

$\alpha_s(s)$, 4 Loops

Chunks

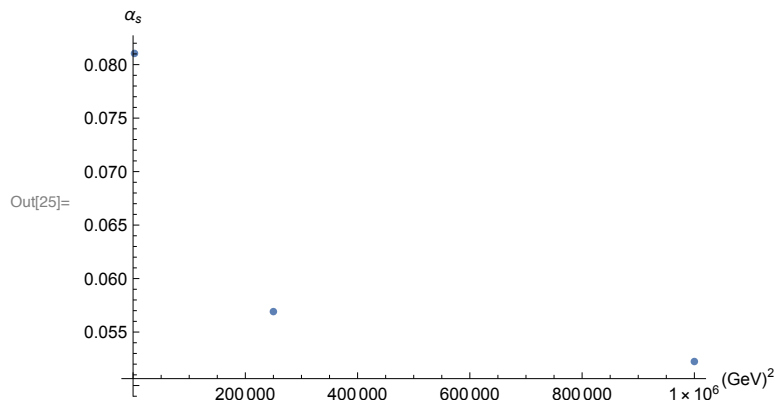
```
In[21]:= As50sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 502, 4];
As500sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5002, 4];
As1000sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 10002, 4];
```

```
In[24]:= Tablesq = TableForm[{{502, As50sq}, {5002, As500sq}, {10002, As1000sq}},
TableHeadings → {None, {"(GeV)2", " $\alpha_s$ "}}]
```

Out[24]//TableForm=

$(\text{GeV})^2$	α_s
2500	0.081047442862068354220
250 000	0.056911852763441925541
1 000 000	0.052245851714598850914

```
A = ListPlot[%, AxesLabel → {"(GeV)2", " $\alpha_s$ "}]
```



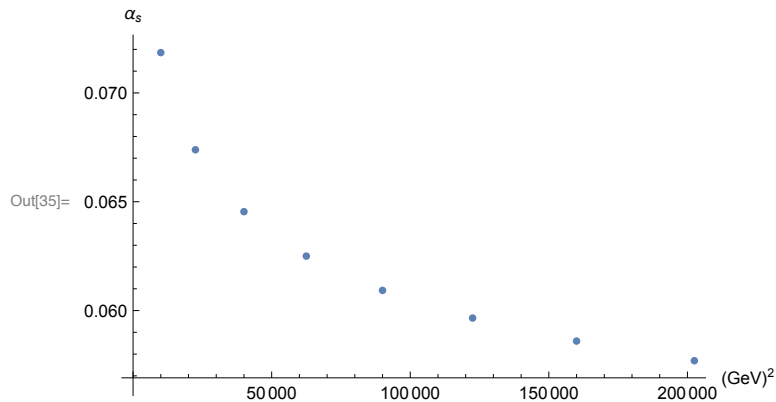
```
In[26]:= As100sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1002, 4];
As150sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1502, 4];
As200sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 2002, 4];
As250sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 2502, 4];
As300sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 3002, 4];
As350sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 3502, 4];
As400sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 4002, 4];
As450sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 4502, 4];
```

```
In[34]:= Tablesq =
  TableForm[{{1002, As100sq}, {1502, As150sq}, {2002, As200sq}, {2502, As250sq},
    {3002, As300sq}, {3502, As350sq}, {4002, As400sq}, {4502, As450sq}},
  TableHeadings → {None, {"(GeV)2", "αs"}}]
```

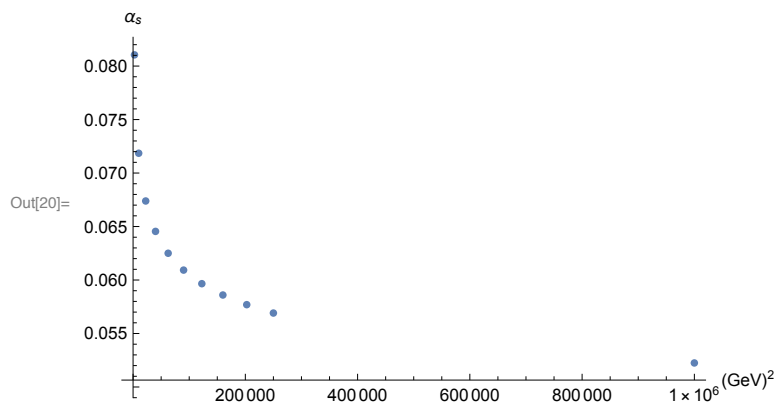
Out[34]//TableForm=

$(\text{GeV})^2$	α_s
10 000	0.071851606589246904918
22 500	0.067387616701294621139
40 000	0.064545398679831175395
62 500	0.062502069417089455757
90 000	0.060926962639263847121
122 500	0.059656383325729758176
160 000	0.058598181747164769227
202 500	0.057695714440271760104

```
In[35]:= B = ListPlot[%, AxesLabel → {"(GeV)2", "αs"}]
```



```
In[20]:= Show[A, B]
```



