

Association Rule - Apriori Algorithm

Generate rules using Apriori Algorithm. Consider the values as SUPPORT = 50% & CONFIDENCE = 75%.

ID	Items
1	Bread, Butter, Jam, Milk
2	Bread, Butter, Milk
3	Bread, Juice, Cud
4	Bread, Milk, Juice
5	Butter, Milk, Juice

Total 5 transactions.

* Itemset	Support Count ⁽⁴⁾ ₍₁₎	Support (count / total no. of transaction)
Item	Count	
Bread	4	$4/5 = 80\%$ ✓
Butter	3	$3/5 = 60\%$ ✓
Jam	1	$1/5 = 20\%$ ✗
Milk	4	$4/5 = 80\%$ ✓
Juice	3	$3/5 = 60\%$ ✓
Cud	1	$1/5 = 20\%$ ✗

Support value = 50%. (Given in Question)

2. Itemsets Support Count (L2)

Find the combinations of valid transactions

Item	Count	Support
{Bread, Butter}	2	$2/5 = 40\%$ ✗
{Bread, Milk}	3	$3/5 = 60\%$ ✓
{Bread, Juice}	2	$2/5 = 40\%$ ✗
{Butter, Milk}	3	$3/5 = 60\%$ ✓
{Butter, Juice}	1	$1/5 = 20\%$ ✗
{Milk, Juice}	2	$2/5 = 40\%$ ✗

Valid transactions

{Bread, Milk}, {Butter, Milk}

If we can combine these also.

{Bread, Milk, Butter}

count = 2

support = $2/5 = 40\%$ ✗

so will consider combinations upto 2.

{Bread, Milk}

Bread \rightarrow Milk

confidence = $\frac{\text{support}(\text{Bread} \cup \text{Milk})}{\text{support}(\text{Bread})} = \frac{60\%}{80\%} = 75\%$

Milk \rightarrow Bread

Confidence = $60\% / 80\% = 75\%$

$$\text{confidence}(x \rightarrow y) = \frac{s(x \cup y)}{s(x)}$$

$$\text{Confidence (Butter} \rightarrow \text{Milk)} = 60\% / 60\% = 100\%$$

$$\text{Confidence (Milk} \rightarrow \text{Butter)} = 60\% / 80\% = 75\%$$

In Question the threshold value of
Confidence = 75%.

So these rules are valid

Bread \rightarrow Milk

If a person buys bread, ~~the~~ 75% probability
for that person to buy milk.

Milk \rightarrow Bread

Butter \rightarrow Milk

Milk \rightarrow Butter

- a. Consider the transaction dataset of a store where each transaction contains the list of items purchased by the customers. Our goal is to find frequent set of items that are purchased by the customers and generate association rules for them.

Transaction id	Item purchased
T ₁	I ₁ , I ₂ , I ₃
T ₂	I ₂ , I ₅
T ₃	I ₄ , I ₅
T ₄	I ₁ , I ₂ , I ₅
T ₅	I ₂ , I ₃ , I ₅

Minimum support count = 2 and
confidence = 50%.

Solution

Step 1: Item set Count

Create a table which has support count of all items in the transaction database

Item	Support Count
I_1	2 ✓
I_2	4 ✓
I_3	2 ✓
I_4	1 ✗
I_5	4 ✓

So frequent 1-Itemsets = I_1, I_2, I_3, I_5

2. 2-Itemsets.

Check pairs of the frequent 1-Itemsets.

Itemset	Support Count
I_1, I_2	2 ✓
I_1, I_3	1
I_1, I_5	1
I_2, I_3	2 ✓
I_2, I_5	3 ✓
I_3, I_5	1

valid item set by removing itemset having support count < 2

I_1, I_2 , I_2, I_3 , I_2, I_5

3. 3-Itemset

Itemset	Count		
$I_1 I_2 I_3$	1	X	All are having count < 2
$I_1 I_2 I_5$	1	X	
$I_2 I_3 I_5$	1	X	

Since no more frequent items, go back to the previous itemset.

$I_1 I_2$	$I_2 I_1$
$I_2 I_3$	$I_3 I_2$
$I_2 I_5$	$I_5 I_2$

Find confidence of all rules.

$$\text{Confidence } (I_1 \rightarrow I_2) =$$

$$\frac{\text{Support } (I_1 \cup I_2)}{\text{Support } (I_1)}$$

$$= \frac{2}{2} = 1 = 100\% \checkmark$$

Confidence ($I_2 \rightarrow I_1$)

$$= \frac{2}{4} = 50\% \quad \checkmark$$

Confidence ($I_2 \rightarrow I_3$)

$$= \frac{2}{4} = 50\% \quad \checkmark$$

Confidence ($I_3 \rightarrow I_2$)

$$= \frac{2}{2} = 100\% \quad \checkmark$$

Confidence ($I_2 \rightarrow I_5$)

$$= \frac{3}{4} = 75\% \quad \checkmark$$

Confidence ($I_5 \rightarrow I_2$)

$$= \frac{3}{4} = 75\% \quad \checkmark$$

Given that minimum Confidence = 50%.

So all association rules has confidence $\geq 50\%$.
so all rules are strong association rules.

Calculate strong association rules.

$$\text{Lift}(x \rightarrow y) = \frac{\text{Confidence}(x \rightarrow y)}{\text{support}(y)}$$

$$\text{Lift}(I_1 \rightarrow I_2) = \frac{\text{Confidence}(I_1 \rightarrow I_2)}{\text{Support}(I_2)}$$

$$= \frac{100}{4} = 25\%$$

Lift

Association Rules

Lift (%)

$I_1 \rightarrow I_2$

25%

$I_2 \rightarrow I_1$

25%

$I_2 \rightarrow I_3$

25%

$I_3 \rightarrow I_2$

25%

$I_2 \rightarrow I_5$

18.75%

$I_5 \rightarrow I_2$

18.75%