Assignment 3

AI1110: Probability and Random Variables Indian Institute of Technology Hyderabad

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10.15.1.25 Question: Which of the following arguments are correct and which are not correct? Give reasons for your answer.

- 1) If two coins are tossed simultaneously there are three possible outcomes—two heads, two tails or one of each. Therefore, for each of these outcomes, the probability is $\frac{1}{3}$.
- 2) If a die is thrown, there are two possible outcomes—an odd number or an even number. Therefore, the probability of getting an odd number is $\frac{1}{2}$.

Solution: Let us define the random variables X and Y:

Parameter	Value	Description
X	{0,1,2}	Number of Heads in two coin tosses
Y	{1,2,3,4,5,6}	Number appering on a Die throw
n	2	Number of coin tossed
р	$\frac{1}{2}$	Probability of getting heads on a coin

PMF of X:

$$X \sim Bin(n, p)$$
 (1)

$$\Pr(X = i) = {}^{n}C_{i} \times p^{i} \times (1 - p)^{n - i} = {}^{2}C_{i} \times \frac{1}{2^{2}}$$
 (2)

PMF OF Y:

$$\Pr(X = i) = \frac{1}{6}, i = 1, 2, 3, 4, 5, 6 \tag{3}$$

1) There are 3 possible outcomes i.e X = 0, 1, 2For 1st outcome (Two Heads) X=2,

$$\Pr(X=2) = {}^{2}C_{2} \times \frac{1}{2^{2}} = \frac{1}{4}$$
 (4)

For 2nd outcome(Two Tails) X=0,

$$\Pr(X=0) = {}^{2}C_{0} \times \frac{1}{2^{2}} = \frac{1}{4}$$
 (5)

For 3rd outcome (One Head and One Tail) X=1,

$$\Pr(X=1) = {}^{2}C_{1} \times \frac{1}{2^{2}} = 2 \times \frac{1}{4} = \frac{1}{2} \quad (6)$$

From (4), (5) and (6), the probabilities are not equal to $\frac{1}{3}$. Hence, the statement is false.

2) There are 2 possible outcomes i.e Y=Odd,Even

$$Pr(Y = Odd) = Pr(Y = 1) + Pr(Y = 3) + Pr(Y = 5) = \frac{1}{2}$$
(7)

Hence, the statement is true.