

Q1 a. Output is as follows:

0 (0.5 marks)

Child. 10 (0.5 marks)

Parent (0.5 marks)

0.5 marks for the correct order.

Q1 b.

Output pattern: 0 1 2... 2... 1 2... 2... Because the question mentions What's printed in what order (1 mark)

Mentioning Pre-order traversal, each node prints its depth or if n is the number of nodes at a depth d then d is printed n times. (3 marks)

Q3

'Suppose the pivot is the first element' is a flaw since it does not guarantee worst case partitioning. (2 marks)

'Partition takes  $= kn+c$ ' is a flaw since there is no support to it in the proof because it must be  $\leq kn+c$  (2marks)

Q4

Mentioning that 'An algorithm must search through all  $k+1$  elements' is a flaw. (2 marks)

Reasoning for above flaw is that to find the element which is going to be obtained in the  $(k+1)$ th comparison, we need not search through all the  $k+1$  elements again because binary search algorithm divides the search domain by half in every iteration. So we don't need to search through all  $k+1$  elements. (2 marks)

Q9

-intuition

1) pick the middle element.

2) If  $\text{arr}[\text{mid}+1] > \text{arr}[\text{mid}]$  and  $\text{arr}[\text{mid}-1] < \text{arr}[\text{mid}]$ , we recur for right half.

3) If  $\text{arr}[\text{mid}+1] < \text{arr}[\text{mid}]$  and  $\text{arr}[\text{mid}-1] > \text{arr}[\text{mid}]$ , we recur for left half.

4) If  $\text{arr}[\text{mid}+1] < \text{arr}[\text{mid}]$  and  $\text{arr}[\text{mid}-1] < \text{arr}[\text{mid}]$ , return mid

-algo

find\_k(arr[],start,end)

{ mid=(start+end)/2

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if(arr[mid+1]>arr[mid] && arr[mid-1]<arr[mid])
    find_k(arr[],mid+1,end)
else if(arr[mid+1]<arr[mid] && arr[mid-1]>arr[mid] )
    find_k(arr[],start,mid-1)
else if(arr[mid+1]<arr[mid] and arr[mid-1]<arr[mid] )
    return mid
else
    return -1 //no such element exist

}

```

-analysis

At each iteration we reduce the size of an array to half, and at each iteration constant time operation is being done(comparison operation), so clearly ,  
 $tc=O(\log(n))$