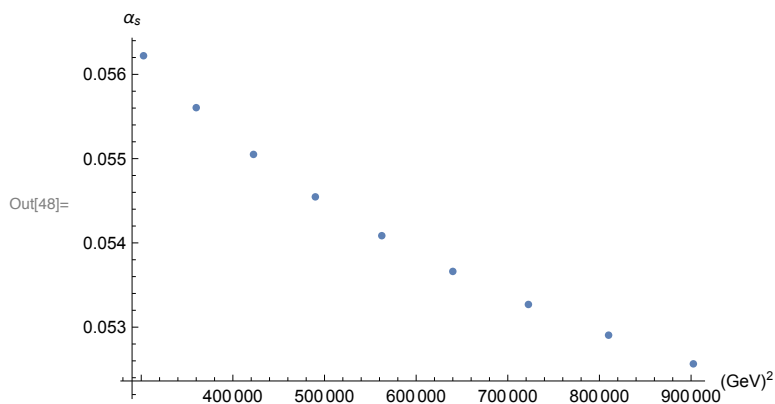
```
In[36]:= As550sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5502, 4];
As600sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 6002, 4];
As650sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 6502, 4];
As700sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 7002, 4];
As750sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 7502, 4];
As800sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 8002, 4];
As850sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 8502, 4];
As900sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 9002, 4];
As950sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 9502, 4];
```

```
In[47]:= Tablesq = TableForm[{{5502, As550sq}, {6002, As600sq}, {6502, As650sq},
{7002, As700sq}, {7502, As750sq}, {8002, As800sq}, {8502, As850sq},
{9002, As900sq}, {9502, As950sq}}, TableHeadings → {None, {"(GeV)2", "αs"}}]
```

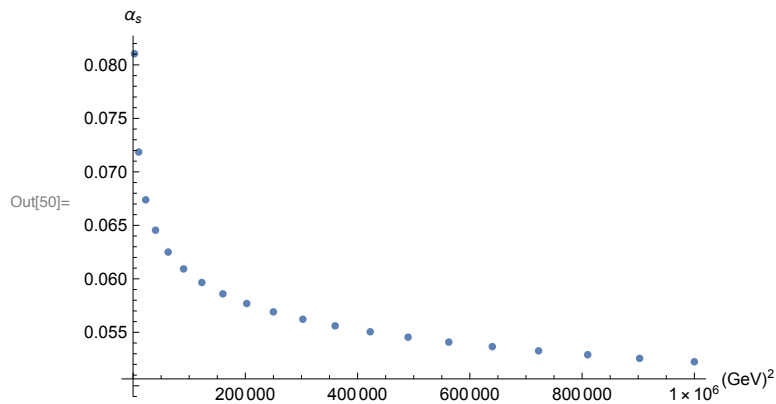
Out[47]//TableForm=

(GeV) ²	α _s
302 500	0.056221034863166959406
360 000	0.055604966134750124812
422 500	0.055050134856295275995
490 000	0.054546298709304271396
562 500	0.054085521843304228367
640 000	0.053661539550037010488
722 500	0.053269325948238549657
810 000	0.052904791891815312328
902 500	0.052564568941381061881

```
In[48]:= F = ListPlot[%, AxesLabel → {"(GeV)2", "αs"}]
```



In[50]:= Show[A, B, F]



