## Run Cross Section $\alpha_s$ (s), 2 Loops

```
In[1737]:= g = 2;
        \alpha = 1/137;
        Conversion = 389379;
        n = 3;
       C_F = \frac{n^2 - 1}{2 n};
       Born = \frac{4\pi\alpha^2}{3 \text{ s}};
In[1743]:= CrossBorn[s ] = Conversion * Born;
        CrossBorn50sq = CrossBorn[50<sup>2</sup>];
        CrossBorn60sq = CrossBorn[60<sup>2</sup>];
        CrossBorn70sq = CrossBorn[70<sup>2</sup>];
        CrossBorn80sq = CrossBorn[80<sup>2</sup>];
        CrossBorn90sq = CrossBorn[90<sup>2</sup>];
ln[1749] = CrossBorn100sq = CrossBorn[100<sup>2</sup>];
        CrossBorn110sq = CrossBorn[110<sup>2</sup>];
        CrossBorn120sq = CrossBorn[120<sup>2</sup>];
        CrossBorn130sq = CrossBorn[130<sup>2</sup>];
        CrossBorn140sq = CrossBorn[140<sup>2</sup>];
        CrossBorn150sq = CrossBorn[150<sup>2</sup>];
        CrossBorn160sq = CrossBorn[160<sup>2</sup>];
        CrossBorn170sq = CrossBorn[170<sup>2</sup>];
        CrossBorn180sq = CrossBorn[180<sup>2</sup>];
        CrossBorn190sq = CrossBorn[190<sup>2</sup>];
ln[1759] = CrossBorn200sq = CrossBorn[200<sup>2</sup>];
        CrossBorn210sq = CrossBorn[210<sup>2</sup>];
        CrossBorn220sq = CrossBorn[220<sup>2</sup>];
        CrossBorn230sq = CrossBorn[230<sup>2</sup>];
        CrossBorn240sq = CrossBorn[240<sup>2</sup>];
        CrossBorn250sq = CrossBorn[250<sup>2</sup>];
        CrossBorn260sq = CrossBorn[260<sup>2</sup>];
        CrossBorn270sq = CrossBorn[270<sup>2</sup>];
        CrossBorn280sq = CrossBorn[280<sup>2</sup>];
        CrossBorn290sq = CrossBorn[290<sup>2</sup>];
```

