DESCRIPTION

Reduce the time a Mercedes-Benz spends on the test bench.

Problem Statement Scenario: Since the first automobile, the Benz Patent Motor Car in 1886, Mercedes-Benz has stood for important automotive innovations. These include the passenger safety cell with a crumple zone, the airbag, and intelligent assistance systems. Mercedes-Benz applies for nearly 2000 patents per year, making the brand the European leader among premium carmakers. Mercedes-Benz is the leader in the premium car industry. With a huge selection of features and options, customers can choose the customized Mercedes-Benz of their dreams.

To ensure the safety and reliability of every unique car configuration before they hit the road, the company's engineers have developed a robust testing system. As one of the world's biggest manufacturers of premium cars, safety and efficiency are paramount on Mercedes-Benz's production lines. However, optimizing the speed of their testing system for many possible feature combinations is complex and time-consuming without a powerful algorithmic approach.

You are required to reduce the time that cars spend on the test bench. Others will work with a dataset representing different permutations of features in a Mercedes-Benz car to predict the time it takes to pass testing. Optimal algorithms will contribute to faster testing, resulting in lower carbon dioxide emissions without reducing Mercedes-Benz's standards.

Following actions should be performed:

- 1. If for any column(s), the variance is equal to zero, then you need to remove those variable(s).
- 2. Check for null and unique values for test and train sets.
- 3. Apply label encoder.
- 4. Perform dimensionality reduction.
- 5. Predict your test_df values using XGBoost.

```
# Create an ML algorithm that can accurately predict the time a car
will spend on the test bench
# based on the vehicle configuration

# Agenda
# 1. If for any column(s), the variance is equal to zero, then you
need to remove those variable(s)
# 2. Check for null and unique values for test and train sets
# 3. Apply label encoder for categorical variables
# 4. Perform dimensaionlity reduction with PCA
# 5. Predict the test_df values using xgboost
```

```
# import required libraries
import pandas as pd
import numpy as np
# load train dataset
train = pd.read csv("train.csv")
# first few rows of train dataset
train.head()
   ID
            y X0 X1 X2 X3 X4 X5 X6 X8
                                          . . .
                                               X375
                                                     X376 X377
                                                                  X378
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[5 rows x 378 columns]
# size of train dataset
print("Size of train dataset: {}".format(train.shape))
Size of train dataset: (4209, 378)
# train dataset info
train.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 4209 entries, 0 to 4208
Columns: 378 entries, ID to X385
dtypes: float64(1), int64(369), object(8)
memory usage: 12.1+ MB
# Get y train by separating y column as this is for prediction output
y train = train["y"].values
y train
array([130.81, 88.53, 76.26, ..., 109.22, 87.48, 110.85])
```

```
# loading test dataset
test = pd.read csv("test.csv")
test.head()
   ID X0 X1 X2 X3 X4 X5 X6 X8 X10
                                            X375 X376 X377
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X379 X380 \
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                  0
                         0
[5 rows x 377 columns]
# size of test dataset
print("Size of test dataset: {}".format(test.shape))
Size of test dataset: (4209, 377)
# info of test dataset
print(test.info())
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 4209 entries, 0 to 4208
Columns: 377 entries, ID to X385
dtypes: int64(369), object(8)
memory usage: 12.1+ MB
None
train.columns
Index(['ID', 'y', 'X0', 'X1', 'X2', 'X3', 'X4', 'X5', 'X6', 'X8',
       'X375', 'X376', 'X377', 'X378', 'X379', 'X380', 'X382', 'X383',
'X384',
       'X385'1.
      dtype='object', length=378)
# Creating the final dataset
# Removing unwanted columns ID, y from dataset
```

```
column = list(set(train.columns) - set(['ID', 'v']))
X train = train[column]
X test = test[column]
print (X train.shape)
print (X test.shape)
(4209, 376)
(4209, 376)
Check for NULL and unique value for test and train data sets
# check for NULL value
def IsNULL (df):
      if df.isnull().any().any():
             print ("YES")
      else:
             print ("NO")
IsNULL(X train)
IsNULL(X test)
NO
NO
## Exploratory Data Analysis (EDA)
# Integer Columns Analysis
unique value dict = {}
for col in X train.columns:
      if col not in ["ID", "y", "X0", "X1", "X2", "X3", "X4", "X5",
"X6", "X8"]:
             unique value = str(np.sort(X train[col].unique()).tolist())
             t list = unique value dict.get(unique value, [])
             t list.append(col)
             unique value dict[unique value] = t list[:]
for unique val, columns in unique value dict.items():
       print("Columns containing the unique values: {} Columns {}:
".format(unique val, columns))
print("-----
Columns containing the unique values: [0, 1] Columns ['X248', 'X272'
COLUMNS CONTAINING THE UNIQUE VALUES: [0, 1] COLUMNS ['X248', 'X272', 'X156', 'X204', 'X184', 'X240', 'X320', 'X221', 'X309', 'X165', 'X31', 'X367', 'X258', 'X236', 'X143', 'X364', 'X291', 'X328', 'X222', 'X88', 'X206', 'X161', 'X249', 'X343', 'X212', 'X215', 'X105', 'X85', 'X171', 'X119', 'X69', 'X102', 'X363', 'X207', 'X225', 'X90', 'X150', 'X344', 'X166', 'X47', 'X261', 'X44', 'X81', 'X368', 'X46', 'X211', 'X182', 'X37', 'X359', 'X378', 'X326', 'X369', 'X155', 'X253', 'X241', 'X29', 'X95', 'X71', 'X199', 'X179', 'X255', 'X76', 'X130', 'X73', 'X147', 'X299', 'X287', 'X109', 'X163', 'X126', 'X101', 'X218', 'X327', 'X349', 'X41', 'X128', 'X229', 'X82', 'X357', 'X177', 'X383', 'X21', 'X242', 'X323', 'X180', 'X66', 'X190', 'X60', 'X280', 'X42', 'X194',
```

```
'X247',
                                   'X315', 'X277', 'X244', 'X324', 'X238', 'X198',
'X115',
                                                                     'X87',
                                   'X350',
                                                     'X168',
                                                                                                     ′X113',
'X304',
                  'X264',
                                                                                    'X99',