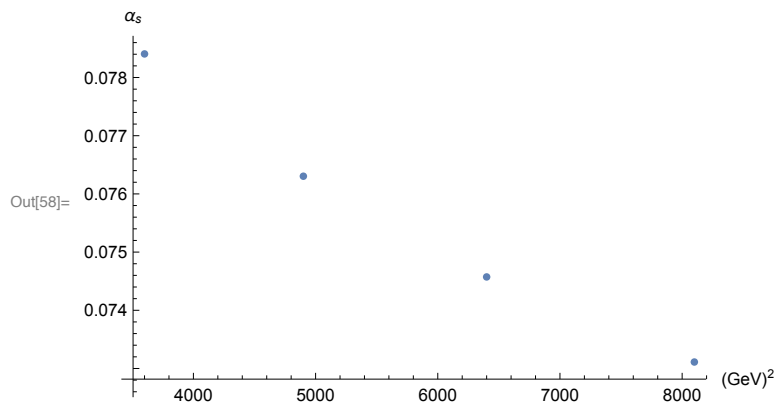
```
In[53]:= As60sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 60^2, 4];
As70sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 70^2, 4];
As80sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 80^2, 4];
As90sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 90^2, 4];
```

```
In[57]:= Tablesq = TableForm[{{60^2, As60sq}, {70^2, As70sq}, {80^2, As80sq}, {90^2, As90sq}},
TableHeadings -> {None, {"(GeV)^2", "\alpha_s"}}]
```

Out[57]/TableForm=

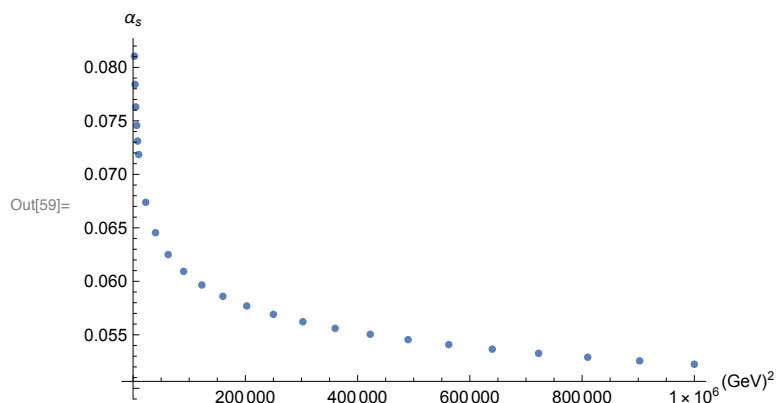
$(\text{GeV})^2$	α_s
3600	0.078405375366205428314
4900	0.076303717116715597241
6400	0.074573114316542665601
8100	0.073111154629109787553

```
In[58]:= G = ListPlot[%, AxesLabel -> {"(GeV)^2", "\alpha_s"}]
```



Partial Plot

In[59]:= Show[A, B, F, G]



Chunk 100

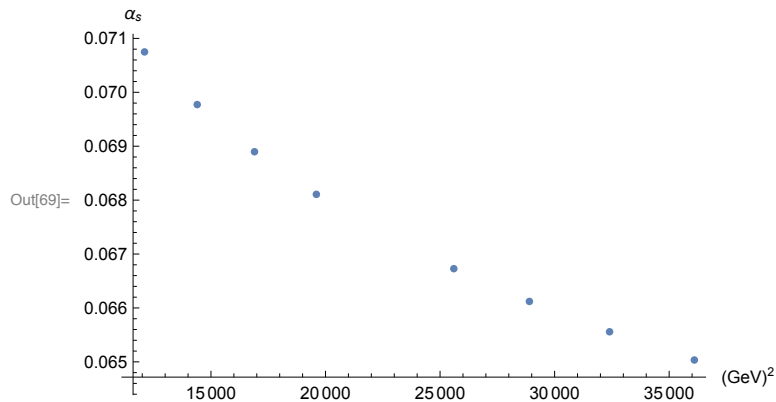
In[60]:= `As110sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1102, 4];`
`As120sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1202, 4];`
`As130sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1302, 4];`
`As140sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1402, 4];`
`As160sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1602, 4];`
`As170sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1702, 4];`
`As180sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1802, 4];`
`As190sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1902, 4];`

In[68]:= `Tablesq =`
`TableForm[{{1102, As110sq}, {1202, As120sq}, {1302, As130sq}, {1402, As140sq},`
`{1602, As160sq}, {1702, As170sq}, {1802, As180sq}, {1902, As190sq}},`
`TableHeadings → {None, {"(GeV)2", " α_s "}}]`

