



Final Project – Mortality Rates Prediction

Time Series Analysis

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Acronyms

ARIMA – Autoregressive integrated moving average

ACF – Autocorrelation Factors

PACF – Partial Autocorrelation Factors

VaR – Value at risk

TVaR – Tail value at risk

BP test – Breusch Pagan test

LB test – Ljung-Box test

ADF test – Augmented Dickey Fuller test

KPSS test –Kwiatkowski–Phillips–Schmidt–Shin test

AICc – Akaike Information Criterion

BIC – Bayesian Information Criterion

1. Overview

In this Project, an insurance company risk for the next year is going to be calculated by the estimation of the mortality rates of the policyholders. The objective of the model is to properly evaluate the premium risk (the risk of having more claims than expected) so the economic capital can be estimated.

The insurance company to be modelled is composed by the following number of policies for each age:

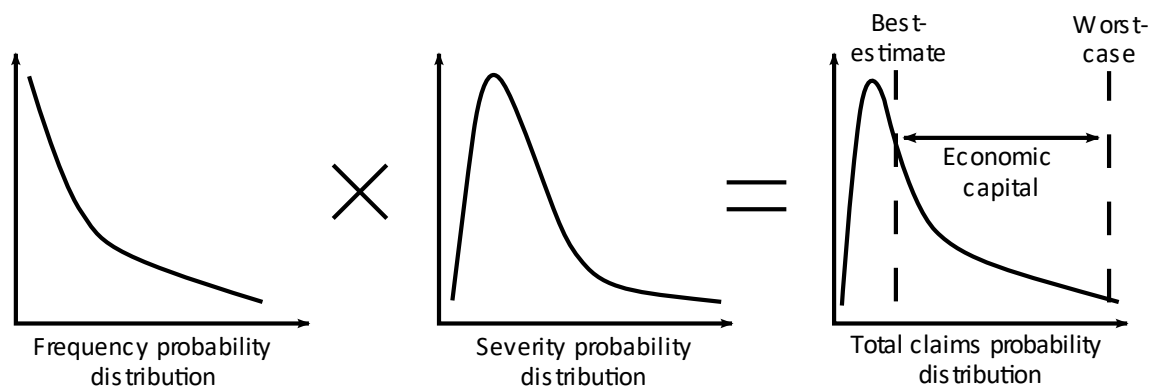
| Age | Policies |
|-----|----------|
| 67 | 902 |
| 68 | 659 |
| 69 | 1471 |
| 70 | 978 |
| 71 | 675 |
| 72 | 850 |
| 73 | 882 |
| 74 | 1035 |
| 75 | 995 |

The historical mortality rates of the policyholders age is available since 1935 up to 2021.

The project has four main parts:

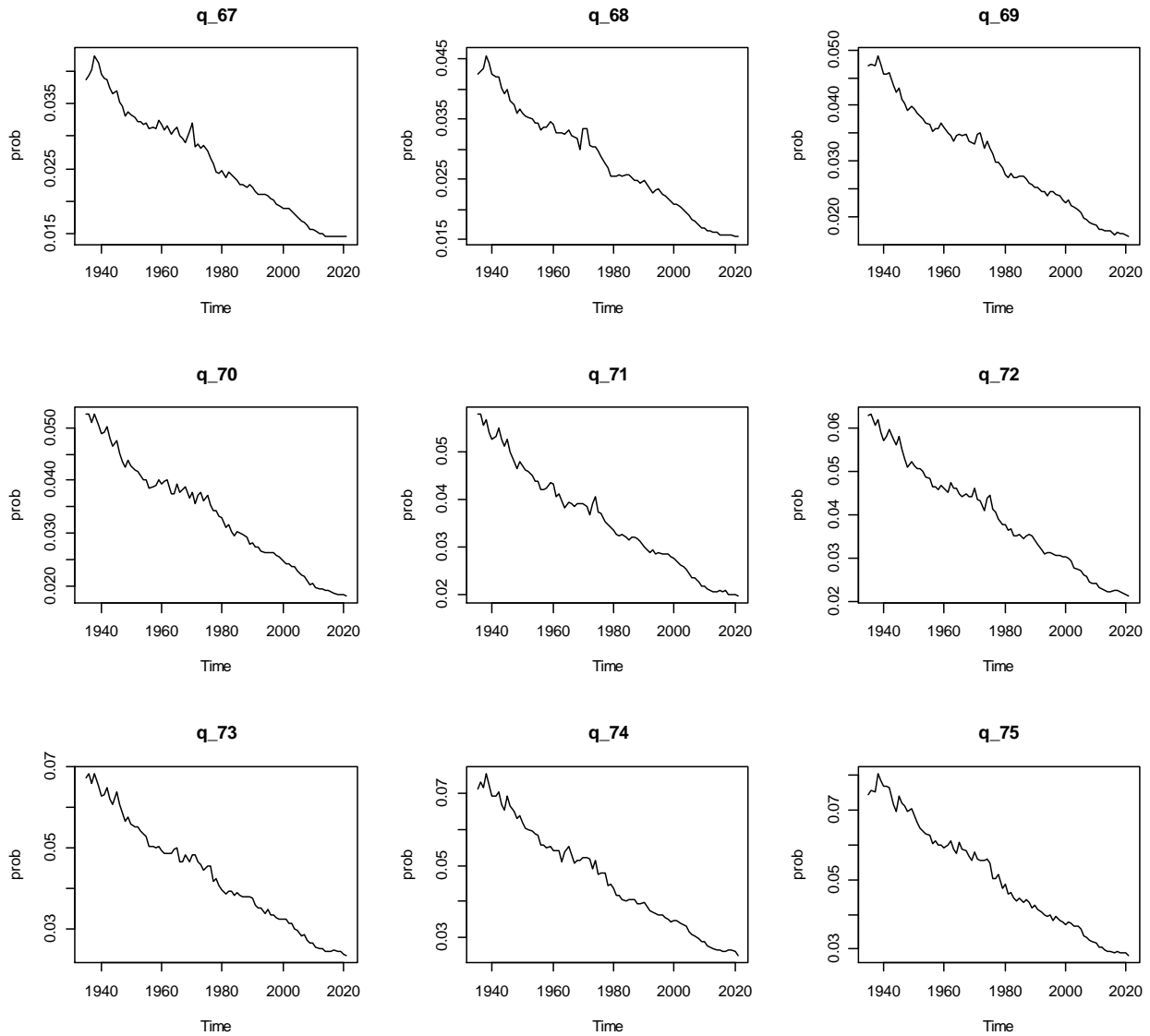
1. Mortality rates time series ARIMA functional form estimation by Box-Jenkins procedure
2. Estimation and diagnosis of the ARIMA model
3. One year period mortality rate prediction
4. Cost estimation and economic capital calculation

With this model, the expected cost will be evaluated together with the VaR_{99} (maximum expected cost in the 99% of the cases, or which is the same, maximum expected cost in 1 out 100 years) and TVaR_{99} (expected cost if the cost surpasses the VaR_{99}). This way the worst-case scenarios will be quantified, and the company solvency capital requirement will be determined.



2. Available data

The following [mortality time series](#) are available for which we need to predict the 2022 value.



3. Functional form identification by Box-Jenkins procedure

According to previous studies, Lee and Carter model (1992), the log-mortality rates are ARIMA processes. Therefore, for all time series, the log-qx have been calculated. Additionally, it has been checked that the time series are not stationary (see the code lines 93 to 117) so directly the analysis will be performed on the differentiated time series. The diagnosis and all the test are coded in lines 155 to 274.

3.1. Mortality rate q_{67} ARIMA estimation

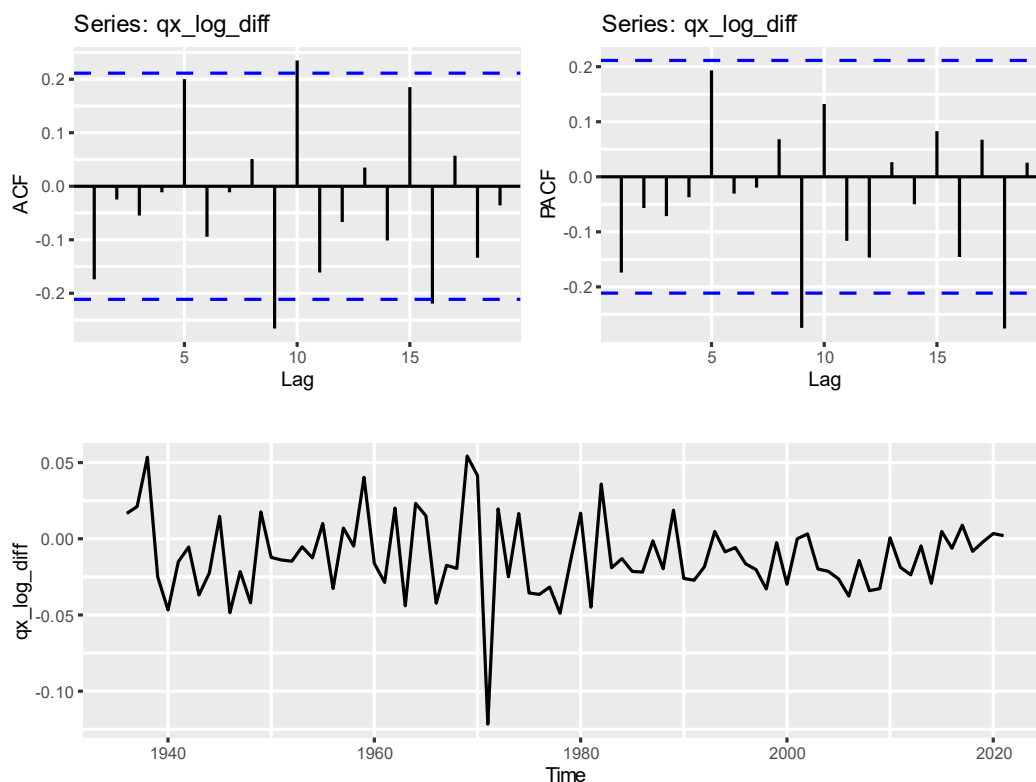
The ADF (Augmented Dickey-Fuller), PP (Phillips Perron) and KPSS (Kwiatkowski–Phillips–Schmidt–Shin) tests have been performed showing the following results for the $I(0)$ and $I(1)$ time series.

| $I(0)$ | p.value | stationary 0.05 |
|--------|---------|-----------------|
| ADF | 0.75961 | FALSE |
| PP | 0.31752 | FALSE |
| KPSS | 0.01000 | FALSE |

| $I(1)$ | p.value | stationary 0.05 |
|--------|---------|-----------------|
| ADF | 0.04017 | TRUE |
| PP | 0.01000 | TRUE |
| KPSS | 0.10000 | TRUE |

It is checked that all the test show the differentiated time series to be stationary for the significance level of 0.05.

For the log-mortality rates of the age 67, the differentiated time series visualization and its ACF and PACF are shown:



According to Box-Jenkins procedure, the time series appears to be an ARIMA of orders:

- (0,1,0)
- (1,0,1)
- (0,1,1)
- (1,1,1)

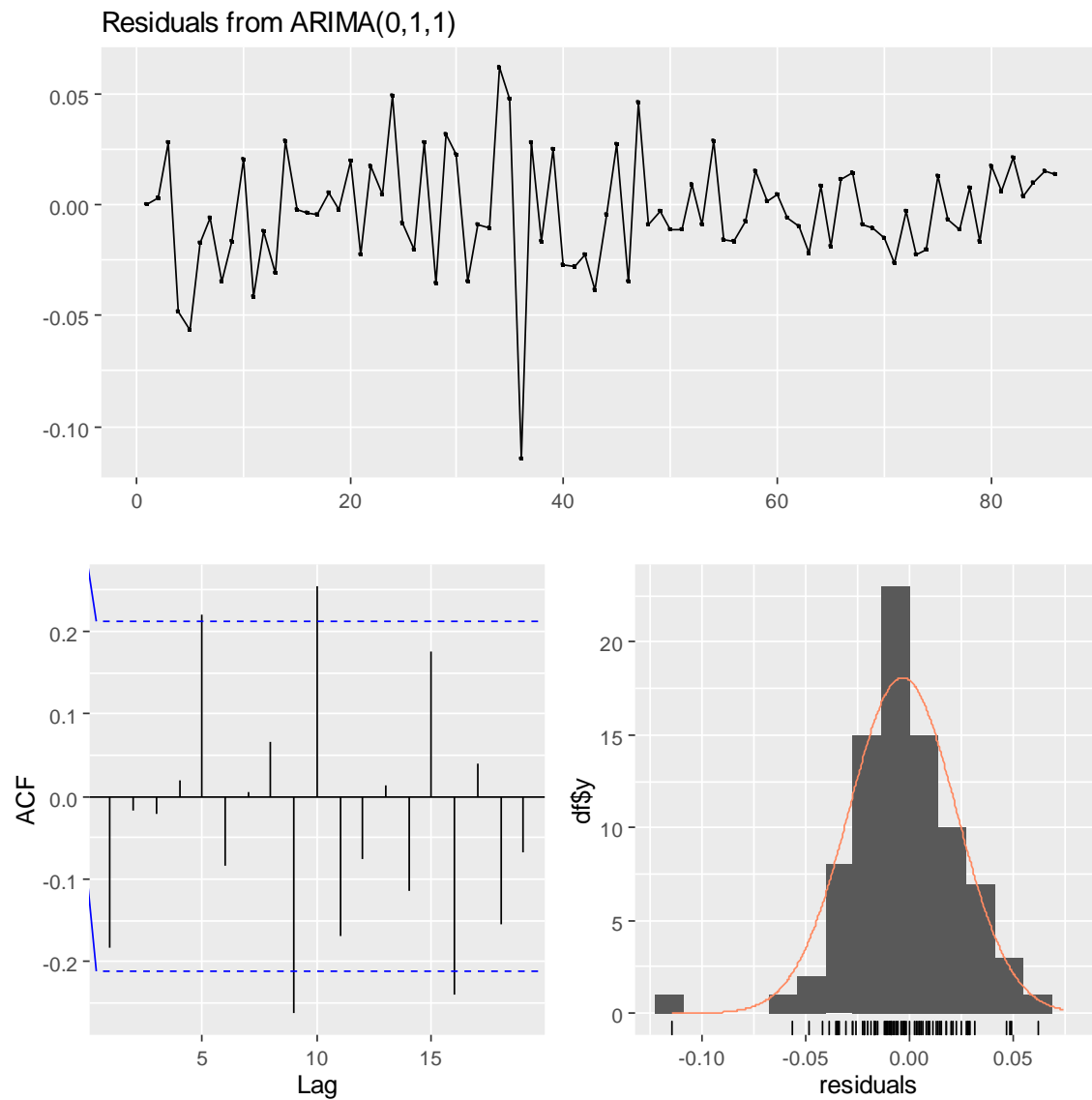
According to the ACF and PACF the most reliable form is (0,1,0). In any case all mentioned will be tested to confirm. All the results of the diagnosis for the time series up to an order (2,1,2) are summarized in the annex.

