Homework 6

Group 3
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Homework 6

Problem 8.1

Question 8.1.a

```
UniversalBank$Personal.Loan<-as.factor(UniversalBank$Personal.Loan)</pre>
UniversalBank$online<-as.factor(UniversalBank$Online)</pre>
UniversalBank$CreditCard<-as.factor(UniversalBank$CreditCard)</pre>
set.seed(123)
split<-sample.split(UniversalBank$Personal.Loan, SplitRatio=0.6)</pre>
train<-subset(UniversalBank,split==TRUE)</pre>
test<-subset(UniversalBank, split==FALSE)</pre>
table(train$CreditCard, train$Online, train$Personal.Loan)
## , ,
##
##
          0
                1
##
     0 809 1126
##
     1 325 452
##
##
## , ,
       = 1
##
##
##
          0
                1
##
         73
             132
     0
## 1
         40
```

Question 8.1.b

```
#The probability is 0.087 that loan offer will be #accepted
43/(452+43)
## [1] 0.08686869
```

Question 8.1.c

```
#online fucntion
table(train$Personal.Loan, train$Online)

##
## 0 1
## 0 1134 1578
## 1 113 175

#Loan function
table(train$Personal.Loan, train$CreditCard)
```

```
##
##
     0 1
## 0 1935 777
## 1 205 83
Question 8.1.d
Task 8.1.d.i
83/(83+205)
## [1] 0.2881944
#i. 0.288
Task 8.1.d.ii
175/(175+113)
## [1] 0.6076389
#ii. 0.608
Task 8.1.d.iii
table(train$Personal.Loan)
##
## 0 1
## 2712 288
288/(288+2712)
## [1] 0.096
#iii. 0.096
Task 8.1.d.iv
777/(777+1935)
## [1] 0.2865044
#iv. 0.58
Task 8.1.d.v
1578/(1578+1134)
## [1] 0.5818584
#v. 0.904
Task 8.1.d.vi
2712/(2712+288)
## [1] 0.904
```

Question 8.1.e

```
(0.096*0.288*0.608)/((0.096*0.288*0.0608)+(0.904*0.29*0.58))
## [1] 0.1093448
```

Question 8.1.f

#the calaculated b value= 0.087 and we get 8.1 e)0.0995 when we have more predictors

Question 8.1.g

```
model<-naiveBayes(Personal.Loan~., data=train)</pre>
y pred<-predict(model, newdata=train[,-3], type="raw")</pre>
## Warning in predict.naiveBayes(model, newdata = train[, -3], type = "raw"):
## mismatch between training and new data for variable 'Experience'. Did you
## factors with numeric labels for training, and numeric values for new data?
valid<-data.frame(CreditCard="1", Online="1")</pre>
y pred1<-predict(model, newdata=valid,type="raw")</pre>
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'ID'. Did you use
factors
## with numeric labels for training, and numeric values for new data?
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'Age'. Did you use
factors
## with numeric labels for training, and numeric values for new data?
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'Experience'. Did you
use
## factors with numeric labels for training, and numeric values for new data?
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'Income'. Did you use
## factors with numeric labels for training, and numeric values for new data?
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'ZIP.Code'. Did you
## factors with numeric labels for training, and numeric values for new data?
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'Family'. Did you use
## factors with numeric labels for training, and numeric values for new data?
```

```
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'CCAvg'. Did you use
factors
## with numeric labels for training, and numeric values for new data?
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'Education'. Did you
## factors with numeric labels for training, and numeric values for new data?
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'Mortgage'. Did you
## factors with numeric labels for training, and numeric values for new data?
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'Securities.Account'.
Did
## you use factors with numeric labels for training, and numeric values for
new
## data?
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'CD.Account'. Did you
use
## factors with numeric labels for training, and numeric values for new data?
## Warning in predict.naiveBayes(model, newdata = valid, type = "raw"): Type
## mismatch between training and new data for variable 'Online'. Did you use
## factors with numeric labels for training, and numeric values for new data?
y_pred1
## [1,] 0.9034884 0.09651163
#the value is 0.1003 is more
```

Problem 8.2

Question 8.2.a

```
scales::percent(injury.table['yes']/(injury.table['yes']+injury.table['no']))
injury.prob
## yes
## "51%"
```

Almost 51% of the total accidents that have been recorded, have resulted in an injury, we must conclude that an accident is more probable to have an injury.

Question 8.2.b

Task 8.2.b.i

```
newdf <- accidents[1:12, c('INJURY', 'WEATHER_R', 'TRAF_CON_R')]</pre>
newdf
## # A tibble: 12 x 3
     INJURY WEATHER R TRAF CON R
##
##
     <chr>
               <dbl>
                           <dbl>
## 1 yes
                    1
                               0
## 2 no
                    2
                               0
                    2
## 3 no
                               1
## 4 no
                    1
                               1
## 5 no
                    1
                               0
## 6 yes
                    2
                               0
                    2
                               0
## 7 no
## 8 yes
                    1
                               0
## 9 no
                    2
                               0
## 10 no
                    2
                               0
## 11 no
                               0
## 12 no
```

Task 8.2.b.ii

```
#To find P(Injury=yes|WEATHER_R = 1, TRAF_CON_R =0):
numerator1 <- 2/3 * 3/12
denominator1 <- 3/12
prob1 <- numerator1/denominator1

#To find P(Injury=yes|WEATHER_R = 1, TRAF_CON_R =1):
numerator2 <- 0 * 3/12
denominator2 <- 1/12
prob2 <- numerator2/denominator2

#To find P(Injury=yes| WEATHER_R = 1, TRAF_CON_R =2):
numerator3 <- 0 * 3/12
denominator3 <- 1/12
prob3 <- numerator3/denominator3

#To find P(Injury=yes| WEATHER_R = 2, TRAF_CON_R =0):
numerator4 <- 1/3 * 3/12
denominator4 <- 6/12</pre>
```

```
prob4 <- numerator4/denominator4</pre>
#To find P(Injury=yes| WEATHER_R = 2, TRAF_CON_R =1):
numerator5 <- 0 * 3/12
denominator5 <- 1/12</pre>
prob5 <- numerator5/denominator5</pre>
#To find P(Injury=yes | WEATHER R = 2, TRAF CON R = 2):
numerator6 <- 0 * 3/12
denominator6 <- 0
prob6 <- numerator6/denominator6</pre>
a < -c(1,2,3,4,5,6)
b<-c(prob1,prob2,prob3,prob4,prob5,prob6)
prob.df<-data.frame(a,b)</pre>
names(prob.df)<-c('Record No.', 'Probability')</pre>
prob.df %>% mutate if(is.numeric, round, 3)
     Record No. Probability
##
## 1
              1
                       0.667
## 2
               2
                       0.000
               3
## 3
                       0.000
## 4
               4
                       0.167
               5
## 5
                       0.000
## 6
                         NaN
Task 8.2.b.iii
probinj \leftarrow c(0.667, 0.167, 0, 0, 0.667, 0.167, 0.167, 0.667, 0.167,
0.167, 0)
newdfprob <- newdf
newdfprob$PROB_INJ <- probinj</pre>
newdfprob$PREDICT <- ifelse(newdfprob$PROB INJ>.5, 'YES', 'NO')
newdfprob
## # A tibble: 12 x 5
##
      INJURY WEATHER_R TRAF_CON_R PROB_INJ PREDICT
                  <dbl>
                             <dbl>
                                       <dbl> <chr>
##
      <chr>
## 1 yes
                      1
                                  0
                                       0.667 YES
                      2
                                  0
                                       0.167 NO
## 2 no
                      2
## 3 no
                                  1
                                       0
                                              NO
## 4 no
                      1
                                  1
                                              NO
                                       0
## 5 no
                      1
                                  0
                                       0.667 YES
## 6 yes
                      2
                                  0
                                       0.167 NO
## 7 no
                      2
                                  0
                                       0.167 NO
## 8 yes
                      1
                                  0
                                       0.667 YES
## 9 no
                      2
                                  0
                                       0.167 NO
                      2
## 10 no
                                  0
                                       0.167 NO
                      2
## 11 no
                                  0
                                       0.167 NO
## 12 no
                                              NO
```

Task 8.2.b.iv

```
# Find p(INJURY = yes|WEATHER R = 1, TRAF CON R=1):
manprob <- 2/3 * 0/3 * 3/12
manprob
## [1] 0
```

Task 8.2.b.v

```
nbmodel <- naiveBayes(INJURY~.,data = newdf)</pre>
predict(nbmodel, newdata = newdf, type = 'raw')
## Warning in data.matrix(newdata): NAs introduced by coercion
##
                  no
                              yes
## [1,] 0.001916916 0.9980830837
## [2,] 0.006129754 0.9938702459
## [3,] 0.999548668 0.0004513316
## [4,] 0.998552097 0.0014479028
## [5,] 0.001916916 0.9980830837
## [6,] 0.006129754 0.9938702459
## [7,] 0.006129754 0.9938702459
## [8,] 0.001916916 0.9980830837
## [9,] 0.006129754 0.9938702459
## [10,] 0.006129754 0.9938702459
## [11,] 0.006129754 0.9938702459
## [12,] 0.989399428 0.0106005719
x=newdf[,-3]
y=newdf$INJURY
model <- train(x,y,'nb', trControl = trainControl(method = 'cv',number=10))</pre>
## Warning: Setting row names on a tibble is deprecated.
## Warning: NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
```

```
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning: model fit failed for Fold5: usekernel=FALSE, fL=0, adjust=1 Error
in NaiveBayes.default(x, y, usekernel = FALSE, fL = param$fL, ...) :
     Zero variances for at least one class in variables: WEATHER_R
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning: Setting row names on a tibble is deprecated.
## Warning in data.matrix(newdata): NAs introduced by coercion
## Warning in nominalTrainWorkflow(x = x, y = y, wts = weights, info =
trainInfo, :
## There were missing values in resampled performance measures.
```

```
## Warning: Setting row names on a tibble is deprecated.
model
## Naive Bayes
## 12 samples
## 2 predictor
## 2 classes: 'no', 'yes'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 11, 10, 11, 11, 10, 10, ...
## Resampling results across tuning parameters:
##
##
     usekernel Accuracy
                           Kappa
##
     FALSE
                0.8750000
##
     TRUE
                0.8333333 0
##
## Tuning parameter 'fL' was held constant at a value of 0
## Tuning
## parameter 'adjust' was held constant at a value of 1
## Accuracy was used to select the optimal model using the largest value.
## The final values used for the model were fL = 0, usekernel = FALSE and
adjust
## = 1.
model.pred <- predict(model$finalModel,x)</pre>
## Warning in data.matrix(newdata): NAs introduced by coercion
model.pred
## $class
## [1] no no
## Levels: no yes
##
## $posterior
##
                no
                         ves
## [1,] 0.6272018 0.3727982
## [2,] 0.8438158 0.1561842
## [3,] 0.8438158 0.1561842
## [4,] 0.6272018 0.3727982
## [5,] 0.6272018 0.3727982
## [6,] 0.8438158 0.1561842
## [7,] 0.8438158 0.1561842
## [8,] 0.6272018 0.3727982
## [9,] 0.8438158 0.1561842
## [10,] 0.8438158 0.1561842
## [11,] 0.8438158 0.1561842
## [12,] 0.6272018 0.3727982
```

```
table(model.pred$class,y)
##
##
         no yes
##
          9
     no
              3
##
     yes 0
              0
# Comparing this to exact Bayes classification
newdfprob$PREDICT PROBNB <- model.pred$class</pre>
newdfprob
## # A tibble: 12 x 6
      INJURY WEATHER_R TRAF_CON_R PROB_INJ PREDICT PREDICT_PROBNB
##
      <chr>>
                 <dbl>
                            <dbl>
                                      <dbl> <chr>
                                                    <fct>
## 1 ves
                     1
                                      0.667 YES
                                                    no
                     2
## 2 no
                                 0
                                      0.167 NO
                                                    no
                     2
## 3 no
                                 1
                                      0
                                            NO
                                                    no
## 4 no
                     1
                                 1
                                      0
                                            NO
                                                    no
## 5 no
                     1
                                 0
                                      0.667 YES
                                                    no
## 6 yes
                     2
                                 0
                                      0.167 NO
                                                    no
                     2
                                 0
## 7 no
                                      0.167 NO
                                                    no
                     1
## 8 yes
                                 0
                                      0.667 YES
                                                    no
## 9 no
                     2
                                 0
                                      0.167 NO
                                                    no
## 10 no
                     2
                                 0
                                      0.167 NO
                                                    no
## 11 no
                     2
                                 0
                                      0.167 NO
                                                    no
## 12 no
                                            NO
                                                    no
```

Question 8.2.c

```
Task 8.2.c.i
set.seed(1)
train.index <- sample(c(1:dim(accidents)[1]), dim(accidents)[1]*0.6)
train.df <- accidents[train.index,]
valid.df <- accidents[-train.index,]</pre>
```

We can use predictors that describe the road condition and calendar time:HOUR_I_R, ALIGN_I, WRK_ZONE, WKDY_I_R, INT_HWY, LGTCON_I_R, PROFIL_I_R SPD_LIM, SUR_CON, TRAF_CON_R, TRAF_WAY, WEATHER_R

Task 8.2.c.ii

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                no yes
##
          no 5097 7405
##
          yes 4230 8577
##
##
                  Accuracy : 0.5403
##
                    95% CI: (0.5341, 0.5464)
##
       No Information Rate: 0.6315
##
       P-Value [Acc > NIR] : 1
##
##
                     Kappa: 0.0776
##
##
    Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.5367
##
               Specificity: 0.5465
            Pos Pred Value : 0.6697
##
##
            Neg Pred Value : 0.4077
                Prevalence: 0.6315
##
##
            Detection Rate: 0.3389
##
      Detection Prevalence: 0.5060
##
         Balanced Accuracy: 0.5416
##
##
          'Positive' Class : yes
##
nerror <- 1 - 0.5403 #(1 - accuracy)
nerrp <- scales::percent(nerror,0.01)</pre>
```

Task 8.2.c.iii