Out[68]//TableForm=

(GeV) ²	α_s
12 100	0.070749388383036940445
14 400	0.069772550569333984470
16 900	0.068897698925862461739
19 600	0.068107235029174489852
25 600	0.066728219678487325452
28 900	0.066120568731252369726
32 400	0.065557803987584704392
36 100	0.065034301634386674162

```
In[69]:= A1 = ListPlot[%, AxesLabel -> {"(GeV)2", "αs"}]
```



Chunk 200

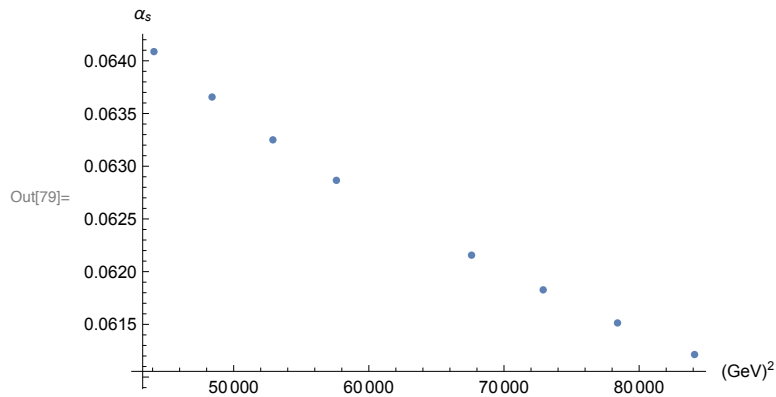
```
In[70]:= As210sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 2102, 4];
As220sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 2202, 4];
As230sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 2302, 4];
As240sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 2402, 4];
As260sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 2602, 4];
As270sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 2702, 4];
As280sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 2802, 4];
As290sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 2902, 4];
```

```
In[78]:= Tablesq =
TableForm[{{2102, As210sq}, {2202, As220sq}, {2302, As230sq}, {2402, As240sq},
{2602, As260sq}, {2702, As270sq}, {2802, As280sq}, {2902, As290sq}},
TableHeadings -> {None, {"(GeV)2", "αs"}}]
```

Out[78]/TableForm=

(GeV) ²	α _s
44 100	0.064087189521932243891
48 400	0.063656373106459043788
52 900	0.063250136393961376339
57 600	0.062866064324965214842
67 600	0.062156336107537810806
72 900	0.061827276309937617759
78 400	0.061513493598224224030
84 100	0.061213754097401342640

```
In[79]:= A2 = ListPlot[%, AxesLabel -> {"(GeV)2", "αs"}]
```



Chunk 300

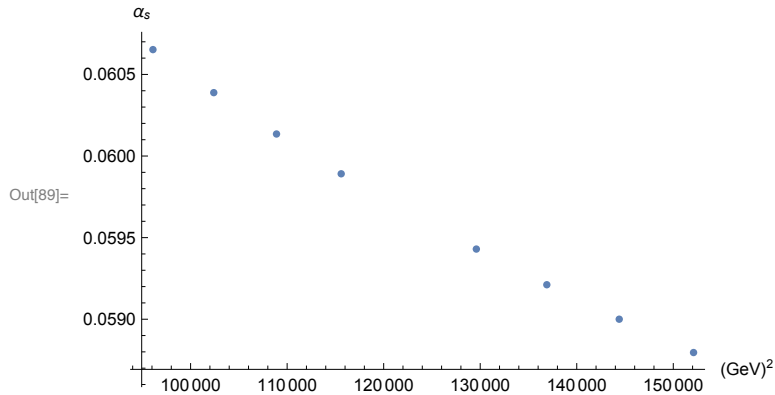
```
In[80]:= As310sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 3102, 4];
As320sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 3202, 4];
As330sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 3302, 4];
As340sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 3402, 4];
As360sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 3602, 4];
As370sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 3702, 4];
As380sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 3802, 4];
As390sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 3902, 4];
```

```
In[88]:= Tablesq =
TableForm[{{3102, As310sq}, {3202, As320sq}, {3302, As330sq}, {3402, As340sq},
{3602, As360sq}, {3702, As370sq}, {3802, As380sq}, {3902, As390sq}},
TableHeadings -> {None, {"(GeV)2", "αs"}}]
```

Out[88]/TableForm=

(GeV) ²	α _s
96 100	0.060652143088477628239
102 400	0.060388421999658314592
108 900	0.060135014955767075100
115 600	0.059891215080553203371
129 600	0.059429940216145267932
136 900	0.059211358799911389780
144 400	0.059000158599969752471
152 100	0.058795900402374475734

```
In[89]:= A3 = ListPlot[%, AxesLabel → {"(GeV)2", "αs"}]
```



