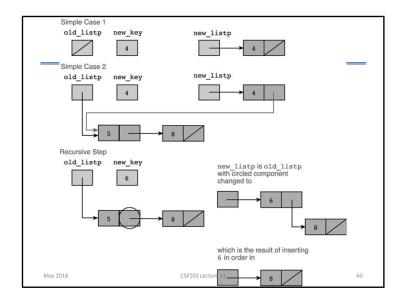
```
* Removes and frees first node of queue, returning value stored there.
   queue_element_t
   remove_from_q(queue_t *qp) /* input/output - queue */
28.
        queue_node_t *to_freep; /* pointer to node removed
        queue_element_t ans;
                                      /* initial queue value which is to
                                        be returned
                                            /* saves pointer to node being deleted */
         to_freep = qp->frontp;
         ans = to_freep->element;
                                            /* retrieves value to return
         qp->frontp = to_freep->restp;
                                            /* deletes first node
         free(to_freep);
                                            /* deallocates space
         --(qp->size);
         if (qp->size == 0)
                                            /* queue's ONLY node was deleted
               qp->rearp = NULL;
         return (ans);
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```

```
Case Study: Ordered Lists
   • The position of elements is determined by their key value

    Increasing or decreasing order

    * Program that builds an ordered list through insertions and then modifies
3.
    * it through deletions.
6. typedef struct list_node_s {
         struct list_node_s *restp;
9. } list_node_t;
10.
11. typedef struct {
       list_node_t *headp;
        int
                    size;
14. } ordered_list_t;
16. list_node_t *insert_in_order(list_node_t *old_listp, int new_key);
17. void insert(ordered_list_t *listp, int key);
18. int delete(ordered list t *listp, int target);
19. void print_list(ordered_list_t list);
                                  CSE102 Lecture 11
   #define SENT -999
```

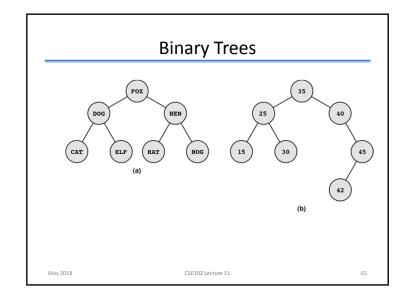
```
main(void)
25.
26.
                            next_key;
27.
            ordered_list_t my_list = {NULL, 0};
28.
29.
30.
31.
32.
33.
34.
35.
36.
37.
38.
39.
40.
41.
42.
43.
44.
45.
46.
47.
48.
49.
50.
51.
            /* Creates list through in-order insertions */
            printf("Enter integer keys--end list with %d\n", SENT);
           for (scanf("%d", &next_key);
                 next key != SENT;
                  scanf("%d", &next_key)) {
                 insert(&my_list, next_key);
            /* Displays complete list */
            printf("\nOrdered list before deletions:\n");
            print_list(my_list);
            /* Deletes nodes as requested */
            printf("\nEnter a value to delete or %d to quit> ", SENT);
            for (scanf("%d", &next_key);
                   next key != SENT;
                   scanf("%d", &next_key)) {
                 if (delete(&my_list, next_key)) {
                       printf("%d deleted. New list:\n", next_key);
                       print_list(my_list);
                } else {
                       printf("No deletion. %d not found\n", next key);
52.
53.
54.
                                          CSE102 Lecture 11
            return (0);
```

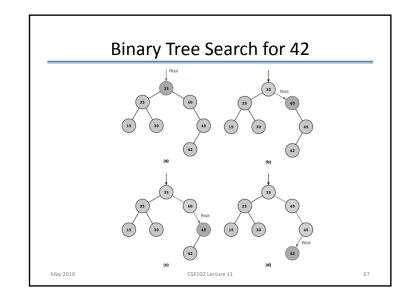