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ln[1769] = CrossBorn300sq = CrossBorn[300<sup>2</sup>];
       CrossBorn310sq = CrossBorn[310<sup>2</sup>];
       CrossBorn320sq = CrossBorn[320<sup>2</sup>];
       CrossBorn330sq = CrossBorn[330<sup>2</sup>];
       CrossBorn340sq = CrossBorn[340<sup>2</sup>];
       CrossBorn350sq = CrossBorn[350<sup>2</sup>];
       CrossBorn360sq = CrossBorn[360<sup>2</sup>];
       CrossBorn370sq = CrossBorn[370<sup>2</sup>];
       CrossBorn380sq = CrossBorn[380<sup>2</sup>];
       CrossBorn390sq = CrossBorn[390<sup>2</sup>];
ln[1779] = CrossBorn400sq = CrossBorn[400<sup>2</sup>];
       CrossBorn410sq = CrossBorn[410<sup>2</sup>];
       CrossBorn420sq = CrossBorn [420<sup>2</sup>];
       CrossBorn430sq = CrossBorn[430<sup>2</sup>];
       CrossBorn440sq = CrossBorn[440<sup>2</sup>];
       CrossBorn450sq = CrossBorn[450<sup>2</sup>];
       CrossBorn460sq = CrossBorn [460<sup>2</sup>];
       CrossBorn470sq = CrossBorn [470<sup>2</sup>];
       CrossBorn480sq = CrossBorn [480<sup>2</sup>];
       CrossBorn490sq = CrossBorn[490<sup>2</sup>];
ln[1789]:= CrossBorn500sq = CrossBorn[500<sup>2</sup>];
       CrossBorn510sq = CrossBorn[510<sup>2</sup>];
       CrossBorn520sq = CrossBorn[520<sup>2</sup>];
       CrossBorn530sq = CrossBorn[530<sup>2</sup>];
       CrossBorn540sq = CrossBorn[540<sup>2</sup>];
       CrossBorn550sq = CrossBorn[550<sup>2</sup>];
       CrossBorn560sq = CrossBorn[560<sup>2</sup>];
       CrossBorn570sq = CrossBorn[570<sup>2</sup>];
       CrossBorn580sq = CrossBorn[580<sup>2</sup>];
       CrossBorn590sq = CrossBorn[590<sup>2</sup>];
ln[1799] = CrossBorn600sq = CrossBorn[600<sup>2</sup>];
       CrossBorn610sq = CrossBorn[610<sup>2</sup>];
       CrossBorn620sq = CrossBorn[620<sup>2</sup>];
       CrossBorn630sq = CrossBorn[630<sup>2</sup>];
       CrossBorn640sq = CrossBorn[640<sup>2</sup>];
       CrossBorn650sq = CrossBorn[650<sup>2</sup>];
       CrossBorn660sq = CrossBorn[660<sup>2</sup>];
       CrossBorn670sq = CrossBorn[670<sup>2</sup>];
       CrossBorn680sq = CrossBorn[680<sup>2</sup>];
       CrossBorn690sq = CrossBorn[690<sup>2</sup>];
```

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In[1809]:= CrossBorn700sq = CrossBorn[700<sup>2</sup>];
       CrossBorn710sq = CrossBorn[710<sup>2</sup>];
       CrossBorn720sq = CrossBorn[720<sup>2</sup>];
       CrossBorn730sq = CrossBorn[730<sup>2</sup>];
       CrossBorn740sq = CrossBorn[740<sup>2</sup>];
       CrossBorn750sq = CrossBorn[750<sup>2</sup>];
       CrossBorn760sq = CrossBorn[760<sup>2</sup>];
       CrossBorn770sq = CrossBorn[770<sup>2</sup>];
       CrossBorn780sq = CrossBorn[780<sup>2</sup>];
       CrossBorn790sq = CrossBorn[790<sup>2</sup>];
ln[1819] = CrossBorn800sq = CrossBorn[800^2];
       CrossBorn810sq = CrossBorn[810<sup>2</sup>];
       CrossBorn820sq = CrossBorn[820<sup>2</sup>];
       CrossBorn830sq = CrossBorn[830<sup>2</sup>];
       CrossBorn840sq = CrossBorn[840<sup>2</sup>];
       CrossBorn850sq = CrossBorn[850<sup>2</sup>];
       CrossBorn860sq = CrossBorn[860<sup>2</sup>];
       CrossBorn870sq = CrossBorn[870<sup>2</sup>];
       CrossBorn880sq = CrossBorn[880<sup>2</sup>];
       CrossBorn890sq = CrossBorn[890<sup>2</sup>];
ln[1829]:= CrossBorn900sq = CrossBorn[900<sup>2</sup>];
       CrossBorn910sq = CrossBorn[910<sup>2</sup>];
       CrossBorn920sq = CrossBorn[920<sup>2</sup>];
       CrossBorn930sq = CrossBorn[930<sup>2</sup>];
       CrossBorn940sq = CrossBorn[940<sup>2</sup>];
       CrossBorn950sq = CrossBorn[950<sup>2</sup>];
       CrossBorn960sq = CrossBorn[960<sup>2</sup>];
       CrossBorn970sq = CrossBorn[970<sup>2</sup>];
       CrossBorn980sq = CrossBorn[980<sup>2</sup>];
       CrossBorn990sq = CrossBorn[990<sup>2</sup>];
       CrossBorn1000sq = CrossBorn[1000<sup>2</sup>];
In[1840]:= As50sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 50<sup>2</sup>, g];
       As60sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 60<sup>2</sup>, g];
       As70sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 70<sup>2</sup>, g];
       As80sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 80<sup>2</sup>, g];
       As90sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 90<sup>2</sup>, g];
```

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ln(1845) = As100sq = AsRunDec[asMz/.NumDef, Mz/.NumDef, 100^2, g];
       As110sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 110<sup>2</sup>, g];
       As120sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 120<sup>2</sup>, g];
       As130sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 130<sup>2</sup>, g];
       As140sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 140<sup>2</sup>, g];
       As150sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 150<sup>2</sup>, g];
       As160sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 160<sup>2</sup>, g];
       As170sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 170<sup>2</sup>, g];
       As180sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 180<sup>2</sup>, g];
       As190sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 190<sup>2</sup>, g];
ln[1855] = As200sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 200<sup>2</sup>, g];
       As210sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 210<sup>2</sup>, g];
       As220sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 220<sup>2</sup>, g];
       As230sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 230<sup>2</sup>, g];
       As240sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 240<sup>2</sup>, g];
       As250sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 250<sup>2</sup>, g];
       As260sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 260<sup>2</sup>, g];
       As270sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 270<sup>2</sup>, g];
       As280sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 280<sup>2</sup>, g];
       As290sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 290<sup>2</sup>, g];
ln[1865]:= As300sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 300<sup>2</sup>, g];
       As310sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 310<sup>2</sup>, g];
       As320sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 320<sup>2</sup>, g];
       As330sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 330<sup>2</sup>, g];
       As340sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 340<sup>2</sup>, g];
       As350sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 350<sup>2</sup>, g];
       As360sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 360<sup>2</sup>, g];
       As370sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 370<sup>2</sup>, g];
       As380sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 380<sup>2</sup>, g];
       As390sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 390<sup>2</sup>, g];
ln[1875]: As400sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 400<sup>2</sup>, g];
       As410sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 410<sup>2</sup>, g];
       As420sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 420<sup>2</sup>, g];
       As430sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 430<sup>2</sup>, g];
       As440sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 440<sup>2</sup>, g];
       As450sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 450<sup>2</sup>, g];
       As460sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 460<sup>2</sup>, g];
       As470sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 470<sup>2</sup>, g];
       As480sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 480<sup>2</sup>, g];
       As490sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 490<sup>2</sup>, g];
```

