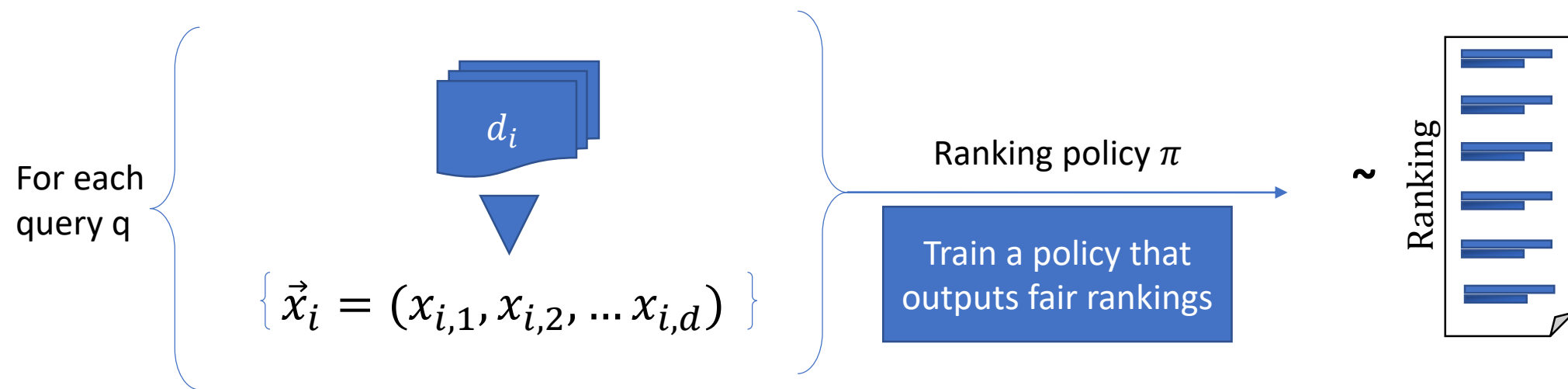
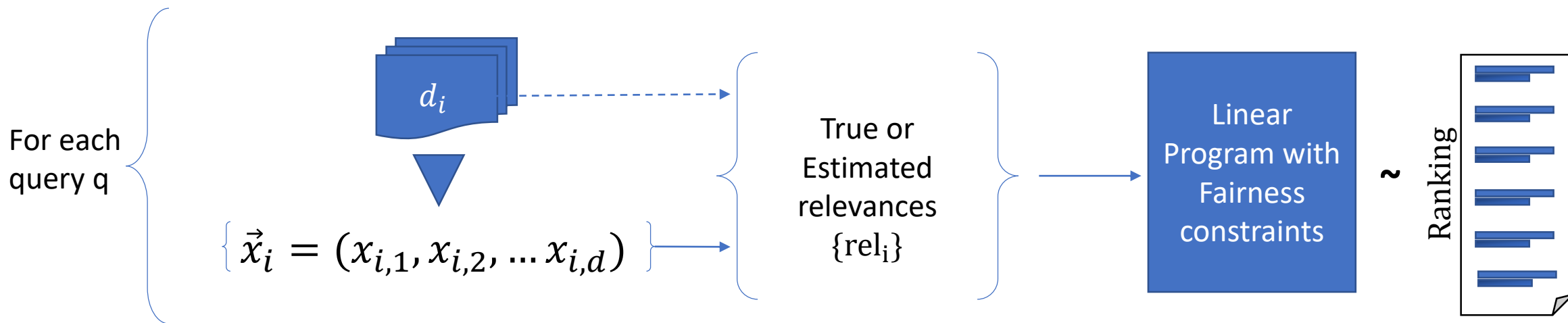


# Policy Learning for Fairness in Ranking

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Learning to Rank with Fairness constraints

