COL106: Assignment 4

Trie, Red-Black tree and Priority queue

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Logistics:

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Brief description:

In this assignment you need to work with *Tries, Red-Black trees* and *Priority queues*. There will be **Four** components of the assignment. The first three will check *tries, red-black trees* and *priority queues* independently. The last part of the assignment will be a combination of all the previous components.

1 General instructions

The grading will be done automatically. To ensure a smooth process, an interface will be provided to you, which you are **NOT** suppose to change. Your solution classes will implement these interfaces.

For each of the component, you will be given and *input* file, which will contain the commands that your code must execute. As per the command, the program will produce the *output*, which will be compared against an expected output for grading. Please ensure that you follow the proper formatting criteria, failing to do so will results in *0* for that particular component.

1.1 Code skeleton

You are provided with the skeleton of the code. This contains the interfaces and other relevant information. Your task is to fill up the empty functions. The code also contains *driver code* for all the components of assignment. These will be used to check the correctness of the code. Please **DO NOT** modify the interface and the driver code. You are free to change and implement other parts in any way you like.

Code can be downloaded from here: Download code

1.1.1 Building and Running

In the code, within the src folder, you can use the following commands to check your code.

make

This will check all the components. Components can also be checked independently:

```
make trie
make rbtree
make pq
make pm
```

for Trie, Red-Black tree, Priority-Queue and Project-Management (4th Component) respectively.

2 Trie [1 Mark]

Trie is an efficient information reTrieval data structure. Using Trie, search complexities can be brought to optimal limit (key length) [2].

In this part of the assignment, you need to implement a Trie data structure. To make things interesting, you will be implementing a telephone directory using Tries. Name of a person will be the key (assuming all names are unique). Associate with every name will be a Person object.

```
package Trie;
public class Person {
    public Person(String name, String phone_number) {
    }
    public String getName() {
        return "";
    }
}
Listing 1: Person class.
```

2.1 Interface

You version of Trie must implement the TrieInterface as shown in Listing 2 and also provided as code.

```
1 package Trie;
```

```
public interface TrieInterface<T> {
   boolean insert(String word, T value);
   TrieNode<T> search(String word);
   TrieNode<T> startsWith(String prefix);
   void printTrie(TrieNode trieNode);
   boolean delete(String word);
   void print();
   void printLevel(int level);
   listing 2: Interface specifications for Trie.
```

2.2 Input specifications

Commands:

- 1. INSERT: It takes a String as input and inserts that into the trie.
- 2. DELETE: It takes a String as an input and deletes that from the trie.
- 3. SEARCH: It takes a String as input and returns *true* or *false*, based on whether that word is present in trie or now.
- 4. MATCH: It takes a String as an input, and return all words where the suffix is the entered String.
- 5. PRINT: Print all the words inside the trie.
- 6. PRINTLEVEL: Print the specified level.

Sample input file:

```
1 INSERT
<sup>2</sup> Diljeet Singh, +91987654321
3 INSERT
4 Bhavesh Kumar, +91987654321
5 INSERT
6 Chayan Malhotra, +91987654321
7 INSÉRT
8 Ekta Mittal, +91987654321
9 INSERT
10 Farhan Khan, +91987654321
11 INSERT
12 Dishant Goyal, +91987654321
13 INSERT
14 Dishant Kumar, +91987654321
15 INSERT
16 Dishant Gupta, +91987654321
17 SEARCH
18 Dishant Goyal
19 MATCH Di
20 MATCH di
_{21} DELETE
22 Dishant Goyal
23 SEARCH
24 Dishant Goyal
25 MATCH SK
26 PRINTLEVEL 2
27 PRINT
  Listing 3: Input for Trie.
Expected Output file:
1 Inserting: Diljeet Singh
2 Inserting: Bhavesh Kumar
₃ Inserting: Chayan Malhotra
4 Inserting: Ekta Mittal
₅ Inserting: Farhan Khan
6 Inserting: Dishant Goyal
7 Inserting: Dishant Kumar
8 Inserting: Dishant Gupta
9 Searching: Dishant Goyal
10 FOUND
11 [Name: Dishant Goyal, Phone=+91987654321]
12 Matching: Di
13 MATCHED:
14 [Name: Diljeet Singh, Phone=+91987654321]

    Is [Name: Dishant Kumar, Phone=+91987654321]
    [Name: Dishant Goyal, Phone=+91987654321]

17 [Name: Dishant Gupta, Phone=+91987654321]
18 Matching: di
19 NOT FOUND
20 Deleting: Dishant Goyal
```

```
21 Searching: Dishant Goyal
22 NOT FOUND
23 Matching: SK
24 NOT FOUND
25 Level 2: h h i k a
27 Printing Trie
_{\mbox{\tiny 28}} Level 1: B C D E F
29 Level 2: h h i k a
₃₀ Level 3: a a s l t r
31 Level 4: v y h j a h
32 Level 5: e a a e
33 Level 6: s n n e M n
34 Level 7: h
                tti
              М
35 Level 8:
35 Level 8: M t K
36 Level 9: K a G K S t h
37 Level 10: uluuiaa
38 Level 11: m h p m n l n
39 Level 12: a o t a g
40 Level 13: rtarh
41 Level 14: r
42 Level 15: a
43 Level 16:
  Listing 4: Ouput for Trie.
```

