

```

In [40]: 1 import networkx as nx
2 import matplotlib.pyplot as plt
3
4 def is_safe(graph, v, color, c):
5     for i in range(len(graph)):
6         if graph[v][i] == 1 and color[i] == c:
7             return False
8     return True
9
10 def graph_coloring_backtracking(graph, m, color, v):
11     if v == len(graph):
12         return True
13
14     for c in range(1, m + 1):
15         if is_safe(graph, v, color, c):
16             color[v] = c
17             if graph_coloring_backtracking(graph, m, color, v + 1):
18                 return True
19             color[v] = 0
20
21     return False
22
23 def branch_and_bound(graph, m, color, v, best_solution):
24     if v == len(graph):
25         return True
26
27     for c in range(1, m + 1):
28         if is_safe(graph, v, color, c):
29             color[v] = c
30             if branch_and_bound(graph, m, color, v + 1, best_solution):
31                 return True
32             color[v] = 0
33
34     return False
35
36 def solve_graph_coloring(n, edges, m):
37     graph = [[0] * n for _ in range(n)]
38
39     for u, v in edges:
40         graph[u][v] = 1
41         graph[v][u] = 1
42
43     color = [0] * n
44
45     print("Solving using Backtracking...")
46     if graph_coloring_backtracking(graph, m, color, 0):
47         print("Solution Found:", color)
48     else:
49         print("No solution exists with given number of colors")
50
51     best_solution = [0] * n
52     print("Solving using Branch and Bound...")
53     if branch_and_bound(graph, m, best_solution, 0, color):
54         print("Solution Found:", best_solution)
55     else:
56         print("No solution exists with given number of colors")
57
58     return color
59
60 def draw_graph(n, edges, color):
61     G = nx.Graph()
62     for i in range(n):
63         G.add_node(i)
64     for u, v in edges:
65         G.add_edge(u, v)
66
67     pos = nx.spring_layout(G)
68     nx.draw(G, pos, with_labels=True, node_color=color, cmap=plt.cm.rainbow, edge_color='black',
69             plt.show())
70
71 if __name__ == "__main__":
72     n = int(input("Enter number of vertices: "))
73     e = int(input("Enter number of edges: "))
74     edges = []
75     for _ in range(e):
76         u, v = map(int, input("Enter edge (u v): ").split())

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77     edges.append((u, v))
78     m = int(input("Enter number of colors: "))
79
80     color = solve_graph_coloring(n, edges, m)
81     draw_graph(n, edges, color)
```