The ARIMA(0,1,1) proves to be the best fitting model with the following results:

| time_series | q_67_log |
|----------------------|------------|
| ARIMA | (0,1,1) |
| AICc | -381.44546 |
| BIC | -374.37510 |
| AR1 | 0.00000 |
| AR1_H0_inf | #N/A |
| AR1_H0_sup | #N/A |
| AR1_H0 | #N/A |
| AR2 | 0.00000 |
| AR2_H0_inf | #N/A |
| AR2_H0_sup | #N/A |
| AR2_H0 | #N/A |
| MA1 | -0.20214 |
| MA1_H0_inf | -0.47090 |
| MA1_H0_sup | -0.00162 |
| MA1_H0 | REJECTED |
| MA2 | 0.00000 |
| MA2_H0_inf | #N/A |
| MA2_H0_sup | #N/A |
| MA2_H0 | #N/A |
| drift | -0.01151 |
| drift_H0_inf | -0.01593 |
| drift_H0_sup | -0.00749 |
| drift_H0 | REJECTED |
| Normality_CVM_pvalue | 0.57427 |
| Normality_AD_pvalue | 0.46396 |
| Normality_JB_pvalue | 0.00015 |
| Incorrelation_LB | 0.26379 |
| Homocedasticity_BP_B | 0.99784 |
| Zero_mean | 0.98219 |

All the diagnosis has been properly tested so the AR parameter and the constant are significant, the residuals are normal, uncorrelated, constant in variance and have zero mean.

The residuals can be summarized in the following graph:



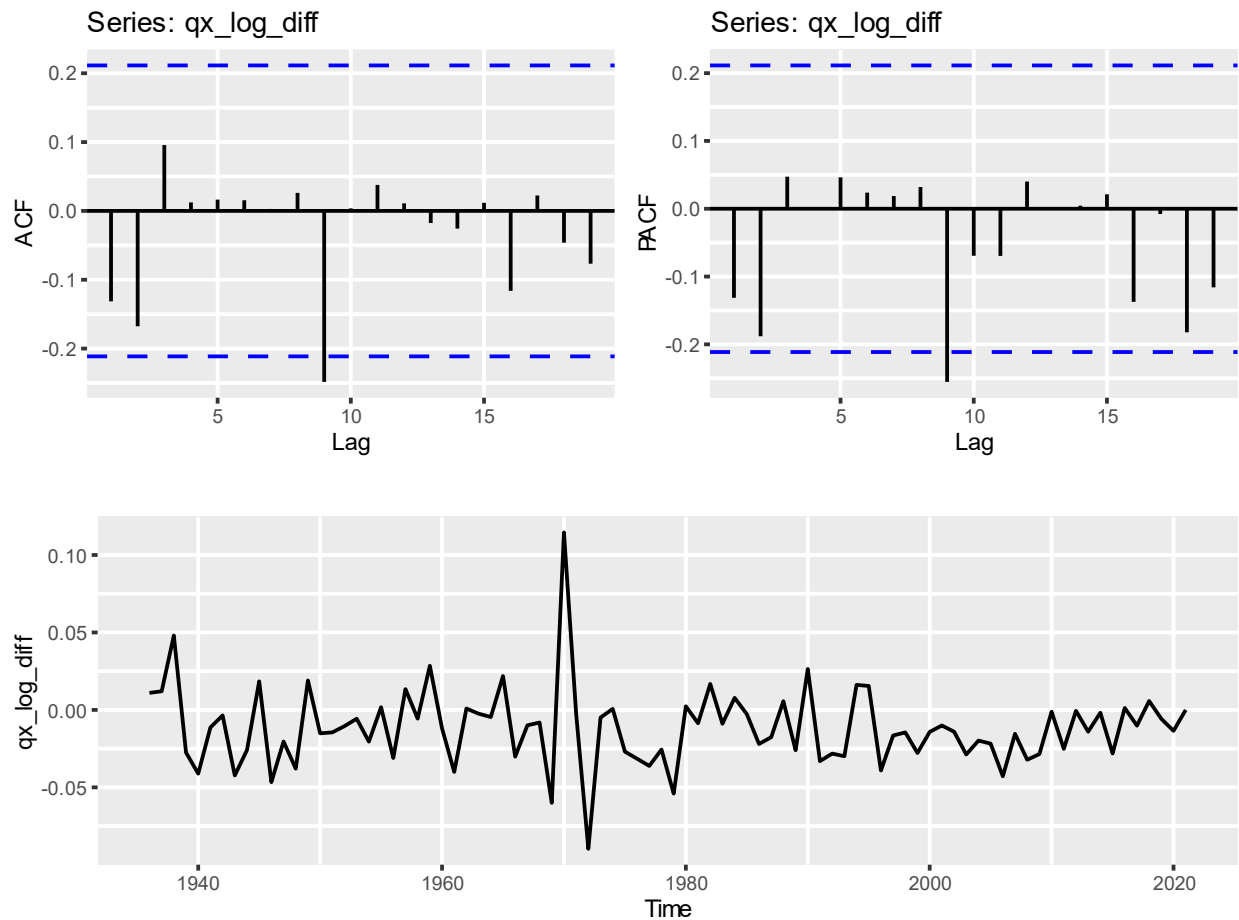
3.2. Mortality rate q_{68} ARIMA estimation

The following stationary test have been performed.

| I(0) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.69155 | FALSE |
| PP | 0.41466 | FALSE |
| KPSS | 0.01000 | FALSE |

| I(1) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.01523 | TRUE |
| PP | 0.01000 | TRUE |
| KPSS | 0.10000 | TRUE |

The differentiated time series visualization and its ACF and PACF are shown:



According to Box-Jenkins procedure, the time series appears to be an ARIMA of orders:

- (0,1,0)
- (1,0,1)
- (0,1,1)
- (1,1,1)

According to the ACF and PACF the most reliable form is (0,1,0). In any case all mentioned will be tested to confirm. All the results of the diagnosis for the time series up to an order (2,1,2) are summarized in the annex.

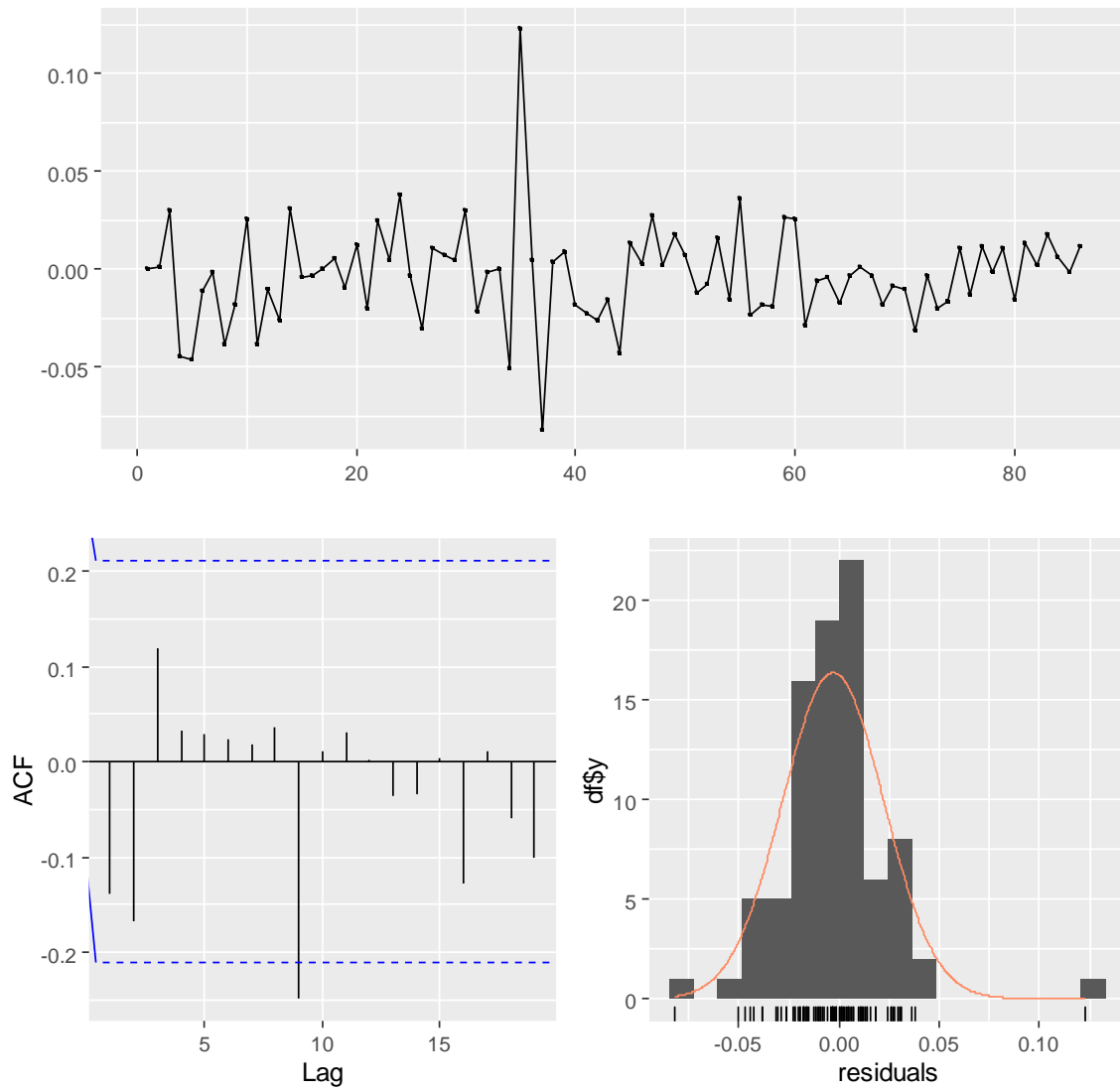
The ARIMA(0,1,1) proves to be the best fitting model with the following results:

| | |
|-----------------------------|------------|
| time_series | q_68_log |
| ARIMA | (0,1,1) |
| AICc | -384.38390 |
| BIC | -377.31354 |
| AR1 | 0.00000 |
| AR1_H0_inf | #N/A |
| AR1_H0_sup | #N/A |
| AR1_H0 | #N/A |
| AR2 | 0.00000 |
| AR2_H0_inf | #N/A |
| AR2_H0_sup | #N/A |
| AR2_H0 | #N/A |
| MA1 | -0.19205 |
| MA1_H0_inf | -0.43452 |
| MA1_H0_sup | -0.00261 |
| MA1_H0 | REJECTED |
| MA2 | 0.00000 |
| MA2_H0_inf | #N/A |
| MA2_H0_sup | #N/A |
| MA2_H0 | #N/A |
| drift | -0.01188 |
| drift_H0_inf | -0.01601 |
| drift_H0_sup | -0.00751 |
| drift_H0 | REJECTED |
| Normality_CVM_pvalue | 0.43926 |
| Normality_AD_pvalue | 0.36454 |
| Normality_JB_pvalue | 0.00000 |
| Incorrelation_LB | 0.49218 |
| Homocedasticity_BP_B | 0.58348 |
| Zero_mean | 0.98894 |

All the diagnosis has been properly tested so the AR parameter and the constant are significant, the residuals are normal, uncorrelated, constant in variance and have zero mean.

The residuals can be summarized in the following graph:

Residuals from ARIMA(0,1,1)



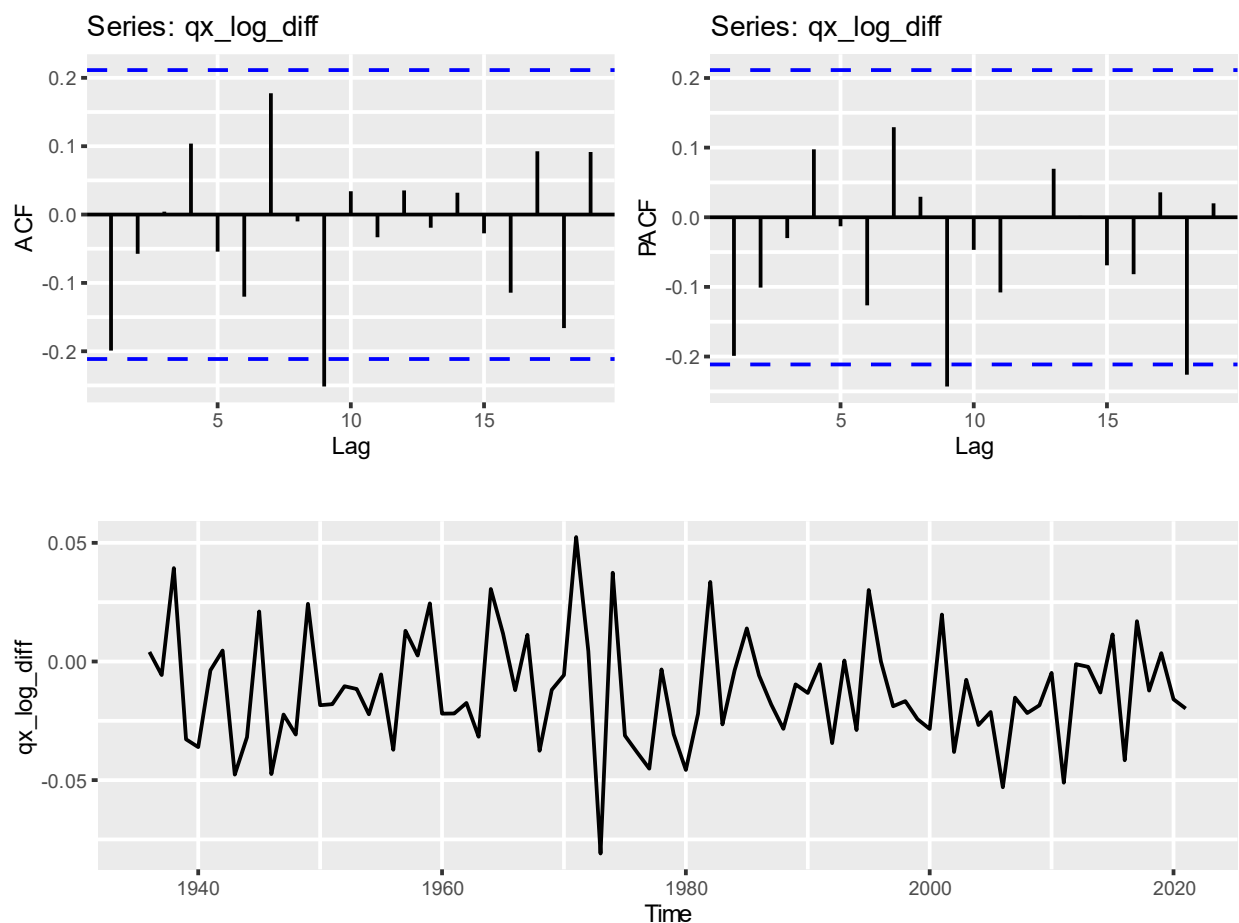
3.3. Mortality rate q_{69} ARIMA estimation

The following stationary test have been performed.

| I(0) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.56396 | FALSE |
| PP | 0.42881 | FALSE |
| KPSS | 0.01000 | FALSE |

| I(1) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.01857 | TRUE |
| PP | 0.01000 | TRUE |
| KPSS | 0.10000 | TRUE |

The differentiated time series visualization and its ACF and PACF are shown:



According to Box-Jenkins procedure, the time series appears to be an ARIMA of orders:

- (0,1,0)
- (1,0,1)
- (0,1,1)
- (1,1,1)

According to the ACF and PACF the most reliable form is (0,1,0). In any case all mentioned will be tested to confirm. All the results of the diagnosis for the time series up to an order (2,1,2) are summarized in the annex.