3 Red-Black Tree [1 Mark]

In this part you need to implement a Red-Black tree. A tutorial on Red-Black tree can be found here [1]. In the part the basic operations on a Red-Black tree, insert and search will be tested. You will be given an input file, whose format is listed in Section 3.2. A sample output for the input command given in Section 3.2 is shown in 7

In this case also you will implement a telephone directory, with an added feature that a person can have multiple numbers.

3.1 Specifications

You Red-Black tree, must implement the interface as shown in listing 5.

```
package RedBlack;
public interface RBTreeInterface<T extends Comparable, E> {

void insert(T key, E value);

RedBlackNode<T, E> search(T key);

Listing 5: Input for Trie.
```

Things to keep in mind:

• All the items insert into the RB-Tree has a key and the corresponding value with it. In this version of Red-Black tree, a *key* can have multiple items. If we are trying to insert an element with a key which is already present in the tree, the value will get attached to that key. This can be seen in the Listing 6, Line 11 and 13.

3.2 Input specifications

Commands:

- 1. INSERT int: Insert an element to the tree.
- 2. SEARCH int: Searches for a particular element in the tree.

Sample input (ignore the line numbers):

```
1 INSERT
2 Diljeet Singh, +91987654321
₃ INSERT
4 Bhavesh Kumar, +91987654321
5 TNSFRT
6 Chayan Malhotra, +91987654321
7 INSERT
8 Ekta Mittal, +91987654321
9 INSERT
10 Farhan Khan, +91987654321
11 INSERT
12 Dishant Goyal, +91987654321
13 INSERT
14 Dishant Goyal, +91999999999
15 INSERT
16 Dishant Kumar, +91987654321
17 INSERT
18 Dishant Gupta, +91987654321
```

```
19 SEARCH
20 Dishant Goyal
21 SEARCH
22 Sandeep
  Listing 6: Input for RedBlack Tree.
Expected Output (ignore the line numbers):
1 Inserting: Diljeet Singh
2 Inserting: Bhavesh Kumar
₃ Inserting: Chayan Malhotra
4 Inserting: Ekta Mittal
_{\scriptscriptstyle{5}} Inserting: Farhan Khan
6 Inserting: Dishant Goyal
7 Inserting: Dishant Goyal
8 Inserting: Dishant Kumar
9 Inserting: Dishant Gupta
10 Searching for: Dishant Goyal
11 [Name: Dishant Goyal, Phone=+91987654321]
12 [Name: Dishant Goyal, Phone=+91999999999]
13 Searching for: Sandeep
14 Not Found
  Listing 7: Output for RedBlack Tree.
```

4 Priority queues [1 Mark]

In this part you need to implement a priority queue. Specifically, you will be implementing a max-heap which is an implementation of priority queue.

You will need to implement a scoring record using Max Heap. This will contains, students name and their corresponding marks. The max-heap will use the marks to arrange the students, i.e. the student with the highest marks will be on the top.

4.1 Specifications

```
package PriorityQueue;
public interface PriorityQueueInterface<T extends Comparable> {
    void insert(T element);
    T extractMax();
}
Listing 8: Interface for PriorityQueue.
```

Commands

- 1. INSERT
 - name marks: Insert the current integer in the tree.
- 2. EXTRACTMAX: Extract the student with highest marks and print it. Extract operations also removes this from the max-heap.