Chunk 400

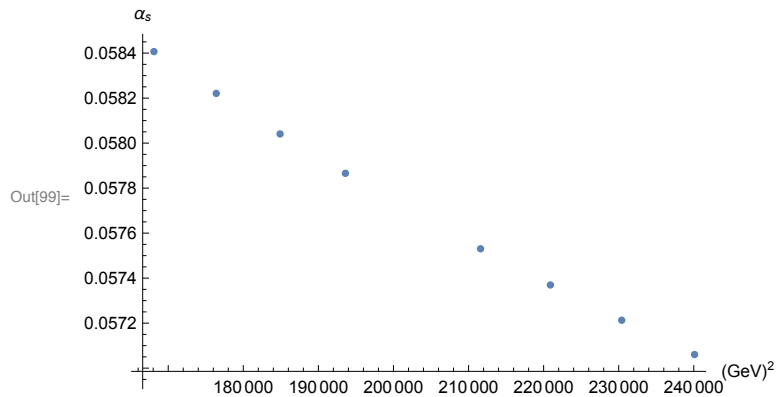
```
In[90]:= As410sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 4102, 4];
As420sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 4202, 4];
As430sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 4302, 4];
As440sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 4402, 4];
As460sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 4602, 4];
As470sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 4702, 4];
As480sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 4802, 4];
As490sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 4902, 4];
```

```
In[98]:= Tablesq =
TableForm[{{4102, As410sq}, {4202, As420sq}, {4302, As430sq}, {4402, As440sq},
{4602, As460sq}, {4702, As470sq}, {4802, As480sq}, {4902, As490sq}},
TableHeadings → {None, {"(GeV)2", "αs"}}]
```

Out[98]/TableForm=

(GeV) ²	α _s
168 100	0.058406633011998791438
176 400	0.058220913998135429581
184 900	0.058040710943952376694
193 600	0.057865733903804160227
211 600	0.057530403586227731609
220 900	0.057369570040011472818
230 400	0.057212998562673099505
240 100	0.057060488550937935285


```
In[99]:= A4 = ListPlot[%, AxesLabel → {"(GeV)2", "αs"}]
```



Chunk 500

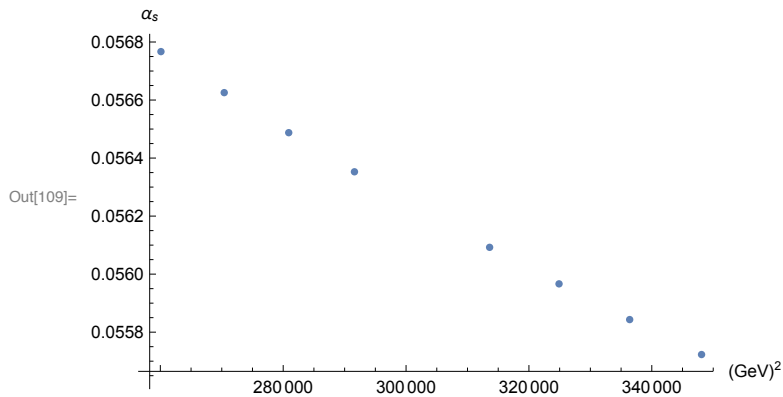
```
In[100]:= As510sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5102, 4];
As520sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5202, 4];
As530sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5302, 4];
As540sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5402, 4];
As560sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5602, 4];
As570sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5702, 4];
As580sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5802, 4];
As590sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5902, 4];
```

```
In[108]:= Tablesq =
TableForm[{{5102, As510sq}, {5202, As520sq}, {5302, As530sq}, {5402, As540sq},
{5602, As560sq}, {5702, As570sq}, {5802, As580sq}, {5902, As590sq}},
TableHeadings → {None, {"(GeV)2", "αs"}}]
```

Out[108]/TableForm=

(GeV) ²	α _s
260 100	0.056766916181049859718
270 400	0.056625514984794638203
280 900	0.056487495637276966348
291 600	0.056352714055300979127
313 600	0.056092330717436679044
324 900	0.055966481695178615353
336 400	0.055843374738718490020
348 100	0.055722903150791890158

```
In[109]:= A5 = ListPlot[%, AxesLabel → {"(GeV)2", "αs"}]
```