```
predictvalid <- predict(nbmodel,valid.df[,vars])</pre>
predictvalid
##
        [1] no
                 no
                     no
                          no
                               no
                                    no
                                        no
                                             no
                                                  no
                                                      no
                                                           no
                                                                no
                                                                    no
                                                                         no
                                                                              no
                                                                                  no
                                                                                       no
no
##
       [19] no
                 no
                      no
                          no
                               no
                                    no
                                        no
                                             no
                                                  no
                                                      no
                                                           no
                                                                no
                                                                    no
                                                                         no
                                                                              no
                                                                                  no
                                                                                       no
no
##
       [37] no
                 no
                     no
                          no
                               yes no
                                        no
                                             no
                                                  no
                                                      no
                                                           no
                                                                no
                                                                    no
                                                                         no
                                                                                  no
                                                                                       no
                                                                              no
no
##
       [55] no
                                             no
                 no
                     no
                          no
                               no
                                    no
                                        no
                                                  no
                                                      no
                                                           no
                                                               no
                                                                    no
                                                                         no
                                                                              no
                                                                                  no
                                                                                       no
no
##
       [73] no
                 no
                     no
                          no
                               no
                                    no
                                        no
                                             yes no
                                                      yes no
                                                               no
                                                                    no
                                                                         no
                                                                              no
                                                                                  yes no
no
##
       [91] no
                 no
                      no
                          no
                               no
                                    no
                                        no
                                             no
                                                  no
                                                      no
                                                           no
                                                                no
                                                                    no
                                                                         no
                                                                              no
                                                                                  no
                                                                                       no
no
##
      [109] no
                          yes no
                 yes no
                                    no
                                        no
                                             no
                                                  no
                                                      no
                                                           no
                                                                no
                                                                    no
                                                                         no
                                                                              no
                                                                                  no
                                                                                       no
no
##
      [127] no no
                    no
                          no
                               no
                                    no no
                                             no
                                                 no
                                                      no no
                                                               no
                                                                    no
                                                                             no
                                                                                  no
                                                                                       no
                                                                        no
```

```
no
##
   [145] no no
           no
              yes no
                    no no
                         no
                            no
                              no
                                 no
                                    no
                                      no
                                        no no
no
##
   [163] no
         no
            no
               no
                 no
                      no
                                   yes no
                                         yes yes yes
                    no
                         no
                            no
                              no
                                 no
yes no
##
   [181] no
                    yes yes yes yes yes yes yes yes no
         no
            no
               no
                 no
yes yes
   [199] no
##
         no
            yes no
                 yes yes yes no no yes yes yes yes yes no
no
##
   [217] no yes no yes yes yes yes yes yes yes no no no yes no no
no
##
   [235] yes yes yes yes yes yes yes yes no no no
                                      yes yes yes yes
yes no
##
   [253] yes yes yes yes no no yes yes yes yes no
                                      no no no yes no
no
##
   [271] no yes no yes yes no yes yes no yes yes no yes no yes no
no
##
   ves
##
   yes yes
##
   yes yes
##
   yes yes
##
   yes yes
##
   [379] yes yes no yes yes yes yes no yes yes yes yes yes yes yes
yes yes
   [397] no yes yes yes yes yes yes yes yes no no yes yes yes
##
yes yes
   [415] yes yes yes no yes yes yes yes yes yes yes no no yes
##
ves ves
   [433] yes yes yes no yes yes no yes no yes yes yes yes yes
yes yes
##
   yes yes
##
   yes yes
   [487] yes yes yes no yes yes yes yes no yes yes yes yes yes yes
yes yes
##
   [505] yes yes yes yes no no no no yes yes yes yes yes yes yes
   [523] yes yes yes yes yes no yes yes no
##
                                no
                                    no
                                      no
                                         yes yes yes
ves ves
##
   [541] yes yes yes yes yes no no no no
                                      no yes yes yes
                                   no
yes yes
##
   yes yes
   [577] yes yes no no yes yes no no no yes yes yes yes yes yes
```

```
yes yes
##
     [595] no no yes yes yes no yes yes no no no
                                                          no
                                                               no
                                                                  no yes yes
yes yes
##
     no
no
##
               yes no
     [631] no
                                             yes no
                        no
                            no
                                 no
                                     no
                                         no
                                                      no
                                                          no
                                                               no
                                                                   no
                                                                       no
                                                                            no
                                                                                no
no
##
     [649] no
               no
                    no
                        no
                            no
                                 no
                                     no
                                         no
                                              no
                                                  no
                                                      no
                                                          no
                                                               no
                                                                   no
                                                                       no
                                                                            no
                                                                                no
no
##
     [667] no
               no
                    no
                        no
                            no
                                     no
                                              no
                                                               no
                                                                   no
                                                                       no
                                 no
                                         no
                                                  no
                                                      no
                                                          no
                                                                            no
                                                                                no
no
##
     [685] no
               no
                    no
                        no
                            no
                                 no
                                     no
                                         no
                                              no
                                                  no
                                                      no
                                                               no
                                                                   no
                                                                       no
                                                                            no
                                                          no
                                                                                no
no
##
     [703] no
               no
                    no
                        no
                            no
                                 no
                                     no
                                         no
                                              no
                                                  no
                                                      no
                                                          no
                                                               no
                                                                   no
                                                                       no
                                                                            no
                                                                                no
no
##
     [721] no
               no
                    no
                        no
                            no
                                 no
                                     no
                                         no
                                              no
                                                  no
                                                      no
                                                          no
                                                               yes no
                                                                       no
                                                                            no
                                                                                no
no
##
     [739] no
               no
                    no
                        no
                            no
                                 no
                                     no
                                         no
                                              no
                                                  no
                                                      no
                                                          no
                                                               no
                                                                   no
                                                                       no
                                                                                no
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yes
##
     [757] no
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
     [865] no
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##
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no
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no
##
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no
##
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no
##
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no
##
     [973] no
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no
##
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no
##
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##
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yes yes
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no
##
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ves no
##
    [1081] no
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yes no
##
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no
##
    [1117] no
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no
##
    [1135] no
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yes no
##
    [1153] yes yes no
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                                                                   yes yes no
no
##
    [1171] no
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no
##
    [1189] no
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yes yes
    [1207] no
##
               yes yes yes no
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no
##
    [1225] no
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no
##
    [1243] no
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yes
##
    [1261] yes yes yes yes yes yes no
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yes yes
##
    [1279] yes yes yes yes yes yes no no yes yes yes yes yes no
no
##
    [1297] no
              no
                   no
                       no
                           no
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yes
##
    [1315] no
              no
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                          yes no
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                                                       yes no
                                                               yes yes yes
ves ves
    [1333] yes yes yes yes no
                                  yes yes yes yes no yes yes yes yes no
yes
##
    [1351] yes yes yes yes no yes no no yes no yes no yes yes yes
yes yes
   [1369] yes yes no yes yes yes yes yes yes no yes yes yes no no
yes yes
   [1387] yes no
                  no
                       no
                           no
                              no
                                  yes yes yes yes yes no yes yes yes
yes yes
##
    [1405] yes yes no yes no no
                                  yes no no no yes yes yes yes yes
##
   [1423] yes yes yes yes yes yes no yes yes yes yes yes yes yes yes
ves ves
## [1441] yes no yes yes yes yes yes yes no yes no no yes yes yes
yes yes
##
    [1459] yes yes yes yes no yes yes yes yes no yes no no
no
##
    [1477] no no no no yes no yes yes yes yes yes yes yes yes yes
```

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yes yes
yes yes
## [1513] yes yes yes yes yes yes yes no yes yes no yes no
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                                    no
ves
##
 [1531] yes no yes yes yes yes yes no yes no yes yes yes no yes
yes no
##
 [1549] yes no no
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yes yes
 [1567] yes yes yes yes no
                no
                   no
                    no
                      ves ves ves ves ves ves
ves ves
##
 [1585] yes no
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           no
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               no
                 no
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                     no
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                                    no
no
##
  [1603] no no
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                      yes yes no
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yes
##
  [1621] yes yes no yes yes no yes yes yes yes yes yes yes yes yes
yes yes
 [1639] yes yes yes yes yes yes yes yes no yes no yes no
yes
##
 [1657] no no
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          no
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              no no
                  yes yes yes no yes yes yes no
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yes yes
 [1675] yes yes yes no yes no yes yes yes yes no
                            yes no
                                   no
ves no
##
 [1693] no no
        no
          no
             yes yes no no yes yes no
                           no
                             no
                              no
                                   no
yes no
##
  [1711] no no
         yes no
             no yes yes yes no no
                           no
                             no
                              no
                                   no
no
##
  [1729] no
      no
        no
          no
            yes yes
 ##
yes yes
ves ves
 yes yes
yes yes
 ves ves
 yes yes
 ##
ves ves
yes yes
 yes yes
```

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yes yes
yes yes
## [1963] yes yes yes yes yes no yes yes yes yes yes yes yes yes yes
ves ves
 yes yes
 yes yes
##
 yes
##
 yes yes
ves ves
yes yes
yes yes
 ves ves
 ves ves
 [2161] yes yes yes yes yes yes no no yes yes yes yes yes yes yes
yes yes
yes yes
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yes yes
## [2215] yes yes yes no yes yes no no yes yes yes yes yes yes yes yes
ves ves
 yes yes
 no
##
 [2269] no yes yes no yes no yes yes yes yes yes yes yes yes yes
ves ves
 yes yes
 ## [2323] yes yes yes no no no yes yes yes yes no no yes yes
ves no
## [2341] yes no yes yes yes no no yes yes yes yes yes yes yes yes
yes yes
 [2359] yes yes yes yes yes yes yes yes yes no no no yes yes yes
##
yes yes
## [2377] yes yes yes yes yes yes no no yes no yes yes no no no no
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no
##
 [2395] no yes yes yes
yes yes
ves ves
 yes yes
[2449] yes yes yes yes yes yes yes no yes yes yes yes yes yes yes
yes yes
ves ves
yes yes
yes yes
ves ves
yes yes
yes
##
 ves ves
 [2593] yes no yes no yes yes yes yes no yes no yes yes yes yes
##
yes yes
yes yes
yes yes
##
yes yes
ves ves
yes yes
yes
##
 yes yes
 yes yes
##
 [2755] yes no yes no no yes yes yes yes yes yes yes no yes yes
## [2773] yes yes yes yes yes no yes no yes yes yes yes no no
ves no
## [2791] no no no no no no no yes no yes no no yes yes yes
yes yes
##
 yes yes
```

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yes yes
  yes yes
  [2863] no yes yes yes no yes yes no yes yes yes yes yes yes yes
ves ves
   [2881] yes no yes yes yes yes no no yes no yes yes yes yes yes
yes yes
##
   yes no
   [2917] yes no
##
              ves ves ves no
                           no
                              no
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                                    ves no
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no
##
   [2935] no
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no
##
   [2953] no
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no
##
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no
##
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                        no
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yes yes
   yes yes
   ves ves
   ##
yes yes
  yes yes
##
  yes yes
   [3097] yes no
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yes yes
   [3115] yes yes no
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
   [3277] no
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```

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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
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yes
##
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no
##
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no
##
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no
##
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yes
    no
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##
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no
     [3601] no
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no
##
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no
##
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no
##
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no
##
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no
##
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no
##
    [3709] no
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                      no
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yes yes
   [3727] no yes no
                           yes yes yes no yes no no yes yes no no yes no
```

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no
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no
##
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no
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##
    [3781] yes no
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no
##
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no
##
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no
##
    [3835] no
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yes no
##
    [3853] no
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                    no
                        no
                            yes yes no
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yes no
##
    [3871] yes no
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no
##
    [3889] no
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no
##
    [3907] no
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no
##
    [3925] no
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                                     no
                                         yes yes yes no
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                        no
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yes yes
##
    [3943] yes no
                    no
                        no
                            no
                                 yes yes no
                                             yes yes yes yes no
                                                                   yes yes yes no
yes
##
    [3961] no
              no
                            yes yes yes no
                                             yes yes no
                                                                       yes no
                    no
                        no
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yes
##
    [3979] yes yes no
                        no
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                                 no
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yes no
##
    [3997] yes no
                    no
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                                                      yes no
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nο
##
    [4015] no
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no
##
    [4033] no
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no
##
    [4051] no
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no
##
    [4069] no
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                                         yes yes yes no
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no
##
    [4087] no
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no
##
    [4105] no
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                    no
                        no
                            no
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                                         yes no
                                                  yes yes no
                                                               yes yes yes no
yes no
##
    [4123] yes yes no
                       yes yes yes no
                                         yes no
                                                  no
                                                      no
                                                          yes no
                                                                   yes yes yes no
ves
##
    [4141] yes yes yes yes no
                                    no
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                                                                   yes no yes
yes yes
   [4159] no yes no
##
                            no
                                no
                                    yes yes yes yes yes yes yes yes yes
                        no
yes no
   [4177] no no no yes yes no yes no no yes yes no yes no no no
```

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no
##
   [4195] yes yes yes no no yes yes no no yes no no yes no no
yes
   [4213] no no
##
               no
                   yes yes yes yes no yes yes yes yes yes yes yes
yes no
##
   [4231] yes no
                   yes yes no yes yes yes no no no no no no
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no
   [4249] no yes no
##
                   no
                      no no yes yes no yes yes yes yes yes yes
yes yes
##
   [4267] yes yes yes no
                      yes yes yes no no no no no
                                                  no no no
no
##
   [4285] no no no
                   no
                      yes
##
   [4303] no yes yes yes yes yes yes yes no yes yes yes yes yes
yes yes
##
   [4321] yes yes yes yes no yes no yes yes no
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                                                  yes yes yes no no
ves
##
   [4339] no no yes no
                      no no no
                                 no no
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                                                      yes yes yes
ves ves
   yes yes
##
   [4375] yes yes no no yes no no yes no yes yes yes yes yes no
no
##
   [4393] yes yes yes no yes yes yes no
                                       no no yes no yes no
no
##
   [4411] yes yes yes yes no yes yes no
                                    no
                                        yes no
                                               no
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yes no
##
   [4429] yes yes yes no
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                             yes no
                                     no
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                                           ves no
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yes
##
   [4447] no
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no
##
   [4465] no no
                no
                   no
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                             no
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                                    yes yes yes yes yes yes yes
ves ves
   [4483] yes yes yes yes yes yes yes yes yes no
                                               no ves ves ves ves
yes yes
   [4501] yes no
                no
                   no
                       yes no yes yes no no no
                                               yes no no
                                                                 no
no
##
   [4519] no no
                       no yes yes yes yes yes no yes yes no
                no
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no
##
   [4537] no no
                yes no
                       no
                          yes no no
                                    no no no
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ves no
##
   [4555] yes yes yes no
                       yes yes no no yes yes yes no
   [4573] yes no yes no
##
                      yes yes no yes yes yes no no yes no
                                                          yes yes no
no
##
   [4591] no
               yes no yes yes yes no yes no yes yes no
            no
                                                                 no
no
##
   [4609] no
            no
                yes yes yes yes yes yes yes no yes no
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no
##
   [4627] no no no yes no yes no no no yes no no no
```