Sample input (ignore the line numbers):

```
1 INSERT
2 Diljeet Singh, 10
₃ INSERT
4 Bhavesh Kumar, 100
5 INSERT
6 Dishant Kumar, 67
7 FXTRACTMAX
8 EXTRACTMAX
9 EXTRACTMAX
10 EXTRACTMAX
  Listing 9: Input for PriorityQueue.
Expected Output (ignore the line numbers):
1 Inserting: Diljeet Singh
2 Inserting: Bhavesh Kumar
₃ Inserting: Dishant Kumar
 Student{name='Bhavesh Kumar', marks=100}
5 Student{name='Dishant Kumar', marks=67}
6 Student{name='Diljeet Singh', marks=10}
 Heap is empty
```

5 Project Management (Scheduler) [2 Marks]

Listing 10: Output for PriorityQueue.

In this part of the assignment you need to combine all the previous components of the assignment, Trie, Red-Black Tree and Priority Queue to implement a Job scheduler. The main part of this part are:

1. Project:

```
The project class will be have a name, budget and priority (as shown in Listing 11).
package ProjectManagement;
public class Project {
 Listing 11: Project class
```

```
2. User:
```

```
package ProjectManagement;
public class User implements Comparable<User> {
     @Override
     public int compareTo(User user) {
          return 0:
  Listing 12: User class
Job:
package ProjectManagement;
public class Job implements Comparable<Job> {
     @Override
     public int compareTo(Job job) {
          return 0;
  Listing 13: Job class
```

A job can have two status: REQUESTED, COMPLETED.

5.1 Specifications

The main component is *Job*. As shown in Listing 13, each Job will belong to a Project and created by an User. The name of the Jobs will be unique (this is guaranteed in the test cases). All the jobs have a running time, i.e. the time required to run this job. The priority of a job is same as of that its project and a job can only run if its running time is less than the current budget of the Project. Successfully running a Job, will reduce the budget of that project by running time of the project.

All the projects will be stored in a Trie, using the project name as the key. Project names will be unique. All the Jobs will be stored in a *Priority Queue*, specifically a Max-Heap, using their priorities as the key.

5.2 Commands

A sample input file is shown in Listing 15.

- 1. USER: Create the user with given user name.
- 2. PROJECT: Create a project. NAME PRIORITY BUDGET
- 3. JOB: Create a job. NAME PROJECT USER RUNTIME
- 4. QUERY: Return the status of the Job queried.
- 5. ADD: Increase the budget of the project. PROJECT BUDGET
- 6. EMPTY_LINE: Let the scheduler execute a single JOB.

5.3 Scheduler specifications

The scheduler will execute a single whenever it will encounter an empty line in the input specifications. After the end of the INP file, scheduler will continue to execute jobs till there are jobs left that can be executed.

Each time the scheduler executes a job, it will do the following:

- 1. It selects the job with the highest priority from the MAX HEAP.
- 2. It first check the running time of the Job, say *t*.
- 3. It will then fetch the project from the RB-Tree and check its budget, say *B*.
- 4. If $B \ge t$ then the code is executed.
 - Executing a job means:
 - Set the status of the job to complete.
 - Increase the global time by job time.
 - Set the completed time of the job as the current global time.
 - Decrease the budget of the project by run-time of the job. i.e. B = B t, where B is the new budget of the project.
- 5. If: B < t, then select the next job and try to execute this.
- 6. A scheduler will return in following cases:
 - It successfully executed a job.
 - There are no jobs to be executed.
 - None of the jobs can be executed because of the budget issue.
- 7. After the execution returns, process the next batch of commands (all the commands till next EMPTY_LINE or EOF).