```
ln(1885) = As500sq = AsRunDec[asMz/.NumDef, Mz/.NumDef, 500^2, g];
       As510sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 510<sup>2</sup>, g];
       As520sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 520<sup>2</sup>, g];
       As530sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 530<sup>2</sup>, g];
       As540sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 540<sup>2</sup>, g];
       As550sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 550<sup>2</sup>, g];
       As560sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 560<sup>2</sup>, g];
       As570sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 570<sup>2</sup>, g];
       As580sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 580<sup>2</sup>, g];
       As590sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 590<sup>2</sup>, g];
ln[1895] = As600sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 600<sup>2</sup>, g];
       As610sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 610<sup>2</sup>, g];
       As620sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 620<sup>2</sup>, g];
       As630sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 630<sup>2</sup>, g];
       As640sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 640<sup>2</sup>, g];
       As650sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 650<sup>2</sup>, g];
       As660sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 660<sup>2</sup>, g];
       As670sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 670<sup>2</sup>, g];
       As680sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 680<sup>2</sup>, g];
       As690sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 690<sup>2</sup>, g];
ln[1905] = As700sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 700<sup>2</sup>, g];
       As710sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 710<sup>2</sup>, g];
       As720sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 720<sup>2</sup>, g];
       As730sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 730<sup>2</sup>, g];
       As740sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 740<sup>2</sup>, g];
       As750sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 750<sup>2</sup>, g];
       As760sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 760<sup>2</sup>, g];
       As770sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 770<sup>2</sup>, g];
       As780sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 780<sup>2</sup>, g];
       As790sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 790<sup>2</sup>, g];
ln[1915]= As800sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 800<sup>2</sup>, g];
       As810sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 810<sup>2</sup>, g];
       As820sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 820<sup>2</sup>, g];
       As830sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 830<sup>2</sup>, g];
       As840sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 840<sup>2</sup>, g];
       As850sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 850<sup>2</sup>, g];
       As860sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 860<sup>2</sup>, g];
       As870sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 870<sup>2</sup>, g];
       As880sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 880<sup>2</sup>, g];
       As890sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 890<sup>2</sup>, g];
```

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ln[1925]: As900sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 900<sup>2</sup>, g];
         As910sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 910<sup>2</sup>, g];
         As920sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 920<sup>2</sup>, g];
         As930sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 930<sup>2</sup>, g];
         As940sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 940<sup>2</sup>, g];
         As950sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 950<sup>2</sup>, g];
         As960sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 960<sup>2</sup>, g];
         As970sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 970<sup>2</sup>, g];
         As980sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 980<sup>2</sup>, g];
         As990sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 990<sup>2</sup>, g];
         As1000sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1000<sup>2</sup>, g];
In[1936]:= Correction50sq = \left(1 + \frac{3 \text{ As50sq}}{4 \pi} C_F\right);
         Correction60sq = \left(1 + \frac{3 \text{ As60sq}}{4 \pi} C_F\right);
         Correction70sq = \left(1 + \frac{3 \text{ As70sq}}{4 \pi} C_F\right);
         Correction80sq = \left(1 + \frac{3 \text{ As80sq}}{4 \pi} C_F\right);
         Correction 90 sq = \left(1 + \frac{3 \text{ As } 90 \text{ sq}}{4 - 100 \text{ cg}}\right);
ln[1941] = Correction100sq = \left(1 + \frac{3 As100sq}{4 \pi} C_F\right);
         Correction110sq = \left(1 + \frac{3 \text{ As110sq}}{4 \pi} C_F\right);
         Correction120sq = \left(1 + \frac{3 \text{ As120sq}}{4 \pi} C_F\right);
         Correction130sq = \left(1 + \frac{3 \text{ As130sq}}{4 \pi} C_F\right);
         Correction140sq = \left(1 + \frac{3 \text{ As140sq}}{4 \pi} C_F\right);
         Correction150sq = \left(1 + \frac{3 \text{ As150sq}}{4 \pi} C_F\right);
         Correction160sq = \left(1 + \frac{3 \text{ As160sq}}{4 \pi} C_F\right);
         Correction170sq = \left(1 + \frac{3 \text{ As170sq}}{4 \pi} C_F\right);
         Correction180sq = \left(1 + \frac{3 \text{ As180sq}}{4 \pi} C_F\right);
         Correction190sq = \left(1 + \frac{3 \text{ As190sq}}{4 \pi} C_F\right);
```