Enter number of vertices: 3

Enter number of edges: 3

Enter edge (u v): 0 1

Enter edge (u v): 1 2

Enter edge (u v): 2 0

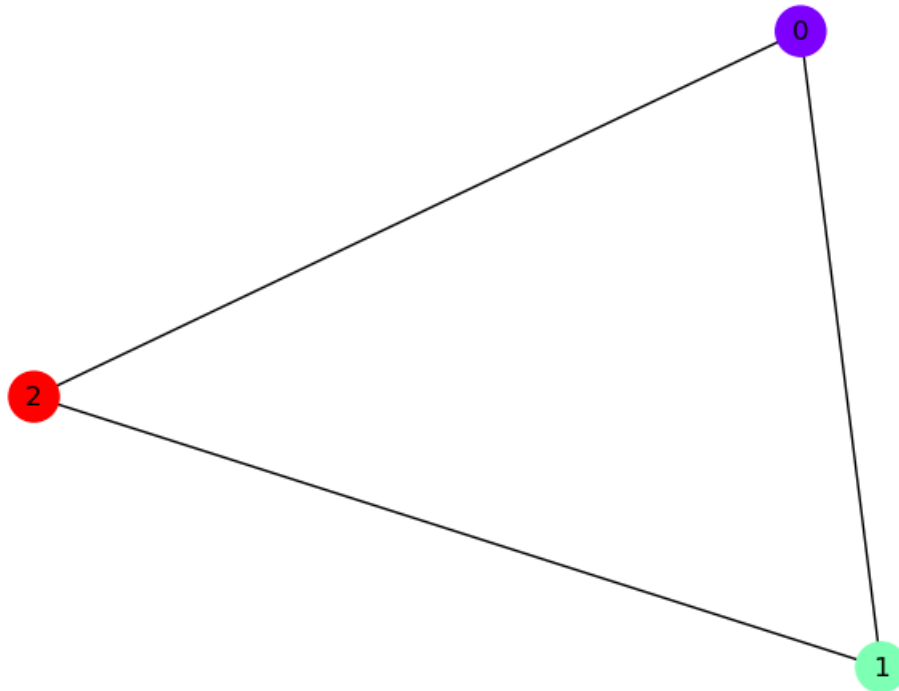
Enter number of colors: 3

Solving using Backtracking...

Solution Found: [1, 2, 3]

Solving using Branch and Bound...

Solution Found: [1, 2, 3]



```

In [30]: 1 import networkx as nx
2 import matplotlib.pyplot as plt
3
4 def is_safe(graph, v, color, c):
5     for i in range(len(graph)):
6         if graph[v][i] == 1 and color[i] == c:
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10 def graph_coloring_backtracking(graph, m, color, v):
11     if v == len(graph):
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13
14     for c in range(1, m + 1):
15         if is_safe(graph, v, color, c):
16             color[v] = c
17             if graph_coloring_backtracking(graph, m, color, v + 1):
18                 return True
19             color[v] = 0
20
21     return False
22
23 def branch_and_bound(graph, m, color, v, best_solution):
24     if v == len(graph):
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27     for c in range(1, m + 1):
28         if is_safe(graph, v, color, c):
29             color[v] = c
30             if branch_and_bound(graph, m, color, v + 1, best_solution):
31                 return True
32             color[v] = 0
33
34     return False
35
36 def solve_graph_coloring(n, edges, m):
37     graph = [[0] * n for _ in range(n)]
38
39     for u, v in edges:
40         graph[u][v] = 1
41         graph[v][u] = 1
42
43     color = [0] * n
44
45     print("Solving using Backtracking...")
46     if graph_coloring_backtracking(graph, m, color, 0):
47         print("Solution Found:", color)
48     else:
49         print("No solution exists with given number of colors")
50
51     best_solution = [0] * n
52     print("Solving using Branch and Bound...")
53     if branch_and_bound(graph, m, best_solution, 0, color):
54         print("Solution Found:", best_solution)
55     else:
56         print("No solution exists with given number of colors")
57
58     return color
59
60 def draw_graph(n, edges, color):
61     G = nx.Graph()
62     for i in range(n):
63         G.add_node(i)
64     for u, v in edges:
65         G.add_edge(u, v)
66
67     pos = nx.spring_layout(G)
68     nx.draw(G, pos, with_labels=True, node_color=color, cmap=plt.cm.rainbow, edge_color='black',
69             plt.show())
70
71 if __name__ == "__main__":
72     n = int(input("Enter number of vertices: "))
73     e = int(input("Enter number of edges: "))
74     edges = []
75     for _ in range(e):
76         u, v = map(int, input("Enter edge (u v): ").split())

```

```
77     edges.append((u, v))
78     m = int(input("Enter number of colors: "))
79
80     color = solve_graph_coloring(n, edges, m)
81     draw_graph(n, edges, color)
```

