## **20MCA14**

- 5 a. Define partial order relation R defined on the set A. Let A = {1, 2, 3, 4, 6, 12}, define the relation R by aRb, if and only if a divides b. Prove that R- is a partial order on A, draw (06 Marks)

  Hasse diagram for the relation.
  - b. Consider  $A = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$ . The relation R is defined as  $(x, y) \in R$ , if and only if x y is multiple of 5. Verify that R- is an equivalence relation. (07 Marks)
  - c. Let  $A = \{1, 2, 3\}$ , and  $B = \{1, 2, 3, 4\}$ . The relations R and S from A to B are represented by the matrices.

$$\mathbf{M}_{R} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{bmatrix}, \quad \mathbf{M}_{S} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}$$

Determine the relations  $\overline{R}$ ,  $\overline{S}$ ,  $R \cup S$ ,  $R \cap S$ ,  $S^c$  and their matrix representations. (07 Marks)

- a. Let A = {1, 2, 3, 4, 6} and R be the relation on A defined by aRb if and only if a is multiple of b. Represent the relation R as a matrix and draw its diagraph. (06 Marks)
  - b. Let A = {a, b, c}, and R and S be relations on A whose matrices are given as

$$\mathbf{M}_{R} = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 1 \\ 0 & 1 & 0 \end{bmatrix}; \quad \mathbf{M}_{S} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix}$$

Find the composite relations ROS, SOR, ROR, SOS and their matrices.

- c. Let  $A = \{1, 2, 3, 4, 5\}$ . Define a relation R on  $A \times A$  by  $(x_1, y_1)$   $R(x_2, y_2)$  if and only if  $x_1 + y_1 = x_2 + y_2$ 
  - i) Verify that R- is an equivalence relation on A × A.
  - ii) Determine the equivalent classes [(1, 3)], [(2, 4)] and [(1, 1)]. (07 Marks)
- 7 a. The probability distribution function P(X) of a variate X is given by the following table.

X: 0 1 2 3 4 5 6 P(X): K 3K 5K 7K 9K 11K 13K

- i) For what value of K, above data represent a valid probability distribution.
- ii) Find P(X < 4),  $P(X \ge 5)$  and  $P(3 < X \le 6)$ . (06 Marks)
- b. Given 2% of fuses manufactured by a firm are defective. Find the probability that a box containing 200 fuses has
- i) At least one ii) 3 or more iii) exactly two, defective fuses. (07 Marks)
  c. In a test on electric bulbs, it was found that the life of a particular brand was distributed normally with an average life of 2000 hours and standard deviation of 60 hours. If a firm purchases 2500 bulbs find the number of bulbs that are likely to last for
  - i) More than 2100 hrs
  - ii) Less than 1950 hrs
  - iii) Between 1900 to 2100 hrs.

(07 Marks)

(07 Marks)

- 8 a. For the standard normal distribution of a random variable Z, evaluate the followings:
  - i)  $P(0 \le z \le 1.45)$  ii)  $P(-3-40 \le z \le 2.65)$
- iii)  $P(-2.55 \le z \le -0.8)$

(06 Marks)

iv)  $P(z \le -3.35)$ .

- b. The length of a telephone conversation has an exponential distribution with a mean of 3-minutes. Find the probability that a call ends.
- i) in less than 3-minutes ii) taken between 3 and 5 minutes.

(07 Marks)

c. A random variable X has the following probability function for various values of x

x:	0	1	2	3	4	5	6	7
p(x):	0	k	2k	2k	3k	k <sup>2</sup>	$2k^2$	$7k^2 + k$

i) Find k ii) evaluate p(x < 6),  $p(x \ge 6)$ ,  $p(3 < x \le 6)$ 

(07 Marks)