$$\begin{array}{l} \text{In[1951]=} & \text{Correction200sq} = \left(1 + \frac{3 \text{ As200sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction210sq} = \left(1 + \frac{3 \text{ As210sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction220sq} = \left(1 + \frac{3 \text{ As220sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction230sq} = \left(1 + \frac{3 \text{ As230sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction240sq} = \left(1 + \frac{3 \text{ As240sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction250sq} = \left(1 + \frac{3 \text{ As250sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction260sq} = \left(1 + \frac{3 \text{ As260sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction270sq} = \left(1 + \frac{3 \text{ As270sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction280sq} = \left(1 + \frac{3 \text{ As280sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction300sq} = \left(1 + \frac{3 \text{ As300sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction310sq} = \left(1 + \frac{3 \text{ As310sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction320sq} = \left(1 + \frac{3 \text{ As330sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction330sq} = \left(1 + \frac{3 \text{ As330sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction340sq} = \left(1 + \frac{3 \text{ As330sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction350sq} = \left(1 + \frac{3 \text{ As330sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction350sq} = \left(1 + \frac{3 \text{ As330sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction350sq} = \left(1 + \frac{3 \text{ As330sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{Correction360sq} = \left(1 + \frac{3 \text{ As360$$

Correction370sq =  $\left(1 + \frac{3 \text{ As370sq}}{4 \pi} C_F\right)$ ;

Correction380sq =  $\left(1 + \frac{3 \text{ As380sq}}{4 \pi} C_F\right)$ ;

Correction390sq =  $\left(1 + \frac{3 \text{ As390sq}}{4 \pi} C_F\right)$ ;

In[1971]:= Correction400sq = 
$$\left(1 + \frac{3 \text{ As400sq}}{4 \pi} \text{ C}_F\right)$$
;

Correction410sq =  $\left(1 + \frac{3 \text{ As410sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction420sq =  $\left(1 + \frac{3 \text{ As420sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction430sq =  $\left(1 + \frac{3 \text{ As430sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction440sq =  $\left(1 + \frac{3 \text{ As440sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction450sq =  $\left(1 + \frac{3 \text{ As450sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction460sq =  $\left(1 + \frac{3 \text{ As460sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction470sq =  $\left(1 + \frac{3 \text{ As470sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction480sq =  $\left(1 + \frac{3 \text{ As480sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction490sq =  $\left(1 + \frac{3 \text{ As480sq}}{4 \pi} \text{ C}_F\right)$ ;

$$\begin{array}{l} \text{In} [1981] \coloneqq \text{ Correction500sq} = \left(1 + \frac{3 \text{ As500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction510sq} = \left(1 + \frac{3 \text{ As510sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction520sq} = \left(1 + \frac{3 \text{ As520sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction530sq} = \left(1 + \frac{3 \text{ As530sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction540sq} = \left(1 + \frac{3 \text{ As540sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction550sq} = \left(1 + \frac{3 \text{ As550sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction560sq} = \left(1 + \frac{3 \text{ As550sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction570sq} = \left(1 + \frac{3 \text{ As550sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction580sq} = \left(1 + \frac{3 \text{ As550sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As550sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As550sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As550sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As550sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As5500sq}}{4 \, \pi} \text{$$