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                                                  'X281', 'X84', 'X185', 'X57', 'X62', 'X123',
'X321',
                                   'X28',
                  'X282',
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                                   'X256',
                  'X237',
'X216',
                                                                                                                  'X75', 'X354'
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                  'X217',
                                   'X136',
                                                    'X232', 'X341', 'X65', 'X370', 'X195', 'X284',
                                                  'X311',
                                'X224',
                                                                   'X338',
                                                                                                       'X56', 'X18',
                                                                                     'X167',
                  'X54',
'X124'
                                                                                                                                       'X329'
                                'X154', 'X246', 'X306', 'X322', 'X53', 'X223', 'X50', 'X337', 'X189', 'X96', 'X48', 'X157', 'X139', 'X210', 'X245', 'X205', 'X382', 'X17', 'X305', 'X365', 'X376', 'X214', 'X226', 'X286', 'X52', 'X64', 'X144', 'X183', 'X15', 'X111', 'X183', 'X15', 'X111', 'X183', 'X15', 'X111', 'X183', 'X15', 'X145', 'X15', 'X15', 'X145', 'X15', 
                 'X58',
'X270',
                                                                                                   'X48', 'X157', 'X148',
'X13'
               'X302'
                'X263',
'X260',
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'X61',
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'X234'
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'X178',
                                   'X308', 'X292', 'X20', 'X30',
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                  'X271',
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'X151', 'X142',
                  'X116',
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'X377'
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'X40',
               'X80',
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'X267',
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'X307'
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'X118',
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'X77', 'X114', 'X351',
'X35', 'X45', 'X335',
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'X353'
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'X108',
                 'X319',
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                                                    'X331', 'X372',
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                               'X318',
'X153',
                                                  'X333', 'X34', 'X43', 'X169', 'X360', 'X191', 'X141', 'X380', 'X134', 'X162', 'X97', 'X265', 'X186', 'X10', 'X213', 'X373', 'X83', 'X133',
                  'X63',
                 'X172',
                                  'X38',
'X227',
'X170'
                  'X137',
                                  'X22',
'X202', 'X362', 'X273', 'X122', 'X352', 'X300']:
Columns containing the unique values: [0] Columns ['X293', 'X290'
'X233', 'X93', 'X107', 'X235', 'X297', 'X11', 'X289', 'X347', 'X330',
'X268']:
Remove columns with variance zero
# Remove columns with a variance of 0
for colmn in column:
        colmn len = len(np.unique(X train[colmn]))
        if colmn len == 1:
                 X train = X train.drop(colmn, axis = 1)
                 X test = X test.drop(colmn, axis = 1)
X train.head()
                  X272 X156 X204
                                                         X184 X240
                                                                                     X320
                                                                                                X221
                                                                                                               X309
      X248
                                                                                                                            X165
X213
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[5 rows x 364 columns]
Apply label encoder
# Label encoding the Categorical columns
from sklearn import preprocessing
for col in ['X0', 'X1', 'X2', 'X3', 'X4', 'X5', 'X6', 'X8']:
    label encoder = preprocessing.LabelEncoder()
    label encoder.fit(list(X train[col].values))
    X train[col] = label encoder.transform(list(X train[col].values))
Perform dimensionality reduction
# performing dimentionality reduction with PCA
from sklearn.decomposition import PCA
n comp = 12
pca = PCA(n components = n comp, random state = 42)
pca_result_train = pca.fit transform(X train)
#pca result test = pca.transform(X test)
print(pca result train)
#print(pca result test)
[ 0.6147646
                 -0.13300945
                              15.62446002 ...
                                                 1.73751747
                                                               0.28952955
    0.35790984]
   0.56540665
                  1.56033294
                              17.9095812
                                                 -0.13654979
                                                               0.76262443
                                           . . .
   -0.365085121
 [ 16.20171258
                12.29284626
                              17.6335395
                                           . . .
                                                 -0.48524615
                                                              -1.03728745
    3.90819297]
 [ 29.00466039
                14.86090532
                              -7.75333217 ...
                                                 -1.09559585
                                                               1.40194745
   -0.358391371
                              -9.03124768 ...
                                                 0.254992
 [ 22.97242171
                  1.68482437
                                                               1.27428371
   -1.10552034]
 [-17.28304831 -9.95198181
                             -3.71935977 ...
                                                 0.28690991
                                                               0.43211075
   -0.7158175 ]]
```