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no
##
    [4645] yes no no
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                              no no yes yes yes yes yes yes no no
yes no
##
    [4663] no
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              yes yes no
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no
##
    [4681] no
                                   yes yes yes no
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              no
                   no
                      no
                           no
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yes
##
    [4699] yes no
                   yes yes yes no
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yes
##
    [4717] no
              no
                   ves no
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yes
##
    [4735] yes no
                   yes no
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no
##
    [4753] no
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no
##
    [4771] no
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no
##
    [4789] no
              no
                   yes no
                           no
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                                               yes no
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yes yes
   yes yes
   [4825] yes yes yes yes no yes yes yes yes yes yes yes yes yes
ves ves
    [4843] yes no
##
                  yes yes no yes no no yes yes yes no yes yes no
yes yes
   [4861] yes no
                  no
                      yes no yes yes yes no no
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yes no
##
    [4879] no yes no
                      yes yes no no yes yes yes no
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yes no
    [4897] no
##
              no
                  no
                      yes yes yes no
                                           yes no
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yes
    [4915] no
##
              yes yes no
                           yes no
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ves
##
    [4933] yes no
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yes
##
    [4951] yes no
                   no
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                           yes no
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no
##
    [4969] no
                              yes yes no
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no
##
    [4987] no
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                           yes no
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no
##
    [5005] no
               yes yes yes no
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                                   yes no
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no
##
    [5023] no
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                           yes no
                                   yes yes no
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no
##
    [5041] no
               yes yes no
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no
##
    [5059] no
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no
##
    [5077] no no
                  yes no
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no
##
     [5095] no
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no
##
     [5113] no
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                  no
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yes no
##
     [5131] no
                       no
                                               yes no
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no
##
     [5149] no
                  no
                       yes no
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no
##
     [5167] no
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##
     [5185] no
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no
##
     [5203] no
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no
##
     [5221] no
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no
##
     [5239] no
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no
##
     [5257] no
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##
     [5275] no
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no
##
     [5293] no
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no
##
     [5311] no
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no
##
     [5329] no
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no
##
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no
##
     [5365] no
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no
##
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no
##
     [5401] no
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no
##
     [5419] no
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no
##
     [5437] no
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no
##
     [5455] no
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no
##
     [5473] no
                  no
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no
##
     [5491] no
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no
##
     [5509] no
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no
##
     [5527] no
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```

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no
##
     [5545] no
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no
##
     [5563] no
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yes
##
     [5581] no
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                  no
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no
##
     [5599] no
                  no
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                                          no
                                               yes yes no
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no
##
                  no
     [5617] no
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no
##
     [5635] no
                  no
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yes
##
     [5653] no
                  yes no
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                                yes no
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no
##
     [5671] no
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                                                                  yes no
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no
##
     [5689] no
                  no
                      no
                           no
                                no
                                     no
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                                               yes no
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no
##
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                      no
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no
##
     [5725] no
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no
##
     [5743] no
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yes
##
     [5761] no
                  no
                      no
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                                          no
                                                   yes no
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no
##
     [5779] no
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no
##
    [5797] no
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no
##
     [5815] yes no
                      yes no
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no
##
     [5833] no
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no
##
    [5851] no
                  no
                      no
                           yes no
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yes no
##
    [5869] no
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##
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     [5887] no
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##
     [5905] no
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##
     [5923] no
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##
     [5941] no
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##
     [5959] no
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##
    [5977] no
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no
##
    [5995] no
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                                           yes no yes yes yes yes no
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no
##
    [6013] no
                         yes no
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no
##
    [6031] no
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no
##
    [6049] no
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                              yes no
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no
##
    [6067] no
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##
    [6085] no
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                         yes yes yes no
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yes yes
##
    [6103] yes yes no
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no
##
    [6121] no
                no
                     yes yes yes no
                                       no
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##
    [6139] no
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##
    [6157] no
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no
##
    [6175] no
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                              yes no
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no
##
    [6193] no
                yes yes yes yes no
                                           yes yes no
                                                         yes no
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yes no
##
    [6211] no
                no
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no
##
    [6229] yes no
                     yes yes yes no
                                           no
                                                yes no
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yes yes
##
    [6247] yes no
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##
    [6265] no
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yes
##
    [6283] yes yes yes no
                              yes no
                                       yes no
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no
##
    [6301] no
                no
                     no
                         no
                              no
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                                                yes no
                                                         yes yes no
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no
##
    [6319] no
                     yes yes no
                                  yes yes yes yes yes no
                no
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yes no
##
    [6337] no
                no
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no
##
    [6355] no
                                                         yes yes yes yes yes no
                no
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no
##
    [6373] no
                yes yes yes no
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no
##
    [6391] no
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no
##
    [6409] no
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                                                                  yes yes yes no
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no
##
    [6427] no
               no
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                                                    yes no
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no
##
    [6445] no
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no
##
    [6463] no
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no
##
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    [6481] no
                                            yes yes no
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no
##
    [6499] yes yes yes yes no
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no
##
    [6517] no
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##
    [6535] no
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no
##
    [6553] no
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                              yes yes no
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no
##
    [6571] no
                no
                     yes no
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yes
##
    [6589] yes yes yes yes yes yes yes yes no
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##
    [6607] no
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##
    [6625] no
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no
##
    [6643] no
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                              yes yes yes no
                                                yes yes yes yes no
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no
##
    [6661] no
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no
##
    [6679] no
                 yes yes no
                              yes yes yes yes yes yes yes yes no
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no
##
    [6697] no
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no
##
    [6715] no
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no
##
    [6733] no
                 yes no
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                                       yes yes no
                                                     yes yes no
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yes yes
##
    [6751] no
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no
##
    [6769] no
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no
##
    [6787] no
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yes
##
    [6805] yes no
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yes no
##
    [6823] no
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yes no
##
    [6841] no
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no
##
    [6859] no
                 no
                     yes yes no
                                   yes no
                                            yes yes yes no
                                                              yes no
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yes no
    [6877] no no
                        no
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                                  yes no no no no no
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no
##
    [6895] no
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no
##
    [6913] no
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no
##
    [6931] no
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##
    [6949] no
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no
##
    [6967] no
                  yes yes no
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no
##
    [6985] no
              no
                  no
                      yes yes no
                                  yes no
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yes
##
    [7003] no
              no
                  yes no
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no
##
    [7021] no
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no
##
    [7039] no
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##
    [7057] no
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no
##
    [7075] no
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no
##
    [7093] no
              no
                  yes no
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no
##
    [7111] no
              yes no
                          yes yes no
                                          yes no
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no
##
    [7129] no
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no
##
    [7147] no
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no
##
    [7165] no
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no
##
    [7183] no
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no
##
    [7201] no
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no
##
    [7219] no
              no
                              yes no
                                          yes no
                                                      yes yes yes yes
                  no
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yes yes
##
    [7237] yes no
                  no
                      no
                          yes yes yes yes yes yes no
                                                         no
                                                             yes yes yes
yes yes
##
    ##
                                                                 yes yes
##
   [7291] yes no yes yes no yes yes no yes yes no yes yes yes
yes yes
##
    no
    [7327] yes yes yes yes no no yes yes no no no no no
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yes no
   [7345] yes yes yes yes yes yes no yes yes yes yes yes yes no yes no
yes
##
   [7363] yes yes yes yes no yes yes yes yes yes no
                                            no
                                               no
                                                  ves no
                                                         no
no
##
   [7381] yes yes yes yes yes yes yes yes no no no
                                               no yes no
no
##
   [7399] no no
             no
                no
                    no no no yes yes no yes yes yes yes yes
yes yes
   [7417] yes no
##
              yes yes no yes yes no no yes yes no yes yes no
                                                         no
no
##
   [7435] no
           no
              no
                 no
                    no
                       no
                          no
                             yes yes yes no
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no
##
   [7453] no
                          yes no
                                         yes yes no
                                                  yes yes no
           no
              no
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                    yes no
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no
##
   [7471] no
           no
              no
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                    no
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                          no
                             yes no
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                                          ves no
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yes no
##
   [7489] no
           no
              yes no
                    yes yes no
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no
##
   [7507] no
          no
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                 no
                    no
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                                                      yes
yes yes
                         yes yes yes yes yes yes yes yes yes
  [7525] yes yes yes yes no no
ves ves
   [7543] yes yes yes yes no no yes yes yes yes yes yes yes yes yes
yes yes
  yes yes
##
 [7579] yes yes yes yes no no no yes yes yes yes yes yes yes yes no
no
##
   [7597] yes yes yes no no no yes yes yes yes yes yes no no
yes yes
  [7615] yes yes yes no yes yes yes yes no no yes yes yes yes yes
##
ves no
   [7633] no no yes no yes no yes no no no
                                      no yes no yes yes yes
yes yes
## [7651] yes yes yes yes yes no no yes yes yes yes yes yes yes yes
yes yes
  [7669] yes yes yes yes yes yes yes yes yes no no yes no yes
ves no
   yes yes
##
   yes
##
   ves ves
yes yes
  [7759] yes yes no no yes no yes yes no no no yes yes yes
yes yes
  [7777] yes yes yes yes yes yes no yes yes yes yes yes yes yes yes
```

```
yes yes
yes yes
ves ves
 yes yes
 [7849] yes yes no yes yes yes yes no yes yes no yes yes yes yes
yes yes
 ves ves
##
 yes yes
yes yes
 ves ves
## [7939] yes yes yes no yes yes yes no yes yes no
                    no no no yes
yes yes
yes yes
 [7975] yes yes yes yes yes yes yes yes yes no no
                     no no
                        no
ves
##
 [7993] yes yes yes yes yes yes yes yes yes no no yes yes yes
yes yes
 yes yes
yes yes
 [8047] yes yes yes yes yes yes no no yes no yes yes yes yes yes
##
yes yes
ves ves
 yes yes
yes yes
 ves ves
 [8137] yes yes yes yes no no yes yes yes yes no no
                      ves ves
yes yes
##
 [8155] yes yes no no no no no no no no
yes
##
 ves ves
yes yes
 ##
yes yes
## [8227] yes yes yes yes yes no yes yes yes yes no yes yes yes no
```

```
no
##
  [8245] no no
         no
           no
              no
                no no
                   no no no no
                            no no no no
no
##
  [8263] no no
         no
                 no
                   yes yes yes yes yes yes yes yes
           no
              no
               no
yes yes
##
  yes
##
  [8299] no no no no no no yes yes yes yes yes yes yes yes yes
yes no
  ##
ves ves
##
  [8335] yes yes no yes no no no yes no yes yes yes yes yes yes
yes yes
##
  [8353] yes yes yes yes yes yes yes yes yes no
                            no
                              no
                                no no
                                    no
                                      no
no
##
  [8371] no no no no no no no
                     no
                        no no
                            no
                              no
                                yes no
                                    no
                                      nο
no
##
  [8389] yes yes yes yes yes yes yes no yes yes yes yes yes yes yes no
no
##
  yes yes
##
  [8425] yes yes yes yes yes yes no yes yes no no yes yes yes no
ves
##
  yes yes
 yes yes
##
 yes
##
  [8497] yes yes yes yes no yes yes no yes yes yes yes yes yes yes
yes yes
ves ves
 [8533] yes yes yes no no no yes yes yes yes yes no no yes no
ves
##
  yes yes
 ves ves
 [8587] no yes no yes yes yes yes no yes no yes no no yes no
yes yes
##
  yes yes
 [8623] yes yes yes yes yes yes yes yes no no yes no no yes no
##
ves ves
## [8641] no no no no yes no yes yes yes yes yes yes yes yes yes
yes yes
##
 yes yes
```