$$| \text{In}[1991] = \text{Correction} 600 \text{sq} = \left(1 + \frac{3 \text{ As} 600 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 610 \text{sq} = \left(1 + \frac{3 \text{ As} 610 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 620 \text{sq} = \left(1 + \frac{3 \text{ As} 620 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 630 \text{sq} = \left(1 + \frac{3 \text{ As} 630 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 640 \text{sq} = \left(1 + \frac{3 \text{ As} 640 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 650 \text{sq} = \left(1 + \frac{3 \text{ As} 650 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 660 \text{sq} = \left(1 + \frac{3 \text{ As} 660 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 680 \text{sq} = \left(1 + \frac{3 \text{ As} 680 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 690 \text{sq} = \left(1 + \frac{3 \text{ As} 690 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 710 \text{sq} = \left(1 + \frac{3 \text{ As} 700 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 720 \text{sq} = \left(1 + \frac{3 \text{ As} 700 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 730 \text{sq} = \left(1 + \frac{3 \text{ As} 730 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 740 \text{sq} = \left(1 + \frac{3 \text{ As} 740 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 750 \text{sq} = \left(1 + \frac{3 \text{ As} 750 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 760 \text{sq} = \left(1 + \frac{3 \text{ As} 760 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 760 \text{sq} = \left(1 + \frac{3 \text{ As} 760 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 770 \text{sq} = \left(1 + \frac{3 \text{ As} 770 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 770 \text{sq} = \left(1 + \frac{3 \text{ As} 780 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 770 \text{sq} = \left(1 + \frac{3 \text{ As} 780 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 770 \text{sq} = \left(1 + \frac{3 \text{ As} 770 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$| \text{Correction} 780 \text{sq} = \left(1 + \frac{3 \text{ As} 780 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

Correction790sq =  $\left(1 + \frac{3 \text{ As790sq}}{4 \pi} C_F\right)$ ;

```
In[2032]:= PlotCross50sq = CrossBorn50sq * Correction50sq;
      PlotCross60sq = CrossBorn60sq * Correction60sq;
      PlotCross70sq = CrossBorn70sq * Correction70sq;
      PlotCross80sq = CrossBorn80sq * Correction80sq;
      PlotCross90sq = CrossBorn90sq * Correction90sq;
In[2037]:= PlotCross100sq = CrossBorn100sq * Correction100sq;
      PlotCross110sq = CrossBorn110sq * Correction110sq;
      PlotCross120sq = CrossBorn120sq * Correction120sq;
      PlotCross130sq = CrossBorn130sq * Correction130sq;
      PlotCross140sq = CrossBorn140sq * Correction140sq;
      PlotCross150sq = CrossBorn150sq * Correction150sq;
      PlotCross160sq = CrossBorn160sq * Correction160sq;
      PlotCross170sq = CrossBorn170sq * Correction170sq;
      PlotCross180sq = CrossBorn180sq * Correction180sq;
      PlotCross190sq = CrossBorn190sq * Correction190sq;
In[2047]:= PlotCross200sq = CrossBorn200sq * Correction200sq;
      PlotCross210sq = CrossBorn210sq * Correction210sq;
      PlotCross220sq = CrossBorn220sq * Correction220sq;
      PlotCross230sq = CrossBorn230sq * Correction230sq;
      PlotCross240sq = CrossBorn240sq * Correction240sq;
      PlotCross250sq = CrossBorn250sq * Correction250sq;
      PlotCross260sq = CrossBorn260sq * Correction260sq;
      PlotCross270sq = CrossBorn270sq * Correction270sq;
      PlotCross280sq = CrossBorn280sq * Correction280sq;
      PlotCross290sq = CrossBorn290sq * Correction290sq;
In[2057]:= PlotCross300sq = CrossBorn300sq * Correction300sq;
      PlotCross310sq = CrossBorn310sq * Correction310sq;
      PlotCross320sq = CrossBorn320sq * Correction320sq;
      PlotCross330sq = CrossBorn330sq * Correction330sq;
      PlotCross340sq = CrossBorn340sq * Correction340sq;
      PlotCross350sq = CrossBorn350sq * Correction350sq;
      PlotCross360sq = CrossBorn360sq * Correction360sq;
```

