Department of Mathematics MTL 106 (Introduction to Probability and Stochastic Processes) Tutorial Sheet No. 1

Answer for selected Problems

- $\begin{array}{l} 1. \ \mid \Omega \mid = 12 \\ \Omega = \{DD, NDD, NDND, NNDD, NNDN, NNNN, NNND, NDNN, DNNN, DNNN, DNND, DNND, DNDD\} \end{array}$
- 2. No
- 3. $\frac{1}{2}$
- 4. (a) $\frac{1}{N+1} \sum_{i=1}^{N} \frac{1}{i}$ (b) Updated Answer: Required probability= P(exactly one)+P(exactly two)+P(none)= $\sum_{i=1}^{n} P(A_i \cap (\cup_{j=1, j \neq i}^{n} A_j)^C) + \sum_{i=1}^{n} \sum_{k < i} P((A_k \cap A_i) \cap (\cup_{j=1, j \neq i, k}^{n} A_j)^C) + P(\cup_{j=1}^{n} A_j)^C = \frac{1}{N+1} \sum_{i=1}^{N} \frac{1}{i} + \frac{1}{N+1} \sum_{j=2}^{N} \sum_{i=1}^{j} \frac{1}{ij} + \frac{1}{N+1}$
- 7. $\frac{4}{35}$
- 9. $({}^{12}C_2-1)\left(\frac{1}{3}\right)^{12}\left(\frac{2}{3}\right)^2$
- 10. (a) $\mathcal{F}_1 = \{\phi, \Omega\}, \mathcal{F}_1 = \{\phi, \{1\}, \{2, 3, 4\}, \Omega\}, \mathcal{F}_3 = P(\Omega)$ (b) Define P(i) = 0.25, for i = 1, 2, 3, 4
- 11. $\frac{23}{64}$
- 12. Yes
- 14. 0, 1

15.
$$\frac{3! \times 2^3}{6 \times 6 \times 6} = \frac{2}{9}$$

- 16. (a) $\frac{\lfloor \frac{N}{3} \rfloor + \lfloor \frac{N}{4} \rfloor \lfloor \frac{N}{12} \rfloor}{N}$ where $\lfloor . \rfloor$ =floor function (b) $\frac{1}{2}$
- 17. $\frac{1}{4}$
- 19. A, B, C are pairwise as well as mutually independent
- 20. P(A|B)
- 21. $p_0 + p_1 p_0 + p_2 (p_0)^2$
- 22. $\frac{30}{61}$
- 23. $\frac{40! \times {}^{41}P_4}{44!}$
- 24. $2 \times (0.5)^4$
- 25. $\frac{43}{216}$, $\frac{173}{216}$
- 26. $(a)\frac{1}{2}$ $(b)\frac{1}{7}$
- 27. (a) $R^4 + {}^4C_3R^3(1-R) + {}^4C_2R^2(1-R)^2$ (b) $R^4 + {}^4C_3R^3(1-R) + {}^2C_1R(1-R) \times {}^2C_1R(1-R)$
- $28. \ p^4 + 4p^3q + 2p^2q^2$
- 29. $\frac{b}{b+r+c}$

30.
$$\frac{1}{2}(1 + \ln 2)$$

$$31. \ \frac{{}^{(N-D)}C_n}{{}^{N}C_n}$$

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