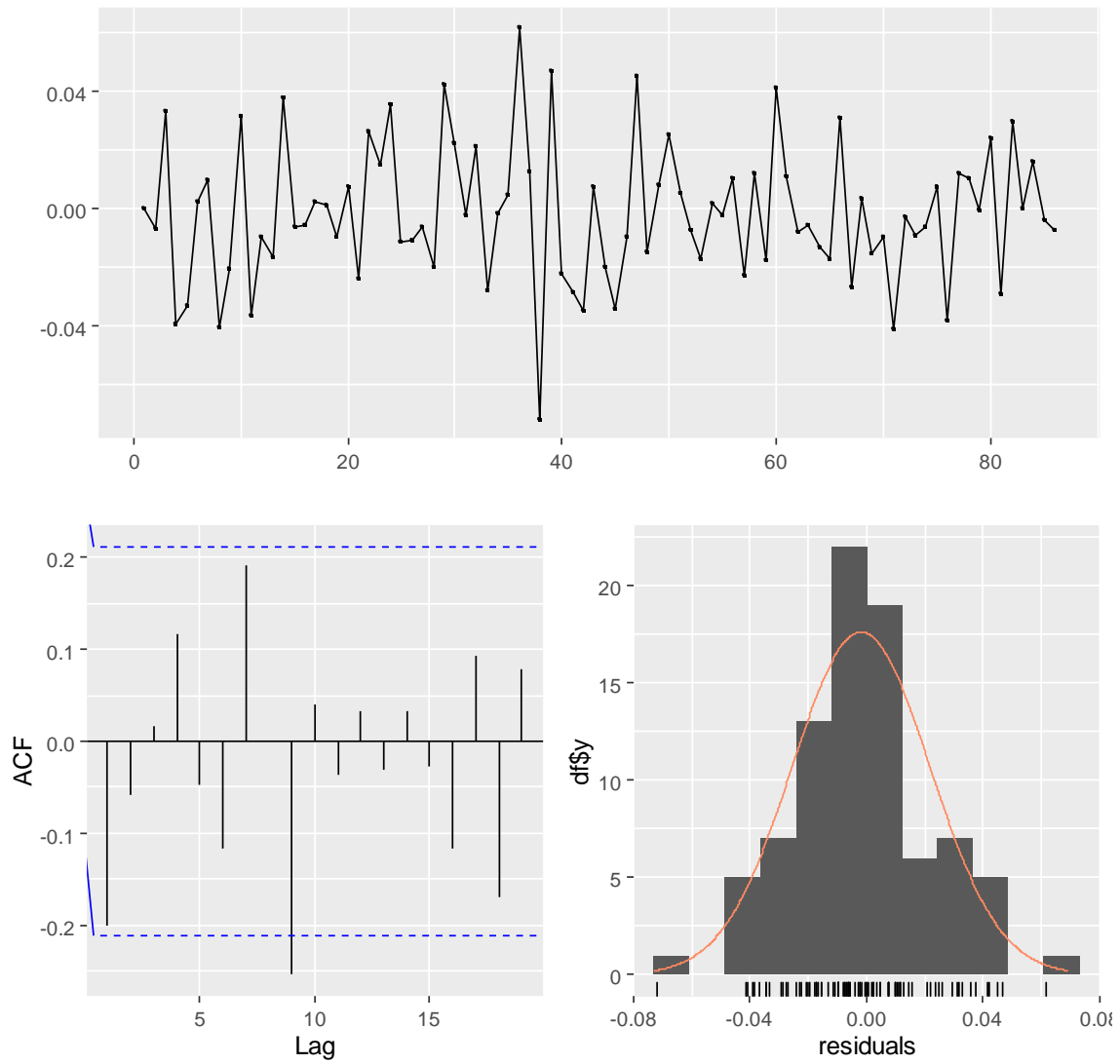
The ARIMA(0,1,1) proves to be the best fitting model with the following results:

| time_series | q_69_log |
|-----------------------------|-----------------|
| ARIMA | (0,1,1) |
| AICc | -398.27097 |
| BIC | -391.20061 |
| AR1 | 0.00000 |
| AR1_H0_inf | #N/A |
| AR1_H0_sup | #N/A |
| AR1_H0 | #N/A |
| AR2 | 0.00000 |
| AR2_H0_inf | #N/A |
| AR2_H0_sup | #N/A |
| AR2_H0 | #N/A |
| MA1 | -0.23209 |
| MA1_H0_inf | -0.49352 |
| MA1_H0_sup | -0.01913 |
| MA1_H0 | REJECTED |
| MA2 | 0.00000 |
| MA2_H0_inf | #N/A |
| MA2_H0_sup | #N/A |
| MA2_H0 | #N/A |
| drift | -0.01226 |
| drift_H0_inf | -0.01577 |
| drift_H0_sup | -0.00824 |
| drift_H0 | REJECTED |
| Normality_CVM_pvalue | 0.76858 |
| Normality_AD_pvalue | 0.87554 |
| Normality_JB_pvalue | 0.57133 |
| Incorrelation_LB | 0.31720 |
| Homocedasticity_BP_B | 0.12939 |
| Zero_mean | 0.99118 |

All the diagnosis has been properly tested so the AR parameter and the constant are significant, the residuals are normal, uncorrelated, constant in variance and have zero mean.

The residuals can be summarized in the following graph:

Residuals from ARIMA(0,1,1)



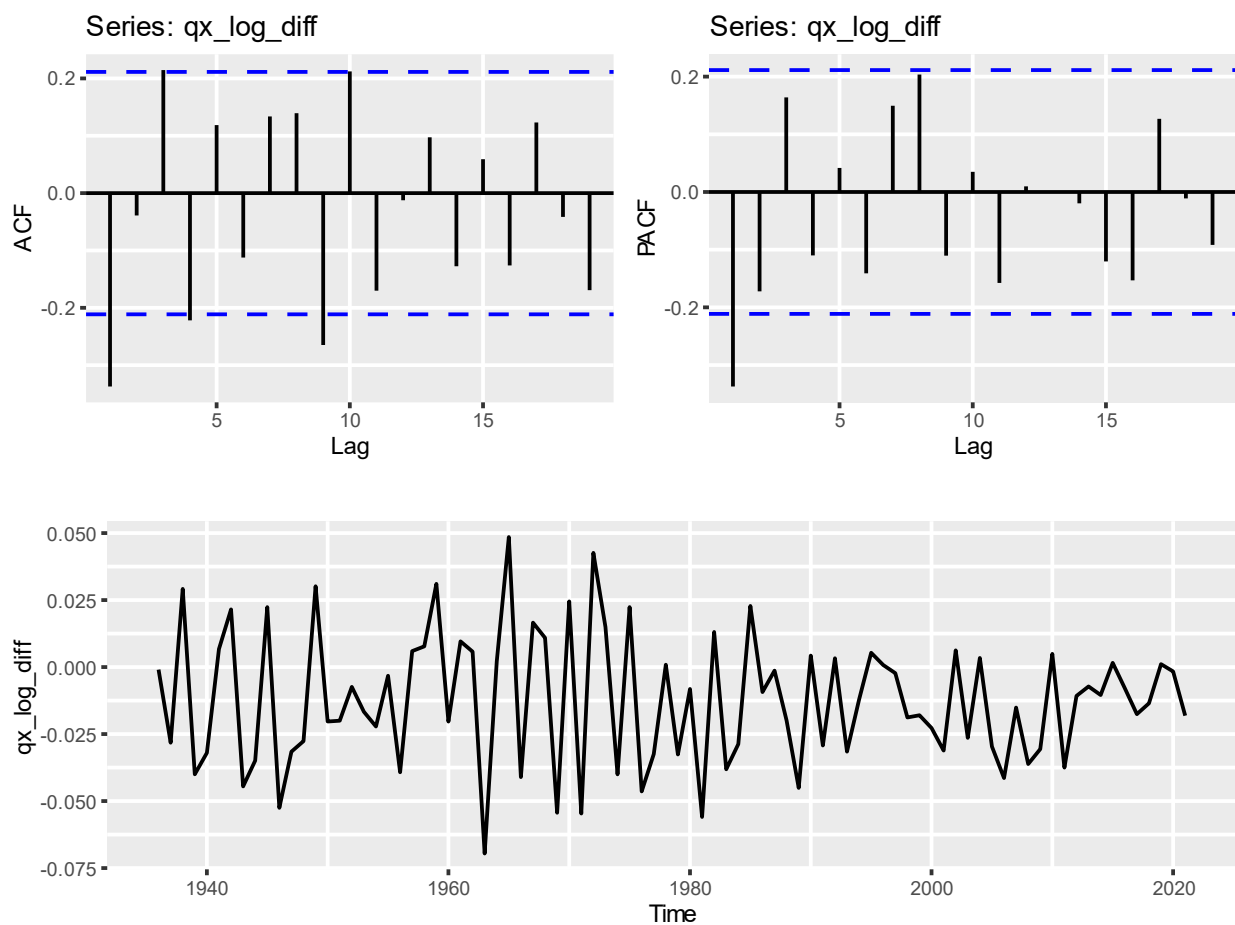
3.4. Mortality rate q_{70} ARIMA estimation

The following stationary test have been performed.

| I(0) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.81072 | FALSE |
| PP | 0.61122 | FALSE |
| KPSS | 0.01000 | FALSE |

| I(1) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.01000 | TRUE |
| PP | 0.01000 | TRUE |
| KPSS | 0.10000 | TRUE |

The differentiated time series visualization and its ACF and PACF are shown:



According to Box-Jenkins procedure, the time series appears to be an ARIMA of orders:

- (0,1,0)
- (1,0,1)
- (0,1,1)
- (1,1,1)

According to the ACF and PACF the most reliable form is (0,1,0). In any case all mentioned will be tested to confirm. All the results of the diagnosis for the time series up to an order (2,1,2) are summarized in the annex.

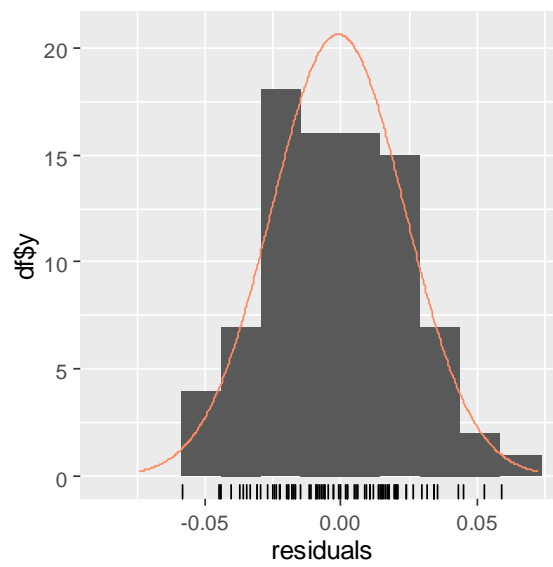
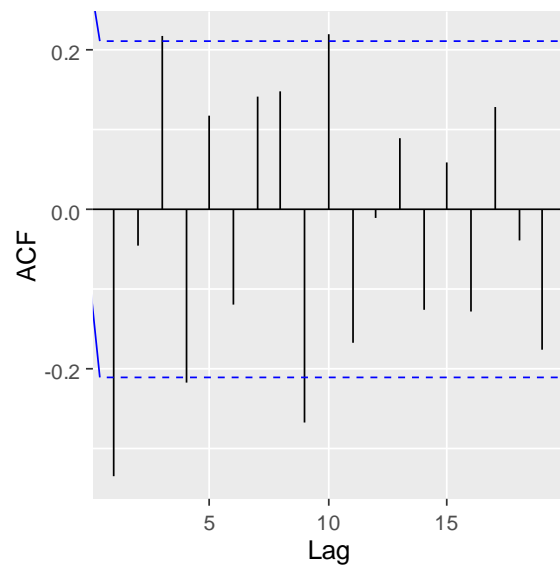
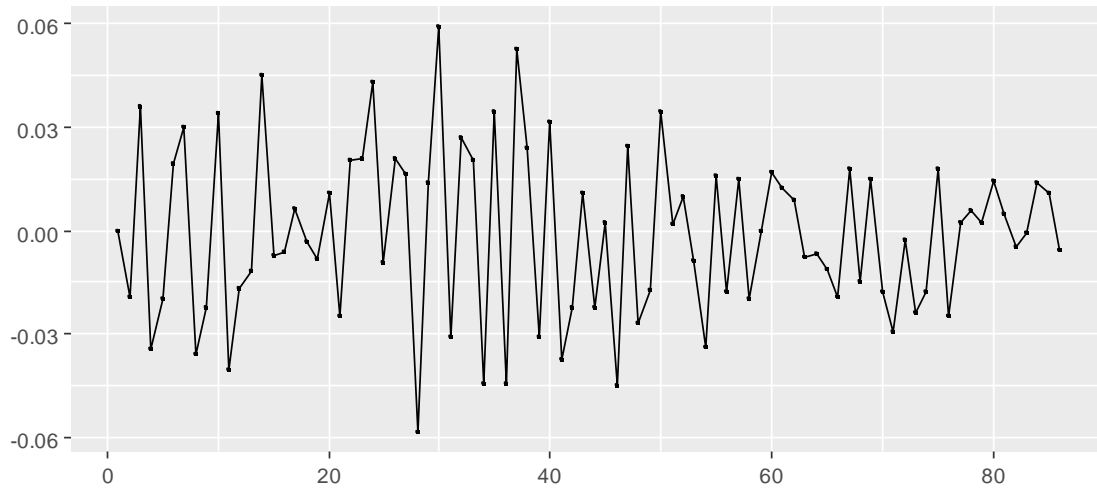
The ARIMA(0,1,1) proves to be the best fitting model with the following results:

| time_series | q_70_log |
|-----------------------------|-----------------|
| ARIMA | (0,1,1) |
| AICc | -400.18847 |
| BIC | -393.11811 |
| AR1 | 0.00000 |
| AR1_H0_inf | #N/A |
| AR1_H0_sup | #N/A |
| AR1_H0 | #N/A |
| AR2 | 0.00000 |
| AR2_H0_inf | #N/A |
| AR2_H0_sup | #N/A |
| AR2_H0 | #N/A |
| MA1 | -0.35757 |
| MA1_H0_inf | -0.62077 |
| MA1_H0_sup | -0.16846 |
| MA1_H0 | REJECTED |
| MA2 | 0.00000 |
| MA2_H0_inf | #N/A |
| MA2_H0_sup | #N/A |
| MA2_H0 | #N/A |
| drift | -0.01247 |
| drift_H0_inf | -0.01534 |
| drift_H0_sup | -0.00937 |
| drift_H0 | REJECTED |
| Normality_CVM_pvalue | 0.92672 |
| Normality_AD_pvalue | 0.91772 |
| Normality_JB_pvalue | 0.46602 |
| Incorrelation_LB | 0.15678 |
| Homocedasticity_BP_B | 0.41163 |
| Zero_mean | 0.99543 |

All the diagnosis has been properly tested so the AR parameter and the constant are significant, the residuals are normal, uncorrelated, constant in variance and have zero mean.