PlotCross370sq = CrossBorn370sq \* Correction370sq; PlotCross380sq = CrossBorn380sq \* Correction380sq; PlotCross390sq = CrossBorn390sq \* Correction390sq;

```
In[2067]:= PlotCross400sq = CrossBorn400sq * Correction400sq;
      PlotCross410sq = CrossBorn410sq * Correction410sq;
      PlotCross420sq = CrossBorn420sq * Correction420sq;
      PlotCross430sq = CrossBorn430sq * Correction430sq;
      PlotCross440sq = CrossBorn440sq * Correction440sq;
      PlotCross450sq = CrossBorn450sq * Correction450sq;
      PlotCross460sq = CrossBorn460sq * Correction460sq;
      PlotCross470sq = CrossBorn470sq * Correction470sq;
      PlotCross480sq = CrossBorn480sq * Correction480sq;
      PlotCross490sq = CrossBorn490sq * Correction490sq;
In[2077]:= PlotCross500sq = CrossBorn500sq * Correction500sq;
      PlotCross510sq = CrossBorn510sq * Correction510sq;
      PlotCross520sq = CrossBorn520sq * Correction520sq;
      PlotCross530sq = CrossBorn530sq * Correction530sq;
      PlotCross540sq = CrossBorn540sq * Correction540sq;
      PlotCross550sq = CrossBorn550sq * Correction550sq;
      PlotCross560sq = CrossBorn560sq * Correction560sq;
      PlotCross570sq = CrossBorn570sq * Correction570sq;
      PlotCross580sq = CrossBorn580sq * Correction580sq;
      PlotCross590sq = CrossBorn590sq * Correction590sq;
In[2087]:= PlotCross600sq = CrossBorn600sq * Correction600sq;
      PlotCross610sq = CrossBorn610sq * Correction610sq;
      PlotCross620sq = CrossBorn620sq * Correction620sq;
      PlotCross630sq = CrossBorn630sq * Correction630sq;
      PlotCross640sq = CrossBorn640sq * Correction640sq;
      PlotCross650sq = CrossBorn650sq * Correction650sq;
      PlotCross660sq = CrossBorn660sq * Correction660sq;
      PlotCross670sq = CrossBorn670sq * Correction670sq;
      PlotCross680sq = CrossBorn680sq * Correction680sq;
      PlotCross690sq = CrossBorn690sq * Correction690sq;
```

```
In[2097]:= PlotCross700sq = CrossBorn700sq * Correction700sq;
      PlotCross710sq = CrossBorn710sq * Correction710sq;
     PlotCross720sq = CrossBorn720sq * Correction720sq;
     PlotCross730sq = CrossBorn730sq * Correction730sq;
      PlotCross740sq = CrossBorn740sq * Correction740sq;
      PlotCross750sq = CrossBorn750sq * Correction750sq;
      PlotCross760sq = CrossBorn760sq * Correction760sq;
     PlotCross770sq = CrossBorn770sq * Correction770sq;
     PlotCross780sq = CrossBorn780sq * Correction780sq;
      PlotCross790sq = CrossBorn790sq * Correction790sq;
In[2107]:= PlotCross800sq = CrossBorn800sq * Correction800sq;
     PlotCross810sq = CrossBorn810sq * Correction810sq;
     PlotCross820sq = CrossBorn820sq * Correction820sq;
     PlotCross830sq = CrossBorn830sq * Correction830sq;
     PlotCross840sq = CrossBorn840sq * Correction840sq;
      PlotCross850sq = CrossBorn850sq * Correction850sq;
     PlotCross860sq = CrossBorn860sq * Correction860sq;
      PlotCross870sq = CrossBorn870sq * Correction870sq;
      PlotCross880sq = CrossBorn880sq * Correction880sq;
      PlotCross890sq = CrossBorn890sq * Correction890sq;
In[2117]:= PlotCross900sq = CrossBorn900sq * Correction900sq;
     PlotCross910sq = CrossBorn910sq * Correction910sq;
     PlotCross920sq = CrossBorn920sq * Correction920sq;
     PlotCross930sq = CrossBorn930sq * Correction930sq;
      PlotCross940sq = CrossBorn940sq * Correction940sq;
     PlotCross950sq = CrossBorn950sq * Correction950sq;
      PlotCross960sq = CrossBorn960sq * Correction960sq;
      PlotCross970sq = CrossBorn970sq * Correction970sq;
      PlotCross980sq = CrossBorn980sq * Correction980sq;
     PlotCross990sq = CrossBorn990sq * Correction990sq;
     PlotCross1000sq = CrossBorn1000sq * Correction1000sq;
```

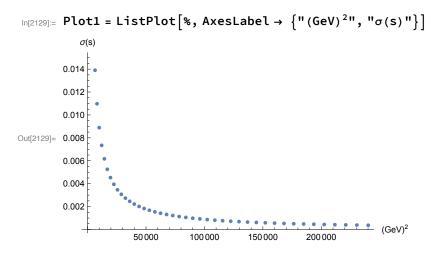
#### Plot Cross Section $\alpha_s$ (s), 2 Loops

