

Assignment 3

In this assignment you will find optimal portfolios. To your help, the handout “Mean-variance analysis with many assets in Python” is available.

Consider a mean-variance problem of a US investor investing in US cash, US bonds, US stocks, developed market (DM) stocks, and emerging market (EM) stocks.

Assume the following about the capital markets:

| | Mean | Standard deviation | Correlations | | | | |
|--------------|------|-----------------------|--------------|------|------|------|------|
| | | | 1. | 2. | 3. | 4. | 5. |
| 1. US cash | 0.5 | 0.5 | 1.00 | | | | |
| 2. US bonds | 4.0 | 7.0 | 0.05 | 1.00 | | | |
| 3. US stocks | 7.5 | 16.0 | −0.05 | 0.50 | 1.00 | | |
| 4. DM stocks | 8.5 | 17.0 | −0.05 | 0.50 | 0.80 | 1.00 | |
| 5. EM stocks | 9.5 | 20.0 | 0.05 | 0.50 | 0.70 | 0.90 | 1.00 |

These assumptions are inspired by J.P. Morgan’s 2023 long-term capital market assumptions. They are in real terms. Means and standard deviations are annualized and expressed in %.

1. Study the equal-weighted portfolio (no optimization involved here). What is the mean and standard deviation of this portfolio?
2. Find the optimal portfolio with the same mean as the equal-weighted portfolio. What is the standard deviation on this portfolio? How much lower is the risk compared with the equal-weighted portfolio? What are the weights? Is the portfolio well diversified? If not, which assets dominate, and why?
3. Trace out the minimum-variance frontier with means between 0% and 10%. Plot the frontier together with the individual assets. Print portfolio means, standard deviations, and weights for target means of 2%, 3%, 4%, 5%, 6%, and 7%.
4. Find the global minimum-variance portfolio. What are the mean and standard deviation on this portfolio? Does its location in the plot above make sense?

5. Add a short-sale constraint. Trace out the new frontier with means between 0% and 10%. Print portfolio means, standard deviations, and weights for target means of 2%, 3%, 4%, 5%, 6%, and 7%. Comment on the differences between these portfolios and the ones without short-sale constraints.
6. Change the mean assumptions by adding 0.5% to US stocks and subtracting 0.5% to DM stocks. Find the portfolio with a target mean of 6%. How does it differ from the one with the original assumptions. Do you find the differences small or large?