The residuals can be summarized in the following graph:

Residuals from ARIMA(0,1,1)



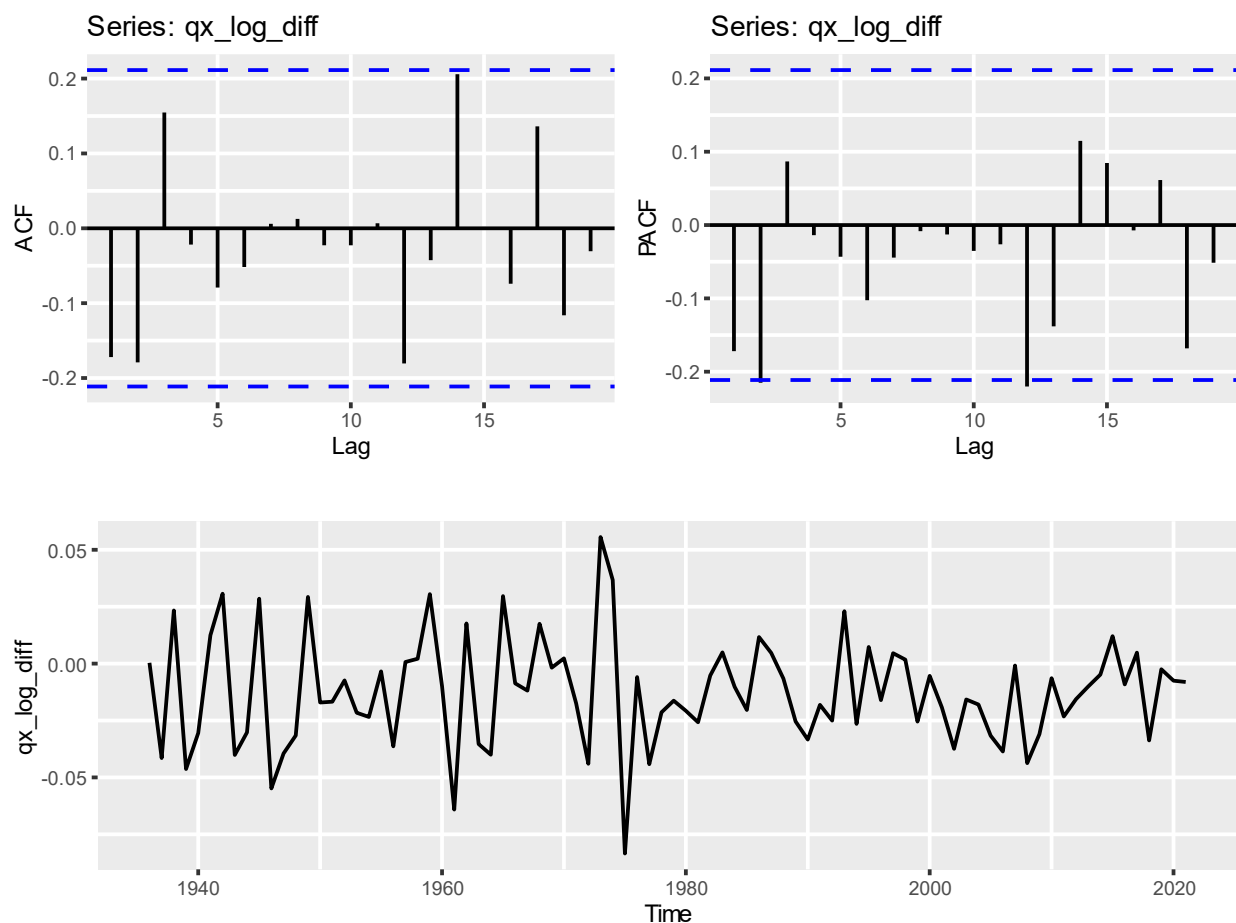
3.5. Mortality rate q_{71} ARIMA estimation

The following stationary test have been performed.

| I(0) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.46113 | FALSE |
| PP | 0.25084 | FALSE |
| KPSS | 0.01000 | FALSE |

| I(1) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.0100 | TRUE |
| PP | 0.0100 | TRUE |
| KPSS | 0.1000 | TRUE |

The differentiated time series visualization and its ACF and PACF are shown:



According to Box-Jenkins procedure, the time series appears to be an ARIMA of orders:

- (0,1,0)
- (1,0,1)
- (0,1,1)
- (1,1,1)

According to the ACF and PACF the most reliable form is (0,1,0). In any case all mentioned will be tested to confirm. All the results of the diagnosis for the time series up to an order (2,1,2) are summarized in the annex.

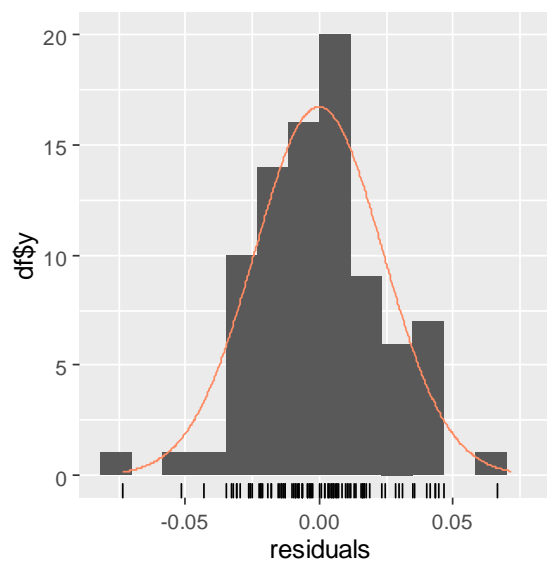
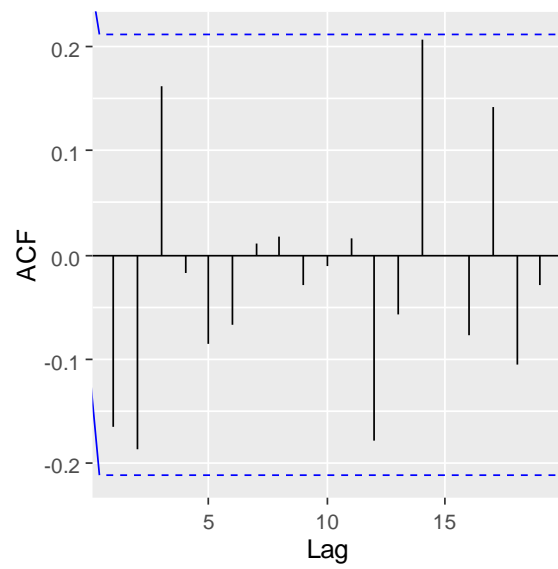
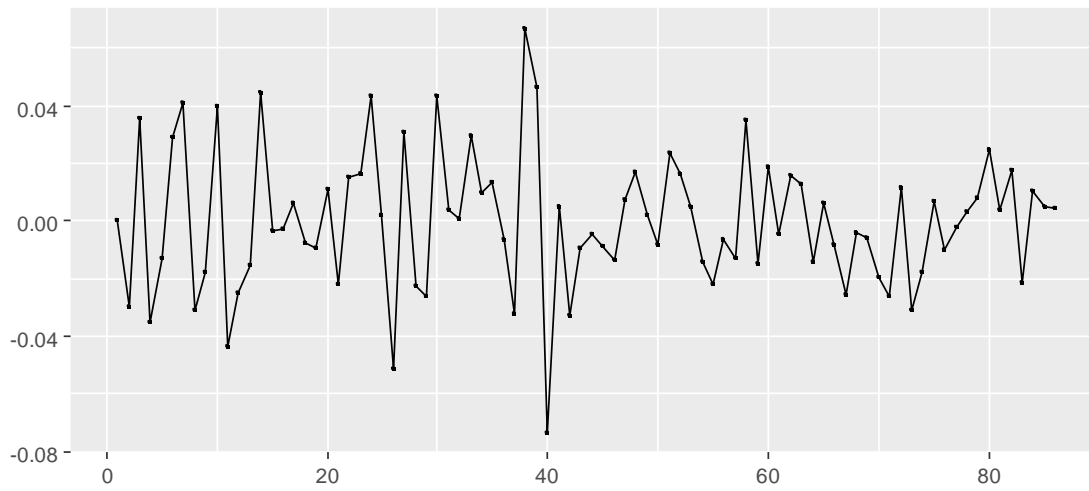
The ARIMA(0,1,1) proves to be the best fitting model with the following results:

| time_series | q_71_log |
|-----------------------------|-----------------|
| ARIMA | (0,1,1) |
| AICc | -396.24571 |
| BIC | -389.17535 |
| AR1 | 0.00000 |
| AR1_H0_inf | #N/A |
| AR1_H0_sup | #N/A |
| AR1_H0 | #N/A |
| AR2 | 0.00000 |
| AR2_H0_inf | #N/A |
| AR2_H0_sup | #N/A |
| AR2_H0 | #N/A |
| MA1 | -0.24286 |
| MA1_H0_inf | -0.52452 |
| MA1_H0_sup | -0.03119 |
| MA1_H0 | REJECTED |
| MA2 | 0.00000 |
| MA2_H0_inf | #N/A |
| MA2_H0_sup | #N/A |
| MA2_H0 | #N/A |
| drift | -0.01253 |
| drift_H0_inf | -0.01614 |
| drift_H0_sup | -0.00871 |
| drift_H0 | REJECTED |
| Normality_CVM_pvalue | 0.96312 |
| Normality_AD_pvalue | 0.95826 |
| Normality_JB_pvalue | 0.52026 |
| Incorrelation_LB | 0.89443 |
| Homocedasticity_BP_B | 0.86741 |
| Zero_mean | 0.99405 |

All the diagnosis has been properly tested so the AR parameter and the constant are significant, the residuals are normal, uncorrelated, constant in variance and have zero mean.

The residuals can be summarized in the following graph:

Residuals from ARIMA(0,1,1)



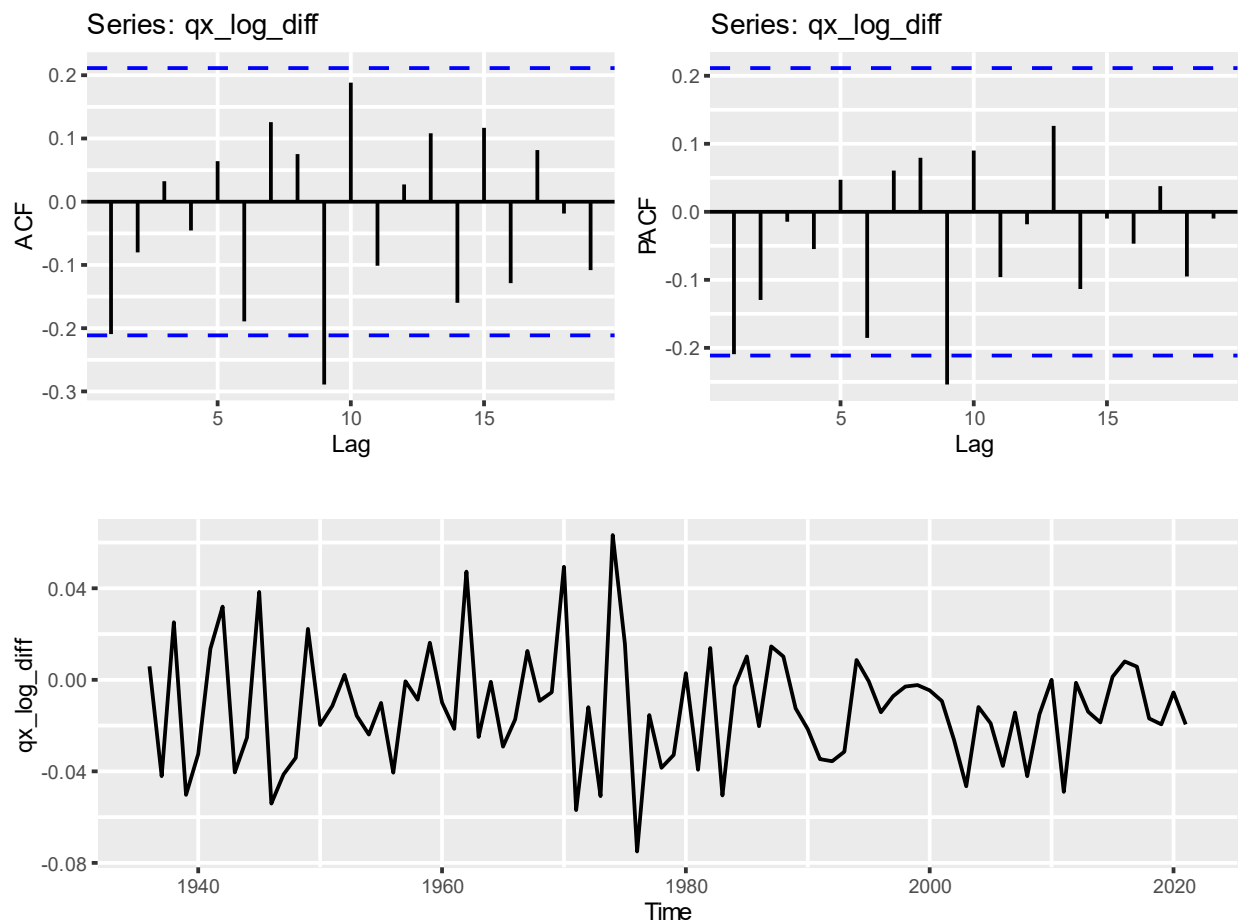
3.6. Mortality rate q_{72} ARIMA estimation

The following stationary test have been performed.

| I(0) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.65098 | FALSE |
| PP | 0.43575 | FALSE |
| KPSS | 0.01000 | FALSE |

| I(1) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.01000 | TRUE |
| PP | 0.01000 | TRUE |
| KPSS | 0.10000 | TRUE |

The differentiated time series visualization and its ACF and PACF are shown:



According to Box-Jenkins procedure, the time series appears to be an ARIMA of orders:

- (0,1,0)
- (1,0,1)
- (0,1,1)
- (1,1,1)

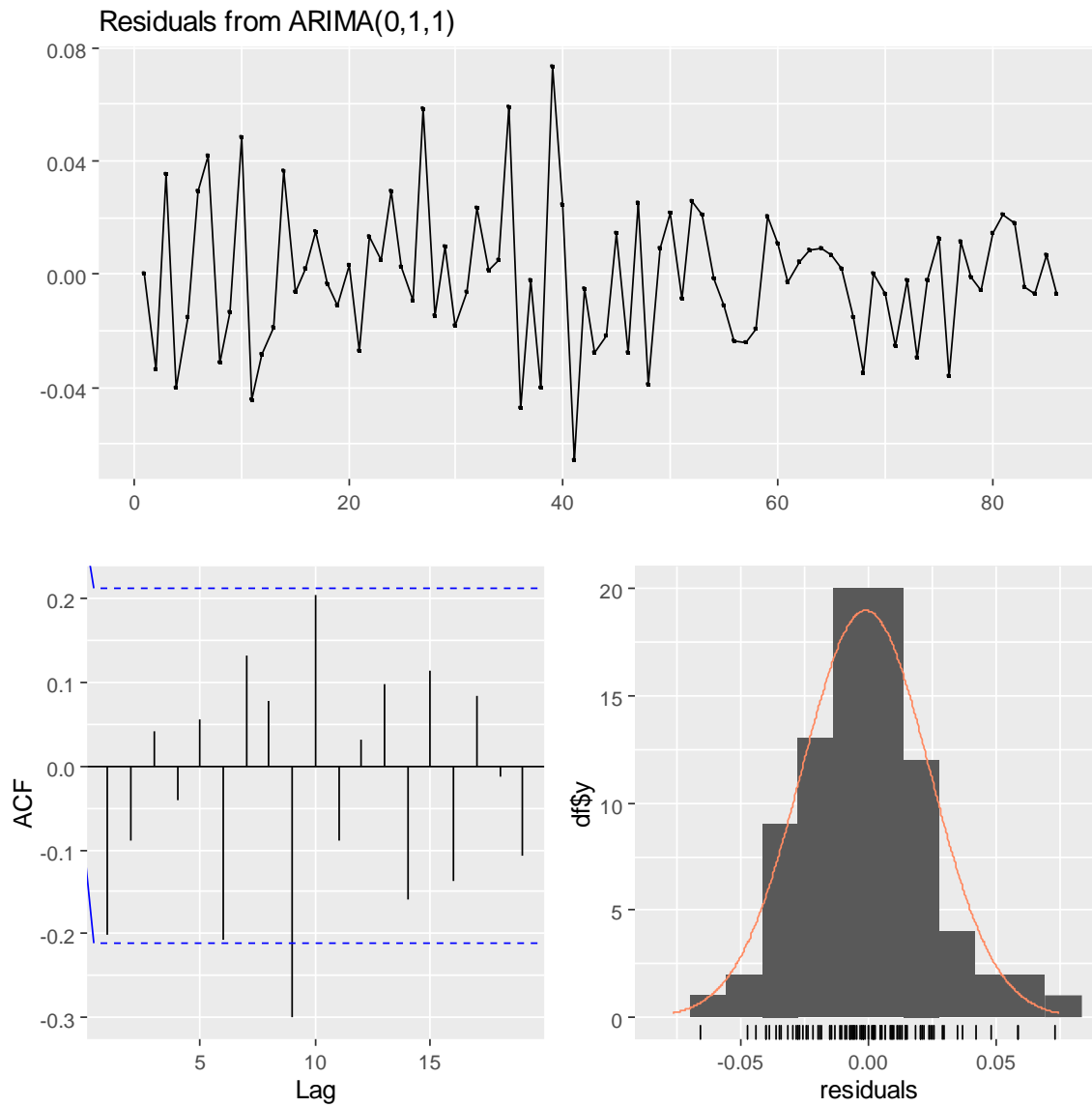
According to the ACF and PACF the most reliable form is (0,1,0). In any case all mentioned will be tested to confirm. All the results of the diagnosis for the time series up to an order (2,1,2) are summarized in the annex.