Predict your test_df values using XGBoost.

```
# ML Modeling with XGboost
import xgboost as xgb
from sklearn.metrics import r2 score
from sklearn.model selection import train test split
# Splitting the data by 80/20
x train, x valid, y_train, y_valid =
train test split(pca result train, y train, test size = 0.2,
random state = 42)
# Building the final feature set
f train = xgb.DMatrix(x train, label = y train)
f_valid = xgb.DMatrix(x_valid, label = y_valid)
#f test = xqb.DMatrix(x test)
#f test = xgb.DMatrix(pca result test)
# Setting the parameters for XGB
params = \{\}
params['objective'] = 'reg:linear'
params['eta'] = 0.02 ## eta means learning rate
params['max depth'] = 4
# Create function to Predict the score
def scorer(m, w):
    labels = w.get label()
    return 'r2', r2 score(labels, m)
final set = [(f train, 'train'), (f valid, 'valid')]
P = xgb.train(params, f train, 1000, final set,
early stopping rounds=50, feval=scorer, maximize=True,
verbose eval=10)
[22:19:51] WARNING: /workspace/src/objective/regression obj.cu:167:
reg:linear is now deprecated in favor of reg:squarederror.
     train-rmse:98.99704
                           valid-rmse:98.88675 train-r2:-59.49743
[0]
     valid-r2:-61.82424
Multiple eval metrics have been passed: 'valid-r2' will be used for
early stopping.
Will train until valid-r2 hasn't improved in 50 rounds.
                           valid-rmse:81.05431
                                                train-r2:-39.64615
[10] train-rmse:81.14532
     valid-r2:-41.20883
                           valid-rmse:66.52771 train-r2:-26.38061
[20] train-rmse:66.60017
     valid-r2:-27.43520
[30] train-rmse:54.76085
                           valid-rmse:54.72092 train-r2:-17.51112
     valid-r2:-18.23791
```

