

Optimization Assignment 1

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Question 1. Minimize : $(x_1 - 3x_2)$. Subject to:

$$-x_1 + 2x_2 \leq 6 \quad (1)$$

$$x_1 + x_2 \leq 5 \quad (2)$$

$$x_1, x_2 \geq 0 \quad (3)$$

Also, write down the dual problem and get an optimal solution

Question 2. Let $S = \{(x_1, x_2, x_3) \mid x_1 - 2x_2 \leq 3; 2x_2 + 3x_3 \geq 4\}$

1. Is it a convex set?
2. Does it have a direction vector d ?
3. Find an extreme point of S ?

Question 3. Let $A = \begin{bmatrix} -1 & 2 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{bmatrix}$.

Let $S = \{(x_1, x_2, x_3) \mid -x_1 + 2x_2 + x_3 = 6; x_1 + x_2 + x_4 = 5; x_1, x_2, x_3, x_4 \geq 0\}$

Write down all extreme solutions of S