Enter number of vertices: 5

Enter number of edges: 4

Enter edge (u v): 0 1

Enter edge (u v): 0 2

Enter edge (u v): 0 3

Enter edge (u v): 0 4

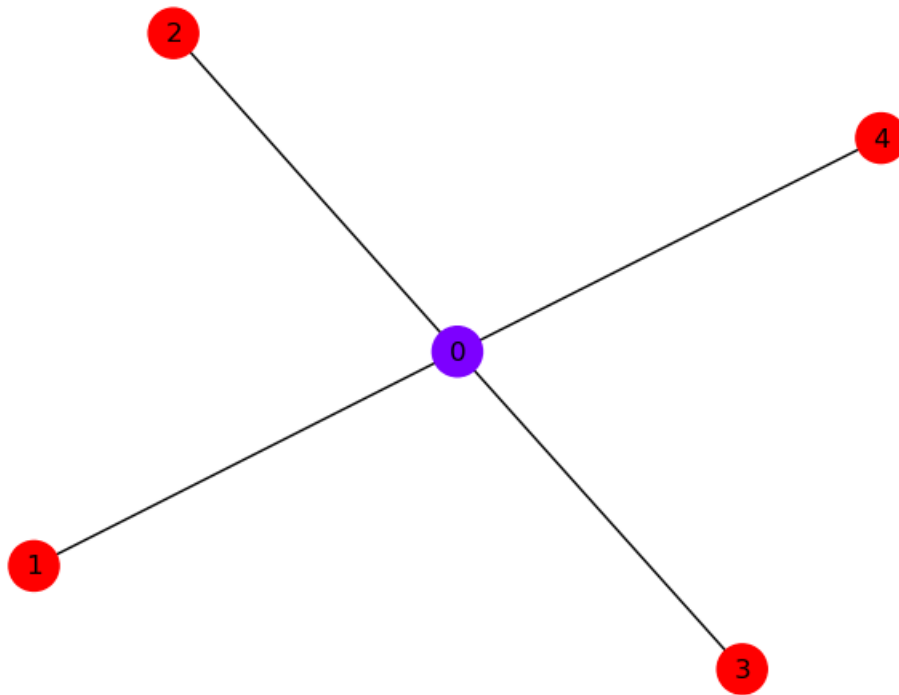
Enter number of colors: 2

Solving using Backtracking...

Solution Found: [1, 2, 2, 2, 2]

Solving using Branch and Bound...

Solution Found: [1, 2, 2, 2, 2]



```

In [32]: 1 import networkx as nx
2 import matplotlib.pyplot as plt
3
4 def is_safe(graph, v, color, c):
5     for i in range(len(graph)):
6         if graph[v][i] == 1 and color[i] == c:
7             return False
8     return True
9
10 def graph_coloring_backtracking(graph, m, color, v):
11     if v == len(graph):
12         return True
13
14     for c in range(1, m + 1):
15         if is_safe(graph, v, color, c):
16             color[v] = c
17             if graph_coloring_backtracking(graph, m, color, v + 1):
18                 return True
19             color[v] = 0
20
21     return False
22
23 def branch_and_bound(graph, m, color, v, best_solution):
24     if v == len(graph):
25         return True
26
27     for c in range(1, m + 1):
28         if is_safe(graph, v, color, c):
29             color[v] = c
30             if branch_and_bound(graph, m, color, v + 1, best_solution):
31                 return True
32             color[v] = 0
33
34     return False
35
36 def solve_graph_coloring(n, edges, m):
37     graph = [[0] * n for _ in range(n)]
38
39     for u, v in edges:
40         graph[u][v] = 1
41         graph[v][u] = 1
42
43     color = [0] * n
44
45     print("Solving using Backtracking...")
46     if graph_coloring_backtracking(graph, m, color, 0):
47         print("Solution Found:", color)
48     else:
49         print("No solution exists with given number of colors")
50
51     best_solution = [0] * n
52     print("Solving using Branch and Bound...")
53     if branch_and_bound(graph, m, best_solution, 0, color):
54         print("Solution Found:", best_solution)
55     else:
56         print("No solution exists with given number of colors")
57
58     return color
59
60 def draw_graph(n, edges, color):
61     G = nx.Graph()
62     for i in range(n):
63         G.add_node(i)
64     for u, v in edges:
65         G.add_edge(u, v)
66
67     pos = nx.spring_layout(G)
68     nx.draw(G, pos, with_labels=True, node_color=color, cmap=plt.cm.rainbow, edge_color='black',
69             plt.show())
70
71 if __name__ == "__main__":
72     n = int(input("Enter number of vertices: "))
73     e = int(input("Enter number of edges: "))
74     edges = []
75     for _ in range(e):
76         u, v = map(int, input("Enter edge (u v): ").split())

