

Central limit theory:

Political view	Populats
1	5%
2	10%
3	15%
4	20%
5	20%
6	10%
7	10%
8	5%
9	3%
10	2%
100%	

any distribution

$$\begin{aligned} \text{true mean} &= 1(0.05) + 2(0.10) + \dots + 10(0.02) \\ &= 4.67 \end{aligned}$$

Sample 1000 times, 100 people each

$[u_1, u_2, \dots, u_{1000}] \rightarrow$  normal dist  
around mean of 4.67

# law of large numbers

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100%	

true  

$$\text{mean} = 1(0.05) + 2(0.10) + \dots + 10(0.02)$$

$$= 4.67$$

Sample  $\frac{n}{10}$  people,

$$\text{mean} \neq 4.67$$

Sample 100 people,

$$\text{mean} \rightarrow 4.67$$

Sample 1000 people

$$\text{mean} \approx 4.67$$

Sample entire population

$$\text{mean} = 4.67$$

$$\text{Sample Size } n = \left( \frac{Z \sigma}{E} \right)^2$$

$Z$  → Z score of confidence level  
 1.96 for 95%

$\sigma$  → sd of population

$E$  → margin of error desired

## Measures of Central tendency

$$\text{Mean}(x) \mu = E[x] = \int_{-\infty}^{\infty} x f(x) dx$$

$$\text{Var}(x) \text{ var}(x) = E(x - \mu)^2 = E(x - E[x])^2 = E(x^2) - (E[x])^2$$

$$\sigma = \sqrt{\text{var}(x)}$$

$$E(x|y=y) = \int_{-\infty}^{\infty} x f_{x|y}(x|y) dx$$

$$\text{cov}(x, y) = E((x - E[x])(y - E[y])) = E(xy) - (E[x])(E[y])$$

$$\rho(x, y) = \frac{\text{cov}(x, y)}{\sigma_x \sigma_y}$$

# Distributions

## Normal

histogram, QQ plot  
Shapiro-Wilk test  
Kolmogorov-Smirnov test

pdf

$$f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

Symmetric, mean = median = mode

## Binomial

## Normal (aka gaussian)

Uniform

Binomial

Poisson

Exponential

chi-sq

t-dist

F-dist

## Uniform



$$f(x) = \frac{1}{b-a}$$



Uniform Dist

$$f(x) = \frac{1}{b-a}$$

$$E[x] = \int_a^b x f(x) dx$$

$$= \int_a^b x \cdot \frac{1}{b-a} dx$$

$$= \frac{b+a}{2}$$

$$= \frac{1}{b-a} \left. \frac{x^2}{2} \right|_a^b = \frac{b^2 - a^2}{2(b-a)}$$