In[2128]:=

```
Table1 = TableForm[\{\{50^2, PlotCross50sq\}, \{60^2, PlotCross60sq\}, \{70^2, PlotCross70sq\}, \{60^2, PlotCross60sq\}, 
            {80<sup>2</sup>, PlotCross80sq}, {90<sup>2</sup>, PlotCross90sq}, {100<sup>2</sup>, PlotCross100sq},
            {110<sup>2</sup>, PlotCross110sq}, {120<sup>2</sup>, PlotCross120sq}, {130<sup>2</sup>, PlotCross130sq},
            {140<sup>2</sup>, PlotCross140sq}, {150<sup>2</sup>, PlotCross150sq}, {160<sup>2</sup>, PlotCross160sq},
            {170<sup>2</sup>, PlotCross170sq}, {180<sup>2</sup>, PlotCross180sq}, {190<sup>2</sup>, PlotCross190sq},
            {200<sup>2</sup>, PlotCross200sq}, {210<sup>2</sup>, PlotCross210sq}, {220<sup>2</sup>, PlotCross220sq},
            {230<sup>2</sup>, PlotCross230sq}, {240<sup>2</sup>, PlotCross240sq}, {250<sup>2</sup>, PlotCross250sq},
            {260<sup>2</sup>, PlotCross260sq}, {270<sup>2</sup>, PlotCross270sq}, {280<sup>2</sup>, PlotCross280sq},
            {290<sup>2</sup>, PlotCross290sq}, {300<sup>2</sup>, PlotCross300sq}, {310<sup>2</sup>, PlotCross310sq},
            {320<sup>2</sup>, PlotCross320sq}, {330<sup>2</sup>, PlotCross330sq}, {340<sup>2</sup>, PlotCross340sq},
            {350<sup>2</sup>, PlotCross350sq}, {360<sup>2</sup>, PlotCross360sq}, {370<sup>2</sup>, PlotCross370sq},
            {380<sup>2</sup>, PlotCross380sq}, {390<sup>2</sup>, PlotCross390sq}, {400<sup>2</sup>, PlotCross400sq},
            {410<sup>2</sup>, PlotCross410sq}, {420<sup>2</sup>, PlotCross420sq}, {430<sup>2</sup>, PlotCross430sq},
            {440<sup>2</sup>, PlotCross440sq}, {450<sup>2</sup>, PlotCross450sq}, {460<sup>2</sup>, PlotCross460sq},
            {470<sup>2</sup>, PlotCross470sq}, {480<sup>2</sup>, PlotCross480sq}, {490<sup>2</sup>, PlotCross490sq}},
       TableHeadings \rightarrow {None, {"(GeV)<sup>2</sup>", "\sigma(s)"}}]
```

Out[2128]//TableForm=

(GeV) <sup>2</sup>	$\sigma(s)$
2500	0.03565653548514648880695
3600	0.02474119068343484478141
4900	0.01816534202561793174945
6400	0.01390036324118763235666
8100	0.01097801251256019782107
10000	0.00888870745269605077281
12 100	0.00734352047954567084093
14 400	0.00616872137529201211145
16900	0.00525475726032605392609
19 600	0.004529772495076414135243
22 500	0.003945050799223668694150
25 600	0.003466617585186924463929
28 900	0.003070194054032957624022
32 400	0.002738057013939467450876
36 100	0.002457024153853344449143
40 000	0.002217126333454707344272
44 100	0.002010711642053881933879
48 400	0.001831827911352092814900
52 900	0.001675788998910741974454
57 600	0.001538864896475641146718
62 500	0.001418056850789147715682
67 600	0.001310931852868189190487
72 900	0.001215499236830135548769
78 400	0.001130117575204063902339
84 100	0.001053423659099270936899
90000	0.000984277773177927934506
96 100	0.000921721128750195805332
102 400	0.000864942463279951194077
108 900	0.000813251617975636249249
115 600	0.000766058475783342147642
122 500	0.000722856052073144606128
129 600	0.000683206828009561903438
136 900	0.000646731634940410653972
144 400	0.000613100559788484951471
152 100	0.000582025462169004874852
160 000 168 100	0.000553253784890405463099 0.0005265634085239783039038
176 400 184 900	0.0005017583535174022683682 0.0004786651739834645567676
	0.0004780651739834645367676
193 600 202 500	0.0004370155603860245242566
202500	0.0004181998103552220366206
220 900	0.0004181998103552220366206
230 400	0.0003840377739235621191843
240 100	0.0003840377739235621191843
240 I00	0.00030030314/034033032220/