Chunk 600

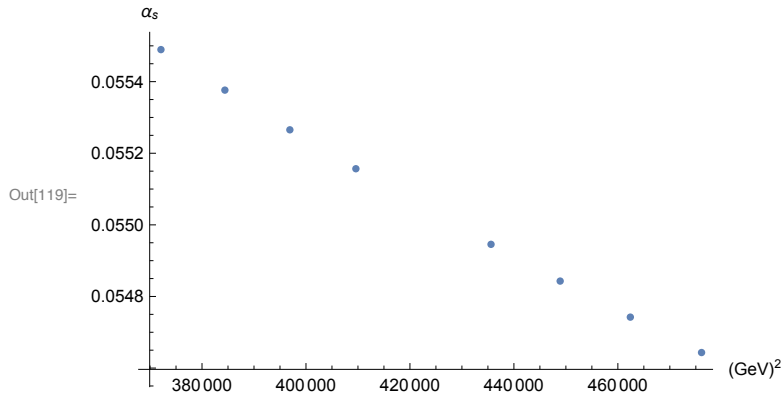
```
In[110]:= As610sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 6102, 4];
As620sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 6202, 4];
As630sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 6302, 4];
As640sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 6402, 4];
As660sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 6602, 4];
As670sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 6702, 4];
As680sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 6802, 4];
As690sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 6902, 4];
```

```
In[118]:= Tablesq =
TableForm[{{6102, As610sq}, {6202, As620sq}, {6302, As630sq}, {6402, As640sq},
{6602, As660sq}, {6702, As670sq}, {6802, As680sq}, {6902, As690sq}},
TableHeadings → {None, {"(GeV)2", "αs"}}]
```

Out[118]//TableForm=

(GeV) ²	α _s
372 100	0.055489468375113863483
384 400	0.055376319654332663219
396 900	0.055265434502091777519
409 600	0.055156731873929174644
435 600	0.054945570395505045860
448 900	0.054842969048315465218
462 400	0.054742264752106250783
476 100	0.054643394612856791230

```
In[119]:= A6 = ListPlot[%, AxesLabel → {"(GeV)2", "αs"}]
```



Chunk 700

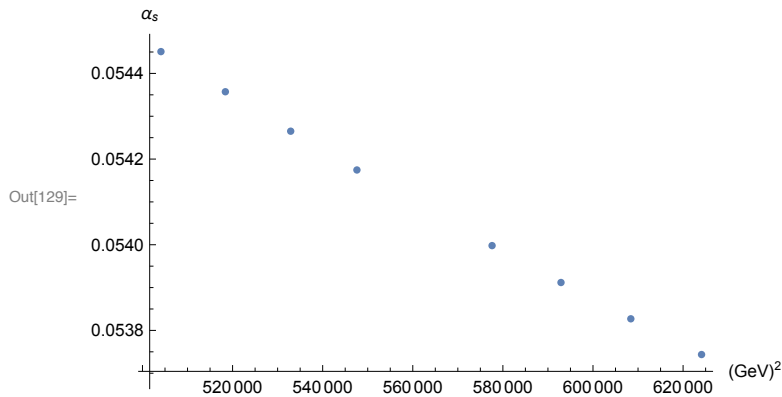
```
In[120]:= As710sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 7102, 4];
As720sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 7202, 4];
As730sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 7302, 4];
As740sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 7402, 4];
As760sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 7602, 4];
As770sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 7702, 4];
As780sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 7802, 4];
As790sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 7902, 4];
```

```
In[128]:= Tablesq =
TableForm[{{7102, As710sq}, {7202, As720sq}, {7302, As730sq}, {7402, As740sq},
{7602, As760sq}, {7702, As770sq}, {7802, As780sq}, {7902, As790sq}},
TableHeadings → {None, {"(GeV)2", "αs"}}]
```

Out[128]/TableForm=

(GeV) ²	α _s
504 100	0.054450919911834203193
518 400	0.054357203714802931817
532 900	0.054265098081123838090
547 600	0.054174553298064412038
577 600	0.053997958260397700041
592 900	0.053911819042865392578
608 400	0.053827062526211801140
624 100	0.053743648787233187404

```
In[129]:= A7 = ListPlot[%, AxesLabel → {"(GeV)2", "αs"}]
```