# Fair-PG-Rank: Learning-to-Rank with Fairness constraints

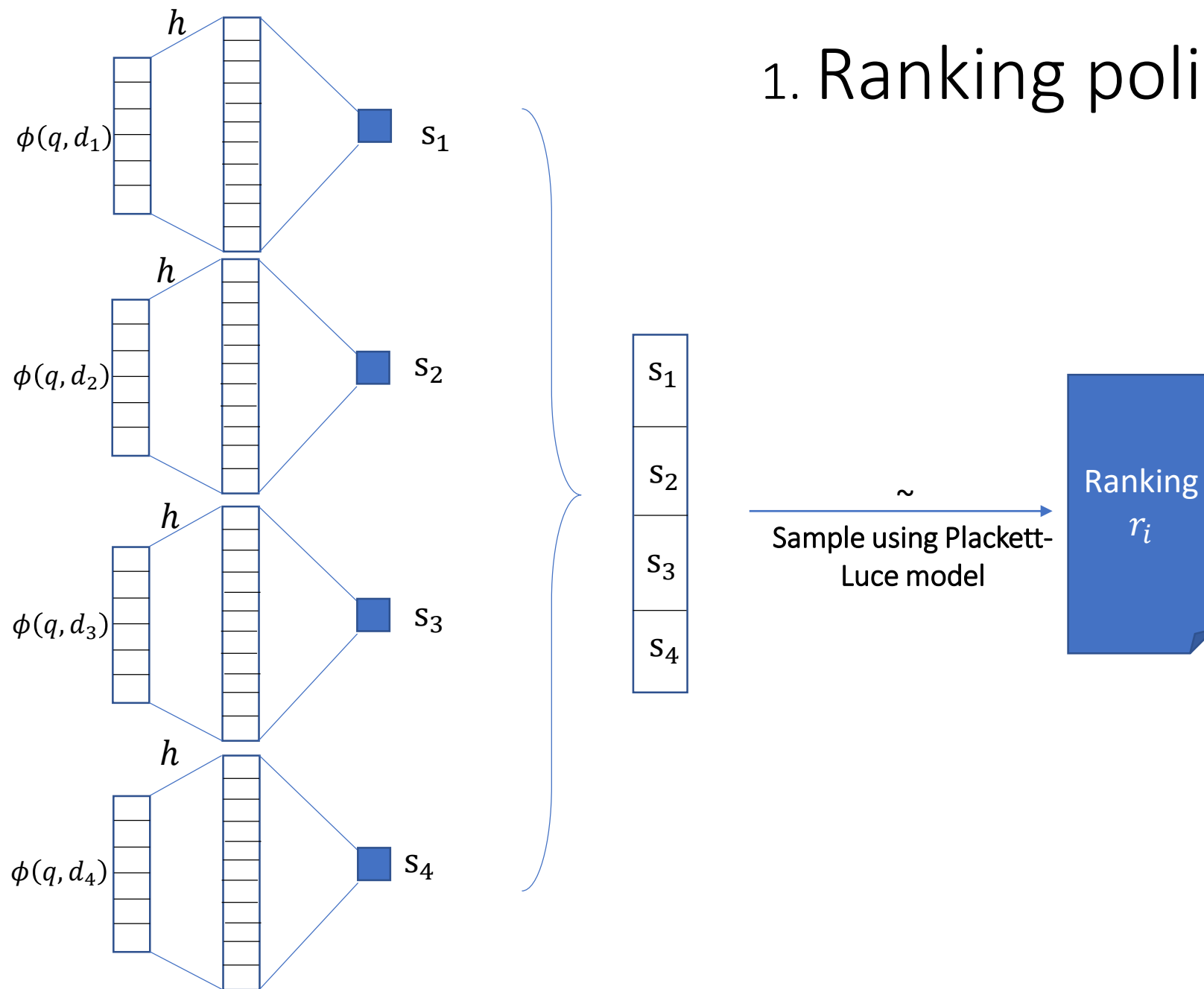
$$\pi_{\delta}^* = \operatorname{argmax}_{\pi} \mathbb{E}_{q \sim \mathcal{Q}} [U(\pi|q)] \quad \text{s.t.} \quad \mathbb{E}_{q \sim \mathcal{Q}} [\mathcal{D}(\pi|q)] \leq \delta$$

Empirical Risk Minimization:

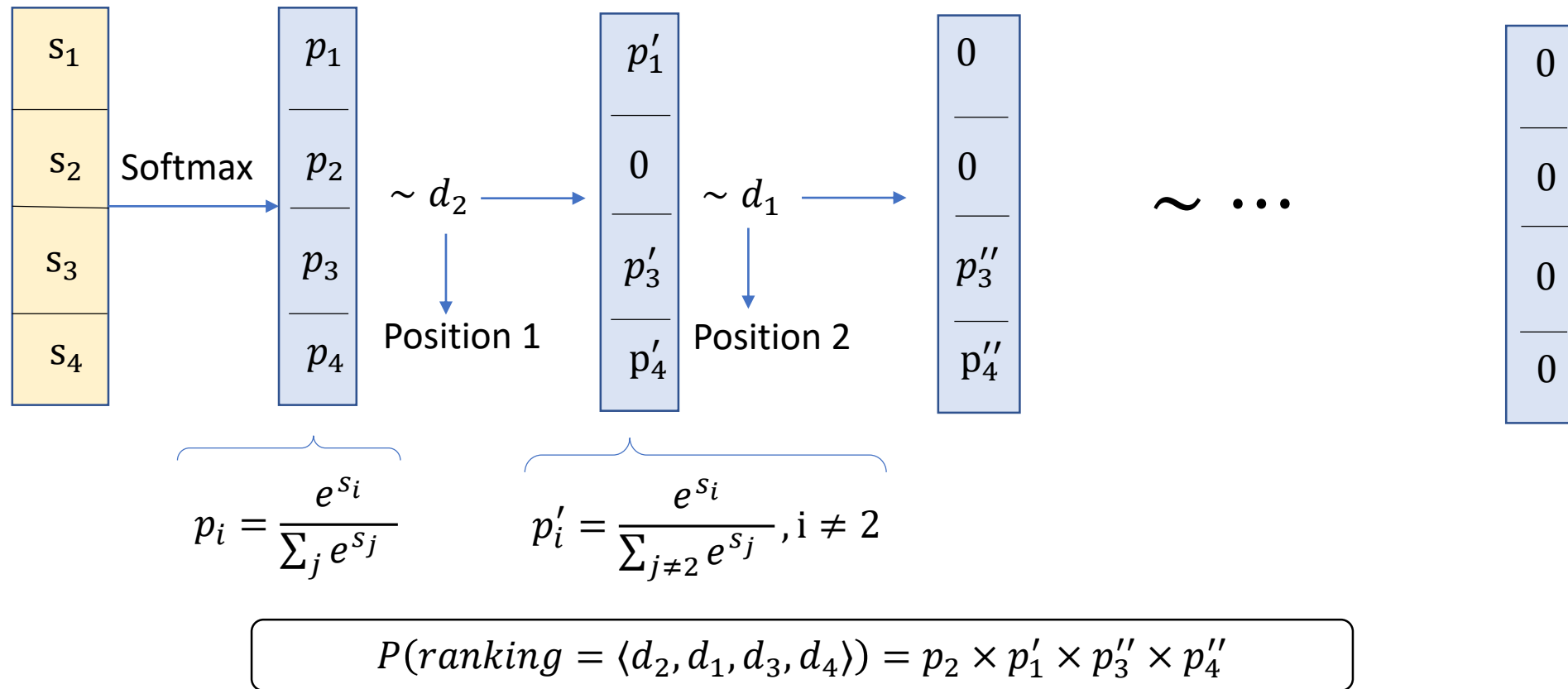
$$\hat{\pi}_{\lambda}^* = \operatorname{argmax}_{\pi} \frac{1}{N} \sum_{q=1}^N \underbrace{U(\pi|q)}_{\text{Utility}} - \lambda \frac{1}{N} \sum_{q=1}^N \underbrace{\mathcal{D}(\pi|q)}_{\text{Disparity}}$$