The ARIMA(0,1,1) proves to be the best fitting model with the following results:

| time_series | q_72_log |
|-----------------------------|-----------------|
| ARIMA | (0,1,1) |
| AICc | -388.78772 |
| BIC | -381.71737 |
| AR1 | 0.00000 |
| AR1_H0_inf | #N/A |
| AR1_H0_sup | #N/A |
| AR1_H0 | #N/A |
| AR2 | 0.00000 |
| AR2_H0_inf | #N/A |
| AR2_H0_sup | #N/A |
| AR2_H0 | #N/A |
| MA1 | -0.25911 |
| MA1_H0_inf | -0.49469 |
| MA1_H0_sup | -0.04240 |
| MA1_H0 | REJECTED |
| MA2 | 0.00000 |
| MA2_H0_inf | #N/A |
| MA2_H0_sup | #N/A |
| MA2_H0 | #N/A |
| drift | -0.01255 |
| drift_H0_inf | -0.01657 |
| drift_H0_sup | -0.00857 |
| drift_H0 | REJECTED |
| Normality_CVM_pvalue | 0.78017 |
| Normality_AD_pvalue | 0.65034 |
| Normality_JB_pvalue | 0.22729 |
| Incorrelation_LB | 0.31635 |
| Homocedasticity_BP_B | 0.07697 |
| Zero_mean | 0.99740 |

All the diagnosis has been properly tested so the AR parameter and the constant are significant, the residuals are normal, uncorrelated, constant in variance and have zero mean.

The residuals can be summarized in the following graph:



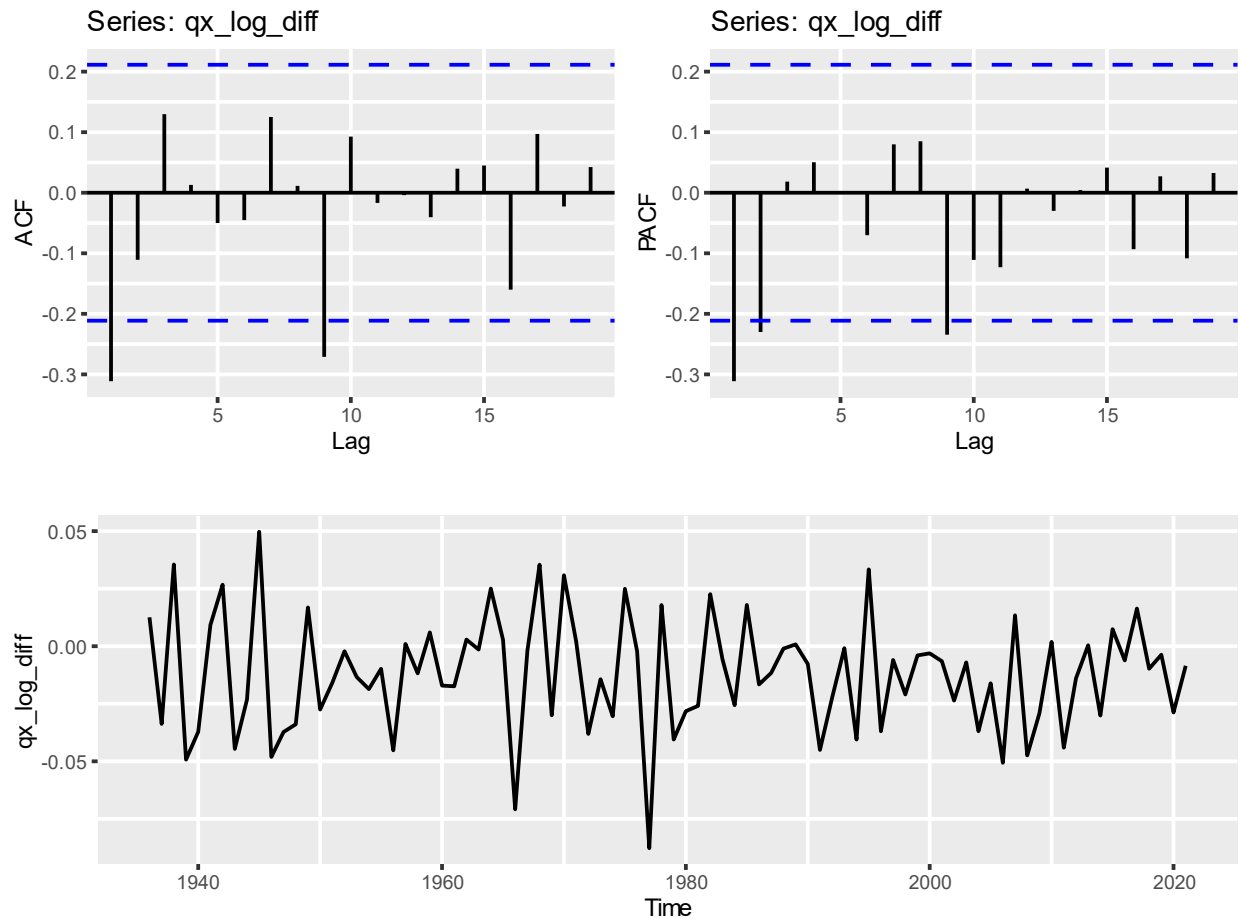
3.7. Mortality rate q_{73} ARIMA estimation

The following stationary test have been performed.

| I(0) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.58792 | FALSE |
| PP | 0.20170 | FALSE |
| KPSS | 0.01000 | FALSE |

| I(1) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.01000 | TRUE |
| PP | 0.01000 | TRUE |
| KPSS | 0.10000 | TRUE |

The differentiated time series visualization and its ACF and PACF are shown:



According to Box-Jenkins procedure, the time series appears to be an ARIMA of orders:

- (0,1,0)
- (1,0,1)
- (0,1,1)
- (1,1,1)
- (2,1,1)
- (2,1,0)
- (2,1,1)

According to the ACF and PACF the most reliable form is (0,1,0). In any case all mentioned will be tested to confirm. All the results of the diagnosis for the time series up to an order (2,1,2) are summarized in the annex.

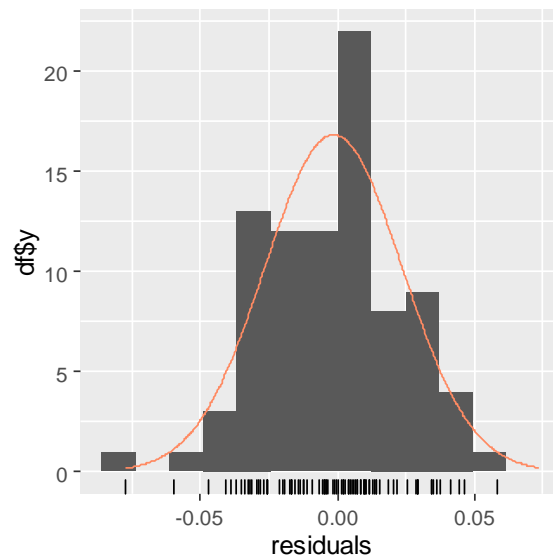
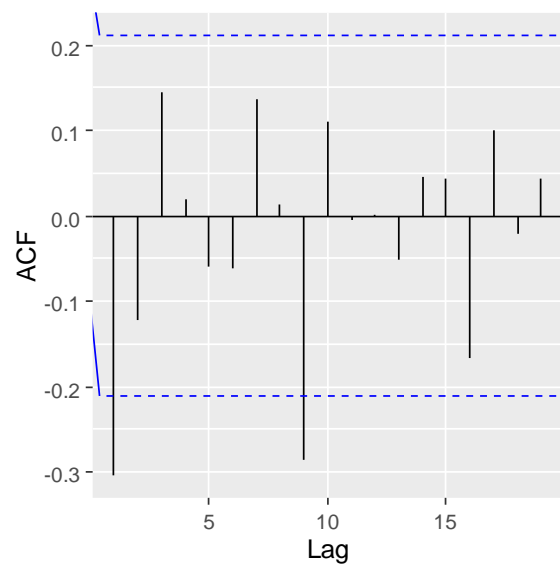
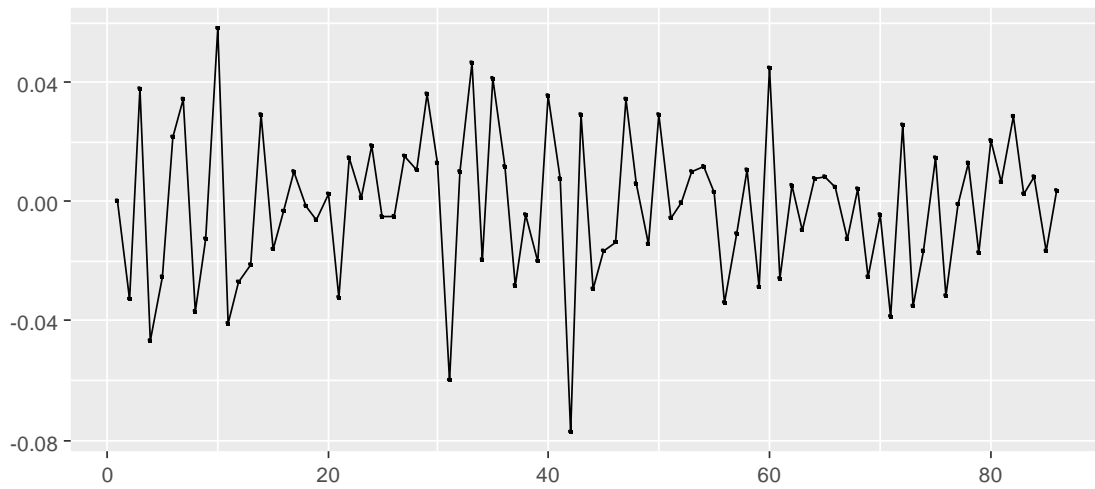
The ARIMA(0,1,1) proves to be the best fitting model with the following results:

| time_series | q_73_log |
|-----------------------------|-----------------|
| ARIMA | (0,1,1) |
| AICc | -396.23492 |
| BIC | -389.16456 |
| AR1 | 0.00000 |
| AR1_H0_inf | #N/A |
| AR1_H0_sup | #N/A |
| AR1_H0 | #N/A |
| AR2 | 0.00000 |
| AR2_H0_inf | #N/A |
| AR2_H0_sup | #N/A |
| AR2_H0 | #N/A |
| MA1 | -0.39198 |
| MA1_H0_inf | -0.63862 |
| MA1_H0_sup | -0.19727 |
| MA1_H0 | REJECTED |
| MA2 | 0.00000 |
| MA2_H0_inf | #N/A |
| MA2_H0_sup | #N/A |
| MA2_H0 | #N/A |
| drift | -0.01236 |
| drift_H0_inf | -0.01530 |
| drift_H0_sup | -0.00935 |
| drift_H0 | REJECTED |
| Normality_CVM_pvalue | 0.99178 |
| Normality_AD_pvalue | 0.98878 |
| Normality_JB_pvalue | 0.99511 |
| Incorrelation_LB | 0.28037 |
| Homocedasticity_BP_B | 0.33750 |
| Zero_mean | 0.97290 |

All the diagnosis has been properly tested so the AR parameter and the constant are significant, the residuals are normal, uncorrelated, constant in variance and have zero mean.