- 8. If there are no more commands in the INP file, then let the scheduler execute jobs till there are no jobs left, or no jobs can be executed because of budget issues. This marks the END of the execution.
- 9. Print the stats of the current system. See Listing 16.

```
package ProjectManagement;
public interface SchedulerInterface {
      void run_to_completion();
      void handle_project(String[] cmd);
      void handle job(String[] cmd);
      void handle_user(String name);
      void handle_query(String key);
     void handle_empty_line();
void handle_add(String[] cmd);
      void print_stats();
      void schedule();
11
12 }
 Listing 14: Interface specification
1 USER Rob
2 USER Harry
₃ USER Carry
4 PROJECT IITD.CS.ML.ICML 10 15
5 PROJECT IITD.CS.OS.ASPLOS 9 100
6 PROJECT IITD.CS.TH.SODA 8 100
7 JOB DeepLearning IITD.CS.ML.ICML Rob 10
3 JOB ImageProcessing IITD.CS.ML.ICML Carry 10
9 JOB Pipeline IITD.CS.OS.ASPLOS Harry 10
10 JOB Kmeans IITD.CS.TH.SODA Carry 10
12 QUERY Kmeans
13 QUERY Doesnotexists
_{15} JOB DeepLearning IITD.CS.ML.ICM Rob 10
16 JOB DeepLearning IITD.CS.ML.ICML Rob2 10
_{\rm 17} JOB DeepLearning IITD.CS.ML.ICML Rob 10 \,
18 JOB ImageProcessing IITD.CS.ML.ICML Carry 10
19 JOB Pipeline IITD.CS.OS.ASPLOS Harry 10
20 JOB Kmeans IITD.CS.TH.SODA Carry 10
22 JOB DeepLearning11 IITD.CS.ML.ICML Rob 10
23 JOB ImageProcessingl IITD.CS.ML.ICML Carry 10
24 JOB Pipelinel IITD.CS.OS.ASPLOS Harry 10
25 JOB Kmeans1 IITD.CS.TH.SODA Carry 10
27 JOB DeepLearning2 IITD.CS.ML.ICML Rob 10
Job Pipeline2 IITD.CS.ML.ICML Carry 10
Job Pipeline2 IITD.CS.S.ASPLOS Harry 10
_{\mbox{\tiny 30}} JOB Kmeans2 IITD.CS.TH.SODA Carry 10
32 ADD IITD.CS.ML.ICML 60
33 JOB DeepLearning3 IITD.CS.ML.ICML Rob 10
34 JOB ImageProcessing3 IITD.CS.ML.ICML Carry 10
35 JOB Pipeline3 IITD.CS.OS.ASPLOS Harry 10
36 JOB Kmeans3 IITD.CS.TH.SODA Carry 10
38 QUERY Kmeans
40 JOB DeepLearning4 IITD.CS.ML.ICML Rob 10
41 JOB ImageProcessing4 IITD.CS.ML.ICML Carry 10
42 JOB Pipeline4 IITD.CS.OS.ASPLOS Harry 10
43 JOB Kmeans4 IITD.CS.TH.SODA Carry 10
_{45} QUERY Kmeans
 Listing 15: Input specification
1 Creating user
2 Creating user
₃ Creating user
₄ Creating project
5 Creating project
6 Creating project
7 Creating job
8 Creating job
9 Creating job
_{\scriptsize 10} Creating job
11 Running code
    Remaining jobs: 4
    Executing: DeepLearning from: IITD.CS.ML.ICML
    Project: IITD.CS.ML.ICML budget remaining: 5
15 Execution cycle completed
_{16} Querying
17 Kmeans: NOT FINISHED
18 Querying
19 Doesnotexists: NO SUCH JOB
20 Running code
    Remaining jobs: 3
```

```
Executing: ImageProcessing from: IITD.CS.ML.ICML
    Un-sufficient budget.
    Executing: Pipeline from: IITD.CS.OS.ASPLOS
    Project: IITD.CS.OS.ASPLOS budget remaining: 90
26 Execution cycle completed
27 Creating job
_{\mbox{\tiny 28}} No such project exists. IITD.CS.ML.ICM
_{29} Creating job
30 No such user exists: Rob2
31 Creating job
32 Creating job
33 Creating job
34 Creating job
35 Running code
    Remaining jobs: 5
    Executing: DeepLearning from: IITD.CS.ML.ICML
    Un-sufficient budget.
    Executing: ImageProcessing from: IITD.CS.ML.ICML
39
    Un-sufficient budget.
    Executing: Pipeline from: IITD.CS.OS.ASPLOS
Project: IITD.CS.OS.ASPLOS budget remaining: 80
43 Execution cycle completed
44 Creating job
45 Creating job
46 Creating job
47 Creating job
48 Running code
    Remaining jobs: 6
    Executing: DeepLearning11 from: IITD.CS.ML.ICML
    Un-sufficient budget.
    Executing: ImageProcessing1 from: IITD.CS.ML.ICML
    Un-sufficient budget.
    Executing: Pipeline1 from: IITD.CS.OS.ASPLOS
    Project: IITD.CS.OS.ASPLOS budget remaining: 70