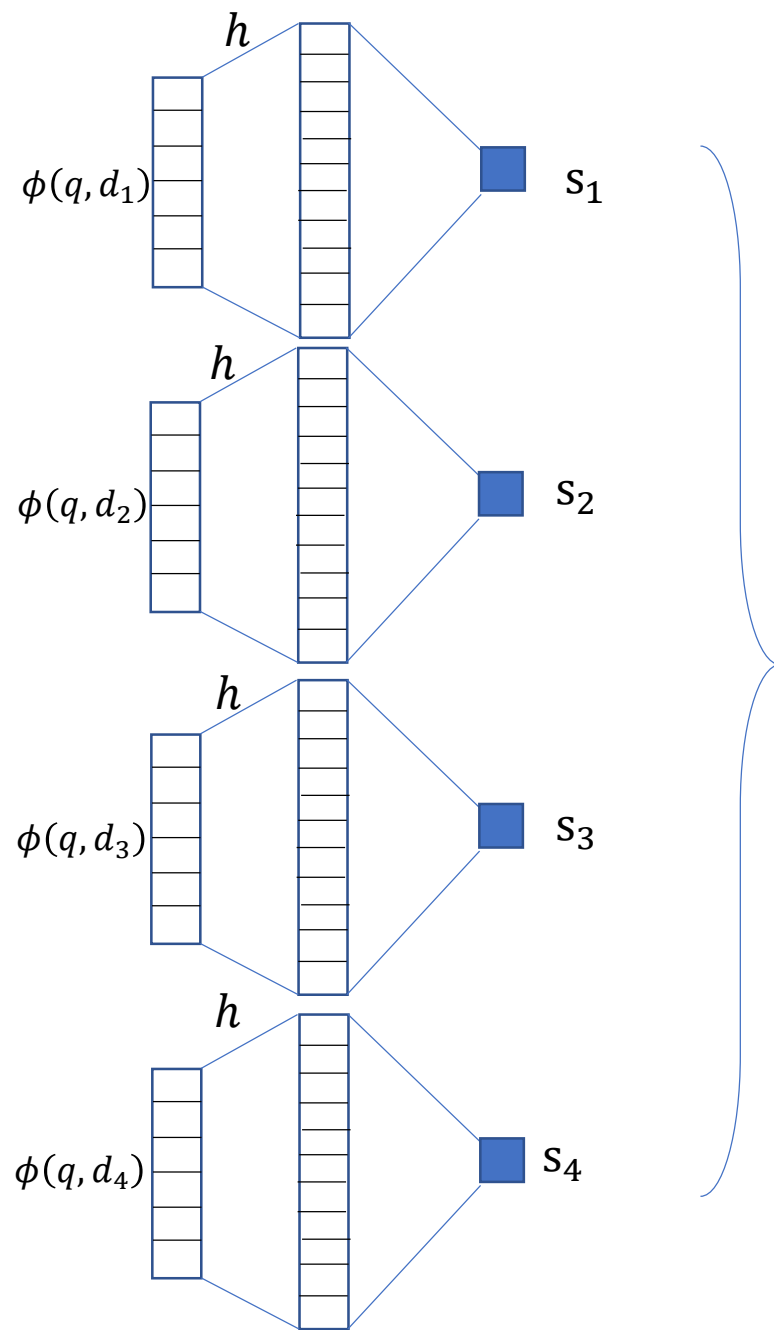
1. Ranking policy  $\pi$
2. Utility of  $\pi$
3. Disparity measure w.r.t.  $\pi$

# 1. Ranking policy $\pi$



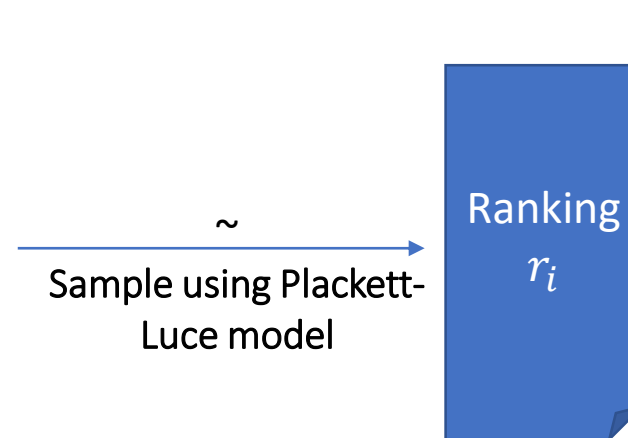
# Sampling from $\pi$ : Plackett-Luce Model





# 1. Ranking policy $\pi$

- Parameterized Model  $h_\theta$
- Plackett-Luce (PL) Sampling



## 2. User Utility

$$U(\pi|q) = \mathbb{E}_{r \sim \pi(r|q)} [\Delta(r, \text{rel}_q)]$$

For example:

- $\Delta_{\text{DCG}}(r, \text{rel}_q) = \sum_{j=1}^{n_q} \frac{u(r(j)|q)}{\log(1+j)}$
- $\Delta_{\text{NDCG}}(r, \text{rel}_q) = \frac{\Delta_{\text{DCG}}(r, \text{rel}_q)}{\Delta_{\text{DCG}}(r^*, \text{rel}_q)}$