```
yes yes
  [8695] yes yes yes yes yes no yes yes no no no yes yes yes
yes yes
##
  [8713] no
          ves no no
                   no
                     no
                         no
                            no
                              no
                                  no
                                     yes yes yes yes yes no
no
                                                   yes
##
  [8731] no
          yes yes yes no
                         no
                            yes no
                                  no
                                     no
                                       no
                                          no
                                             no
                                                no
yes no
##
  [8749] no
          no
             yes no
                   no
                      no
                         no
                            no
                               no
                                  no
                                     no
                                       no
                                          no
                                             no
                                                no
                                                   no
                                                      no
no
##
  [8767] no
             no
                   no
                         no
          no
                no
                      no
                            no
                               no
                                  no
                                     no
                                       no
                                          no
                                             no
yes
##
  [8785] no
          no
             no
                no
                   yes yes yes no yes yes no
                                       yes yes yes no
                                                      no
yes
##
  [8803] no yes no
               yes yes yes yes yes no no yes yes yes yes no
yes yes
  ves ves
yes yes
  yes yes
  ves ves
##
  [8893] yes yes yes yes no yes no yes yes yes yes no yes yes yes no
ves
##
  [8911] yes yes yes yes yes yes yes yes yes no yes yes yes yes
yes yes
  [8929] no
##
          no
             no
                no
                  yes yes yes no yes yes yes no no yes no
yes
##
  [8947] no no
             no
                no
                   no no no
                           no
                              yes no yes yes yes yes yes
yes yes
##
  [8965] yes yes yes yes yes no
                            yes no
                                  no
                                     no
                                       yes yes no yes yes no
no
##
  [8983] no no
             no
                no
                   no
                     no
                         no
                            no
                               no
                                  no
                                     no
                                       no
                                          no
                                             no
                                                no
no
##
  [9001] no no yes yes yes yes yes no no
                                    yes yes yes yes yes
yes yes
  ves ves
  ves ves
  [9055] yes yes yes yes no no no no no yes no yes yes yes
##
  [9073] yes no yes yes no no yes yes yes yes yes yes yes no yes no
no
##
  [9091] yes yes yes no yes no
                                 yes yes no yes no yes no
                           no
                               no
no
##
  [9109] no no
             no
                no
                   yes yes no
                               no
                                  yes no
                                       yes no
                                             yes no
                            no
                                                   yes
yes yes
  [9127] yes no no
                   no no no
                no
                           no
                               no
                                 no no
                                       no
                                          no
                                             no no
```

```
no
##
   [9145] no
          no
             no
                no
                   no
                      no
                         no
                            no
                               no
                                  no
                                     no
                                        no
                                           no
                                              no
                                                no
                                                   no
                                                      no
no
##
  [9163] no
             no
                   no
                      no
                         no
          no
                no
                            no
                               no
                                  no
                                     no
                                        no
                                           no
                                              no
                                                no
                                                   no
                                                      no
no
##
   [9181] no
          no
             no
                no
                   no
                      no
                         no
                            no
                               no
                                  no
                                     no
                                        no
                                           no
                                              no
                                                 no
                                                   no
                                                      no
no
##
  [9199] no
          no
             no
                no
                   no
                      yes yes no
                               no
                                  yes no
                                        yes yes no
                                                   yes
yes no
  [9217] no
##
             yes yes yes no yes no yes yes yes no no
                                                   ves no
          no
                                                no
ves
##
  yes yes
  ##
yes yes
  ves ves
yes yes
 yes no
  [9325] yes yes yes yes yes yes yes no yes yes yes yes yes yes yes
ves ves
  [9343] yes yes yes yes yes no yes yes no yes yes no yes no
##
  [9361] no yes yes yes yes yes yes yes yes yes no no yes yes
yes no
##
  [9379] yes no yes no yes yes no yes no no no yes yes yes no yes
yes yes
  [9397] yes yes no no yes yes no yes no yes no yes no yes
##
yes no
  ##
no
##
  [9433] yes no yes no
                   yes yes yes yes yes no
                                        ves ves no
                                                ves no
yes yes
##
  [9451] no yes no
               no
                   no
                      no
                        no
                           no
                               no
                                  no
                                     no
                                        no
                                           no
                                              no
                                                no
                                                   no
                                                      no
no
##
  [9469] no
          yes yes yes no yes yes yes no
                                     no
                                        no
                                           no
                                              no
                                                yes no
                                                      no
yes
##
  [9487] no
          no
             no
                no
                  no no no no
                                 no
                                     no
                                        yes no
                                              no
                                                no
                                                   no
yes yes
##
  [9505] no yes yes yes yes yes yes yes no no
                                       no yes yes yes yes
##
  [9523] yes yes no yes yes yes yes yes yes yes yes yes no yes no
no
##
  [9541] yes yes no no yes yes no no no yes yes no yes no
yes
##
  [9559] no no yes yes yes yes yes no yes no yes no yes yes no
                                                      no
no
##
  [9577] no no no yes yes yes no no yes no yes yes no yes yes no
```

```
yes no
##
 [9595] no
      no
        no
          yes no yes no no
                    no
                      no
                        no
                          no
                            no no no
no
##
 [9613] no
       no
         no
           no
             no
              no
                yes no
                      no
                        yes yes yes yes yes
                    no
yes yes
##
 [9631] no
       yes yes no
            yes no
                  yes no
                            yes no
                no
                      yes no
                          no
                                yes no
                                    no
yes
##
 [9649] yes no
        yes no
             no
              no
                no
                  no
                    no
                      no
                        no
                          no
                            no
                              no
                                no
                                  no
                                    no
yes
 [9667] no
##
         no
             no
                no
                          ves ves ves no
       no
           no
              no
                  no
                    no
                      no
                        no
no
##
 [9685] no
       no
         no
           no
            yes yes
##
 [9703] no
       yes yes yes yes yes no
                          yes no
                    no
                      yes no
                              no
                                no
                                  yes
yes no
##
 [9721] no no
        yes yes no
              no
                no
                  no
                    no
                      no
                        no
                          no
                            no
                              no
                                no
                                  no
                                    no
no
##
 [9739] yes no
        no
           no
             no
              no
                no
                  no
                    no
                      no
                        no
                          no
                            no
                              no
                                no
                                  no
yes no
 [9757] no yes no
##
                  yes yes no
           no
            no
              no
                no
                        no
                          no
                            no
                              no
                                no
                                  no
                                    no
yes
##
 yes yes
##
 no
##
 yes yes
##
 yes yes
 yes yes
 ##
ves ves
 yes yes
## [9901] yes yes yes yes yes yes yes yes no yes yes no yes yes yes
yes yes
 ves ves
 ves ves
 ves ves
## [9991] yes no no yes yes no yes yes yes yes yes yes yes yes yes
yes yes
yes no
```

```
yes yes
yes
ves ves
yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
```

```
yes yes
ves ves
yes yes
yes yes
yes yes
yes yes
## [10855] yes yes yes yes yes yes yes yes no no yes yes yes yes
yes yes
ves ves
yes yes
yes yes
```

```
yes yes
yes yes
no
yes yes
ves ves
yes yes
## [11251] yes yes yes yes yes no no yes yes yes yes yes yes yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
```

```
yes yes
ves ves
yes yes
yes yes
yes yes
## [11737] yes yes yes yes yes yes yes yes no no no no no
            no
no
## [11755] no yes yes yes yes yes no yes yes yes yes yes yes yes yes
yes yes
ves ves
yes yes
yes yes
## [11827] yes yes no no no no no no yes yes yes no yes no no
```

```
no
yes yes
## [12079] yes yes yes yes yes no no no yes no no
         no no no
           no
yes
## [12097] yes yes yes yes yes yes no no yes yes no yes yes yes yes
yes yes
ves ves
yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
```

```
yes yes
## [12439] yes yes yes yes yes no
           no
            no
             no
              no
               no
                 no
                  no
                   no
no
## [12457] no
    no
     no
      no no no no
                 yes yes yes no
           no
            no
             no
              no
               no
no
## [12475] no no
      no
yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
yes yes
## [12637] yes yes no
      no
       no
        no
         no
           no
            no
             no
              no
               no
                 no
                  no
                   no
                    no
                     no
no
## [12655] no
    no
     no
      no
       no
        no
          no
           no
            no
             no
              no
               no
                 no
                  no
                   no
                    no
                     no
no
## [12673] no
    no
     no
      no
       no
        no
          no
           no
            no
             no
              no
               no
                 no
                  no
                   no
                    no
                     no
no
## [12691] no no
     no
         yes yes yes yes yes yes yes yes yes
      no
       no
        no
yes yes
yes yes
```

```
yes yes
yes yes
## [12763] yes yes yes yes yes yes yes yes no yes yes yes yes yes yes
yes yes
## [12781] yes yes yes yes no no
                no yes yes yes yes yes yes yes
yes no
## [12799] no no
       no
         no
           no
            no
              no
                no
                 no
                   no
                     no
                       yes no
                          no
                           no
                             no
                               no
yes
## [12817] yes no
       no
         no
           ves no
              no
                  no
                        no
                          ves ves no
                no
                   no
                     no
                       no
ves no
## [12835] no no
       no
         no
           no
            no
              no
                no
                 no
                   yes yes yes yes yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes
## [13015] yes yes yes yes yes yes yes no yes yes no no yes no
ves no
yes yes
yes yes
yes yes
yes yes
## [13105] yes yes yes yes no
              yes yes yes no
                       no
                        no
                          no
                            no
                             no
                               no
no
## [13123] no
     no
       no
         no
           no
             no
              no
                no
                 yes no
                     no
                       no
                        no
                          no
                            no
                             no
                               no
no
## [13141] no
      no
       no
         no
           no
             no
              no
                no
                 no no
                     no
                       no
                        no
                          no
                            no
                             no
                               no
no
## [13159] no no
       no
         no
           no
            yes yes yes yes yes yes yes yes yes yes
yes yes
```

```
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
## [13303] no yes yes yes yes no yes yes yes yes yes yes yes yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
## [13393] yes yes no yes no no no no yes yes yes yes yes yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
```

```
yes yes
yes yes
## [13663] yes yes yes yes no yes no no yes yes yes yes yes yes yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
## [13897] yes no no no yes yes yes no no yes no yes no no yes
yes yes
ves ves
yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
```

```
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
## [14203] yes yes yes yes yes yes yes no yes yes yes yes yes yes
yes yes
## [14221] yes yes yes yes no yes no no no no no yes yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
## [14419] yes yes yes yes yes yes no no no yes yes no no yes
yes yes
yes yes
yes yes
ves ves
no
yes
## [14509] yes no no no yes no yes no yes yes yes no yes yes yes
yes yes
```

```
yes yes
yes yes
yes yes
yes yes
yes yes
## [14635] yes yes yes yes yes yes no yes yes no no no yes yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
yes yes
yes yes
yes no
yes yes
yes yes
## [14815] yes yes yes yes no no yes no no no
                     no
                       no
                        no
                          no
                            no
no
yes yes
## [14851] yes yes yes yes yes yes yes yes yes no yes yes no
                            yes yes no
no
## [14869] no no
       no
         no
           no
             no
              no
                  no
                   no no
                no
                       no
                        no
                          no
                            no
                              no
yes yes
## [14887] yes no
       no
         no
           no
             no
              no
                no
                  no
                   yes yes yes no
                          yes no
                             yes no
ves
## [14905] no
       yes yes no
              yes yes no
      no
             no
                   no no
                       ves no
                          no
                            no
                              no
yes yes
## [14923] no
      no
       no
         yes no
             yes no
                yes no
                   yes yes no
                          no
                            no
                              no
ves no
## [14941] no
      no
       no
         no
           no
             no
              no
                no
                  no
                   no
                     no
                       no
                        no
                          no
                            no
                              no
                               no
yes
## [14959] no
      no
       no
         no
           no
             no
              yes no
                        yes yes no
                  no
                   no
                     no
                       no
                              no
                               no
no
## [14977] no no
       no
         no
           yes no no no no
                   yes no
                       no
                        no no no
```

```
no
## [14995] no
  no
   no
    no
    no no
      no
       no
       no
        no
         no
          no
          no
           no
            no
             no
             no
no
## [15013] no
  no
   no
    no
    yes no
      no
       yes no
        no
          no
          no
           no
            no
             no
         no
             no
no
## [15031] no yes no
      no yes no no
    no
    no
     no no
          no
          no
           no
            no
             no
             no
yes
yes yes
ves ves
yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
```

```
yes yes
## [15643] yes yes yes yes no no no yes no no yes no no no
yes yes
yes yes
## [15697] yes yes yes yes yes yes yes yes yes no yes no no
                   no
                    no
nο
## [15715] no no
       yes yes no
    no
      no
          no
           yes no
             no
               no
                no
                 no
                  yes no
ves no
## [15733] no
    yes no
      no
       yes no
         no
          no
           no
            no
              ves no
                no
                 no
                  no
                   no
yes no
## [15751] no
   no
     no
      no
       no
        no
         no
          yes no
            yes no
               no
                no
                 no
                  yes no
no
## [15769] no no yes no
       no
        no no
          no yes no yes yes yes yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
```

```
yes yes
## [16111] yes yes yes yes yes yes no yes yes yes yes yes yes yes yes yes
yes yes
yes yes
yes yes
yes yes
## [16183] yes yes yes no
          no
## [16201] no yes no
         no
           no
            yes no
               no
                 yes no
                    yes yes no
                         no
                           no
                             no
                              no
no
## [16219] no
       no
           no
              no
                 yes no
                      no
      no
         no
            no
               no
                    no
                        no
                         no
                           no
                             no
                              no
no
## [16237] no
     no
       yes no
           no
            no
              no
               no
                 no
                   no
                    no
                      yes no
                         no
                           ves no
                              no
no
##
 [16255] yes no
       no
         no
           no
            no
              no
               yes no
                   no
                    no
                      no
                        no
                         no
                           no
                             no
                              no
no
## [16273] yes no
       no
         yes no
            no
              no
               no
                 no
                   no
                    no
                      no
                        no
                         no
                           yes no
                              no
no
## [16291] no
     no
       no
         no
           no
            no
              no
               yes no
                   no
                    no
                      no
                        no
                         no
                           no
                             no
                              no
no
## [16309] no
     no
       no
         no
           no
            no
              no
               no
                 no
                   no
                    no
                      no
                        no
                         no
                           no
                             no
                              no
no
## [16327] yes no
       no
           no
                 yes no yes no
                         yes no
         no
            no
              no
               no
                        no
```

