Week 5: Clustering

Data Analysis

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Agenda



- 1. What is Cluster Analysis?
 - Clustering application examples
- 2. Cluster Analysis: Basic Concepts
- 3. Cluster methods in general
 - Partitioning Methods
 - Hierarchical Methods
 - Other Methods
- 4. Evaluation of Clustering
- 5. Summary
- 6. Exercises with Orange



WEEK 5: CLUSTERING





Modeling

- 1. Recap of week 3
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Unsupervised learning with Clustering

Machine learning paradigms

Supervised learning

- Classification
- Regression (sometimes called 'prediction')
- Sequence prediction (including time series forecasting)

Unsupervised learning

- Clustering (or 'cluster analysis')
- Association





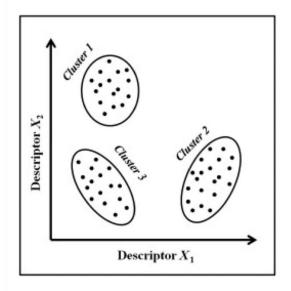
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Unsupervised learning with Clustering

Unsupervised learning is a branch of machine learning that learns from test data that has not been labeled, classified or categorized





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Unsupervised learning with Clustering

What is Cluster Analysis?

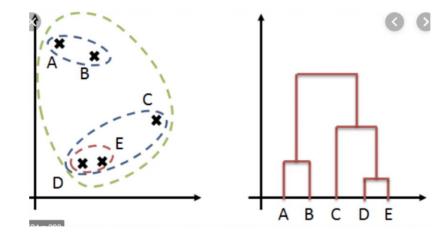
Cluster: A collection of data objects

- similar (or related) to one another within the same group
- dissimilar (or unrelated) to the objects in other groups

Cluster analysis (or Clustering)

 Finding similarities between data according to the characteristics found in the data and grouping similar data objects into clusters

Unsupervised learning: no predefined classes





Modeling

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- **Cluster Analysis: Basic Concepts**
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- **Evaluation of Clustering**
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- **Exercises with Orange**

Unsupervised learning with Clustering

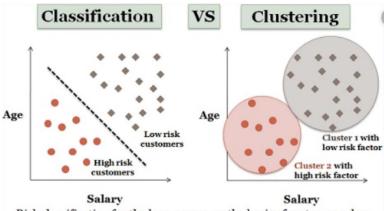
Clustering ≠ Classification

Clustering

- Does our population (f.i. customers.) naturally fall into different groups?
- Find these groups and the characteristics of these groups (f.i. using exploratory data analysis)
- There is no prediction of the group to which new observations belong(!)

Classification

- Groups (f.i. customers) that differ with respect to a particular target characteristic (f.i. risk to churn)
- Find a model to predict (and/or explain) the target characteristic



Risk classification for the loan payees on the basis of customer salary



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What is Cluster Analysis?

Clustering Application Examples

- Biology: taxonomy of living things: kingdom, phylum, class, order, family, genus and species
- Information retrieval: document clustering
- Land use: Identification of areas of similar land use in an earth observation database
- Marketing: Help marketers discover distinct groups in their customer bases, and then use this knowledge to develop targeted marketing programs
- City-planning: Identifying groups of houses according to their house type, value, and geographical location
- Climate: understanding earth climate, find patterns of atmospheric and ocean



Modeling

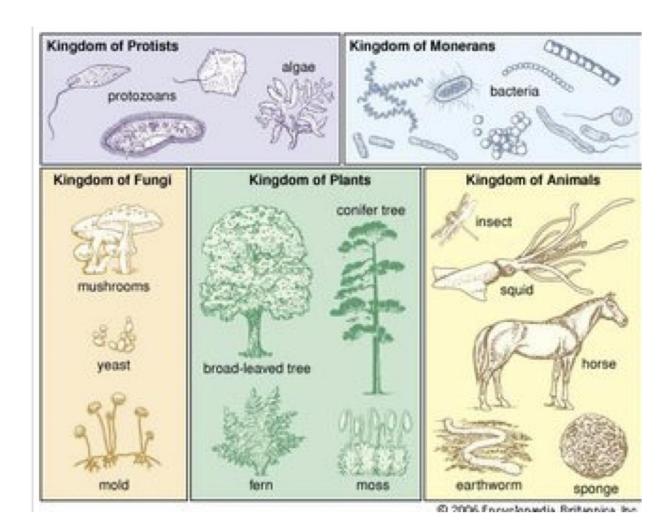
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What is Cluster Analysis?