### 3. Disparity Measures

- $\text{Exposure}(d_i) = v_\pi(d_i) = \mathbb{E}_{r \sim \pi}[\mathbf{v}_{r(d_i)}]$
- $\text{Exposure}(G) = v_\pi(G) = \sum_{d \in G} \text{Exposure}(d_i)$
- Merit of a group  $M(G) = \sum_{d \in G} M(d_i)$

- Group fairness disparity:

$$\mathcal{D}_{\text{group}}(\pi|q) = \max \left( 0, \frac{v_\pi(G_i)}{M_{G_i}} - \frac{v_\pi(G_j)}{M_{G_j}} \right), \text{ where } M_{G_i} \geq M_{G_j}$$

- Individual fairness disparity:

$$\mathcal{D}_{\text{individual}}(\pi|q) = \sum_{\substack{i,j \\ s.t. M_i \geq M_j}} \max \left( 0, \frac{v_\pi(d_i)}{M_i} - \frac{v_\pi(d_j)}{M_j} \right)$$



Learning objective:  $\hat{\pi}_{\lambda}^* = \operatorname{argmax}_{\pi} \frac{1}{N} \sum_{q=1}^N U(\pi|q) - \lambda \frac{1}{N} \sum_{q=1}^N \mathcal{D}(\pi|q)$

Utility:  $U(\pi|q) = \mathbb{E}_{r \sim \pi(r|q)} [\Delta(r, rel^q)] = \mathbb{E}_{r \sim \pi(r|q)} \left[ \sum_{j=1}^{n_q} \frac{u(r(j)|q)}{\log(1+j)} \right]$

Most previous methods optimize a smooth convex proxy of the utility.  
(SVMRank, ListNet, RankNet, SoftRank etc.)

How do we perform a gradient descent update on utility as well as disparity?

# PG-Rank: REINFORCE update for $\pi_\theta$

$$\nabla_\theta U(\pi_\theta|q) = \nabla_\theta \mathbb{E}_{r \sim \pi_\theta(r|q)} \Delta(r, \text{rel}^q)$$