The residuals can be summarized in the following graph:

Residuals from ARIMA(0,1,1)



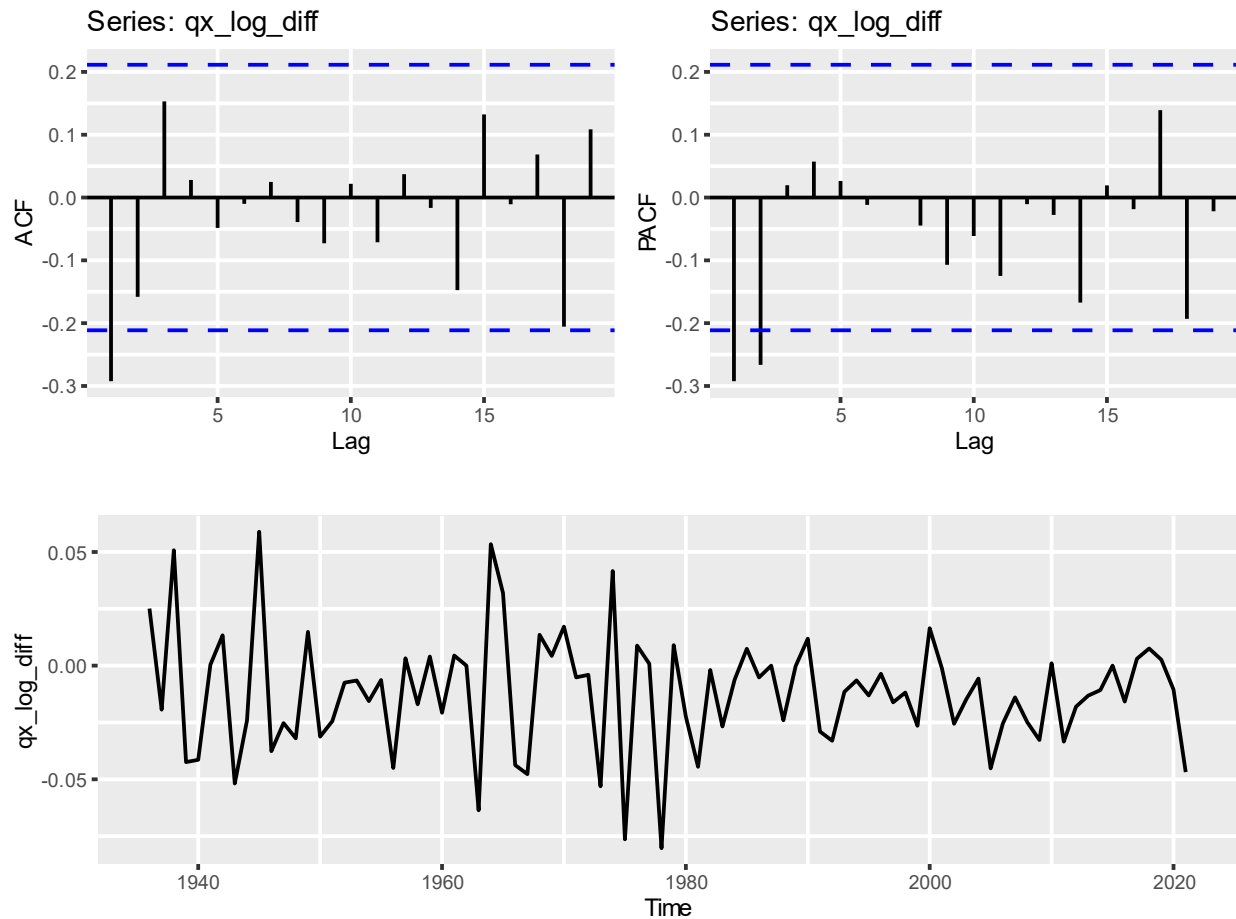
3.8. Mortality rate q_{74} ARIMA estimation

The following stationary test have been performed.

| I(0) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.50764 | FALSE |
| PP | 0.02272 | TRUE |
| KPSS | 0.01 | FALSE |

| I(1) | p.value | stationary 0.05 |
|------|---------|-----------------|
| ADF | 0.01731 | TRUE |
| PP | 0.01 | TRUE |
| KPSS | 0.1 | TRUE |

The differentiated time series visualization and its ACF and PACF are shown:



According to Box-Jenkins procedure, the time series appears to be an ARIMA of orders:

- (0,1,0)
- (1,0,1)
- (0,1,1)
- (1,1,1)
- (2,1,1)
- (2,1,0)
- (2,1,1)

According to the ACF and PACF the most reliable form is (0,1,0). In any case all mentioned will be tested to confirm. All the results of the diagnosis for the time series up to an order (2,1,2) are summarized in the annex.

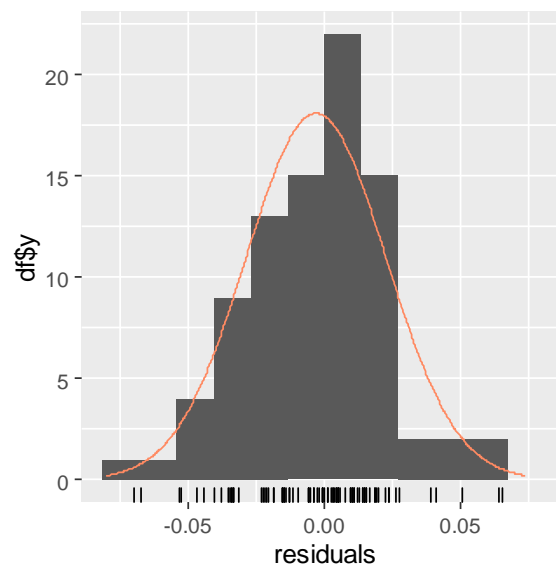
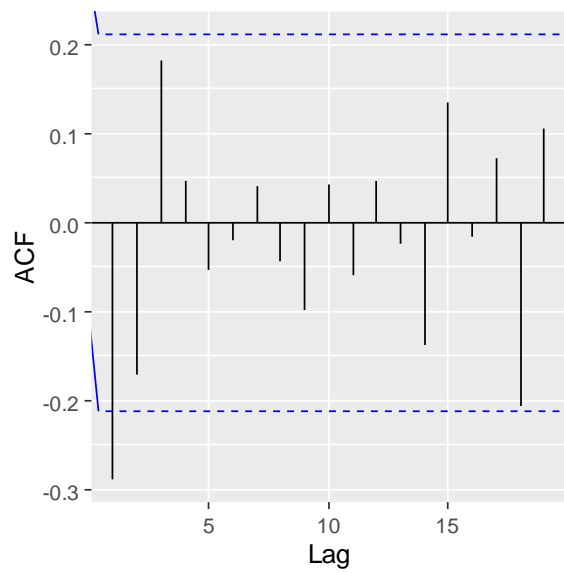
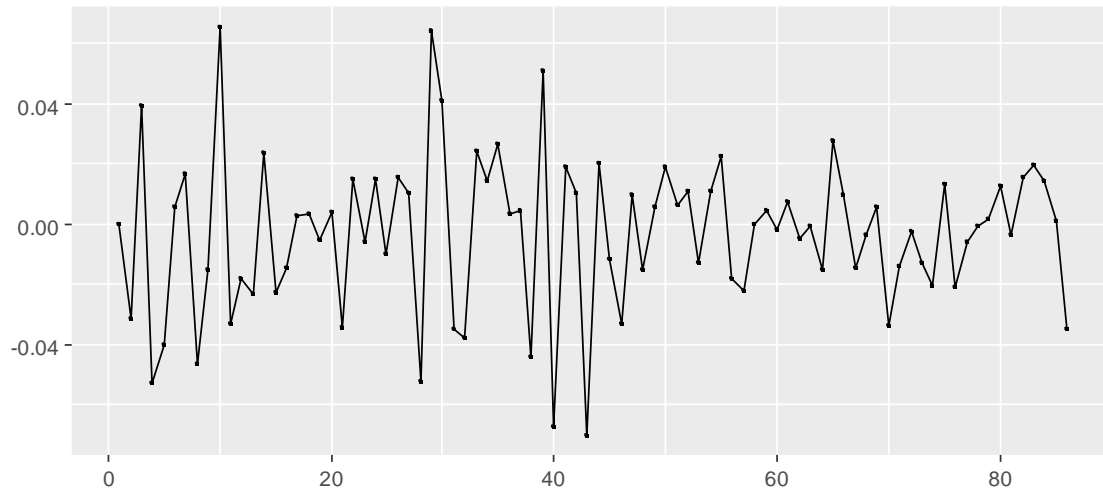
In this case both the ARIMA(0,1,1) and (2,1,0) prove to be a good fit and provide good results in the diagnosis. In any case, since all the other time series are clearly an ARIMA(0,1,1) and the process will probably be the same, the ARIMA(0,1,1) has been selected for modelling.

| time_series | q_74_log | q_74_log |
|-----------------------------|-----------------|-----------------|
| ARIMA | (0,1,1) | (2,1,0) |
| AICc | -391.65912 | -391.95475 |
| BIC | -384.58876 | -382.63119 |
| AR1 | 0.00000 | -0.38687 |
| AR1_H0_inf | #N/A | -0.58247 |
| AR1_H0_sup | #N/A | -0.18588 |
| AR1_H0 | #N/A | REJECTED |
| AR2 | 0.00000 | -0.27679 |
| AR2_H0_inf | #N/A | -0.48076 |
| AR2_H0_sup | #N/A | -0.08426 |
| AR2_H0 | #N/A | REJECTED |
| MA1 | -0.41636 | 0.00000 |
| MA1_H0_inf | -0.66639 | #N/A |
| MA1_H0_sup | -0.23485 | #N/A |
| MA1_H0 | REJECTED | #N/A |
| MA2 | 0.00000 | 0.00000 |
| MA2_H0_inf | #N/A | #N/A |
| MA2_H0_sup | #N/A | #N/A |
| MA2_H0 | #N/A | #N/A |
| drift | -0.01212 | -0.01206 |
| drift_H0_inf | -0.01504 | -0.01014 |
| drift_H0_sup | -0.00925 | -0.00405 |
| drift_H0 | REJECTED | REJECTED |
| Normality_CVM_pvalue | 0.65720 | 0.71482 |
| Normality_AD_pvalue | 0.72732 | 0.76951 |
| Normality_JB_pvalue | 0.32767 | 0.33890 |
| Incorrelation_LB | 0.79649 | 0.96575 |
| Homocedasticity_BP_B | 0.62931 | 0.35359 |
| Zero_mean | 0.92790 | 0.95073 |

All the diagnosis has been properly tested so the AR parameter and the constant are significant, the residuals are normal, uncorrelated, constant in variance and have zero mean.

The residuals can be summarized in the following graph:

Residuals from ARIMA(0,1,1)



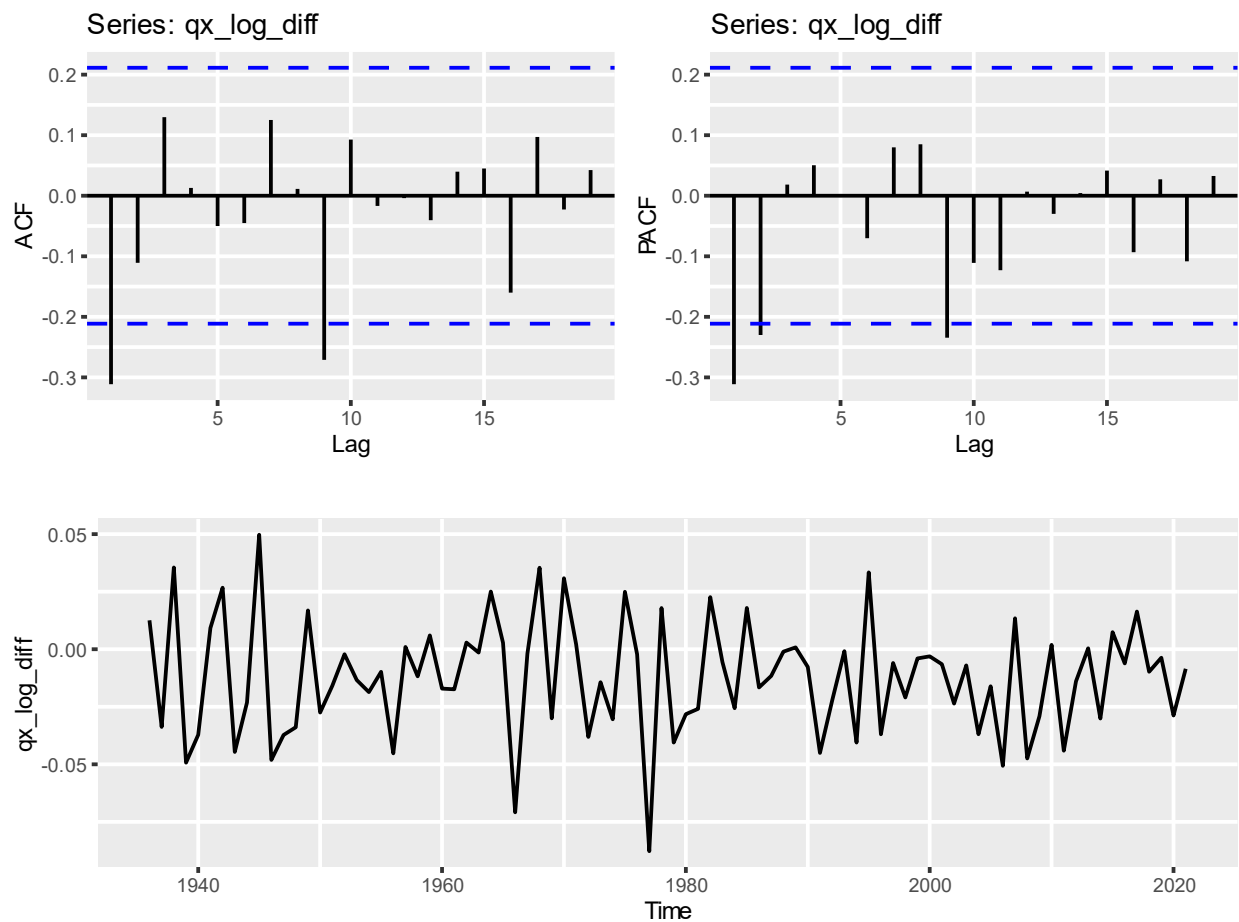
3.9. Mortality rate q_{75} ARIMA estimation

The following stationary test have been performed.

| I(0) | p.value | stationary 0.05 |
|------|------------|-----------------|
| ADF | 0.49425145 | FALSE |
| PP | 0.02324218 | TRUE |
| KPSS | 0.01 | FALSE |

| I(1) | p.value | stationary 0.05 |
|------|------------|-----------------|
| ADF | 0.02318762 | TRUE |
| PP | 0.01 | TRUE |
| KPSS | 0.1 | TRUE |

The differentiated time series visualization and its ACF and PACF are shown:



According to Box-Jenkins procedure, the time series appears to be an ARIMA of orders:

- (0,1,0)
- (1,0,1)
- (0,1,1)
- (1,1,1)
- (2,1,1)
- (2,1,0)
- (2,1,1)

According to the ACF and PACF the most reliable form is (0,1,0). In any case all mentioned will be tested to confirm. All the results of the diagnosis for the time series up to an order (2,1,2) are summarized in the annex.