```
no
## [16345] no no
    yes no
     yes no no
        no
         no
          no
           no
           no
            no
             no
              no
               no
                no
no
## [16363] no
   no
    no
    no
     no
      no
       no
        no
         no
          no
           no
           no
            no
             no
              no
               no
                no
no
## [16381] no
    no
     no
      no
       no
           yes no
   no
     no
        no
         no
          no
            no
             no
              no
               no
                no
no
## [16399] no
   no
    no
    no
     yes no
       no
        no
         no
          no
          no
           no
            yes yes yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
yes yes
yes yes
yes yes
ves ves
yes yes
yes yes
```

```
yes yes
yes yes
yes yes
yes yes
## [16867] no no no yes no yes yes yes
## Levels: no yes
confusionMatrix(valid.df$INJURY,predictvalid,positive ='yes')
## Confusion Matrix and Statistics
##
##
         Reference
## Prediction
           no yes
       no 3203 5016
##
       yes 2862 5793
##
##
##
             Accuracy : 0.5331
##
              95% CI: (0.5256, 0.5407)
     No Information Rate: 0.6406
##
     P-Value [Acc > NIR] : 1
##
##
##
               Kappa: 0.0594
##
##
  Mcnemar's Test P-Value : <2e-16
##
##
           Sensitivity: 0.5359
##
           Specificity: 0.5281
         Pos Pred Value: 0.6693
##
##
        Neg Pred Value: 0.3897
           Prevalence: 0.6406
##
##
        Detection Rate: 0.3433
##
    Detection Prevalence: 0.5129
##
      Balanced Accuracy: 0.5320
##
       'Positive' Class : yes
##
##
validerror <- 1 - 0.5331</pre>
validerrp <- scales::percent(validerror,0.01)</pre>
# Overall Error
validerrp
## [1] "46.69%"
```

Task 8.2.c.iv

```
improvement.percent <- scales::percent(validerror-nerror, 0.01)
# Percent Improvement
improvement.percent
## [1] "0.72%"</pre>
```

Task 8.2.c.v

```
nbmodel
##
## Naive Bayes Classifier for Discrete Predictors
##
## Call:
## naiveBayes.default(x = X, y = Y, laplace = laplace)
## A-priori probabilities:
## Y
##
          no
                   yes
## 0.4939745 0.5060255
##
## Conditional probabilities:
##
        HOUR_I_R
## Y
##
     no 0.5689490 0.4310510
##
     yes 0.5703131 0.4296869
##
##
        ALIGN_I
## Y
                 1
##
     no 0.8712206 0.1287794
##
     yes 0.8652300 0.1347700
##
##
        WRK ZONE
## Y
##
     no 0.97664374 0.02335626
##
     yes 0.97727805 0.02272195
##
##
        WKDY_I_R
## Y
##
     no 0.2194049 0.7805951
##
     yes 0.2381510 0.7618490
##
##
        INT_HWY
## Y
                    0
                                  1
##
     no 0.8513837786 0.1481362982 0.0004799232
##
     yes 0.8593737800 0.1397673147 0.0008589053
##
##
        LGTCON I R
## Y
                 1
                            2
     no 0.6870101 0.1251000 0.1878899
```

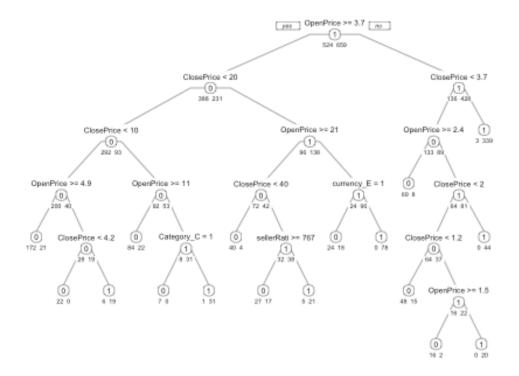
```
##
     yes 0.7014914 0.1096275 0.1888811
##
##
        PROFIL_I_R
## Y
                            1
##
     no 0.7531595 0.2468405
##
     yes 0.7633326 0.2366674
##
##
        SPD_LIM
## Y
                                 10
                                                                          25
                                              15
                                                            20
##
     no 0.0000799872 0.0004799232 0.0043992961 0.0085586306 0.1121420573
##
     yes 0.0001561646 0.0003123292 0.0040602795 0.0039041149 0.0906535488
##
        SPD LIM
## Y
                   30
                                 35
                                              40
                                                            45
                                                                          50
##
     no 0.0860662294 0.1896496561 0.0962246041 0.1553351464 0.0407934730
     yes 0.0860466932 0.2123057703 0.1068946670 0.1574139143 0.0394315609
##
##
        SPD_LIM
## Y
                   55
                                 60
                                              65
                                                            70
                                                                         75
     no 0.1590145577 0.0355143177 0.0645496721 0.0409534474 0.0062390018
##
##
     yes 0.1549152807 0.0430233466 0.0621535098 0.0311548372 0.0075739830
##
##
        SUR COND
                                                                     9
## Y
                   1
                                2
                                            3
                                                         4
##
     no 0.774196129 0.176931691 0.016717325 0.028155495 0.003999360
##
     yes 0.815725775 0.151245413 0.010697275 0.016709612 0.005621926
##
##
        TRAF_CON_R
## Y
                            1
##
     no 0.6566149 0.1902096 0.1531755
##
     yes 0.6213009 0.2191770 0.1595221
##
##
        TRAF_WAY
## Y
                              2
##
     no 0.57998720 0.36690130 0.05311150
##
     yes 0.56063090 0.39743890 0.04193019
##
##
        WEATHER R
## Y
##
     no 0.8390657 0.1609343
##
     yes 0.8744437 0.1255563
```

From the conditional probability output, we can see that P(INJURY = No | SPD_LIM = 5) is 0.0000799872, which is a really small value that's close to zero. Since we cannot rule out the possibility of inflicting injury, that's why the probability is equal to 0.0000799872. Since, the car is such at a low speed, it makes sense to say that there will be no injury.

Problem 9.1

Question 9.1.a

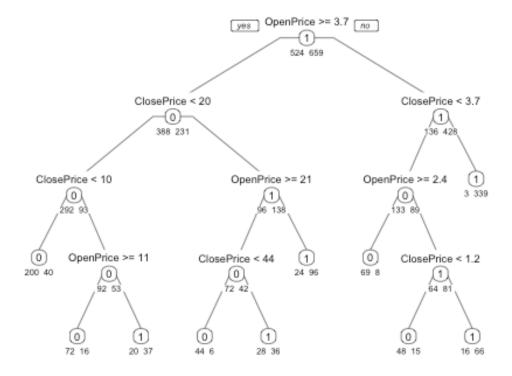
```
ebay <- fastDummies::dummy_cols(eBayAuctions, select_columns = "Category")
ebay <- ebay[,-1]
ebay <- fastDummies::dummy_cols(ebay, select_columns = "currency")
ebay<-ebay[,-1]
ebay <- fastDummies::dummy_cols(ebay, select_columns = "endDay")
ebay<-ebay[,-3]
set.seed(1)
ebaytrainindex<- sample(c(1:dim(ebay)[1]),dim(ebay)[1]*0.6)
ebaytrain <- ebay[ebaytrainindex,]
ebayvalid <- ebay[-ebaytrainindex,]
default.ct <- rpart(Competitive. ~ ., data = ebaytrain, method = "class")
prp(default.ct,type = 1, extra = 1, under = TRUE, split.font = 1, varlen = -10)</pre>
```



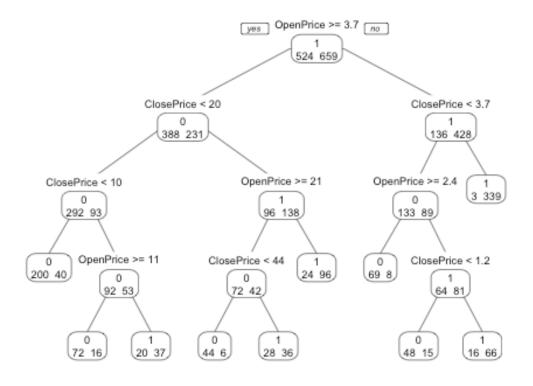
```
deeper.ct <- rpart(Competitive. ~ ., data = ebaytrain, method = "class", cp
= 0, minsplit = 1 )
prp(deeper.ct,type = 1, extra = 1, under = TRUE, split.font = 1, varlen = -
10)
## Warning: labs do not fit even at cex 0.15, there may be some overplotting</pre>
```



```
deeper.ct1 <- rpart(Competitive. ~ ., data = ebaytrain, method = "class", cp
= 0, minsplit = 1, maxdepth=7, minbucket = 50)
prp(deeper.ct1,type = 1, extra = 1, under = TRUE, split.font = 1, varlen = -
10)</pre>
```



```
###Create a pruned tree, prune on the lowest xerror value
prunedtree = prune(deeper.ct1, cp=
deeper.ct1$cptable[which.min(deeper.ct1$cptable[,"xerror"]),"CP"])
prp(prunedtree,type= 1, extra = 1, split.font=1, varlen=-10)
```



```
summary(prunedtree)
## Call:
## rpart(formula = Competitive. ~ ., data = ebaytrain, method = "class",
       cp = 0, minsplit = 1, maxdepth = 7, minbucket = 50)
##
     n = 1183
##
             CP nsplit rel error
##
                                     xerror
                                                  xstd
## 1 0.29961832
                     0 1.0000000 1.0000000 0.03260504
## 2 0.08396947
                     1 0.7003817 0.7500000 0.03091620
## 3 0.08015267
                     2 0.6164122 0.6564885 0.02980825
## 4 0.05725191
                     3 0.5362595 0.5916031 0.02886452
                     4 0.4790076 0.4866412 0.02699109
## 5 0.04770992
## 6 0.01622137
                     6 0.3835878 0.4045802 0.02517410
## 7 0.01526718
                     8 0.3511450 0.4083969 0.02526650
## 8 0.00000000
                     9 0.3358779 0.3702290 0.02430387
##
## Variable importance
##
                   ClosePrice
                                                OpenPrice
##
                            41
                                                        32
##
                  currency_US
                                             currency_EUR
##
##
                 sellerRating
                                                 Duration
```

```
##
##
          Category_Automotive
                                               endDay Mon
##
               Category Books Category Antique/Art/Craft
##
##
##
        Category_Toys/Hobbies
                                               endDay_Tue
##
                                                        1
##
## Node number 1: 1183 observations,
                                        complexity param=0.2996183
##
     predicted class=1 expected loss=0.4429417 P(node) =1
##
       class counts:
                       524
                             659
##
      probabilities: 0.443 0.557
##
     left son=2 (619 obs) right son=3 (564 obs)
##
     Primary splits:
##
         OpenPrice
                      < 3.685 to the right, improve=87.796120, (0 missing)
##
         sellerRating < 3291.5 to the right, improve=31.795140, (0 missing)
                      < 20.015 to the left, improve=30.371070, (0 missing)
##
         ClosePrice
##
         endDay Mon
                               to the left, improve=18.236450, (0 missing)
                      < 0.5
                               to the right, improve= 9.020225, (0 missing)
##
         Duration
                      < 6
##
     Surrogate splits:
##
         ClosePrice
                      < 3.87
                               to the right, agree=0.724, adj=0.422, (0
split)
                               to the right, agree=0.630, adj=0.223, (0
##
         currency US < 0.5
split)
                               to the left, agree=0.604, adj=0.168, (0
##
         currency_EUR < 0.5
split)
         endDay Mon
                               to the left, agree=0.585, adj=0.129, (0
##
                      < 0.5
split)
##
         Duration
                      < 8.5
                               to the left, agree=0.584, adj=0.128, (0
split)
##
## Node number 2: 619 observations,
                                       complexity param=0.08015267
##
     predicted class=0 expected loss=0.3731826 P(node) =0.523246
##
       class counts:
                       388
                             231
##
      probabilities: 0.627 0.373
##
     left son=4 (385 obs) right son=5 (234 obs)
     Primary splits:
##
##
         ClosePrice
                               < 20.195 to the left, improve=35.288760, (0
missing)
         sellerRating
                               < 562
                                        to the right, improve=19.401220, (0
##
missing)
##
         OpenPrice
                               < 9.895 to the left, improve= 6.751646, (0
missing)
         Category_Toys/Hobbies < 0.5</pre>
                                        to the left, improve= 5.474394, (0
##
missing)
##
         endDay Mon
                               < 0.5
                                        to the left,
                                                       improve= 1.902447, (0
missing)
##
     Surrogate splits:
##
         OpenPrice
                                < 19.97 to the left, agree=0.811,
adj=0.500, (0 split)
```

```
## Category_Automotive < 0.5 to the left, agree=0.677,
adj=0.145, (0 split)
                                       to the right, agree=0.670,
        sellerRating
                              < 603
adj=0.128, (0 split)
##
        Category Electronics < 0.5
                                       to the left, agree=0.638,
adj=0.043, (0 split)
        Category_Pottery/Glass < 0.5 to the left, agree=0.632,
adj=0.026, (0 split)
##
## Node number 3: 564 observations,
                                      complexity param=0.08396947
##
    predicted class=1 expected loss=0.2411348 P(node) =0.476754
##
      class counts:
                      136
                            428
     probabilities: 0.241 0.759
##
##
     left son=6 (222 obs) right son=7 (342 obs)
##
    Primary splits:
##
        ClosePrice
                              < 3.685 to the left, improve=93.824340, (0
missing)
                              < 1.805 to the right, improve=15.102490, (0
        OpenPrice
##
missing)
##
        Duration
                              < 6
                                      to the right, improve=12.714280, (0
missing)
        sellerRating
                              < 3263
                                      to the right, improve= 8.780467, (0
##
missing)
##
        Category Toys/Hobbies < 0.5
                                      to the right, improve= 6.192000, (0
missing)
##
    Surrogate splits:
                              < 0.5
##
        Category Books
                                       to the right, agree=0.631,
adj=0.063, (0 split)
        Category_Toys/Hobbies < 0.5
                                       to the right, agree=0.621,
adj=0.036, (0 split)
                                       to the right, agree=0.613,
        sellerRating
                             < 2483
adj=0.018, (0 split)
##
        Category Health/Beauty < 0.5
                                       to the right, agree=0.612,
adj=0.014, (0 split)
                               < 0.5
                                       to the right, agree=0.610,
        endDay Sat
adj=0.009, (0 split)
##
## Node number 4: 385 observations,
                                     complexity param=0.01622137
    predicted class=0 expected loss=0.2415584 P(node) =0.3254438
##
##
      class counts:
                      292
                             93
##
     probabilities: 0.758 0.242
    left son=8 (240 obs) right son=9 (145 obs)
##
##
    Primary splits:
        ClosePrice
                              < 10
                                      to the left, improve=7.1482910, (0
##
missing)
##
        Category_Toys/Hobbies < 0.5 to the left, improve=4.2361510, (0
missing)
        OpenPrice
                              < 4.935 to the right, improve=3.6593840, (0
##
missing)
## sellerRating < 577 to the right, improve=2.7267260, (0
```