Similarly for Disparity  $\mathcal{D}_\pi$

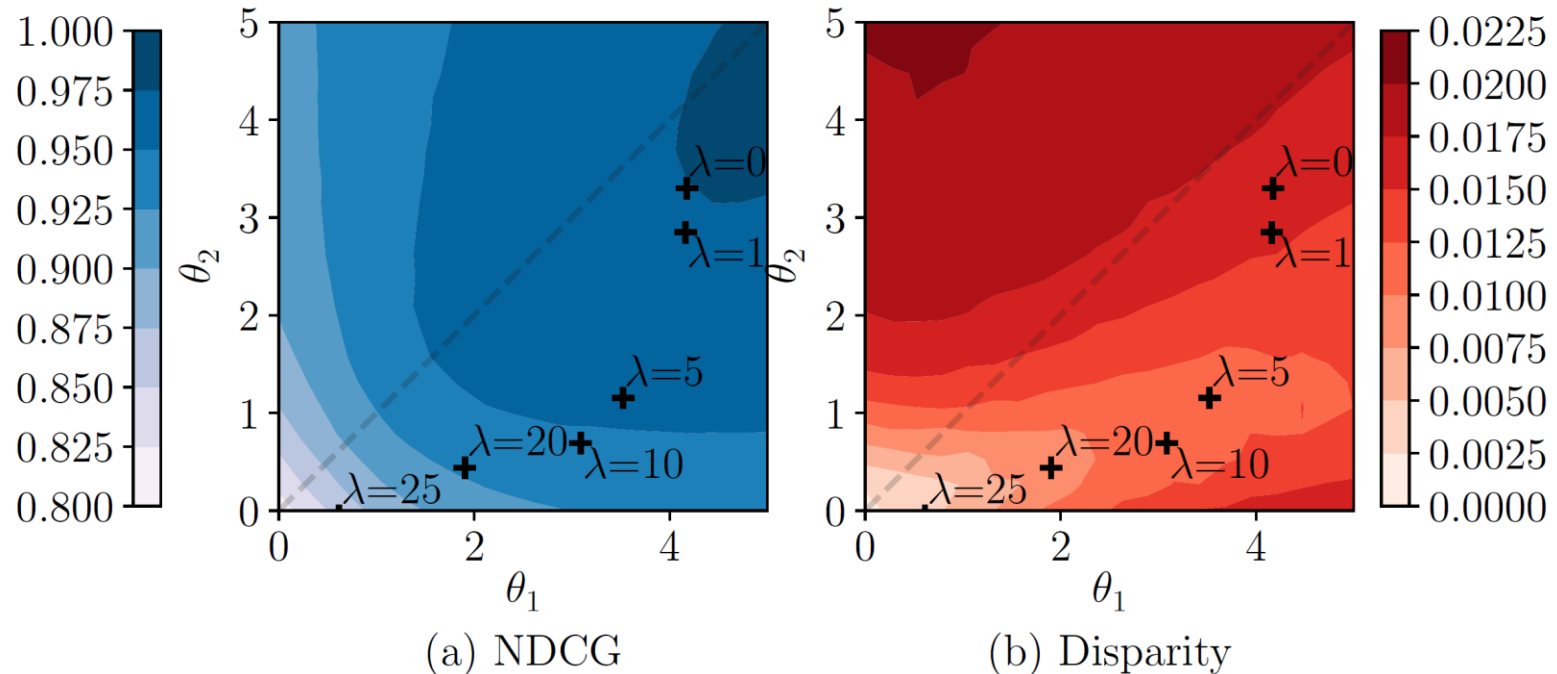
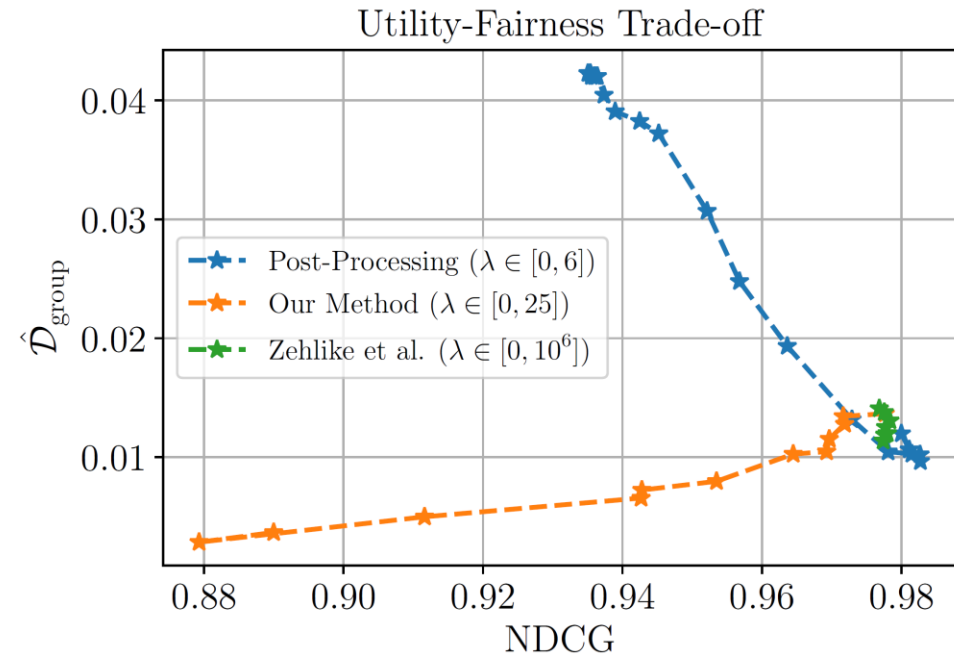
# Fair-PG-Rank: Summary

- **Input:** Queries w/ Candidate sets: features (+ relevances available during training)
- **Ranking policy:** A neural network scoring function + PL-sampling
- **Loss function:** Utility -  $\lambda$  . Disparity
- **Train:** Stochastic gradient descent

# Experiment 1

- Each document  $d_i$  represented by  $(x_{i,1}, x_{i,2}) \in [0,3]^2$
- Two groups:  $G_0, G_1$  (Ratio 4:1)
- $\text{rel}_i = x_{i,1} + x_{i,2}$  (True Model)
- $x_{i,2}$  corrupted for  $G_1$  documents
- $h(x_i) = \theta_1 x_{i,1} + \theta_2 x_{i,2}$
- Train the model  $(\theta_1, \theta_2)$  with different values of  $\lambda$

A fair model only uses the  $x_1$  feature



# Experiment 2: Yahoo! Learning-to-Rank Challenge

