

### Find minimum number of coins

**Problem Statement:** Given a value  $V$ , if we want to make a change for  $V$  Rs, and we have an infinite supply of each of the denominations in Indian currency, i.e., we have an infinite supply of  $\{1, 2, 5, 10, 20, 50, 100, 500, 1000\}$  valued coins/notes, what is the minimum number of coins and/or notes needed to make the change.

#### Examples:

##### Example 1:

**Input:**  $V = 70$

**Output:** 2

**Explanation:** We need a 50 Rs note and a 20 Rs note.

##### Example 2:

**Input:**  $V = 121$

**Output:** 3

**Explanation:** We need a 100 Rs note, a 20 Rs note and a 1 Rs coin.

#### Solution:

**Disclaimer:** Don't jump directly to the solution, try it out yourself first.

#### Solution: Greedy Algorithm

**Approach:** We will keep a pointer at the end of the array  $i$ . Now **while**( $V \geq \text{coins}[i]$ ) we will reduce  $V$  by  $\text{coins}[i]$  and add it to the ans array. We will also ignore the coins which are greater than  $V$  and the coins which are less than  $V$ . We consider them and reduce the value of  $V$  by  $\text{coins}[i]$ .

$\text{Coins}[ ] = [1, 2, 5, 10, 20, 50, 100, 500, 1000]$

$V = 49$

$V = 87$

$20 + 20 + 5 + 2 + 2 + 1$   
(5)

$50 + 20 + 10 + 5 + 2$   
(5)

Consider for,  $V = 49$ ,

$\text{Coins}[ ] = [1, 2, 5, 10, 20, 50, 100, 500, 1000]$

(These values are greater than  $V = 49$ )  
So, we won't consider these.

$\downarrow \quad \downarrow \quad \downarrow$   
 0 1 2 3 4 5 6 7 8  
 Coins[] = [1, 2, 5, 10, 20, 50, 100, 500, 1000]  
 $\uparrow \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow$

$V = 49 \quad 29 \quad 9 \quad 4 \quad 2 \quad 0$

20 ( $\because 20 < 49$ )  
 20 ( $\because 20 < 29$ )  
 5 ( $\because 5 < 9$ )  
 2 ( $\because 2 < 4$ )  
 2 ( $\because 2 + 2 = 4$ )

**Code:**

● C++ Code

● Java Code

● Python Code

```
#include<bits/stdc++.h>

using namespace std;
int main() {
    int V = 49;
    vector<int> ans;
    int coins[] = {1, 2, 5, 10, 20, 50, 100, 500, 1000};
    int n = 9;
    for (int i = n - 1; i >= 0; i--) {
        while (V >= coins[i]) {
            V -= coins[i];
            ans.push_back(coins[i]);
        }
    }
    cout<<"The minimum number of coins is "<<ans.size()<<endl;
    cout<<"The coins are "<<endl;
    for (int i = 0; i < ans.size(); i++) {
        cout<< ans[i]<< " ";
    }

    return 0;
}
```

**Output:**

The minimum number of coins is 5

The coins are

20 20 5 2 2

**Time Complexity:** $O(V)$

**Space Complexity:** $O(1)$