```
missing)
                               < 0.5
##
         endDay_Sat
                                        to the left, improve=0.5686656, (0
missing)
     Surrogate splits:
##
         OpenPrice
                             < 10.47 to the left, agree=0.901, adj=0.738,
(0 split)
                             < 4427.5 to the left, agree=0.696, adj=0.193,
##
         sellerRating
(0 split)
         Category_Automotive < 0.5
                                      to the left, agree=0.647, adj=0.062,
##
(0 split)
                                      to the left, agree=0.647, adj=0.062,
##
         Category Jewelry
                             < 0.5
(0 split)
         Duration
                                      to the right, agree=0.642, adj=0.048,
##
                             < 4
(0 split)
##
## Node number 5: 234 observations,
                                      complexity param=0.05725191
     predicted class=1 expected loss=0.4102564 P(node) =0.1978022
##
                        96
                             138
       class counts:
##
      probabilities: 0.410 0.590
##
     left son=10 (114 obs) right son=11 (120 obs)
##
     Primary splits:
##
         OpenPrice
                             < 20.5
                                      to the right, improve=21.778140, (0
missing)
##
         Category Automotive < 0.5
                                      to the right, improve= 8.581506, (0
missing)
                             < 990.5 to the right, improve= 8.485962, (0
         sellerRating
missing)
##
         ClosePrice
                             < 39.995 to the left, improve= 3.460277, (0</pre>
missing)
                             < 0.5
                                      to the left, improve= 1.539547, (0
##
         endDay Mon
missing)
##
     Surrogate splits:
##
         Category_Automotive < 0.5
                                      to the right, agree=0.697, adj=0.377,
(0 split)
                                      to the right, agree=0.667, adj=0.316,
##
         currency US
                             < 0.5
(0 split)
                                      to the left, agree=0.654, adj=0.289,
##
         currency_EUR
                             < 0.5
(0 split)
##
         ClosePrice
                             < 29.725 to the right, agree=0.620, adj=0.219,
(0 split)
##
         sellerRating
                            < 2179.5 to the right, agree=0.615, adj=0.211,
(0 split)
##
## Node number 6: 222 observations,
                                      complexity param=0.04770992
     predicted class=0 expected loss=0.4009009 P(node) =0.1876585
##
##
       class counts:
                       133
                              89
##
      probabilities: 0.599 0.401
     left son=12 (77 obs) right son=13 (145 obs)
##
##
     Primary splits:
         OpenPrice
                          < 2.445 to the right, improve=20.798530,
##
```

```
(0 missing)
                                   < 6
                                            to the right, improve=11.614950,
##
         Duration
(0 missing)
                                            to the left, improve= 6.984001,
         Category Music/Movie/Game < 0.5
(0 missing)
                                            to the right, improve= 6.271213,
##
         sellerRating
                                  < 3263
(0 missing)
                                            to the right, improve= 5.560722,
##
         currency_EUR
                                   < 0.5
(0 missing)
     Surrogate splits:
##
##
         ClosePrice
                                    < 2.39
                                             to the right, agree=0.842,
adj=0.545, (0 split)
         Category Antique/Art/Craft < 0.5
                                             to the right, agree=0.716,
adj=0.182, (0 split)
                                    < 3377.5 to the right, agree=0.703,</pre>
##
         sellerRating
adj=0.143, (0 split)
         endDay Fri
                                    < 0.5
                                             to the right, agree=0.698,
adj=0.130, (0 split)
         Category Health/Beauty
                                    < 0.5
                                             to the right, agree=0.671,
adj=0.052, (0 split)
##
## Node number 7: 342 observations
     predicted class=1 expected loss=0.00877193 P(node) =0.2890955
##
##
       class counts:
                         3
##
      probabilities: 0.009 0.991
##
## Node number 8: 240 observations
##
     predicted class=0 expected loss=0.1666667 P(node) =0.202874
##
       class counts:
                       200
                              40
##
      probabilities: 0.833 0.167
##
## Node number 9: 145 observations,
                                     complexity param=0.01622137
##
     predicted class=0 expected loss=0.3655172 P(node) =0.1225697
##
       class counts:
                        92
                              53
##
      probabilities: 0.634 0.366
##
     left son=18 (88 obs) right son=19 (57 obs)
##
     Primary splits:
##
         OpenPrice
                      < 11.285 to the right, improve=15.108440, (0 missing)
                      < 13.855 to the right, improve= 4.762865, (0 missing)</pre>
##
         ClosePrice
##
         sellerRating < 3820.5 to the right, improve= 2.000270, (0 missing)
##
                               to the left, improve= 1.925177, (0 missing)
         Duration
                      < 6
##
     Surrogate splits:
##
         ClosePrice
                                < 11.815 to the right, agree=0.807,
adj=0.509, (0 split)
                                < 0.5
                                         to the left, agree=0.703,
         currency EUR
adj=0.246, (0 split)
##
         currency_US
                                < 0.5
                                         to the right, agree=0.703,
adj=0.246, (0 split)
##
         Duration
                                < 8.5
                                         to the left, agree=0.655,
adj=0.123, (0 split)
```

```
Category SportingGoods < 0.5 to the left, agree=0.648,
adj=0.105, (0 split)
##
## Node number 10: 114 observations,
                                       complexity param=0.01526718
##
     predicted class=0 expected loss=0.3684211 P(node) =0.09636517
##
       class counts:
                        72
                              42
##
      probabilities: 0.632 0.368
##
     left son=20 (50 obs) right son=21 (64 obs)
##
     Primary splits:
##
         ClosePrice
                      < 43.64 to the left,
                                              improve=10.992630, (0 missing)
##
         sellerRating < 1074
                               to the right, improve= 2.737039, (0 missing)
##
                      < 44.225 to the left, improve= 2.413674, (0 missing)
         OpenPrice
##
         Duration
                               to the left, improve= 1.043947, (0 missing)
                      < 6
##
     Surrogate splits:
##
                                   < 44.225 to the left, agree=0.895,
         OpenPrice
adj=0.76, (0 split)
         sellerRating
                                   < 2998
                                            to the right, agree=0.667,
adj=0.24, (0 split)
##
         Duration
                                            to the left, agree=0.614,
                                   < 4
adj=0.12, (0 split)
         Category Jewelry
                                   < 0.5
                                            to the right, agree=0.579,
adj=0.04, (0 split)
                                          to the right, agree=0.579,
         Category_Music/Movie/Game < 0.5</pre>
adj=0.04, (0 split)
##
## Node number 11: 120 observations
     predicted class=1 expected loss=0.2 P(node) =0.101437
##
##
       class counts:
                        24
                              96
##
      probabilities: 0.200 0.800
##
## Node number 12: 77 observations
##
     predicted class=0 expected loss=0.1038961 P(node) =0.06508876
##
       class counts:
                        69
##
      probabilities: 0.896 0.104
##
## Node number 13: 145 observations,
                                       complexity param=0.04770992
     predicted class=1 expected loss=0.4413793 P(node) =0.1225697
##
##
       class counts:
                        64
                              81
##
      probabilities: 0.441 0.559
##
     left son=26 (63 obs) right son=27 (82 obs)
##
     Primary splits:
##
         ClosePrice
                      < 1.24
                               to the left, improve=22.890210, (0 missing)
##
                               to the right, improve= 4.869764, (0 missing)
         currency EUR < 0.5
                               to the right, improve= 4.606012, (0 missing)
##
         Duration
                      < 6
                               to the right, improve= 3.297679, (0 missing)
##
         OpenPrice
                      < 1.035
##
         endDay Mon
                      < 0.5
                               to the left, improve= 1.630721, (0 missing)
##
     Surrogate splits:
##
         OpenPrice
                               to the left, agree=0.683, adj=0.270, (0
                      < 1.24
split)
         Duration \langle 8.5 \rangle to the right, agree=0.655, adj=0.206, (0)
##
```

```
split)
                               to the right, agree=0.621, adj=0.127, (0
##
         currency_EUR < 0.5
split)
                               to the right, agree=0.621, adj=0.127, (0
##
         endDay Tue
                    < 0.5
split)
         sellerRating < 5496.5 to the right, agree=0.614, adj=0.111, (0
##
split)
##
## Node number 18: 88 observations
     predicted class=0 expected loss=0.1818182 P(node) =0.07438715
##
##
       class counts:
                        72
                              16
##
      probabilities: 0.818 0.182
##
## Node number 19: 57 observations
     predicted class=1 expected loss=0.3508772 P(node) =0.04818259
##
       class counts:
##
                        20
                              37
##
      probabilities: 0.351 0.649
##
## Node number 20: 50 observations
     predicted class=0 expected loss=0.12 P(node) =0.04226543
##
##
       class counts:
                        44
##
      probabilities: 0.880 0.120
##
## Node number 21: 64 observations
     predicted class=1 expected loss=0.4375 P(node) =0.05409975
##
       class counts:
                        28
                              36
##
      probabilities: 0.438 0.562
##
## Node number 26: 63 observations
##
     predicted class=0 expected loss=0.2380952 P(node) =0.05325444
                        48
##
       class counts:
                              15
##
      probabilities: 0.762 0.238
##
## Node number 27: 82 observations
     predicted class=1 expected loss=0.195122 P(node) =0.0693153
##
##
       class counts:
                        16
                              66
      probabilities: 0.195 0.805
##
### Predicting using the model
predtree = predict(prunedtree,ebayvalid,type="class")
confusionMatrix(predtree,(as.factor(ebayvalid$Competitive.)))
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction
                0
            0 286 57
##
##
            1 96 350
##
```

```
##
                  Accuracy : 0.8061
##
                    95% CI: (0.7767, 0.8331)
       No Information Rate: 0.5158
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                     Kappa: 0.6106
##
    Mcnemar's Test P-Value: 0.002125
##
##
##
               Sensitivity: 0.7487
##
               Specificity: 0.8600
##
            Pos Pred Value: 0.8338
            Neg Pred Value: 0.7848
##
##
                Prevalence: 0.4842
##
            Detection Rate: 0.3625
##
      Detection Prevalence: 0.4347
##
         Balanced Accuracy: 0.8043
##
          'Positive' Class : 0
##
##
### From the summary we can see that a few varibles have not been used by
this model
### and they can be removed from consideration as removing them will not
affect the tree's perfomance
### eq - closeprice
```

Question 9.1.b

The model has an accuracy of 79.47%, but the model places a very high importance on the closing price of the auction, which is impossible to know before the auction has even begun, so it cannot be practical model for use.

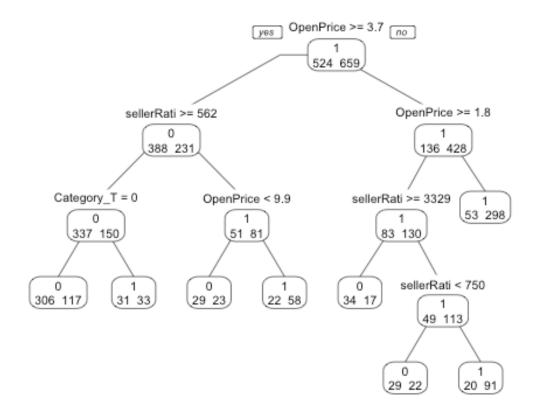
Question 9.1.c

```
#if(closeprice<3)
    #label:0
#else
    #label:1

#The rules show that not all variables have the same importance to determine the competitiveness of the auction. Prices and Seller rating hold the most importance.</pre>
```

Question 9.1.d

```
prunedtree2 = rpart(formula = Competitive. ~
OpenPrice+sellerRating+`Category Music/Movie/Game`+
Category Automotive+Category SportingGoods+`Category Home/Garden`+
Category Books+Category Collectibles+`Category Business/Industrial`+
                      Category_Toys/Hobbies`+Category_Electronics
+Category Computer+
                      Category EverythingElse+`Category Clothing/Accessories`
                      `Category_Coins/Stamps`+`Category_Antique/Art/Craft`+
Category_Jewelry+`Category_Pottery/Glass`+`Category_Health/Beauty`+
Category Photography+currency US+currency GBP+currency EUR+Duration+
                      endDay Mon+endDay Tue+endDay Wed+endDay Thu+endDay Fri+
                      endDay Sat+endDay Sun, data = ebaytrain, method =
"class", cp = 0, minsplit = 1, maxdepth=7, minbucket = 50)
prunedtree2 = prune(prunedtree2, cp=
prunedtree2$cptable[which.min(prunedtree2$cptable[,"xerror"]),"CP"])
prp(prunedtree2, type= 1, extra = 1, split.font=1, varlen=-10)
```



