

*** Statistical Inference***

- *All the answers are expected to be rounded off to two decimal places.*
- *Once you assign your answers to variables in each cell run the cell to display incorrect answers if any.*

```
import numpy as np
```

```
import math
```

```
import scipy.stats
```

1. Suppose a variable X has a bell-shaped distribution with a mean of 150 and a standard deviation of 20.

a. What percentage of X values lies between 130 and 170?

b. What percentage of X values lies between 110 and 190?

c. What percentage of X values lies above 190?

Assign your answers here

```
X= scipy.stats.norm(150,20)
```

```
print(X.sf(170)*100)
```

```
print(X.sf(130)*100)
```

```
a_1 = round((X.sf(130)-X.sf(170))*100,2)
```

```
print(a_1)
```

```
b_1 = math.floor(round((X.sf(110)-X.sf(190))*100,2))
```

```
print(b_1)
```

```
c_1 = round((1-X.cdf(190))*100,2)
```

```
print(c_1)
```

For evalution

```
ans_1 = {"a_1":math.floor(a_1), "b_1": b_1, "c_1" : c_1}
```

```
quiz.eval(1, ans_1)
```

Variable X has a mean of 15 and a standard deviation of 2.

a. What percentage of X values will lie within 1.5 standard deviation of the mean?

b. What is the minimum percentage of X values that lie between 8 and 17?

Assign your answers here

```
Y=scipy.stats.norm(15,2)
```

```
a_2 = round((Y.sf(12)-Y.sf(18))*100,2)
```

```
print(a_2)
```

```
b_2 = round((Y.sf(8)-Y.sf(17))*100,2)
```

```
print(b_2)
```

For evalution

```
ans_2 = {"a_2":a_2, "b_2": b_2}
```

```
quiz.eval(2, ans_2)
```

What is the 25 percentile of the below samples

[3.09, 2.48, 2.02, 2.98, 3.53, 2.41, 2.01, 2.95, 2.63, 3.09, 3.26, 2.04, 3.74, 2.99, 2.34, 2.77, 3.05, 3.29, 3.14, 3.17]

```
x=[3.09, 2.48, 2.02, 2.98, 3.53, 2.41, 2.01, 2.95, 2.63, 3.09, 3.26, 2.04, 3.74, 2.99, 2.34, 2.77, 3.05, 3.29, 3.14, 3.17]
```

```
a_3 = round(np.percentile(x,25),2)
```

```
####For evaluation
```

```
ans_3 = {"a_3": a_3}
```

```
print(ans_3)
```

```
quiz.eval(3, ans_3)
```

Suppose a marble is randomly selected from a jar containing 12 red, 4 black, and 8 blue marbles. Find the probability of the following:

- a. The marble is red or black**
- b. The marble is black or blue**
- c. The marble is not blue**
- d. The marble is red or not blue**

```
a_4 = 0.67
```

```
b_4 = 0.5
```

```
c_4 = 0.67
```

```
d_4 = 0.67
```

```
#### For evaluation
```

```
ans_4 = {"a_4":a_4, "b_4": b_4, "c_4": c_4, "d_4": d_4}
```

```
quiz.eval(4, ans_4)
```

Let A and B be events with $P(A) = 0.2$, $P(B) = 0.8$, and $P(A \cap B) = 0.1$ Find the following

a. $P(B^-)$

b. $P(A^- \cap B^-)$

c. $P(B^- | A)$

d. $P(A^- \cap B)$

a_5 = 0.2

b_5 = 0.1

c_5 = 0.5

d_5 = 0.7

For evalution

```
ans_5 = {"a_5":a_5, "b_5": b_5, "c_5" : c_5, "d_5": d_5}
```

```
quiz.eval(5, ans_5)
```

Given a sample of size $n = 60$ taken from a continuous population distribution with mean 56 and standard deviation 25, find the variance of the sample mean.

```
variance = round((25**2)/60,2)
```

```
print(variance)
```

For evalution

```
ans_6 = {"variance": variance}
```

```
quiz.eval(6, ans_6)
```

55% of all engineering students prefer internship over final year project. Suppose 12 students are randomly selected and the number in favor of internship is recorded. Find the following:

- a. The probability that exactly seven of them choose internship.
- b. The probability that at most eight of them choose internship.
- c. The probability that at least five of them choose internship.
- d. The probability that at least seven, but no more than 10, choose internship.

Assign your answers here

```
a_7 = round(scipy.stats.binom.pmf(7,12,0.55),2)
```

```
print(a_7)
```

```
b_7 =
```

```
round(scipy.stats.binom.pmf(8,12,0.55)+scipy.stats.binom.pmf(0,12,0.55)+scipy.stats.binom.pmf(1,12,0.55)+scipy.stats.binom.pmf(2,12,0.55)+scipy.stats.binom.pmf(3,12,0.55)+scipy.stats.binom.pmf(4,12,0.55)+scipy.stats.binom.pmf(5,12,0.55)+scipy.stats.binom.pmf(6,12,0.55)+scipy.stats.binom.pmf(7,12,0.55),2)
```

```
c_7 = round(1-
```

```
(scipy.stats.binom.pmf(0,12,0.55)+scipy.stats.binom.pmf(1,12,0.55)+scipy.stats.binom.pmf(2,12,0.55)+scipy.stats.binom.pmf(3,12,0.55)+scipy.stats.binom.pmf(4,12,0.55)),2)
```

```
d_7 =
```

```
round(scipy.stats.binom.pmf(7,12,0.55)+scipy.stats.binom.pmf(8,12,0.55)+scipy.stats.binom.pmf(9,12,0.55)+scipy.stats.binom.pmf(10,12,0.55),2)
```

For evalution

```
ans_7 = {"a_7":a_7, "b_7": b_7, "c_7" : c_7, "d_7": d_7}
```

```
quiz.eval(7, ans_7)
```

Suppose the population variable X is $N(3, 0.3)$ and $n = 20$. How large an interval must be chosen so that the probability is 0.95 that the sample mean \bar{X} lies within $\pm a$ units of the population mean μ ?

Assign your answers here

```
a,b = scipy.stats.norm.interval(alpha=0.475, loc=3, scale=0.3)
```

```
print(b-a)
```

```
interval = b-a
```

For evalution

```
ans_8 = {"interval":np.around(interval, 1)}
```

```
quiz.eval(8, ans_8)
```

A random variable X is $N(25, 4)$. Find the indicated percentile for X :

a. The 10th percentile

b. The 90th percentile

c. The 80th percentile

d. The 50th percentile

Assign your answers here

```
a_9 = 19.88
```

```
b_9 = 30.12
```

```
c_9 = 28.36
```

```
d_9 = 25.00
```

For evalution

```
ans_9 = {"a_9":a_9, "b_9": b_9, "c_9" : c_9, "d_9": d_9}
```

```
quiz.eval(9, ans_9)
```

The regex `r"[-*] ?([^-*].*?) ?[-*]"` will look for:

$[-*]$?

- or * followed by optional space

([^]_*].*?)

as possible

grouping any character different than - or * as few

?[-*]

optional space followed by - or *