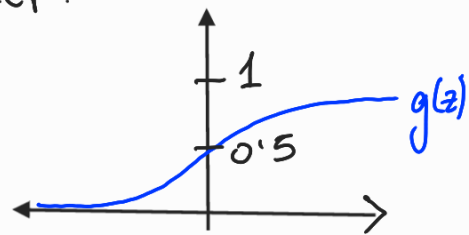


Using $h_\theta(x)$ from linear regression, the hypothesis function can be out of $[0, 1]$. So we need another:

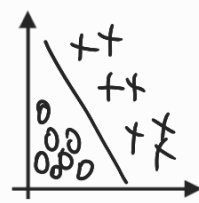
Logistic Regression:

$$h_\theta(x) = g(\theta^T x) ; \text{ where } g(z) = \frac{1}{1 + e^{-z}}$$



- Interpretation: $h_\theta(x) \Rightarrow$ probability that $y=1$ on input x
 $\Rightarrow P(y=1 | x; \theta)$

- Decision boundary $\nearrow h_\theta(x) \geq 0.5 \equiv \theta^T x \geq 0 \Rightarrow 1$
 $\searrow h_\theta(x) < 0.5 \equiv \theta^T x < 0 \Rightarrow 0$



- Cost function: choosing θ .

$$\text{Cost}(h_\theta(x), y) = \begin{cases} -\log(h_\theta(x)) & \text{if } y=1 \\ -\log(1-h_\theta(x)) & \text{if } y=0 \end{cases}$$



- Gradient descent: iteratively $\downarrow -\frac{1}{m} \sum_{i=1}^m \text{cost function}_i$

- Advanced optimization: compute $\frac{\partial}{\partial \theta_j} J(\theta)$ $\left\{ \begin{array}{l} \text{Conjugate gradient} \\ \text{BFGS} \\ \text{L-BFGS} \end{array} \right.$