Clustering Application Example: Biology





Modeling

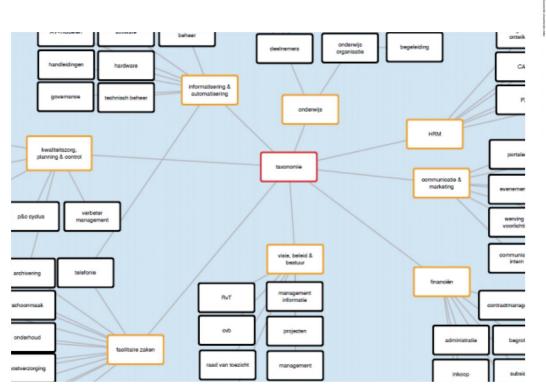
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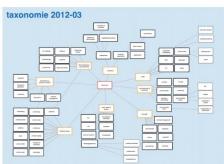
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What is Cluster Analysis?

Clustering Application Example: Information retrieval







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What is Cluster Analysis?

Clustering Application Example: Marketing – Customer Profiles





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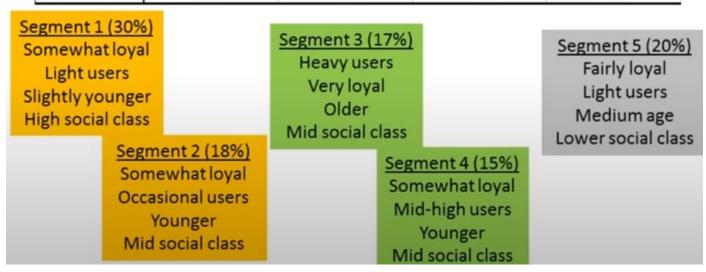
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What is Cluster Analysis?

Clustering Application Example: Marketing – Customer Profiles

Mean/Centroid	Loyalty	Usage	Age	Social Class
Segment 1	4.46	3.67	3.07	8.40
Segment 2	4.44	1.38	2.50	4.19
Segment 3	8.53	8.13	6.82	5.74
Segment 4	4.93	6.63	2.67	4.31
Segment 5	5.29	3.20	4.30	3.23
AVERAGE	5.38	4.37	3.79	5.54





Modeling

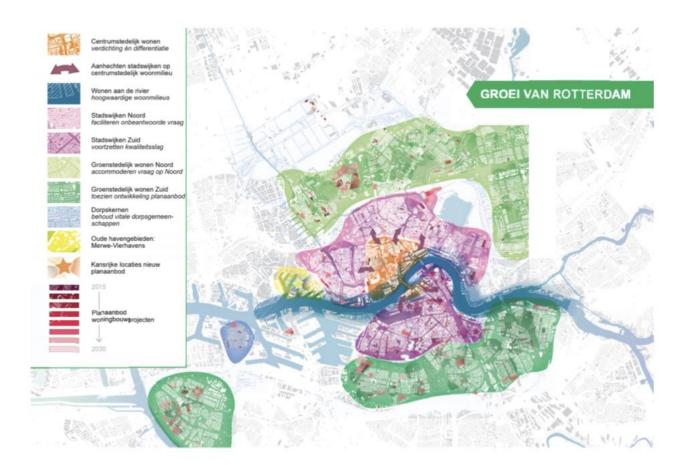
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What is Cluster Analysis?

Clustering Application Example: City planning - Rotterdam





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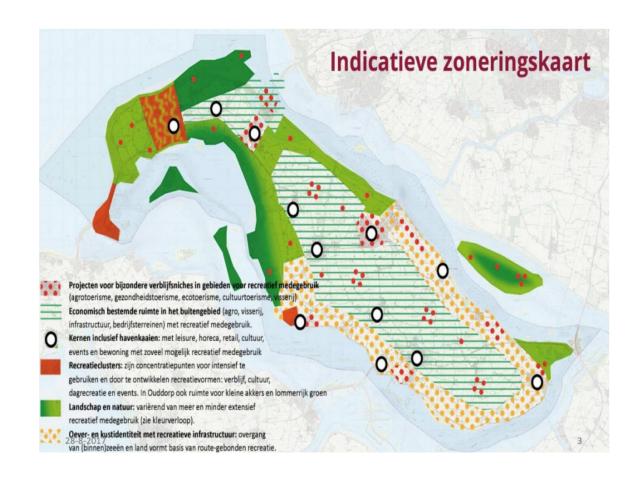
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What is Cluster Analysis?

