Topological Sort Using DFS

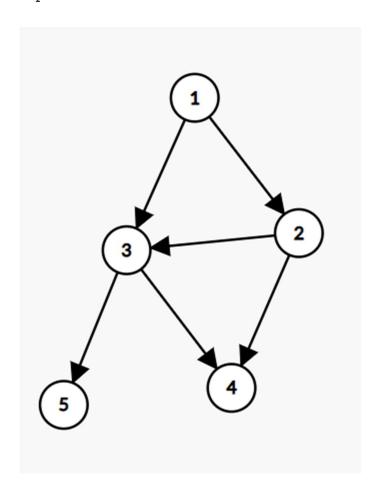
Problem Statement: Given a DAG(Directed Acyclic Graph), print all the vertex of the graph in a topologically sorted order. If there are multiple solutions, print any.

Pre-req: DFS traversal, Graphs, Stack data structure.

Examples:

Example 1:

Input:

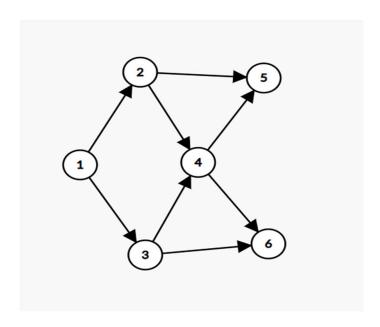


Output:

One of the solutions is 1,2,3,5,4

Example 2:

Input:



Output: One of the solution is 1,2,3,4,5,6

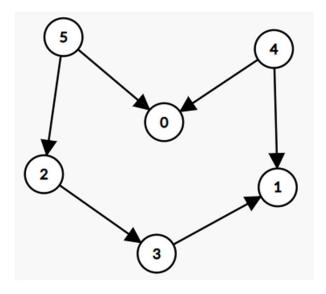
Solution

Disclaimer: Don't jump directly to the solution, try it out yourself first.

Intuition:

-> First of all let's understand Topological Sorting. It means linear ordering of vertices such that there is an edge u—-> v, u appears before v in the ordering.

Suppose for a given graph,



Some of the possible Topological orders can be:

- 1. 5,4,2,3,1,0
- 2. 4,5,2,3,1,0
- -> In both cases we can see, that

4->0 (4 appears before 0), 5>3 (5 appears before 3), ...

- -> Similarly there can be **multiple toposorts order for the given graph** but the condition should be if there is an edge u->v then **u should always appear before v.**
- -> Topological Sorting is applicable only for **DAG(Directed Acyclic Graph)**. Why is it so?

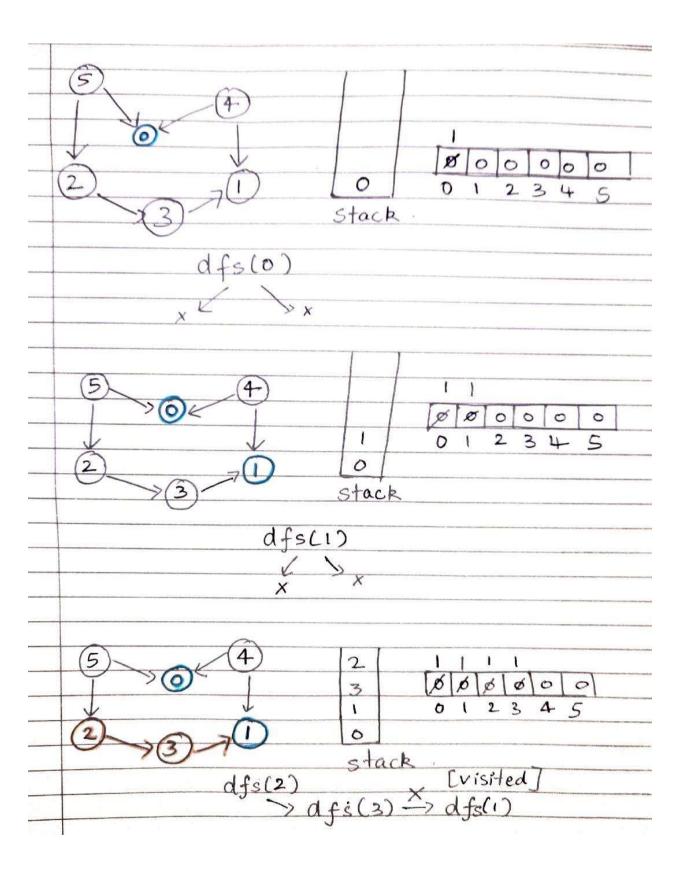
Because of the following reasons:

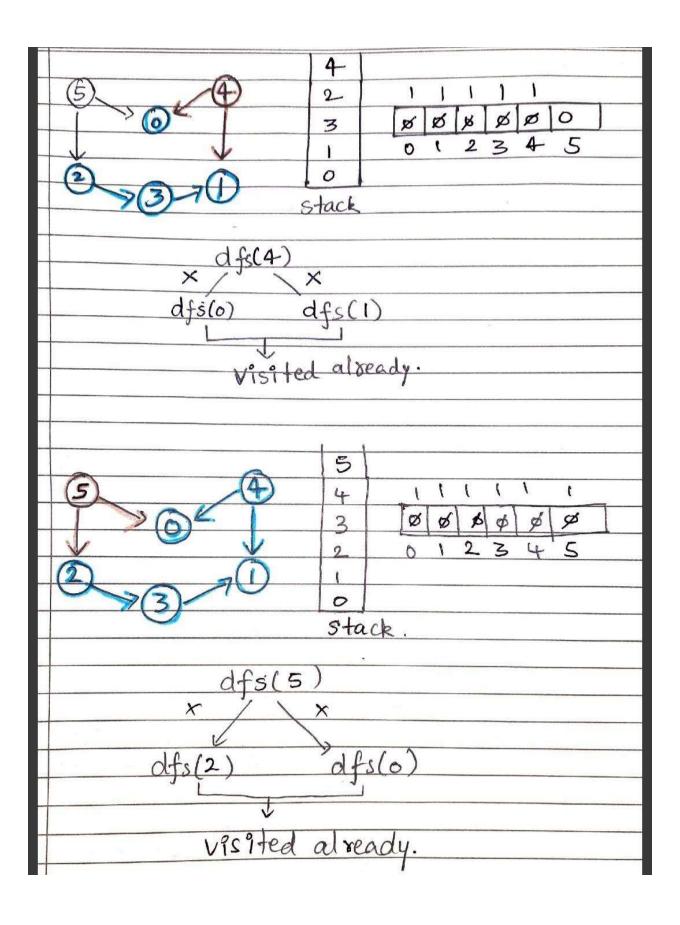
- 1. For Undirected graphs ,only u->v is not applicable . It cannot be sure whether the edge is between u to v or v to u (u-v).
- 2. In a cyclic graph there will always be a dependency factor . You cannot make sure that you can have linear ordering of vertices.
- -> Finally, now you have a clear understanding of what Topological Sorting is. We will be using the **DFS(Depth First Search)** method to solve the problem. What we will be doing is for each vertex we will explore its adjacent vertex. After exploring, we will store the current vertex in a data structure to maintain Topo Sort.

Approach:

We will be using the following data structure to get Topo sort:

- 1. Visited Vector To store visit of each vertex
- 2. Stack To maintain the topo sort order.





Did you notice something while using Stack? Just because there was an edge from u to v. Dfs call will go from u to v. The 1st dfs (v) will get over first and then dfs(u). Here we are making sure that if u->v, then we will **first push v into the stack and then u will be pushed**. This is how Topological order is maintained in the Stack.

Code:

- C++ Code
- Java Code

```
#include <bits/stdc++.h>
using namespace std;
class Solution {
  void findTopoSort(int node, vector < int > & vis, stack < int > & st, vector
< int > adj[]) {
    vis[node] = 1;
    for (auto it: adj[node]) {
      if (!vis[it]) {
        findTopoSort(it, vis, st, adj);
    st.push(node);
  public:
    vector < int > topoSort(int N, vector < int > adj[]) {
      stack < int > st;
      vector < int > vis(N, 0);
      for (int i = 0; i < N; i++) {
        if (vis[i] == 0) {
          findTopoSort(i, vis, st, adj);
      vector < int > topo;
```

```
while (!st.empty()) {
        topo.push_back(st.top());
        st.pop();
      return topo;
};
int main() {
  vector < int > adj[5 + 1];
  adj[5].push_back(2);
  adj[5].push_back(0);
  adj[4].push_back(0);
  adj[4].push back(1);
  adj[2].push_back(3);
  adj[3].push_back(1);
  Solution obj;
  vector < int > res = obj.topoSort(6, adj);
  cout << "Toposort of the given graph is:" << endl;</pre>
  for (int i = 0; i < res.size(); i++) {</pre>
    cout << res[i] << " ";</pre>
  return 0;
```

Output:

Toposort of the given graph is:

542310

Time Complexity: O(N+E)

N = Number of node, E = Number of Edges

Space Complexity: O(N) + O(N)

Visited Array and Stack data structure. Both will be using O(N).

Auxiliary Space Complexity: O(N)