```
summary(prunedtree2)
## Call:
## rpart(formula = Competitive. ~ OpenPrice + sellerRating +
`Category_Music/Movie/Game` +
##
      Category Automotive + Category SportingGoods + `Category Home/Garden`
+
##
      Category_Books + Category_Collectibles +
`Category Business/Industrial` +
       `Category_Toys/Hobbies` + Category_Electronics + Category_Computer +
##
##
      Category_EverythingElse + `Category_Clothing/Accessories` +
##
      `Category_Coins/Stamps` + `Category_Antique/Art/Craft` +
      Category_Jewelry + `Category_Pottery/Glass` + `Category_Health/Beauty`
##
+
##
      Category Photography + currency US + currency GBP + currency EUR +
      Duration + endDay Mon + endDay Tue + endDay Wed + endDay Thu +
##
##
      endDay_Fri + endDay_Sat + endDay_Sun, data = ebaytrain, method =
"class",
      cp = 0, minsplit = 1, maxdepth = 7, minbucket = 50)
##
##
    n = 1183
##
##
             CP nsplit rel error
                                   xerror
```

```
1 0.7003817 0.7251908 0.03064968
## 2 0.057251908
## 3 0.016221374
                      2 0.6431298 0.6755725 0.03005766
## 4 0.013358779
                      4 0.6106870 0.6793893 0.03010607
## 5 0.011450382
                      5 0.5973282 0.6908397 0.03024839
## 6 0.003816794
                      6 0.5858779 0.6908397 0.03024839
                      7 0.5820611 0.6679389 0.02995938
## 7 0.000000000
##
## Variable importance
                    OpenPrice
                                             sellerRating
##
                            43
                                                        16
##
                  currency_US
                                             currency EUR
##
                             8
##
                     Duration
                                Category_Music/Movie/Game
##
##
                   endDay_Mon
                                    Category_Toys/Hobbies
##
## Category_Antique/Art/Craft
                                             currency_GBP
##
                                                         1
##
                   endDay_Sat
                                               endDay_Thu
##
                                                         1
                             1
##
                   endDay Fri
##
                             1
##
## Node number 1: 1183 observations,
                                        complexity param=0.2996183
     predicted class=1 expected loss=0.4429417 P(node) =1
##
       class counts:
                       524
                              659
      probabilities: 0.443 0.557
##
##
     left son=2 (619 obs) right son=3 (564 obs)
##
     Primary splits:
##
         OpenPrice
                              < 3.685 to the right, improve=87.796120, (0)
missing)
         sellerRating
                              < 3291.5 to the right, improve=31.795140, (0</pre>
##
missing)
                                       to the left, improve=18.236450, (0
##
         endDay Mon
                              < 0.5
missing)
                                       to the right, improve= 9.020225, (0
##
         Duration
                              < 6
missing)
##
         Category_Automotive < 0.5 to the right, improve= 5.774742, (0)
missing)
     Surrogate splits:
##
                                    < 0.5
                                             to the right, agree=0.630,
         currency_US
adj=0.223, (0 split)
         currency EUR
                                    < 0.5
                                             to the left, agree=0.604,
adj=0.168, (0 split)
                                    < 0.5
                                             to the left,
         endDay Mon
                                                            agree=0.585,
adj=0.129, (0 split)
##
         Duration
                                    < 8.5
                                             to the left, agree=0.584,
adj=0.128, (0 split)
         Category_Music/Movie/Game < 0.5</pre>
                                             to the left, agree=0.569,
adj=0.096, (0 split)
```

```
##
## Node number 2: 619 observations,
                                      complexity param=0.05725191
     predicted class=0 expected loss=0.3731826 P(node) =0.523246
##
##
       class counts:
                       388
                             231
##
      probabilities: 0.627 0.373
##
     left son=4 (487 obs) right son=5 (132 obs)
##
     Primary splits:
                                        to the right, improve=19.401220, (0
##
         sellerRating
                               < 562
missing)
                               < 9.895 to the left,
                                                      improve= 6.751646, (0
##
         OpenPrice
missing)
         Category Toys/Hobbies < 0.5
                                        to the left, improve= 5.474394, (0
##
missing)
##
         endDay_Mon
                               < 0.5
                                        to the left, improve= 1.902447, (0
missing)
##
         Category Collectibles < 0.5
                                       to the left, improve= 1.716101, (0
missing)
     Surrogate splits:
##
##
         currency GBP < 0.5
                               to the left, agree=0.801, adj=0.068, (0
split)
         endDay Thu
                      < 0.5
                               to the left, agree=0.795, adj=0.038, (0
##
split)
##
## Node number 3: 564 observations,
                                       complexity param=0.01622137
     predicted class=1 expected loss=0.2411348 P(node) =0.476754
##
       class counts:
                       136
                             428
      probabilities: 0.241 0.759
##
     left son=6 (213 obs) right son=7 (351 obs)
##
##
     Primary splits:
                               < 1.805 to the right, improve=15.102490, (0
##
         OpenPrice
missing)
         Duration
                               < 6
                                        to the right, improve=12.714280, (0
##
missing)
                                        to the right, improve= 8.780467, (0
##
         sellerRating
                               < 3263
missing)
                                        to the right, improve= 6.192000, (0
         Category Toys/Hobbies < 0.5
##
missing)
##
         endDay_Mon
                               < 0.5
                                        to the left, improve= 6.053778, (0
missing)
     Surrogate splits:
         Category_Antique/Art/Craft < 0.5
                                             to the right, agree=0.732,
adj=0.291, (0 split)
##
         Duration
                                    < 6
                                             to the right, agree=0.690,
adj=0.178, (0 split)
         endDay Fri
                                    < 0.5
                                             to the right, agree=0.667,
adj=0.117, (0 split)
##
         Category_Toys/Hobbies
                                    < 0.5
                                             to the right, agree=0.654,
adj=0.085, (0 split)
##
         sellerRating
                                    < 3377.5 to the right, agree=0.633,</pre>
adj=0.028, (0 split)
```

```
##
## Node number 4: 487 observations, complexity param=0.003816794
     predicted class=0 expected loss=0.3080082 P(node) =0.4116653
##
##
       class counts:
                       337
                            150
##
      probabilities: 0.692 0.308
##
     left son=8 (423 obs) right son=9 (64 obs)
##
     Primary splits:
##
         Category_Toys/Hobbies < 0.5
                                      to the left, improve=6.352190, (0
missing)
                                       to the left, improve=2.875117, (0
##
         endDay Mon
                               < 0.5
missing)
                               < 9.895 to the left, improve=2.487823, (0
##
         OpenPrice
missing)
##
         sellerRating
                              < 4336.5 to the right, improve=2.175189, (0
missing)
##
        Category Collectibles < 0.5 to the left, improve=1.401587, (0
missing)
##
     Surrogate splits:
##
         Duration < 2
                          to the right, agree=0.873, adj=0.031, (0 split)
##
## Node number 5: 132 observations,
                                      complexity param=0.01145038
##
     predicted class=1 expected loss=0.3863636 P(node) =0.1115807
##
                        51
       class counts:
##
      probabilities: 0.386 0.614
     left son=10 (52 obs) right son=11 (80 obs)
##
##
     Primary splits:
         OpenPrice
##
                     < 9.915 to the left, improve=5.037063, (0 missing)
         sellerRating < 113.5 to the right, improve=4.455299, (0 missing)
##
##
                              to the left, improve=3.544311, (0 missing)
         currency US < 0.5
##
     Surrogate splits:
         Category_Music/Movie/Game < 0.5</pre>
##
                                          to the right, agree=0.758,
adj=0.385, (0 split)
##
         endDay Thu
                                  < 0.5
                                           to the right, agree=0.712,
adj=0.269, (0 split)
                                           to the right, agree=0.682,
         currency_GBP
                                   < 0.5
adj=0.192, (0 split)
                                           to the left, agree=0.667,
##
         currency_US
                                   < 0.5
adj=0.154, (0 split)
        Duration
                                   < 8.5
                                           to the right, agree=0.636,
adj=0.077, (0 split)
##
## Node number 6: 213 observations,
                                      complexity param=0.01622137
     predicted class=1 expected loss=0.3896714 P(node) =0.1800507
##
##
                       83
                             130
       class counts:
##
      probabilities: 0.390 0.610
##
     left son=12 (51 obs) right son=13 (162 obs)
##
     Primary splits:
##
                                    < 3328.5 to the right,
         sellerRating
improve=10.2898600, (0 missing)
                                    < 3.585 to the left, improve=
   OpenPrice
```

```
8.7116640, (0 missing)
         Category_Antique/Art/Craft < 0.5
                                            to the left,
                                                           improve=
5.6831610, (0 missing)
                                    < 8.5
        Duration
                                            to the left,
                                                           improve=
0.4206673, (0 missing)
         currency_US
                                    < 0.5
                                            to the left,
                                                           improve=
0.2727624, (0 missing)
##
    Surrogate splits:
                                < 0.5
                                         to the right, agree=0.812,
         endDay_Sat
adj=0.216, (0 split)
         Category Toys/Hobbies < 0.5
                                        to the right, agree=0.803,
adj=0.176, (0 split)
                                        to the right, agree=0.789,
         Category_Coins/Stamps < 0.5
adj=0.118, (0 split)
         Category_Electronics
                                < 0.5 to the right, agree=0.784,
##
adj=0.098, (0 split)
        Category_SportingGoods < 0.5 to the right, agree=0.779,
adj=0.078, (0 split)
##
## Node number 7: 351 observations
##
     predicted class=1 expected loss=0.1509972 P(node) =0.2967033
##
       class counts:
                       53
                            298
      probabilities: 0.151 0.849
##
##
## Node number 8: 423 observations
##
     predicted class=0 expected loss=0.2765957 P(node) =0.3575655
##
       class counts:
                      306
                            117
##
      probabilities: 0.723 0.277
##
## Node number 9: 64 observations
     predicted class=1 expected loss=0.484375 P(node) =0.05409975
##
##
       class counts:
                       31
                             33
##
      probabilities: 0.484 0.516
##
## Node number 10: 52 observations
     predicted class=0 expected loss=0.4423077 P(node) =0.04395604
##
##
       class counts:
                       29
                             23
##
      probabilities: 0.558 0.442
##
## Node number 11: 80 observations
##
     predicted class=1 expected loss=0.275 P(node) =0.06762468
##
       class counts:
                       22
##
      probabilities: 0.275 0.725
##
## Node number 12: 51 observations
##
     predicted class=0 expected loss=0.3333333 P(node) =0.04311074
##
       class counts:
                        34
                             17
      probabilities: 0.667 0.333
##
##
## Node number 13: 162 observations, complexity param=0.01335878
```

```
predicted class=1 expected loss=0.3024691 P(node) =0.13694
##
##
       class counts:
                        49
                             113
##
      probabilities: 0.302 0.698
     left son=26 (51 obs) right son=27 (111 obs)
##
##
     Primary splits:
                                    < 750
                                             to the left, improve=10.545620,
##
         sellerRating
(0 missing)
##
         OpenPrice
                                    < 3.585 to the left, improve= 4.171749,
(0 missing)
                                             to the left, improve= 2.420448,
##
         currency US
                                    < 0.5
(0 missing)
         Category Antique/Art/Craft < 0.5
                                             to the left, improve= 2.383186,
(0 missing)
##
         currency_EUR
                                    < 0.5
                                             to the right, improve= 2.030186,
(0 missing)
     Surrogate splits:
##
         Category_Music/Movie/Game
                                       < 0.5
                                                to the right, agree=0.747,
adj=0.196, (0 split)
         Category_Clothing/Accessories < 0.5
                                                to the right, agree=0.722,
adj=0.118, (0 split)
                                       < 0.5
                                                to the right, agree=0.716,
         endDay Wed
adj=0.098, (0 split)
                                                to the left, agree=0.710,
         currency_US
                                       < 0.5
adj=0.078, (0 split)
                                                to the right, agree=0.710,
         currency_EUR
                                       < 0.5
adj=0.078, (0 split)
##
## Node number 26: 51 observations
##
     predicted class=0 expected loss=0.4313725 P(node) =0.04311074
                              22
##
       class counts:
                        29
##
      probabilities: 0.569 0.431
##
## Node number 27: 111 observations
     predicted class=1 expected loss=0.1801802 P(node) =0.09382925
##
##
       class counts:
                        20
                              91
      probabilities: 0.180 0.820
##
# Describing the tree
## Shortest set of rules required for classification is Openprice>=3.6 and
Duration>=6
#if(openprice>=3.6)
  #if(duration>=6)
    #Label:0
  #else
    #Label:1
#else
  #if(sellerrating>=589)
    #if(OpenPrice<9)</pre>
     #Label:0
```

```
#else
#label:1
#else
#label:1
```

Question 9.1.e

```
predtree2 = predict(prunedtree2,ebayvalid,type="class")
summary(predtree2)

## 0 1
## 381 408

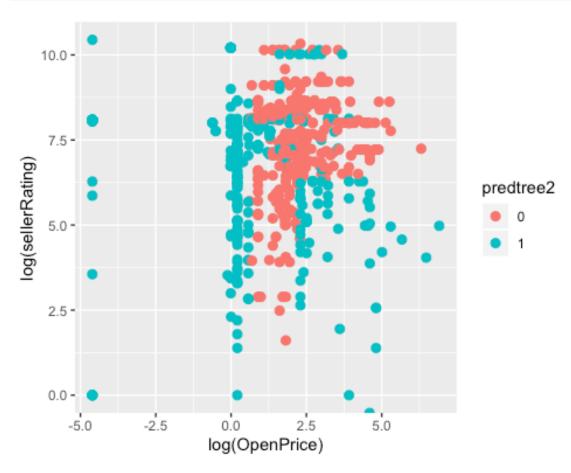
x =confusionMatrix(predtree2,(as.factor(ebayvalid$Competitive.)))
sensitivity(predtree2,as.factor(ebayvalid$Competitive.))

## [1] 0.6780105

specificity(predtree2,as.factor(ebayvalid$Competitive.))