Clustering Application Example: Land use





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What is Cluster Analysis?

Clustering Application Example: Land use / city planning





Modeling

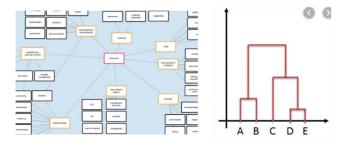
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Basic Concepts

Considerations for Cluster Analysis



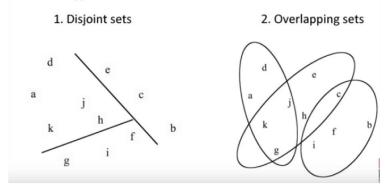
Partitioning criteria

Single level vs. hierarchical partitioning (often, multi-level hierarchical partitioning is desirable)

Separation of clusters

• Exclusive (e.g., one customer belongs to only one region) vs. non-exclusive(e.g., one document may belong to more than one class)

Cluster types



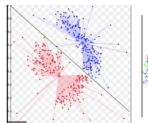
Cluster plot Messessipps North Carbina Configs Alabama Alabama Andrensas Kentucke South Dakota Marylant Marylant Moren Dak Florat Mentucke Messes New Messes Order Person New Heater Texas Order Person New Heater Texas Order Person New Heater Texas Order Person New Heater Configure Texas Order Person New Heater Configure Texas Order Person New Heater Order Person

Similarity measure

 Distance-based (e.g., Euclidian) vs. connectivity-based (e.g., density)

Clustering space

Full space (often when low dimensional) vs. subspaces (often in high-dimensional clustering)







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Basic Concepts

Major Clustering Approaches

Partitioning approach

- Construct various partitions and then evaluate them by some criterion
- Typical methods: k-means, k-medoids, CLARANS

Hierarchical approach

- Create a hierarchical decomposition of the set of data (or objects) using some criterion
- Typical methods: Diana, Agnes, BIRCH, CAMELEON

Density-based approach

- Based on connectivity and density functions
- Typical methods: DBSACN, OPTICS, DenClue

Grid-based approach

- based on a multiple-level granularity structure
- Typical methods: STING, WaveCluster, CLIQUE

Model-based approach



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Cluster methods in general

Partitioning Methods

Partitioning method:

Partitioning a dataset of n objects into a set of k clusters, such that the sum of squared distances is minimized (where c_i is the centroid or medoid of cluster C_i)

Global optimal: exhaustively enumerate all partitions (Volledig opsommen van alle partities)

Heuristic methods:

k-means and *k-medoids* algorithms (distance-based clustering)



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Cluster methods in general

Partitioning Methods: The K-Means Clustering Method

Given *k*, the *k-means* algorithm is implemented in four steps:

- 1. Partition objects into *k* nonempty clusters
- Compute the centroids of the clusters of the current partitioning (the centroid is the center, i.e., <u>mean point</u>, of the cluster) Update cluster centroids
- 3. Assign each object to the cluster with the nearest centroid Reassign objects to clusters
- 4. Go back to Step 2, stop when the assignment does not change



Modeling

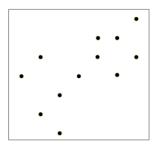
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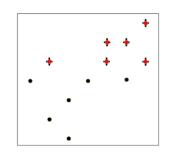
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Partitioning Methods: The K-Means Clustering Method

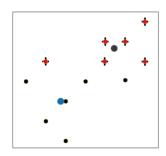


K=2

Arbitrarily partition objects into k groups



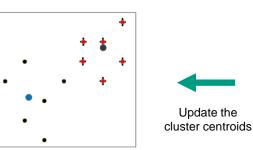




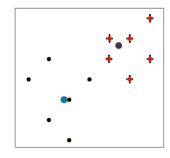
The initial data set

- Partition objects into k nonempty subsets
- Repeat
 - Compute centroid (i.e., mean
 - point) for each partition
 - Assign each object to the cluster of its nearest centroid
- Until no change











Modeling

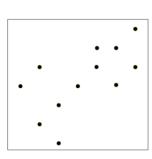
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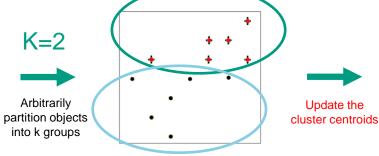
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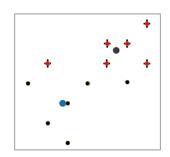
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Cluster methods in general