```

```

77     edges.append((u, v))
78     m = int(input("Enter number of colors: "))
79
80     color = solve_graph_coloring(n, edges, m)
81     draw_graph(n, edges, color)

```

Enter number of vertices: 6

Enter number of edges: 7

Enter edge (u v): 0 1

Enter edge (u v): 0 2

Enter edge (u v): 1 3

Enter edge (u v): 1 4

Enter edge (u v): 2 4

Enter edge (u v): 2 5

Enter edge (u v): 3 5

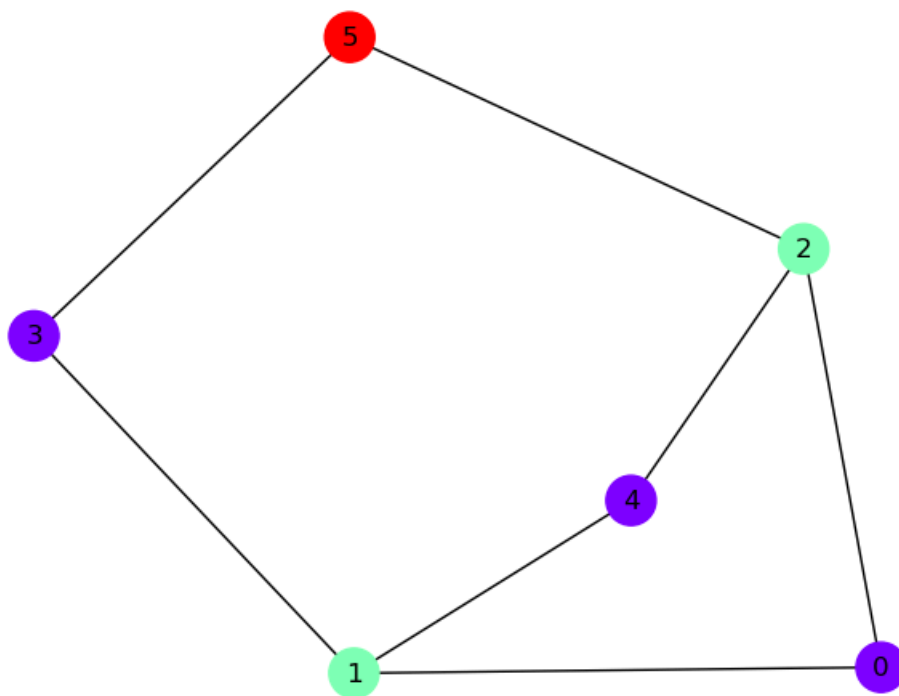
Enter number of colors: 3

Solving using Backtracking...

Solution Found: [1, 2, 2, 1, 1, 3]

Solving using Branch and Bound...