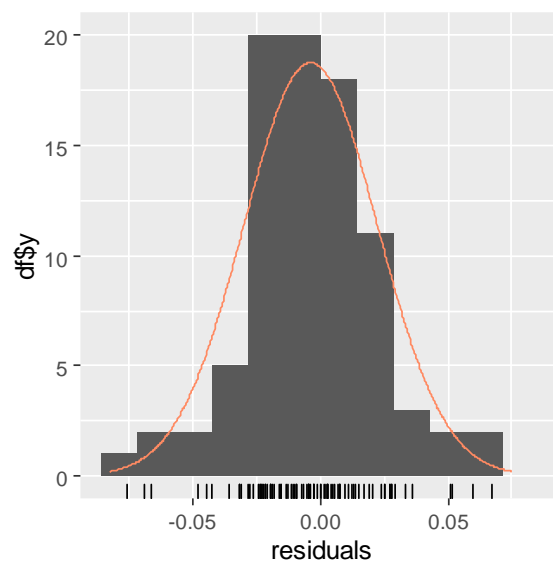
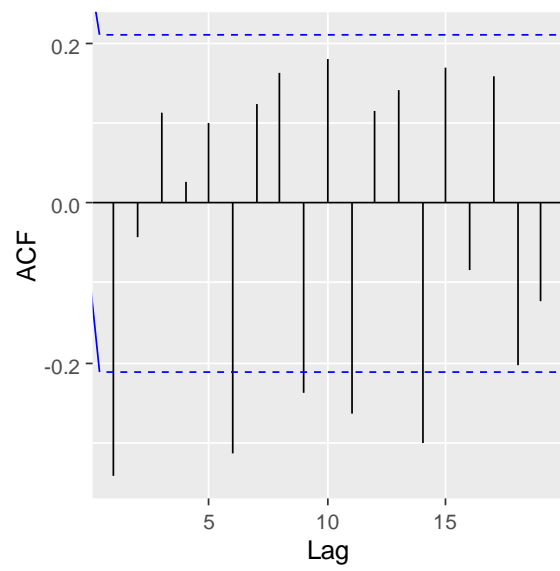
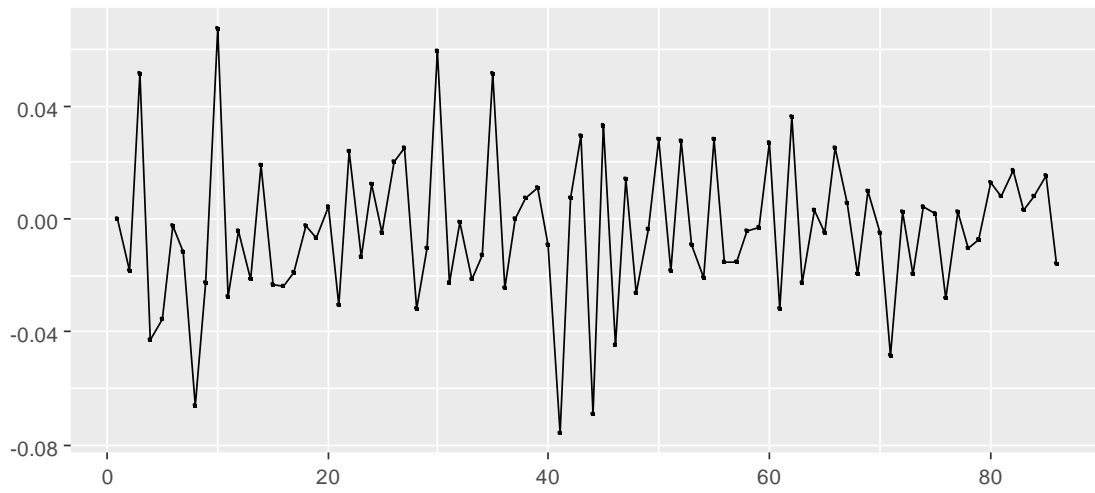
The ARIMA(0,1,1) proves to be the best fitting model with the following results:

| time_series | q_73_log |
|-----------------------------|-----------------|
| ARIMA | (0,1,1) |
| AICc | -396.23492 |
| BIC | -389.16456 |
| AR1 | 0.00000 |
| AR1_H0_inf | #N/A |
| AR1_H0_sup | #N/A |
| AR1_H0 | #N/A |
| AR2 | 0.00000 |
| AR2_H0_inf | #N/A |
| AR2_H0_sup | #N/A |
| AR2_H0 | #N/A |
| MA1 | -0.39198 |
| MA1_H0_inf | -0.63862 |
| MA1_H0_sup | -0.19727 |
| MA1_H0 | REJECTED |
| MA2 | 0.00000 |
| MA2_H0_inf | #N/A |
| MA2_H0_sup | #N/A |
| MA2_H0 | #N/A |
| drift | -0.01236 |
| drift_H0_inf | -0.01530 |
| drift_H0_sup | -0.00935 |
| drift_H0 | REJECTED |
| Normality_CVM_pvalue | 0.99178 |
| Normality_AD_pvalue | 0.98878 |
| Normality_JB_pvalue | 0.99511 |
| Incorrelation_LB | 0.28037 |
| Homocedasticity_BP_B | 0.33750 |
| Zero_mean | 0.97290 |

All the diagnosis has been properly tested so the AR parameter and the constant are significant, the residuals are normal, uncorrelated, constant in variance and have zero mean.

The residuals can be summarized in the following graph:

Residuals from ARIMA(0,1,1)

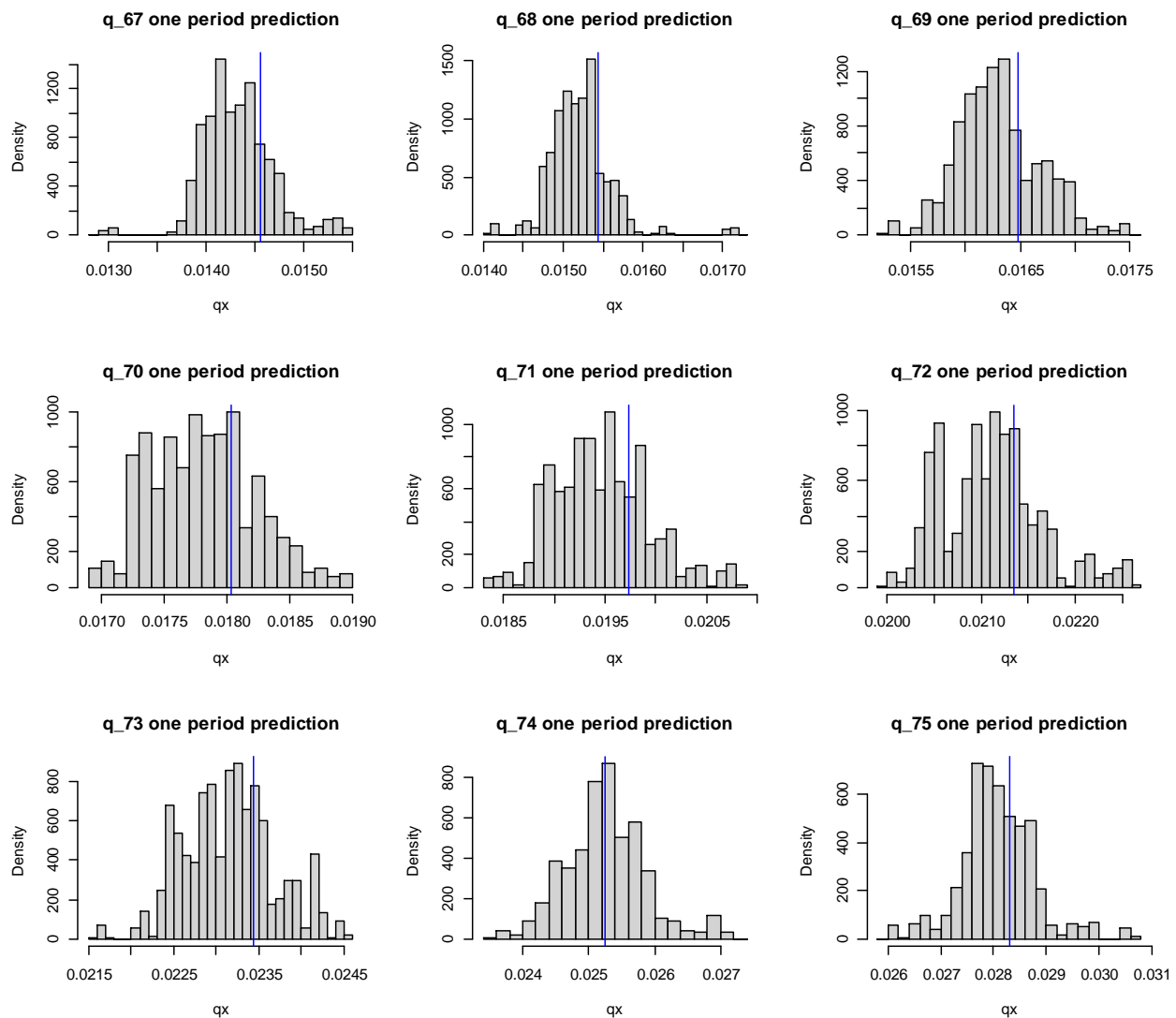


4. Next period qx prediction by bootstrap

Even if all the diagnosis checks are correct and the null hypothesis of the residuals to be white noise cannot be rejected, bootstrap will be used for the estimation instead of the gaussian method since it is more versatile and considers the uncertainties of the ARIMA parameters estimation as well as model specification uncertainty.

The bootstrap prediction algorithm is coded in lines 409 to 449.

The results of the estimation distribution and the 2021 value (marked with the vertical line in blue) are shown in the following graph:



5. Mortality prediction, cost and economic capital summary

The predictions shown in the previous part are used for the computation of the cost and the economic capital required to cover that cost. The calculation is coded in lines 480 to 538.

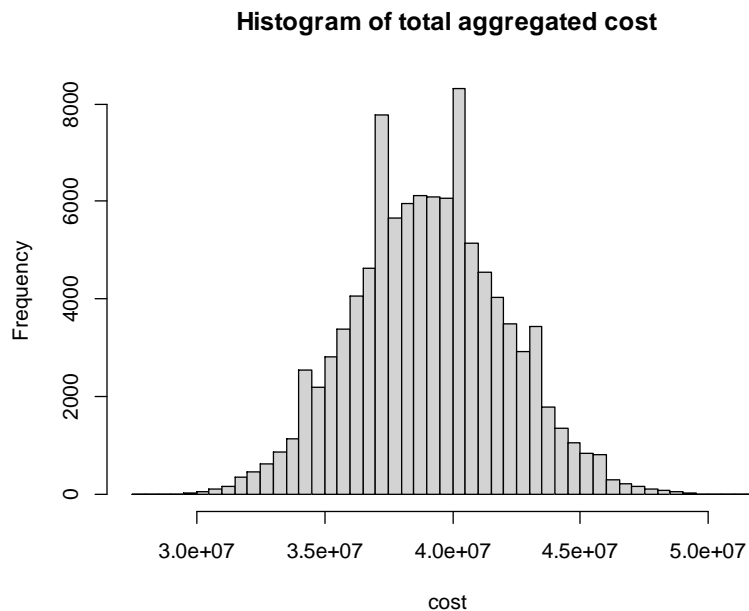
The following table summarizes all the data predicted. The expected q_x and the marginal standard deviation as well as the VaR_{99} and $TVaR_{99}$ for the cost by age groups.

| Age | q_x _current | q_x _expected | q_x _expected_sd | q_x _VaR99 | q_x _TVaR99 | n_policies | cost_expected | cost_sd | cost_VaR99 | cost_TVaR99 | economic_capital |
|-----|----------------|-----------------|--------------------|--------------|---------------|------------|---------------|-----------|------------|-------------|------------------|
| 67 | 0.01455 | 0.01433 | 0.00036 | 0.01536 | 0.01542 | 902 | 2,972,509 | 825,705 | 5,060,000 | 5,512,539 | 2,087,492 |
| 68 | 0.01543 | 0.01521 | 0.00038 | 0.01704 | 0.01711 | 659 | 2,306,376 | 723,342 | 4,140,000 | 4,557,033 | 1,833,624 |
| 69 | 0.01648 | 0.01631 | 0.00038 | 0.01739 | 0.01744 | 1471 | 5,518,827 | 1,122,437 | 8,280,000 | 8,842,602 | 2,761,173 |
| 70 | 0.01803 | 0.01781 | 0.00041 | 0.01888 | 0.01892 | 978 | 4,010,229 | 951,867 | 6,440,000 | 6,963,739 | 2,429,771 |
| 71 | 0.01974 | 0.01946 | 0.00046 | 0.02073 | 0.02077 | 675 | 3,025,271 | 827,874 | 5,060,000 | 5,539,776 | 2,034,730 |
| 72 | 0.02134 | 0.02111 | 0.00052 | 0.02253 | 0.02256 | 850 | 4,128,424 | 968,228 | 6,440,000 | 6,962,181 | 2,311,576 |
| 73 | 0.02343 | 0.02315 | 0.00053 | 0.02443 | 0.02448 | 882 | 4,697,543 | 1,036,329 | 7,360,000 | 7,874,576 | 2,662,457 |
| 74 | 0.02524 | 0.02526 | 0.00061 | 0.02697 | 0.02704 | 1035 | 6,016,671 | 1,165,096 | 8,970,000 | 9,535,517 | 2,953,329 |
| 75 | 0.02831 | 0.02809 | 0.00070 | 0.03048 | 0.03057 | 995 | 6,416,471 | 1,207,581 | 9,430,000 | 9,996,869 | 3,013,529 |

Additionally, the following summary table is provided with the aggregated model considering all the policies globally and running all together.

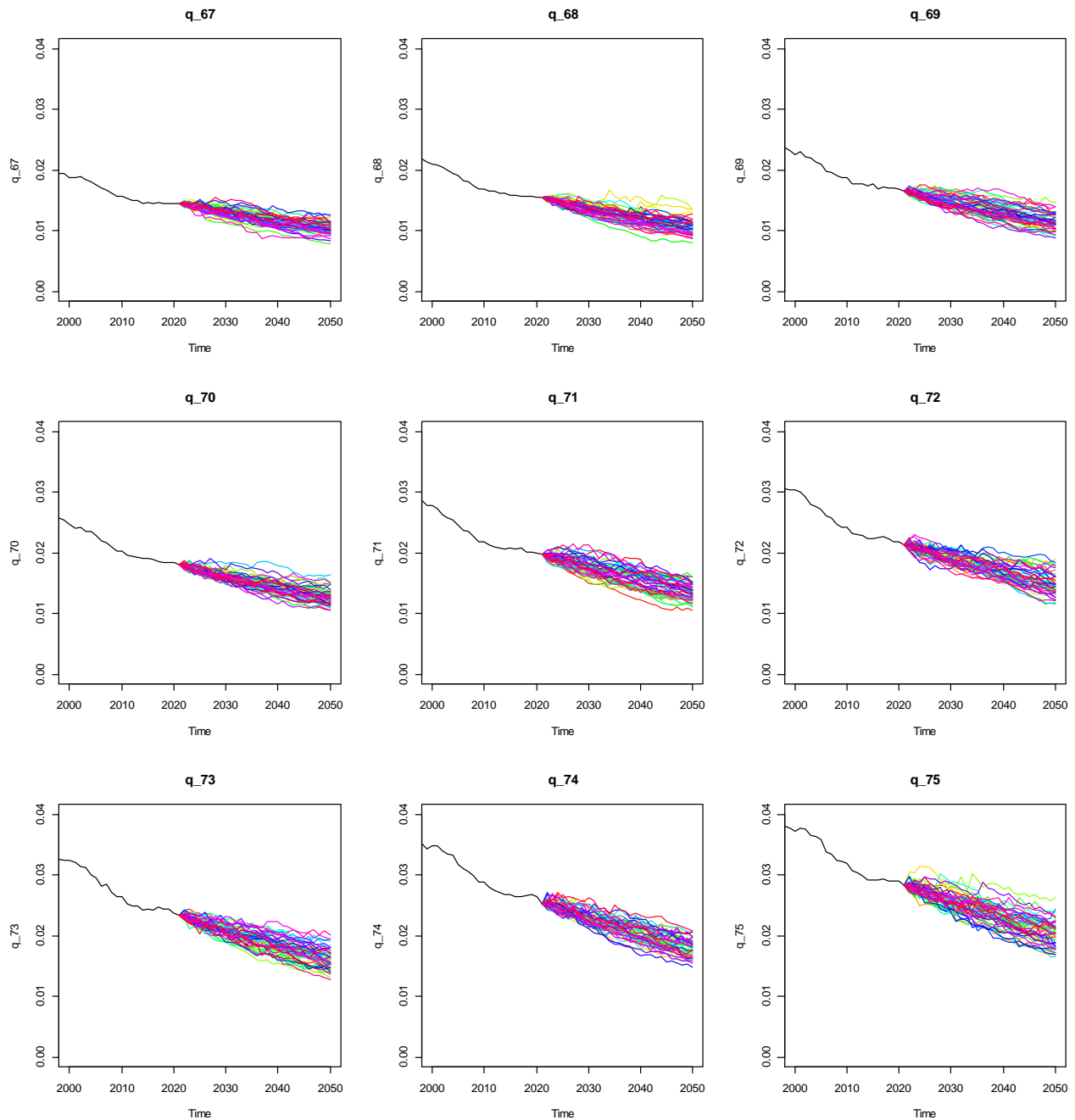
| cost_total_expected | cost_total_sd | cost_total_VaR99 | cost_total_TVaR99 | total_economic_capital |
|---------------------|---------------|------------------|-------------------|------------------------|
| 39,091,145 | 2,980,131 | 46,230,000 | 47,374,907 | 7,138,855 |

The total cost distribution is as follows:



6. Further periods mortality rates prediction

Additionally, further mortality rates estimation predictions are provided for a time horizon greater than one period up to year 2050. The following graphs show these predictions for the ages previously studied with the estimated models. The prediction is performed by the same bootstrap technique used for the one period prediction.