```
Deletes first node containing the target key from an ordered list.
          Returns 1 if target found and deleted, 0 otherwise.
delete(ordered_list_t *listp, /* input/output - ordered list */
    int target) /* input - key of node to delete */
         /* pointer to node to delete
                                                                                                          /* pointer used to traverse list until it
                                                                                                                   points to node preceding node to delete
                                      is_deleted;
           /★ If list is empty, deletion is impossible
          if (listp->size == 0) (
is_deleted = 0;
           /* If target is in first node, delete it
          } else if (listp->headp->key == target) {
   to_freep = listp->headp;
                           listp->headp = to_freep->restp;
                            --(listp->size);
                           is deleted = 1;
            /* Otherwise, look for node before target node; delete target */
                           cur_nodep=vestp != nous es cur_nodep=vestp () {
  if (cur_nodep=vestp != NULL && cur_nodep=vestp + vestp = vur_nodep=vestp != vur_nodep=vestp | cur_nodep=vestp = vur_nodep=vestp | cur_nodep=vestp = vur_nodep=vestp | cur_nodep=vestp = vestp | vestp = vestp = vestp | vestp = vestp = vestp = vestp | vestp = vestp =
                                      free(to_freep);
--(listp->size);
                                       is deleted = 1;
                                       is_deleted = 0;
          return (is deleted);
                                                                                                                   CSE102 Lecture 11
                                                                                                                                                                                                                                                                                                                         62
```

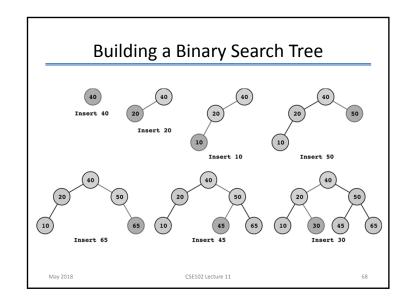
```
/*
    * Deletes first node containing the target key from an ordered list.
    * Returns 1 if target found and deleted, 0 otherwise.
    */
5.
   int
   delete(ordered_list_t *listp, /* input/output - ordered list */
                        target) /* input - key of node to delete */
8.
         int is deleted;
10.
         listp->headp = delete_ordered_node(listp->headp, target,
                                               &is deleted);
13.
         if (is deleted)
               --(listp->size);
         return (is_deleted);
    May 2018
                                    CSE102 Lecture 11
                                                                              63
```

```
* If possible, deletes node containing target key from list whose first
* node is pointed to by listp, returning pointer to modified list and
          freeing deleted node. Sets output parameter flag to indicate whether or
5. 6. 7. 8. 9. 10. 11. 12. 13. 14. 15. 16. 17. 18. 19. 20. 21. 22. 23. 24. 29. 30. 31. 32. 24. 35. 36. 37. 38. 36. 37. 38. 39. 40. 8 41.
      list node t *
       delete_ordered_node(list_node_t *listp,
                                                         /* input/output - list to modify */
/* input - key of node to delete */
                              int
                                              target,
                                              *is_deletedp) /* output - flag indicating
whether or not target node
                                                                      found and deleted
            list_node_t *to_freep, *ansp;
              /* if list is empty - can't find target node - simple case 1 */
             if (listp == NULL) {
                     *is_deletedp = 0;
             /* if first node is the target, delete it
            } else if (listp->key == target) {
                     *is_deletedp = 1;
to_freep = listp;
                      ansp = listp->restp:
                     free(to_freep);
             /* if past the target value, give up
                                                                             - simple case 3
            } else if (listp->key > target) {
   *is_deletedp = 0;
                     ansp = listp;
             /* in case target node is farther down the list, - recursive step
                  have recursive call modify rest of list and then return list
                     ansp = listp;
ansp->restp = delete_ordered_node(listp->restp, target,
                                                                is deletedp);
             return (ansp):
                                                CSE102 Lecture 11
                                                                                                                            64
```





• How to implement? May 2018 CSE102 Lecture 11 66



Creating a Binary Search Tree

```
18. int
19. main(void)
20. {
21. tree
22. int
23. int
24. 25. bs_t
26. 27. /* A
28. d
29. for
30. 31.
32.
33.
34. 35. }
36. 37. if
38. 39. } (
40. 41.
42. }
43. 44. re
45. }
46. May 2018
                  tree_node_t *bs_treep; /* binary search tree
                                 data_key; /* input - keys for tree
                                 status:
                                               /* status of input operation
                 bs_treep = NULL; /* Initially, tree is empty */
                 /* As long as valid data remains, scan and insert keys,
                     displaying tree after each insertion. */
                  for (status = scanf("%d", &data_key);
                        status == 1;
                        status = scanf("%d", &data key)) {
                      bs_treep = tree_insert(bs_treep, data_key);
                      printf("Tree after insertion of %d:\n", data key);
                      tree_inorder(bs_treep);
                 if (status == 0) {
                        printf("Invalid data >>%c\n", getchar());
                         printf("Final binary search tree:\n");
                         tree inorder(bs treep);
                 return (0);
                                                   CSE102 Lecture 11
```

```
* Insert a new key in a binary search tree. If key is a duplicate,
* there is no insertion.
* Pre: rootp points to the root node of a binary search tree
* Post: Tree returned includes new key and retains binary
         search tree properties.
tree node t *
tree_insert(tree_node_t *rootp, /* input/output - root node of
                                   binary search tree */
                        new_key) /* input - key to insert */
     if (rootp == NULL) {
                                     /* Simple Case 1 - Empty tree */
           rootp = TYPED_ALLOC(tree_node_t);
           rootp->key = new key;
           rootp->leftp = NULL;
           rootp->rightp = NULL;
     } else if (new key == rootp->key) {
                                                    /* Simple Case 2 */
           /* duplicate key - no insertion
     } else if (new key < rootp->key) {
                                                    /* Insert in
                                                    /* left subtree */
           rootp->leftp = tree_insert
                           (rootp->leftp, new_key);
                                   /* Insert in right subtree */
           rootp->rightp = tree_insert(rootp->rightp,
                                      new_key);
      return (rootp);
                                CSE102 Lecture 11
```