Partitioning Methods: The K-Means Clustering Method





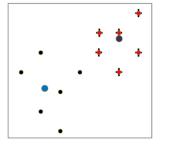


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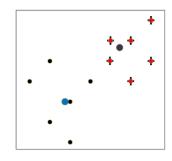
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Modeling

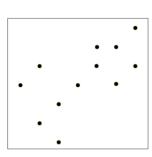
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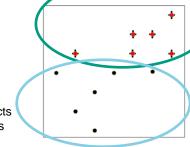
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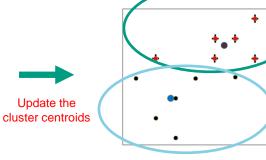
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K=2

Arbitrarily partition objects into k groups

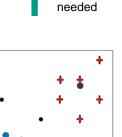




Reassign

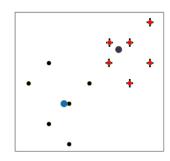
The initial data set

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Loop if







Modeling

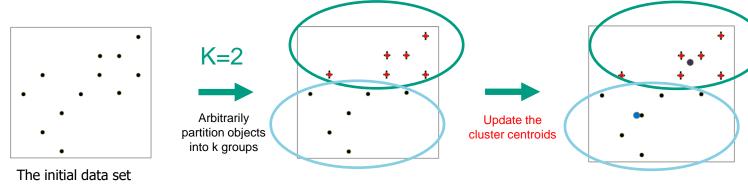
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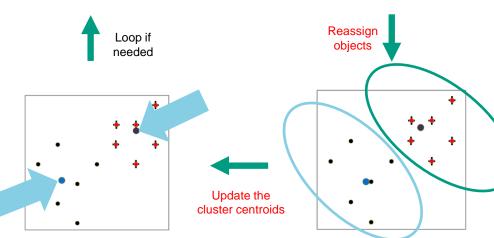
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Cluster methods in general

Partitioning Methods: The K-Means Clustering Method



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Cluster methods in general

Partitioning Methods: The K-Means Clustering Method

What Is the Problem of the K-Means Method?

The k-means algorithm is sensitive to outliers!

Since an object with an extremely large value may substantially distort the distribution of the data

K-Medoids: Instead of taking the **mean** value of the object in a cluster as a reference point, **medoids** can be used, which is the **most centrally located** object in a cluster

We want two or more clusters with a very small cluster sum of squared errors



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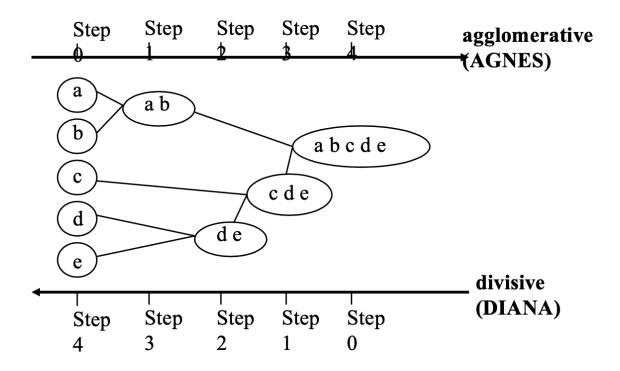
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Cluster methods in general

Hierarchical Clustering

Use distance matrix as clustering criteria. This method starts with all data points assigned to a cluster of their own, merges the two nearest clusters until there is only a single cluster left





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Cluster methods in general

Determine the Number of Clusters

Empirical method:

of clusters: $k \approx \sqrt{(n/2)}$ for a dataset of n points, e.g., n = 200, k = 10

Other methods:

- Silhouette method: average silhouette score of the dataset
- Elbow method (k-means)
- Dendrogram heuristic (hierarchical clustering)

Silhouette score s(i) of point i:

$$s(i) = \frac{b(i) - a(i)}{\max\{a(i), b(i)\}}$$

- a(i): mean distance between i and all other data points in same cluster
- b(i): smallest mean distance of i to all points in any other cluster, of which i is not a member



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Partitioning Methods Hierarchical Methods

Other Methods

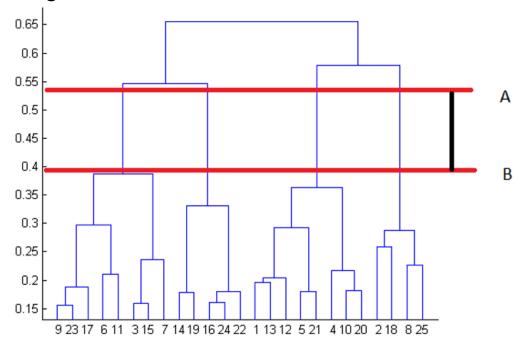
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Dendrogram