56 Execution cycle completed
57 Creating job
58 Creating job
59 Creating job
60 Creating job
61 Running code
    Remaining jobs: 7
Executing: DeepLearning2 from: IITD.CS.ML.ICML
    Un-sufficient budget.
    Executing: ImageProcessing2 from: IITD.CS.ML.ICML
    Un-sufficient budget.
    Executing: Pipeline2 from: IITD.CS.OS.ASPLOS
    Project: IITD.CS.OS.ASPLOS budget remaining: 60
69 Execution cycle completed
70 Creating job
_{71} Creating job
72 Creating job
73 Creating job
74 Running code
    Remaining jobs: 15
    Executing: ImageProcessing from: IITD.CS.ML.ICML Project: IITD.CS.ML.ICML budget remaining: 55
78 Execution cycle completed
79 Querying
80 Kmeans: NOT FINISHED
81 Running code
    Remaining jobs: 14
Executing: Kmeans3 from: IITD.CS.TH.SODA
    Project: IITD.CS.TH.SODA budget remaining: 90
85 Execution cycle completed
86 Creating job
87 Creating job
88 Creating job
89 Creating job
90 Running code
    Remaining jobs: 17
    Executing: Pipeline3 from: IITD.CS.OS.ASPLOS
    Project: IITD.CS.OS.ASPLOS budget remaining: 50
94 Execution cycle completed
95 Querying
96 Kmeans: NOT FINISHED
97 Running code
    Remaining jobs: 16
    Executing: Kmeans4 from: IITD.CS.TH.SODA
Project: IITD.CS.TH.SODA budget remaining: 80
101 System execution completed
102 Running code
    Remaining jobs: 15
103
    Executing: Kmeansl from: IITD.CS.TH.SODA
Project: IITD.CS.TH.SODA budget remaining: 70
104
_{\mbox{\scriptsize 106}} System execution completed
107 Running code
     Remaining jobs: 14
     Executing: ImageProcessing4 from: IITD.CS.ML.ICML
```

```
Project: IITD.CS.ML.ICML budget remaining: 45
 111 System execution completed
 112 Running code
             Remaining jobs: 13
 113
             Executing: DeepLearning4 from: IITD.CS.ML.ICML
 114
             Project: IITD.CS.ML.ICML budget remaining: 35
 116 System execution completed
 117 Running code
             Remaining jobs: 12
             Executing: ImageProcessing3 from: IITD.CS.ML.ICML
             Project: IITD.CS.ML.ICML budget remaining: 25
 120
 121 System execution completed
 122 Running code
 123
             Remaining jobs: 11
             Executing: Kmeans from: IITD.CS.TH.SODA
             Project: IITD.CS.TH.SODA budget remaining: 60
 126 System execution completed
 127 Running code
             Remaining jobs: 10
 128
             Executing: ImageProcessing2 from: IITD.CS.ML.ICML Project: IITD.CS.ML.ICML budget remaining: 15
 131 System execution completed
 132 Running code
             Remaining jobs: 9
             Executing: Kmeans2 from: IITD.CS.TH.SODA
 134
             Project: IITD.CS.TH.SODA budget remaining: 50
 136 System execution completed
 137 Running code
             Remaining jobs: 8
             Executing: Kmeans from: IITD.CS.TH.SODA
             Project: IITD.CS.TH.SODA budget remaining: 40
 141 System execution completed
 142 Running code
             Remaining jobs: 7
Executing: Pipeline4 from: IITD.CS.OS.ASPLOS
             Project: IITD.CS.OS.ASPLOS budget remaining: 40
       System execution completed
 147 Running code
             Remaining jobs: 6
 148
             Executing: ImageProcessing from: IITD.CS.ML.ICML
 149
             Project: IITD.CS.ML.ICML budget remaining: 5
 _{151} System execution completed
 152 Running code
             Remaining jobs: 5
             Executing: DeepLearning3 from: IITD.CS.ML.ICML
             Un-sufficient budget.
 155
             Executing: DeepLearning2 from: IITD.CS.ML.ICML
 156
             Un-sufficient budget.
 157
             Executing: ImageProcessing1 from: IITD.CS.ML.ICML
 158
             Un-sufficient budget.
