

$$f(x) = \left\{ \begin{array}{l} f(x_0, u_0) = x_1 \\ f(x_1, u_1) = x_2 \\ f(x_2, u_2) = x_3 \\ f(x_3, u_3) = x_4 \\ f(x_4, u_4) = x_0 \\ x_0 = 0 \end{array} \right\} \quad \left. \begin{array}{l} \text{odometry constraints} \\ \text{loop closure constraints} \end{array} \right\}$$

$$\left\{ \begin{array}{l} x_0 + u_0 = x_1 \rightarrow b_1 \\ x_1 + u_1 = x_2 \rightarrow b_2 \\ x_2 + u_2 = x_3 \rightarrow b_3 \\ x_3 + u_3 = x_4 \rightarrow b_4 \\ x_0 + u_4 = x_4 \rightarrow b_5 \\ x_0 = 0 \rightarrow b_6 \end{array} \right.$$

$$\frac{\partial b_1}{\partial x_0} = 1, \quad \frac{\partial b_1}{\partial x_1} = -1, \quad \text{all other derivatives} = 0$$

$$\frac{\partial b_2}{\partial x_1} = 1, \quad \frac{\partial b_2}{\partial x_2} = -1, \quad \text{all other derivatives} = 0$$

$$\frac{\partial b_3}{\partial x_2} = 1, \quad \frac{\partial b_3}{\partial x_3} = -1, \quad "$$

$$\frac{\partial b_4}{\partial x_3} = 1, \quad \frac{\partial b_4}{\partial x_4} = -1, \quad "$$

$$\frac{\partial b_5}{\partial x_0} = 1, \quad \frac{\partial b_5}{\partial x_4} = -1, \quad "$$

$$\frac{\partial b_6}{\partial x_0} = 1, \quad "$$

Hence, we get $J =$

(we found derivatives
wrt x_0, x_1, x_2, x_3, x_4)

1	-1	0	0	0
0	1	-1	0	0
0	0	1	-1	0
0	0	0	1	-1
1	0	0	0	-1
1	0	0	0	0