- Shows all clusters (bottom up)
- The height at which two clusters are merged represents the distance between the clusters (agglomerative)

Heuristic: The number of clusters is equal to the number of vertical lines cut by a horizontal line that can transverse the maximum distance without intersecting a cluster





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Evaluation of Clustering

Measuring Clustering Quality

- 3 kinds of measures: External, internal and relative
- External: supervised, employ criteria not inherent to the dataset
 - Compare a clustering against prior or expert-specified knowledge using certain clustering quality measure
- Internal: unsupervised, criteria derived from data itself
 - Evaluate the goodness of a clustering by considering how well the clusters are separated, and how compact the clusters are, e.g., Silhouette coefficient
- Relative: directly compare different clusterings, usually those obtained via different parameter settings for the same algorithm



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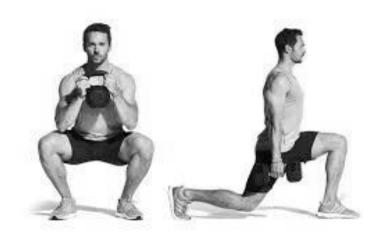
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Summary

- Cluster analysis groups objects based on their similarity and has wide applications
- Clustering algorithms can be categorized into partitioning methods, hierarchical methods, density-based methods, grid-based methods, and model-based methods
- K-means and K-medoids algorithms are popular partitioning-based clustering algorithms
- Birch and Chameleon are interesting hierarchical clustering algorithms, and there are also probabilistic hierarchical clustering algorithms
- DBSCAN, OPTICS, and DENCLU are interesting density-based algorithms
- STING and CLIQUE are grid-based methods, where CLIQUE is also a subspace clustering algorithm
- Quality of clustering results can be evaluated in various ways



EXERCISES

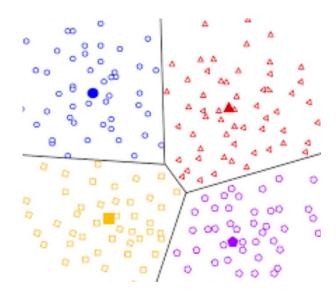




Let's start with the exercises in Orange

Exercise 1 Do the following e-learnings to get familiar with clustering.

- Getting Started with Orange 11: k-Means https://www.youtube.com/watch?v=vgmL808eSw4
- Getting Started with Orange 12: k-Means Explained https://www.youtube.com/watch?v=I0e0Qyev8Ac
- 3. Getting Started with Orange 13: Silhouette https://www.youtube.com/watch?v=5TPldC dC0s
- 4. Text clustering: https://www.youtube.com/watch?v=rH_vQxQL6oM
- Image clustering: https://www.youtube.com/watch?v=lu8g2Twjn9U
- Image clustering predictions: https://www.youtube.com/watch?v=lvgx62a8XQk





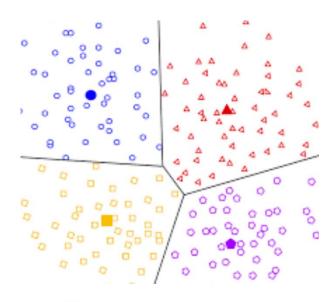


Let's start with the exercises in Orange

Exercise 2

Cleaning and clustering exercise:

- 1. Download the file 'Online Retail small' from Blackboard (week 4).
- 2. Use CRISP-DM (exploratory data analysis and preprocessing)
- 3. Method for this file;
 - We want to make clusters for this file, with Orange;
 - Investigate some interesting clusters for this file;
 - Cluster using the best scoring clustering







Let's start with the exercises in Orange

Column Descriptions

Column Name	Description	Data Type
InvoiceNo	Invoice number.If this code starts with letter 'c', it indicates a cancellation.	Nominal, a 6-digit integral number uniquely assigned to each transaction
StockCode	Product (item) code	Nominal, a 5-digit integral number uniquely assigned to each distinct product
Description	Product (item) name.	Nominal
Quantity	The quantities of each product (item) per transaction.	Numeric
InvoiceDate	Invice Date and time	Numeric, the day and time when each transaction was generated
UnitPrice	Unit price	Numeric, Product price per unit in sterling
CustomerID	Customer number	Nominal, a 5-digit integral number uniquely assigned to each customer
Country	Country name	Nominal, the name of the country where each customer reside