## [1] 0.7002457

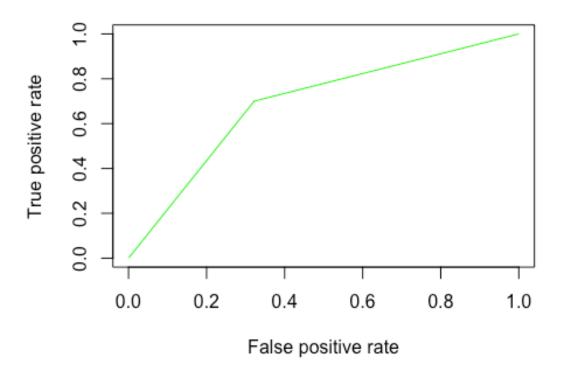
ggplot(ebayvalid,aes(x=log(OpenPrice),
y=log(sellerRating)))+geom_point(aes(color=predtree2),size = 2.5)
```



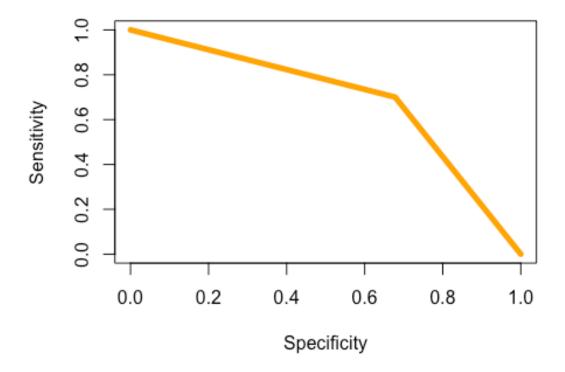
A cursory look at the scatter plot means that a line would do a reasonable job at splitting the data.

Question 9.1.f

```
confusionMatrix(predtree2,(as.factor(ebayvalid$Competitive.)))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                0
##
            0 259 122
            1 123 285
##
##
##
                  Accuracy : 0.6895
##
                    95% CI: (0.6559, 0.7216)
##
       No Information Rate: 0.5158
##
       P-Value [Acc > NIR] : <2e-16
##
##
                     Kappa: 0.3783
##
##
    Mcnemar's Test P-Value : 1
##
##
               Sensitivity: 0.6780
##
               Specificity: 0.7002
##
            Pos Pred Value : 0.6798
##
            Neg Pred Value: 0.6985
                Prevalence: 0.4842
##
##
            Detection Rate: 0.3283
##
      Detection Prevalence: 0.4829
##
         Balanced Accuracy: 0.6891
##
          'Positive' Class : 0
##
##
p = c(predtree2)
pp = prediction(p,ebayvalid$Competitive.)
p3 = performance(pp, "tpr", "fpr")
plot(p3,col="green")
```



```
p4 = performance(pp, "sens", "spec")
plot(p4, col="orange", lwd=5)
```



The model has an okay accuracy and sensitivity to specficty graph. It is not a decent model to be put into use, howEver better models can be made.

Question 9.1.g

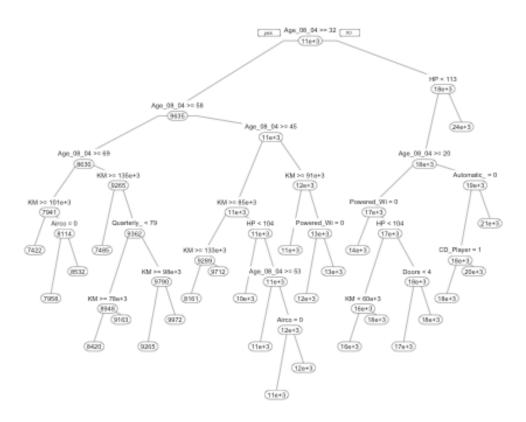
Based on the tree, the seller needs to have a higher rating and needs to keep the opening price higher than 3.6 The duration of auction should be kept longer than 6 days.

Problem 9.2

Question 9.2.a

```
#partition
set.seed(123)
traincars.index <-
sample(c(1:dim(ToyotaCorolla)[1]),dim(ToyotaCorolla)[1]*0.6)
train.cars <- ToyotaCorolla[traincars.index,]
valid.cars <- ToyotaCorolla[-traincars.index,]
class.tree <- rpart(Price
~Age_08_04+KM+Fuel_Type+HP+Automatic+Doors+Quarterly_Tax+Mfr_Guarantee+Guaran
tee Period+Airco+Automatic_airco+CD Player+Powered Windows+Sport Model+Tow Ba</pre>
```

```
r, data =train.cars,control = rpart.control(maxdepth = 30,cp = 0.001))
prp(class.tree,type =1,under = TRUE, split.font = 1,varlen=-10)
```



Task 9.2.a.i

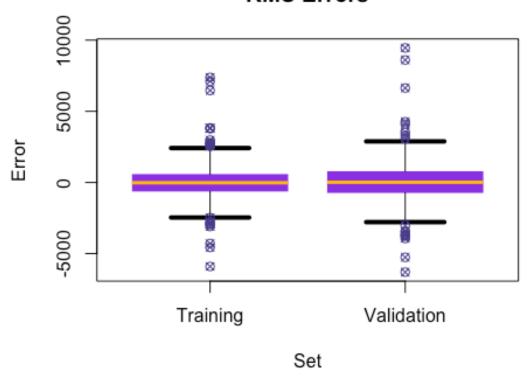
```
t(t(class.tree$variable.importance))
##
                           [,1]
## Age 08 04
                     9188959189
## KM
                     2702017486
## Automatic_airco
                     2465659993
## Quarterly_Tax
                     1153999034
## HP
                     1048448871
## Guarantee_Period
                      730646431
## CD Player
                      455884117
## Airco
                      121014851
## Powered Windows
                      110733220
## Fuel_Type
                       76595911
## Doors
                       55445451
## Sport_Model
                       32463606
## Tow Bar
                       10543296
## Mfr_Guarantee
                        6028598
## Automatic
                        2389898
```

The four most important car specifications for predicting the car's price are Age_08_04, KM, Automatic_airco, Quarterly_Tax.

Task 9.2.a.ii

```
train.err <- train.cars$Price - predict(class.tree,train.cars)</pre>
valid.err <- valid.cars$Price - predict(class.tree,valid.cars)</pre>
train.rmse <- RMSE(predict(class.tree,train.cars),train.cars$Price)</pre>
valid.rmse <- RMSE(predict(class.tree,valid.cars),valid.cars$Price)</pre>
train.rmse
## [1] 1112.902
valid.rmse
## [1] 1328.958
#create a data fram from the training and validation errors in order to plot
err <-data.frame(Error =c(train.err, valid.err),</pre>
                 Set =c(rep("Training", length(train.err)),
                         rep("Validation", length(valid.err))))
#create error box plots
boxplot(Error~Set, data=err, main="RMS Errors",
        xlab = "Set", ylab = "Error",
        col="blueviolet",medcol="darkgoldenrod1",boxlty=0,border="black",
        whisklty=1,staplelwd=4,outpch=13,outcex=1,outcol="darkslateblue")
```

RMS Errors



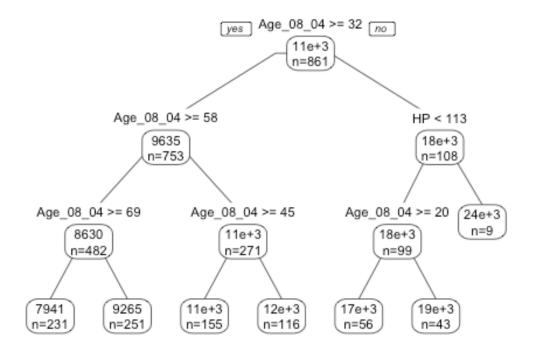
From

the boxplots, we can see that most number of outliers are in the validation data rather than in training which means that we have made the train data into a large enough sample.

Task 9.2.a.iii

```
cross.tree <- rpart(Price</pre>
~Age_08_04+KM+Fuel_Type+HP+Automatic+Doors+Quarterly_Tax+Mfr_Guarantee+Guaran
tee Period+Airco+Automatic_airco+CD Player+Powered_Windows+Sport_Model+Tow_Ba
r, data =train.cars)
printcp(cross.tree)
##
## Regression tree:
## rpart(formula = Price ~ Age 08 04 + KM + Fuel Type + HP + Automatic +
       Doors + Quarterly_Tax + Mfr_Guarantee + Guarantee_Period +
##
       Airco + Automatic_airco + CD_Player + Powered_Windows + Sport_Model +
##
##
       Tow_Bar, data = train.cars)
##
## Variables actually used in tree construction:
## [1] Age_08_04 HP
## Root node error: 1.1075e+10/861 = 12863139
##
## n= 861
```

```
##
##
           CP nsplit rel error xerror
                                           xstd
## 1 0.648917
                   0
                       1.00000 1.00183 0.081301
                       0.35108 0.35592 0.026724
## 2 0.122138
                   1
## 3 0.027146
                   2
                       0.22895 0.23542 0.025091
## 4 0.019048
                       0.20180 0.22853 0.025060
                   3
## 5 0.017894
                   4
                       0.18275 0.19939 0.018977
                   5
                       0.16486 0.19342 0.019179
## 6 0.017794
                       0.14706 0.17054 0.018144
## 7 0.010000
                   6
# From the table we can see that xerror is lowest at CP = 0.01
pruned.ct <- prune(cross.tree,</pre>
cp = cross.tree$cptable[which.min(cross.tree$cptable[,"xerror"]),"CP"])
prp(pruned.ct, type = 1, extra = 1, split.font = 1, varlen = -10)
```



```
trainrmse.prun <- RMSE(predict(pruned.ct,train.cars),train.cars$Price)
validrmse.prun <- RMSE(predict(pruned.ct,valid.cars),valid.cars$Price)
trainrmse.prun
## [1] 1375.392
validrmse.prun
## [1] 1486.168</pre>
```

As expected, compared to the full tree, our pruned tree performs worse on the training set (RMSE=1396.864 compared to 1112.902 for the full tree). The validation set also performed worse(RMSE=1341.264 compared to 1328.958).

Problem 9.2

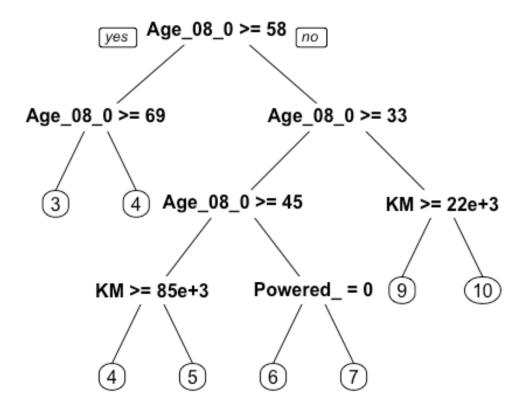
Question 9.2.b

```
bins <- seq(min(ToyotaCorolla$Price),</pre>
           max(ToyotaCorolla$Price),
           (max(ToyotaCorolla$Price) - min(ToyotaCorolla$Price))/20)
bins
## [1] 4350.0 5757.5 7165.0 8572.5 9980.0 11387.5 12795.0 14202.5
15610.0
## [10] 17017.5 18425.0 19832.5 21240.0 22647.5 24055.0 25462.5 26870.0
28277.5
## [19] 29685.0 31092.5 32500.0
Binned_Price <- .bincode(ToyotaCorolla$Price,</pre>
                       bins.
                       include.lowest = TRUE)
Binned_Price <- as.factor(Binned_Price)</pre>
Binned Price
##
     [1] 7 7 7 8
                   7 7 9 11 13 7 12 12 11 13 13 13 14 10 9 9
9
##
              10 9
                    9 10 7
                            9 9 8
                                    8 9
                                          9
                                             8
                                               9
                                                    7 9 7 9 9
                                                                   11
10 9
##
    [49] 10 13 10 9 12 13 8
                           7 8 8 11 9
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## [1033] 5
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## [1057] 2
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## [1105] 3
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## [1177] 4
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## [1201] 4
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## [1225] 4
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## [1273] 3
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## [1297] 3
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## [1321] 4
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## [1345] 4
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## [1393] 3
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## Levels: 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 19 20
train.cars$Binned_Price <- Binned_Price[traincars.index]</pre>
valid.cars$Binned_Price <- Binned_Price[-traincars.index]</pre>
```

Task 9.2.b.i



```
t(t(tr.binned$variable.importance))
##
                          [,1]
                    146.857190
## Age_08_04
## KM
                     53.665182
## CD_Player
                     28.972423
## Airco
                     23.881571
## Automatic_airco
                     17.259249
## Quarterly_Tax
                     14.815708
## Sport_Model
                     13.063749
## Powered_Windows
                      8.212048
## Guarantee_Period
                      3.171908
## Fuel_Type
                      1.926651
## HP
                      1.467326
```

```
## Tow_Bar 1.321867
## Automatic 0.439766
```

When creating bins the intent is to decrease the number of variables. This unsurpisingly results in the binned tree being significantly smaller than the original full tree. One interesting thing to note is the in our binned tree, CD Player replaces Quarterly Tax as one of the top four specifications in indicating price. This could be because tax variations are less significant within bins.

Task 9.2.b.ii

```
newrec <- data.frame(Age 08 04 = 77,
                          KM = 117000,
                          Fuel Type = "Petrol",
                          HP = 110,
                          Automatic = 0,
                          Doors = 5,
                          Quarterly Tax = 100,
                          Mfr Guarantee = 0,
                          Guarantee Period = 3,
                          Airco = 1,
                          Automatic_airco = 0,
                          CD Player = 0,
                          Powered Windows = 0,
                          Sport_Model = 0,
                          Tow Bar = 1)
price.tr <- predict(class.tree, newdata = newrec)</pre>
price.tr.bin <- bins[predict(tr.binned, newdata = newrec, type = "class")]</pre>
price.tr
##
## 7422.414
price.tr.bin
## [1] 7165
```

Task 9.2.b.iii

Our predictions for the two models were very simmilar. The regression tree gave a prediction value of 7422.414 and the classification tree gave 7165. Our binned model returned a whole number while the full model returned a more "accurate" price, but ultimately it is a wash. Both models had comparable accuracy, but the full regression seemed to be better trained.