7. Annex – Diagnosis Results

[See online](#)

| time_series | ARIMA | AICc | BIC | AR1 | AR1_H0_inf | AR1_H0_sup | AR1_H0 | AR2 | AR2_H0_inf | AR2_H0_sup | AR2_H0 | MA1 | MA1_H0_inf | MA1_H0_sup | MA1_H0 | MA2 | MA2_H0_inf | MA2_H0_sup | MA2_H0 | drift | drift_H0_inf | drift_H0_sup | drift_H0 | Normality_CVM_pvalue | Normality_AD_pvalue | Normality_JB_pvalue | Uncorrelation_LB | Homocedasticity_BP_B | Zero_mean |
|-------------|---------|---------|---------|----------|------------|------------|--------------|----------|------------|------------|--------------|----------|------------|------------|--------------|----------|------------|------------|--------------|----------|--------------|--------------|----------|----------------------|---------------------|---------------------|------------------|----------------------|-----------|
| q_67_log | (0,1,0) | -380.58 | -375.81 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01139 | -0.01709 | -0.00606 | REJECTED | 0.49746 | 0.44161 | 0.00000 | 0.02391 | 0.00008 | 0.98931 |
| q_67_log | (1,1,0) | -381.09 | -374.02 | -0.17491 | -0.38539 | 0.02675 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01146 | -0.01425 | -0.00480 | REJECTED | 0.56088 | 0.45484 | 0.00002 | 0.20978 | 0.98938 | 0.99584 |
| q_67_log | (0,1,1) | -381.45 | -374.38 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.20214 | -0.47090 | -0.00162 | REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01151 | -0.01593 | -0.00749 | REJECTED | 0.57427 | 0.46396 | 0.00015 | 0.26379 | 0.99784 | 0.98219 |
| q_67_log | (1,1,1) | -379.50 | -370.18 | 0.23707 | -0.86543 | 0.86011 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.43354 | -1.00000 | 0.83752 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01161 | -0.01916 | -0.01095 | REJECTED | 0.62170 | 0.50616 | 0.00057 | 0.25722 | 0.99721 | 0.95597 |
| q_67_log | (0,1,2) | -379.47 | -370.14 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.19789 | -0.45100 | -0.00224 | REJECTED | -0.04904 | -0.29601 | 0.18458 | NOT REJECTED | -0.01159 | -0.01540 | -0.00733 | REJECTED | 0.61445 | 0.49997 | 0.00066 | 0.26129 | 0.99832 | 0.96287 |
| q_67_log | (1,1,2) | -378.82 | -367.30 | 0.92207 | -0.96271 | 0.89593 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -1.15596 | -1.22835 | 0.82904 | NOT REJECTED | 0.15597 | -0.36341 | 0.31213 | NOT REJECTED | -0.01201 | -0.15535 | -0.15183 | REJECTED | 0.46164 | 0.32291 | 0.00039 | 0.23130 | 0.99949 | 0.58081 |
| q_67_log | (2,1,0) | -379.21 | -369.89 | -0.18737 | -0.40526 | 0.02203 | NOT REJECTED | -0.06253 | -0.29464 | 0.13444 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01151 | -0.01357 | -0.00477 | REJECTED | 0.57239 | 0.46474 | 0.00028 | 0.24738 | 0.99919 | 0.98336 |
| q_67_log | (2,1,1) | -377.25 | -365.73 | 0.20575 | -1.16821 | 0.81369 | NOT REJECTED | -0.01187 | -0.34578 | 0.23821 | NOT REJECTED | -0.40130 | -1.00000 | 0.98959 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01161 | -0.01831 | -0.01048 | REJECTED | 0.62345 | 0.50790 | 0.00067 | 0.25476 | 0.99689 | 0.95650 |
| q_67_log | (2,1,2) | -381.24 | -367.58 | 1.18585 | -1.12126 | 1.22744 | NOT REJECTED | -0.78431 | -0.98270 | 0.69630 | NOT REJECTED | -1.45530 | -1.56451 | 1.00390 | NOT REJECTED | 0.99998 | -0.84957 | 1.00000 | NOT REJECTED | -0.01121 | -0.02341 | -0.01443 | REJECTED | 0.65442 | 0.55780 | 0.00358 | 0.22353 | 0.98783 | 0.99614 |
| q_68_log | (0,1,0) | -384.29 | -379.52 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01179 | -0.01719 | -0.00655 | REJECTED | 0.33446 | 0.26487 | 0.00000 | 0.34223 | 0.98939 | 0.98939 |
| q_68_log | (1,1,0) | -383.64 | -376.57 | -0.13142 | -0.32630 | 0.07750 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01183 | -0.01500 | -0.00580 | REJECTED | 0.40394 | 0.32407 | 0.00000 | 0.43434 | 0.78753 | 0.99883 |
| q_68_log | (0,1,1) | -384.38 | -377.31 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.19205 | -0.43452 | -0.00261 | REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01188 | -0.01601 | -0.00751 | REJECTED | 0.43926 | 0.36454 | 0.00000 | 0.49218 | 0.58348 | 0.98894 |
| q_68_log | (1,1,1) | -382.94 | -373.62 | 0.32092 | -0.86053 | 0.86942 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.50283 | -1.00000 | 0.87481 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01198 | -0.02129 | -0.01343 | REJECTED | 0.44613 | 0.36896 | 0.00000 | 0.56345 | 0.70464 | 0.95895 |
| q_68_log | (0,1,2) | -383.97 | -374.64 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.13732 | -0.38623 | 0.06931 | NOT REJECTED | -0.14985 | -0.40776 | 0.08958 | NOT REJECTED | -0.01200 | -0.01546 | -0.00810 | REJECTED | 0.39323 | 0.32978 | 0.00000 | 0.64148 | 0.81132 | 0.95061 |
| q_68_log | (1,1,2) | -382.22 | -370.70 | -0.34150 | -0.90062 | 0.87554 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | 0.19599 | -1.12366 | 0.77966 | NOT REJECTED | -0.20653 | -0.46335 | 0.21037 | NOT REJECTED | -0.01195 | -0.01245 | -0.00484 | REJECTED | 0.36841 | 0.32356 | 0.00000 | 0.67643 | 0.65711 | 0.96668 |
| q_68_log | (2,1,0) | -384.60 | -375.27 | -0.15890 | -0.37854 | 0.05762 | NOT REJECTED | -0.19024 | -0.39378 | -0.01334 | REJECTED | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01193 | -0.01260 | -0.00502 | REJECTED | 0.35090 | 0.30757 | 0.00000 | 0.66515 | 0.77401 | 0.97325 |
| q_68_log | (2,1,1) | -382.46 | -370.94 | -0.36145 | -1.07685 | 0.80275 | NOT REJECTED | -0.21514 | -0.42342 | 0.11400 | NOT REJECTED | 0.21207 | -1.00000 | 0.97369 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01189 | -0.01164 | -0.00324 | REJECTED | 0.32504 | 0.29345 | 0.00000 | 0.67675 | 0.70605 | 0.98613 |
| q_68_log | (2,1,2) | -387.96 | -374.30 | 1.13145 | -1.24063 | 1.20754 | NOT REJECTED | -0.70200 | -0.98253 | 0.61030 | NOT REJECTED | -1.45150 | -1.55342 | 1.10912 | NOT REJECTED | 1.00000 | -0.78173 | 1.00000 | NOT REJECTED | -0.01146 | -0.02497 | -0.01545 | REJECTED | 0.42159 | 0.38601 | 0.00000 | 0.86840 | 0.88659 | 0.93557 |
| q_69_log | (0,1,0) | -396.32 | -391.56 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01223 | -0.01706 | -0.00654 | REJECTED | 0.75219 | 0.81030 | 0.51871 | 0.03674 | 0.98900 | 0.98900 |
| q_69_log | (1,1,0) | -397.63 | -390.56 | -0.19804 | -0.39990 | 0.01290 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01224 | -0.01434 | -0.00617 | REJECTED | 0.74609 | 0.85382 | 0.58847 | 0.21492 | 0.11356 | 0.99947 |
| q_69_log | (0,1,1) | -398.27 | -391.20 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.23209 | -0.49352 | -0.01913 | REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01226 | -0.01577 | -0.00824 | REJECTED | 0.76858 | 0.87554 | 0.57133 | 0.31720 | 0.12939 | 0.99118 |
| q_69_log | (1,1,1) | -396.20 | -386.88 | 0.13897 | -0.86266 | 0.86611 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.36184 | -1.00000 | 0.79766 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01228 | -0.01773 | -0.01059 | REJECTED | 0.76416 | 0.86531 | 0.56436 | 0.35443 | 0.30118 | 0.98258 |
| q_69_log | (0,1,2) | -396.25 | -386.92 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.21893 | -0.47639 | -0.01804 | REJECTED | -0.04390 | -0.31492 | 0.18672 | NOT REJECTED | -0.01228 | -0.01595 | -0.00858 | REJECTED | 0.75592 | 0.85690 | 0.55302 | 0.37578 | 0.36813 | 0.98290 |
| q_69_log | (1,1,2) | -396.02 | -384.50 | 0.91438 | -0.95237 | 0.89053 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -1.18253 | -1.22210 | 0.81244 | NOT REJECTED | 0.18253 | -0.42279 | 0.28279 | NOT REJECTED | -0.01228 | -0.14454 | -0.14161 | REJECTED | 0.69803 | 0.71426 | 0.23275 | 0.38096 | 0.69086 | 0.69326 |
| q_69_log | (2,1,0) | -396.32 | -386.99 | -0.21869 | -0.00836 | -0.44054 | REJECTED | -0.10051 | -0.33284 | 0.08359 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01226 | -0.01279 | -0.00539 | REJECTED | 0.73978 | 0.84634 | 0.50735 | 0.42580 | 0.44133 | 0.99247 |
| q_69_log | (2,1,1) | -394.10 | -382.57 | -0.10031 | -1.16126 | 0.79930 | NOT REJECTED | -0.07845 | -0.37396 | 0.23155 | NOT REJECTED | -0.12025 | -1.00000 | 0.99998 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01226 | -0.01390 | -0.00662 | REJECTED | 0.74525 | 0.84935 | 0.51885 | 0.42191 | 0.34922 | 0.98894 |
| q_69_log | (2,1,2) | -393.81 | -380.15 | 1.26298 | -1.57724 | 1.36652 | NOT REJECTED | -0.85322 | -0.99451 | 0.78782 | NOT REJECTED | -1.42888 | -1.54824 | 1.62243 | NOT REJECTED | 0.99999 | -0.92915 | 1.00000 | NOT REJECTED | -0.01224 | -0.02489 | -0.01619 | REJECTED | 0.76546 | 0.83393 | 0.50544 | 0.37986 | 0.45862 | 0.99374 |
| q_70_log | (0,1,0) | -390.88 | -386.11 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01243 | -0.01750 | -0.00745 | REJECTED | 0.86210 | 0.93434 | 0.61160 | 0.00007 | 0.00060 | 0.98972 |
| q_70_log | (1,1,0) | -399.03 | -391.96 | -0.34445 | -0.52623 | -0.12959 | REJECTED | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01245 | -0.01290 | -0.00566 | REJECTED | 0.93385 | 0.96271 | 0.51841 | 0.10938 | 0.58374 | 0.99908 |
| q_70_log | (0,1,1) | -400.19 | -393.12 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.35757 | -0.62077 | -0.16846 | REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01247 | -0.01534 | -0.00937 | REJECTED | 0.92672 | 0.91772 | 0.46602 | 0.15678 | 0.41163 | 0.99543 |
| q_70_log | (1,1,1) | -398.17 | -388.85 | -0.10864 | -0.67669 | 0.69004 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.26838 | -1.00000 | 0.41490 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01247 | -0.01434 | -0.00799 | REJECTED | 0.96391 | 0.95743 | 0.49018 | 0.19198 | 0.45469 | 0.99684 |
| q_70_log | (0,1,2) | -398.34 | -389.02 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.38914 | -0.65865 | -0.18165 | REJECTED | 0.07527 | -0.18498 | 0.30244 | NOT REJECTED | -0.01245 | -0.01566 | -0.00903 | REJECTED | 0.97348 | 0.97444 | 0.51629 | 0.21388 | 0.46343 | 0.99956 |
| q_70_log | (1,1,2) | -396.19 | -384.66 | 0.21134 | -0.97790 | 0.90993 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.59636 | -1.35680 | 0.66377 | NOT REJECTED | 0.15084 | -0.45869 | 0.47895 | NOT REJECTED | -0.01244 | -0.01926 | -0.01233 | REJECTED | 0.96896 | 0.97222 | 0.53932 | 0.20636 | 0.55265 | 0.99865 |
| q_70_log | (2,1,0) | -399.34 | -390.02 | -0.39128 | -0.60866 | -0.18186 | REJECTED | -0.16842 | -0.38109 | 0.01688 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01245 | -0.01111 | -0.00476 | REJECTED | 0.96117 | 0.95321 | 0.49859 | 0.23993 | 0.43609 | 0.99828 |
| q_70_log | (2,1,1) | -400.88 | -389.36 | -1.01820 | -1.31623 | 0.57721 | NOT REJECTED | -0.41132 | -0.59933 | 0.24723 | NOT REJECTED | 0.66403 | -1.00000 | 0.99999 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | -0.01242 | -0.00828 | -0.00192 | REJECTED | 0.86613 | 0.82317 | 0.33700 | 0.95989 | 0.89304 | 0.98420 |
| q_70_log | (2,1,2) | -399.21 | -385.55 | -1.18658 | -1.53325 | 0.78300 | NOT REJECTED | -0.59176 | -0.96654 | 0.37536 | NOT REJECTED | 0.87701 | -1.22278 | 1.45464 | NOT REJECTED | 0.21506 | -0.69170 | 0.99999 | NOT REJECTED | -0.01240 | -0.00771 | -0.00093 | REJECTED | 0.80190 | 0.69599 | 0.15062 | 0.55588 | 0.90078 | 0.98022 |
| q_71_log | (0,1,0) | -394.56 | -389.79 | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01249 | -0.01750 | -0.00734 | REJECTED | 0.91293 | 0.91236 | 0.60818 | 0.59977 | 0.00001 | 0.98984 |
| q_71_log | (1,1,0) | -394.97 | -387.90 | -0.17067 | -0.37347 | 0.04595 | NOT REJECTED | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | 0.00000 | #N/A | #N/A | #N/A | -0.01252 | -0.01478 | -0.00653 | REJECTED | 0.94389 | 0.94104 | 0.60701 | 0.77591 | 0.82362 | 0.99698 |
| q_71_log | (0,1,1) | -396.25 | -389.18 | 0.00000 | #N/A | #N/A | #N/A | | | | | | | | | | | | | | | | | | | | | | |