 150
              Executing: DeepLearning from: IITD.CS.ML.ICML
             Un-sufficient budget.
 161
              Executing: DeepLearning11 from: IITD.CS.ML.ICML
 162
             Un-sufficient budget.
 163
 164 System execution completed
 165 -----STATS-
 Job{user='Carry', project='IITD.CS.ML.ICML', jobstatus=COMPLETED, execution_time=10, end_time=60, name='ImageProcessing'}
Job{user='Rob', project='IITD.CS.ML.ICML', jobstatus=COMPLETED, execution_time=10, end_time=10, name='DeepLearning'}
Job{user='Rob', project='IITD.CS.ML.ICML', jobstatus=COMPLETED, execution_time=10, end_time=120, name='DeepLearning4'}
Job{user='Carry', project='IITD.CS.ML.ICML', jobstatus=COMPLETED, execution_time=10, end_time=110, name='ImageProcessing4'}
Job{user='Carry', project='IITD.CS.ML.ICML', jobstatus=COMPLETED, execution_time=10, end_time=130, name='ImageProcessing3'}
Job{user='Carry', project='IITD.CS.ML.ICML', jobstatus=COMPLETED, execution_time=10, end_time=150, name='ImageProcessing2'}
Job{user='Carry', project='IITD.CS.TH.SODA', jobstatus=COMPLETED, execution_time=10, end_time=100, name='Kmeans1'}
Job{user='Carry', project='IITD.CS.TH.SODA', jobstatus=COMPLETED, execution_time=10, end_time=160, name='Kmeans2'}
Job{user='Harry', project='IITD.CS.OS.ASPLOS', jobstatus=COMPLETED, execution_time=10, end_time=20, name='Pipeline'}
Job{user='Carry', project='IITD.CS.TH.SODA', jobstatus=COMPLETED, execution_time=10, end_time=10, end_time=10,
Job{user='Carry', project='IITD.CS.OS.ASPLOS', jobstatus=COMPLETED, execution_time=10, end_time=90, name='Kmeans4'}
Job{user='Harry', project='IITD.CS.OS.ASPLOS', jobstatus=COMPLETED, execution_time=10, end_time=50, name='Pipeline2'}
Job{user='Harry', project='IITD.CS.OS.ASPLOS', jobstatus=COMPLETED, execution_time=10, end_time=40, name='Pipeline1'}
Job{user='Harry', project='IITD.CS.OS.ASPLOS', jobstatus=COMPLETED, execution_time=10, end_time=80, name='Pipeline3'}
Job{user='Harry', project='IITD.CS.OS.ASPLOS', jobstatus=COMPLETED, execution_time=10, end_time=80, name='Pipeline3'}
Job{user='Harry', project='IITD.CS.OS.ASPLOS', jobstatus=COMPLETED, execution_time=10, end_time=180, name='Pipeline4'}
184 OHTHIBATION OF THE PROOF OF
 190 Total unfinished jobs: 5
                          -----STATS DONE-
      Listing 16: Output for INP in Listing 15
```

6 Submission instructions

As always, you need to create all your .java files in a directory named *src*, compress this directory to zip format and rename the zip file in the format entrynumber_assignment3.zip. For example, if your entry number is 2012CSZ8019, the zip file should be named 2012CSZ8019_assignment4.zip. Then you need to convert this zip file to base64 format as follows and submit the .b64 file on Moodle.

base64 entrynumber assignment4.zip > entrynumber assignment4.zip.b64

Inside the src directory, at the minimum you need to have a README and a file named assignment4.java. In the README, you need to report the time complexities of various operations for both the implementations. You should also report any interesting findings based on your experiments with the two implementations.

Please note that we will run MOSS on the submitted code. Anyone found with a copied code, either from Internet or from another student, will be dealt as per the class policy.

7 FAQ

References

- [1] Painting nodes black with red-black trees basecs medium. https://medium.com/basecs/painting-nodes-black-with-red-black-trees-60eacb2be9a5. (Accessed on 09/10/2019).
- [2] Trie (insert and search) geeksforgeeks. https://www.geeksforgeeks.org/trie-insert-and-search/. (Accessed on 09/12/2019).