Chunk 800

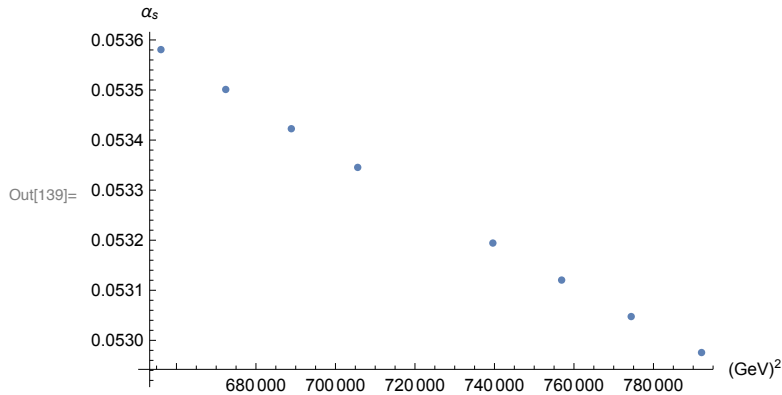
```
In[130]:= As810sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 8102, 4];
As820sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 8202, 4];
As830sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 8302, 4];
As840sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 8402, 4];
As860sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 8602, 4];
As870sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 8702, 4];
As880sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 8802, 4];
As890sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 8902, 4];
```

```
In[138]:= Tablesq =
TableForm[{{8102, As810sq}, {8202, As820sq}, {8302, As830sq}, {8402, As840sq},
{8602, As860sq}, {8702, As870sq}, {8802, As880sq}, {8902, As890sq}},
TableHeadings → {None, {"(GeV)2", "αs"}}]
```

Out[138]/TableForm=

(GeV) ²	α _s
656 100	0.053580698098246867243
672 400	0.053501089192915336083
688 900	0.053422678995707558084
705 600	0.053345434996958318966
739 600	0.053194321799099320302
756 900	0.053120393637688653399
774 400	0.053047513634962049072
792 100	0.052975654992231128607

```
In[139]:= A8 = ListPlot[%, AxesLabel → {"(GeV)2", "αs"}]
```



Chunk 900

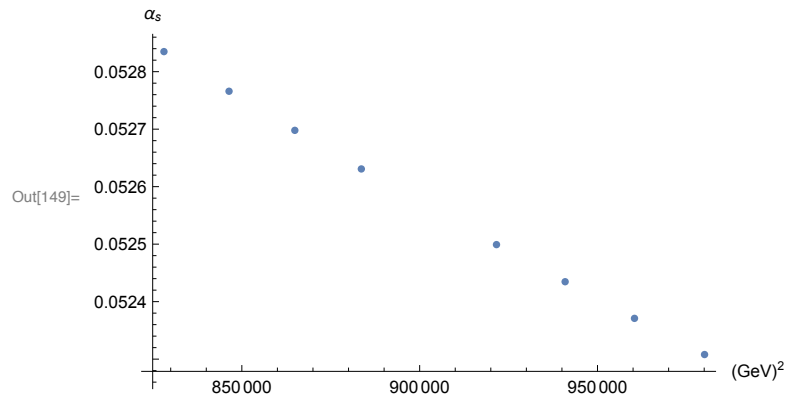
```
In[140]:= As910sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 9102, 4];
As920sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 9202, 4];
As930sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 9302, 4];
As940sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 9402, 4];
As960sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 9602, 4];
As970sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 9702, 4];
As980sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 9802, 4];
As990sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 9902, 4];
```

```
In[148]:= Tablesq =
TableForm[{{9102, As910sq}, {9202, As920sq}, {9302, As930sq}, {9402, As940sq},
{9602, As960sq}, {9702, As970sq}, {9802, As980sq}, {9902, As990sq}},
TableHeadings → {None, {"(GeV)2", "αs"}}]
```

Out[148]/TableForm=

(GeV) ²	α _s
828 100	0.052834899450580376379
846 400	0.052765953676165005014
864 900	0.052697931425712483941
883 600	0.052630810366938817476
921 600	0.052499186329682455245
940 900	0.052434642418781293307
960 400	0.052370917770880756721
980 100	0.052307993594085351674

```
In[149]:= A9 = ListPlot[%, AxesLabel -> {"(GeV)2", "αs"}]
```



Total Plot

```
In[150]:= Show[A, B, F, G, A1, A2, A3, A4, A5, A6, A7, A8, A9]
```

