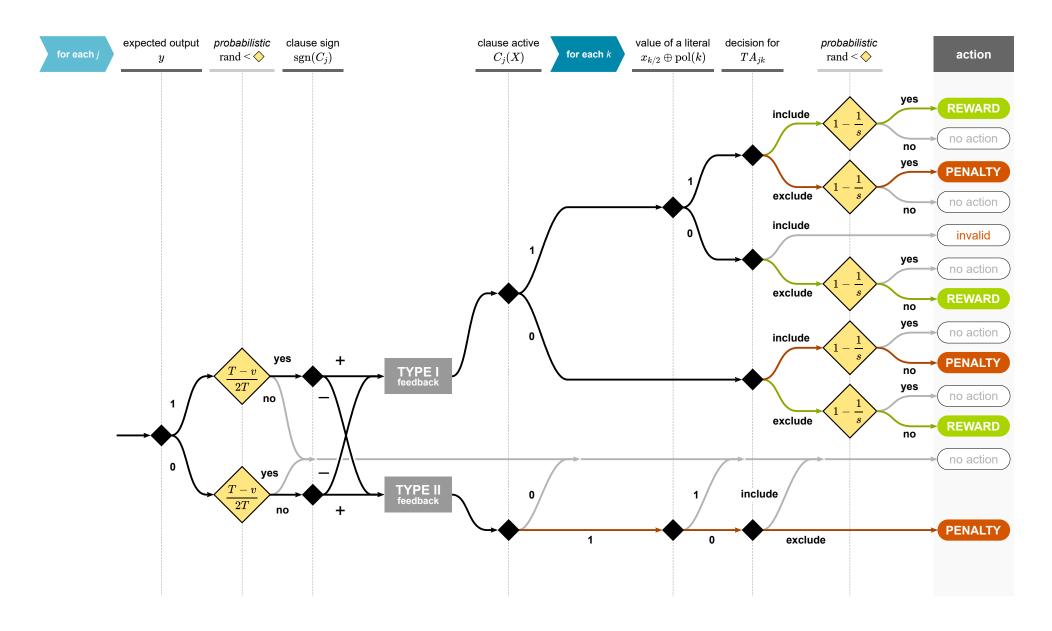
SINGLE-CLASS TSETLIN MACHINE FEEDBACK DECISION TREE



- The decision tree represents a single-class Tsetlin Machine (TM) for Boolean input vector of size m and consisting of n clauses.
- The decision is calculated for a given input vector $X = (x_0, \ldots, x_{m-1})$ and the expected output y; y = 1 if the input vector X matches the class, and y = 0 if it does not.
- Each clause C_j for $0 \le j < n$ has either positive or negative voting defined by the function $\operatorname{sgn}(C_j)$. Usually, even clauses vote (+1), and odd clauses vote (-1).
- Class confidence v is the sum of all clause votes respecting their signs:

$$v = \sum_{j=0}^{n-1} C_j(X) \cdot \operatorname{sgn}(C_j).$$

- Yellow diamonds represent probabilistic choices, such that a uniformly distributed random variable $\mathcal{U}_{[0,1)}$, denoted as "rand", is less than the given probability P, displayed in the diamond. Therefore, the "yes" branch is triggered with an indicated probability P, and "no" is triggered with the probability (1-P).
- The clause feedback probability is calculated once for the entire clause C_j and is based on the class confidence v and the learning threshold T.
- Each clause activation $C_j(X)$ is calculated as a conjunction of 2m literals, one positive and one negative for each of m inputs; i.e., $x_{k/2}$ and $\overline{x}_{k/2}$ for $0 \le k < 2m$:

$$C_{j}(X) = \bigwedge_{k=0}^{2m} (x_{k/2} \wedge \overline{x}_{k/2}).$$

• Positive or negative k-th literal can be expressed as $x_{k/2} \oplus \text{pol}(k)$, where pol(k) is a literal polarity function defined as:

$$pol(k) = \begin{cases} 0 & \text{if } k \text{ is even (positive literal)} \\ 1 & \text{if } k \text{ is odd (negative literal)} \end{cases}$$

therefore, the clause activation $C_{i}(X)$ can also be written as:

$$C_{j}(X) = \bigwedge_{k=0}^{2m} x_{k/2} \oplus \operatorname{pol}(k).$$

- The state of a single Tsetlin automaton TA_{jk} drives the decision to include or exclude k-th literal in the clause C_j .
- The probability of issuing a per-literal feedback action depends on the *learning* rate s > 1.

SINGLE-CLASS TSETLIN MACHINE OPTIMISED DECISION TREE (based on literal feedback)