[40]	train-rmse:45.14306 valid-r2:-12.07891	valid-rmse:45.11907	train-r2:-11.57983
[50]	train-rmse:37.35343	valid-rmse:37.35661	train-r2:-7.61298
[60]	valid-r2:-7.96573 train-rmse:31.07077	valid-rmse:31.08922	train-r2:-4.95932
[70]	valid-r2:-5.20970 train-rmse:26.02810	valid-rmse:26.04551	train-r2:-3.18194
	valid-r2:-3.35830		
[88]	train-rmse:22.00455 valid-r2:-2.11705	valid-rmse:22.02654	train-r2:-1.98894
[90]	train-rmse:18.81812 valid-r2:-1.28175	valid-rmse:18.84555	train-r2:-1.18597
[100]	train-rmse:16.32131	valid-rmse:16.36671	train-r2:-0.64438
[110]	valid-r2:-0.72097		+
	train-rmse:14.38446 valid-r2:-0.34118	valid-rmse:14.44833	train-r2:-0.27726
[120]	train-rmse:12.89840 valid-r2:-0.08360	valid-rmse:12.98699	train-r2:-0.02699
[130]	train-rmse:11.78597 valid-r2:0.08966	valid-rmse:11.90356	train-r2:0.14252
[140]	train-rmse:10.95228	valid-rmse:11.09884	train-r2:0.25954
[150]	valid-r2:0.20858		+ main m2.0 240FF
[150]	train-rmse:10.33580 valid-r2:0.28808	valid-rmse:10.52667	train-r2:0.34055
[160]	train-rmse:9.87566 valid-r2:0.34380	valid-rmse:10.10633	train-r2:0.39796
[170]	train-rmse:9.54199	valid-rmse:9.81491	train-r2:0.43796
[100]	valid-r2:0.38110 train-rmse:9.29620	valid-rmse:9.61114	train-r2:0.46654
[100]	valid-r2:0.40653	valiu-11115e:9.01114	train-12:0.40034
[190]	train-rmse:9.11453 valid-r2:0.42310	valid-rmse:9.47596	train-r2:0.48718
[200]	train-rmse:8.97785	valid-rmse:9.37098	train-r2:0.50245
	valid-r2:0.43582		
[210]	train-rmse:8.85440 valid-r2:0.44407	valid-rmse:9.30220	train-r2:0.51604
[220]	train-rmse:8.74807	valid-rmse:9.24707	train-r2:0.52759
[230]	valid-r2:0.45064 train-rmse:8.66516	valid-rmse:9.20904	train-r2:0.53650
[250]	valid-r2:0.45515	Vac2a 15015120501	
[240]	train-rmse:8.59832 valid-r2:0.45840	valid-rmse:9.18151	train-r2:0.54363
[250]	train-rmse:8.53190	valid-rmse:9.15776	train-r2:0.55065
[260]	valid-r2:0.46120 train-rmse:8.47094	valid-rmse:9.14297	train-r2:0.55705
[270]	valid-r2:0.46294		+
[2/0]	train-rmse:8.41722 valid-r2:0.46413	valid-rmse:9.13281	train-r2:0.56265
[280]	train-rmse:8.37159	valid-rmse:9.12389	train-r2:0.56738
	valid-r2:0.46518		

```
valid-rmse:9.11911
[290] train-rmse:8.32141
                                                   train-r2:0.57255
     valid-r2:0.46574
                            valid-rmse:9.11133
[300] train-rmse:8.27764
                                                   train-r2:0.57703
     valid-r2:0.46665
                            valid-rmse:9.10996
[310] train-rmse:8.23678
                                                   train-r2:0.58120
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[330] train-rmse:8.16416
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                            valid-rmse:9.10184
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[360] train-rmse:8.07291
                            valid-rmse:9.09400
                                                   train-r2:0.59770
     valid-r2:0.46867
                            valid-rmse:9.09156
[370] train-rmse:8.04752
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[380] train-rmse:8.01868
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                                                   train-r2:0.60308
     valid-r2:0.46891
                            valid-rmse:9.09013
[390] train-rmse:7.99414
                                                   train-r2:0.60551
     valid-r2:0.46913
[400] train-rmse:7.95877
                            valid-rmse:9.09192
                                                   train-r2:0.60899
     valid-r2:0.46892
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[430] train-rmse:7.88631
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                            valid-rmse:9.08692
[440] train-rmse:7.86229
                                                   train-r2:0.61842
     valid-r2:0.46950
                            valid-rmse:9.08864
[450] train-rmse:7.84281
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[460] train-rmse:7.81202
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     valid-r2:0.46929
[470] train-rmse:7.79307
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                                                   train-r2:0.62511
     valid-r2:0.46903
[480] train-rmse:7.77274
                            valid-rmse:9.08829
                                                   train-r2:0.62706
     valid-r2:0.46934
                            valid-rmse:9.08790
[490] train-rmse:7.75118
                                                   train-r2:0.62912
     valid-r2:0.46939
Stopping. Best iteration:
[440] train-rmse:7.86229
                            valid-rmse:9.08692
                                                   train-r2:0.61842
     valid-r2:0.46950
```

Predicting on test set
#p test = P.predict(f test)

```
p test = P.predict(f valid)
p test
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Predicted Data = pd.DataFrame()
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Predicted Data['y'] = p_test Predicted Data.head()

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