Solution Found: [1, 2, 2, 1, 1, 3]



```

In [24]: 1 def print_solution(board):
2         for row in board:
3             print(" ".join("Q" if col else "." for col in row))
4         print()
5
6 def is_safe(board, row, col, n):
7     for i in range(row):
8         if board[i][col]:
9             return False
10
11     for i, j in zip(range(row, -1, -1), range(col, -1, -1)):
12         if board[i][j]:
13             return False
14
15     for i, j in zip(range(row, -1, -1), range(col, n)):
16         if board[i][j]:
17             return False
18
19     return True
20
21 def solve_n_queens_backtrack(board, row, n):
22     if row == n:
23         print_solution(board)
24         return
25
26     for col in range(n):
27         if is_safe(board, row, col, n):
28             board[row][col] = 1
29             print(f"Placing queen at ({row}, {col})")
30             solve_n_queens_backtrack(board, row + 1, n)
31             board[row][col] = 0 # Backtrack
32             print(f"Backtracking from ({row}, {col})")
33
34 def branch_and_bound_n_queens(n):
35     board = [[0] * n for _ in range(n)]
36     cols = [False] * n
37     diag1 = [False] * (2 * n - 1)
38     diag2 = [False] * (2 * n - 1)
39
40     def solve(row):
41         if row == n:
42             print_solution(board)
43             return
44
45         for col in range(n):
46             if not cols[col] and not diag1[row - col + n - 1] and not diag2[row + col]:
47                 board[row][col] = 1
48                 cols[col] = diag1[row - col + n - 1] = diag2[row + col] = True
49                 print(f"Branching: Placing queen at ({row}, {col})")
50                 solve(row + 1)
51                 board[row][col] = 0
52                 cols[col] = diag1[row - col + n - 1] = diag2[row + col] = False
53                 print(f"Branching: Backtracking from ({row}, {col})")
54
55     solve(0)
56
57 def n_queens(n):
58     print("Solving with Backtracking:")
59     board = [[0] * n for _ in range(n)]
60     solve_n_queens_backtrack(board, 0, n)
61
62     print("\nSolving with Branch and Bound:")
63     branch_and_bound_n_queens(n)
64
65     n = int(input("Enter the number of queens: "))
66     n_queens(n)
67

```

Enter the number of queens: 4

Solving with Backtracking:

Placing queen at (0, 0)

Placing queen at (1, 2)

Backtracking from (1, 2)

Placing queen at (1, 3)

Placing queen at (2, 1)

Backtracking from (2, 1)

Backtracking from (1, 3)

Backtracking from (0, 0)

Placing queen at (0, 1)

Placing queen at (1, 3)

Placing queen at (2, 0)

Placing queen at (3, 2)

. Q . .

. . . Q

Q . . .

. . Q .

Backtracking from (3, 2)

Backtracking from (2, 0)

Backtracking from (1, 3)

Backtracking from (0, 1)

Placing queen at (0, 2)

Placing queen at (1, 0)

Placing queen at (2, 3)

Placing queen at (3, 1)

. . Q .

Q . . .

. . . Q

. Q . .

Backtracking from (3, 1)

Backtracking from (2, 3)

Backtracking from (1, 0)

Backtracking from (0, 2)

Placing queen at (0, 3)

Placing queen at (1, 0)

Placing queen at (2, 2)

Backtracking from (2, 2)

Backtracking from (1, 0)

Placing queen at (1, 1)

Backtracking from (1, 1)

Backtracking from (0, 3)

Solving with Branch and Bound:

Branching: Placing queen at (0, 0)

Branching: Placing queen at (1, 2)

Branching: Backtracking from (1, 2)

Branching: Placing queen at (1, 3)

Branching: Placing queen at (2, 1)

Branching: Backtracking from (2, 1)

Branching: Backtracking from (1, 3)

Branching: Backtracking from (0, 0)

Branching: Placing queen at (0, 1)

Branching: Placing queen at (1, 3)

Branching: Placing queen at (2, 0)

Branching: Placing queen at (3, 2)

. Q . .

. . . Q

Q . . .

. . Q .

Branching: Backtracking from (3, 2)

Branching: Backtracking from (2, 0)

Branching: Backtracking from (1, 3)

Branching: Backtracking from (0, 1)

Branching: Placing queen at (0, 2)

Branching: Placing queen at (1, 0)

Branching: Placing queen at (2, 3)

Branching: Placing queen at (3, 1)

. . Q .

Q . . .

. . . Q

. Q . .

Branching: Backtracking from (3, 1)

Branching: Backtracking from (2, 3)
Branching: Backtracking from (1, 0)
Branching: Backtracking from (0, 2)
Branching: Placing queen at (0, 3)
Branching: Placing queen at (1, 0)
Branching: Placing queen at (2, 2)
Branching: Backtracking from (2, 2)
Branching: Backtracking from (1, 0)
Branching: Placing queen at (1, 1)
Branching: Backtracking from (1, 1)
Branching: Backtracking from (0, 3)