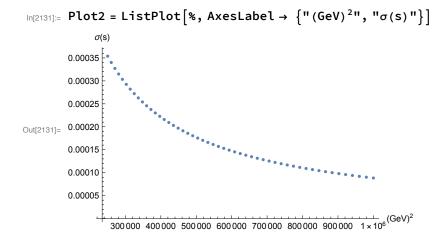


```
In[2130]:= Table2 =
```

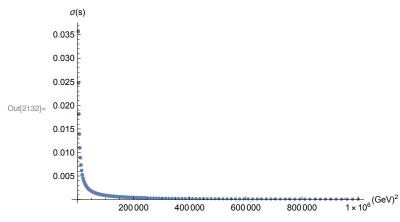
```
TableForm[\{\{500^2, PlotCross500sq\}, \{510^2, PlotCross510sq\}, \{520^2, PlotCross520sq\},
   {530<sup>2</sup>, PlotCross530sq}, {540<sup>2</sup>, PlotCross540sq}, {550<sup>2</sup>, PlotCross550sq},
   {560<sup>2</sup>, PlotCross560sq}, {570<sup>2</sup>, PlotCross570sq}, {580<sup>2</sup>, PlotCross580sq},
   {590<sup>2</sup>, PlotCross590sq}, {600<sup>2</sup>, PlotCross600sq}, {610<sup>2</sup>, PlotCross610sq},
   {620<sup>2</sup>, PlotCross620sq}, {630<sup>2</sup>, PlotCross630sq}, {640<sup>2</sup>, PlotCross640sq},
   {650<sup>2</sup>, PlotCross650sq}, {660<sup>2</sup>, PlotCross660sq}, {670<sup>2</sup>, PlotCross670sq},
   {680<sup>2</sup>, PlotCross680sq}, {690<sup>2</sup>, PlotCross690sq}, {700<sup>2</sup>, PlotCross700sq},
   {710<sup>2</sup>, PlotCross710sq}, {720<sup>2</sup>, PlotCross720sq}, {730<sup>2</sup>, PlotCross730sq},
   {740<sup>2</sup>, PlotCross740sq}, {750<sup>2</sup>, PlotCross750sq}, {760<sup>2</sup>, PlotCross760sq},
   {770<sup>2</sup>, PlotCross770sq}, {780<sup>2</sup>, PlotCross780sq}, {790<sup>2</sup>, PlotCross790sq},
   {800<sup>2</sup>, PlotCross800sq}, {810<sup>2</sup>, PlotCross810sq}, {820<sup>2</sup>, PlotCross820sq},
   {830<sup>2</sup>, PlotCross830sq}, {840<sup>2</sup>, PlotCross840sq}, {850<sup>2</sup>, PlotCross850sq},
   {860<sup>2</sup>, PlotCross860sq}, {870<sup>2</sup>, PlotCross870sq}, {880<sup>2</sup>, PlotCross880sq},
   {890<sup>2</sup>, PlotCross890sq}, {900<sup>2</sup>, PlotCross900sq}, {910<sup>2</sup>, PlotCross910sq},
   {920<sup>2</sup>, PlotCross920sq}, {930<sup>2</sup>, PlotCross930sq}, {940<sup>2</sup>, PlotCross940sq},
   {950<sup>2</sup>, PlotCross950sq}, {960<sup>2</sup>, PlotCross960sq}, {970<sup>2</sup>, PlotCross970sq},
   {980^2, PlotCross980sq}, {990^2, PlotCross990sq}, {1000^2, PlotCross1000sq}},
 TableHeadings \rightarrow {None, {"(GeV)<sup>2</sup>", "\sigma(s)"}}]
```

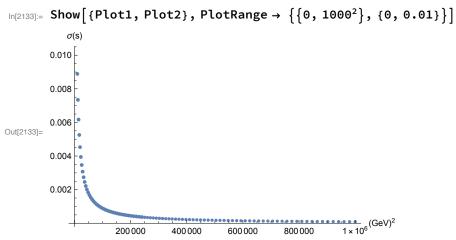
Out[2130]//TableForm=

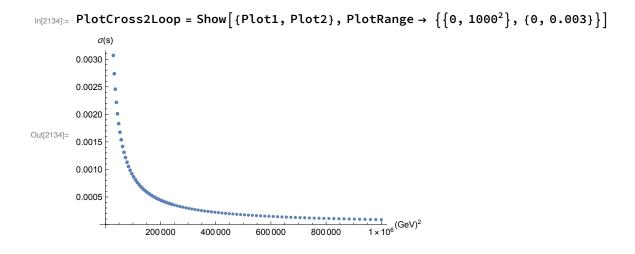
Jiii abiei oiiii=	
(GeV) <sup>2</sup>	$\sigma(s)$
250 000	0.0003538959037497477247292
260 100	0.0003401382860453873465142
270 400	0.0003271673750764959206769
280 900	0.0003149243209428577202867
291 600	0.0003033556749413086575968
302 500	0.0002924128054795029687586
313 600	0.0002924128034793029087380
324 900	0.0002722309474341160903855
336 400	0.0002629144788893210696820
348 100	0.0002540680822938561384707
360 000	0.0002456606618850019547138
372 100	0.0002376636510592280443608
384 400	0.0002300507694940412894614
396 900	0.0002227978070505946527038
409 600	0.0002158824311347640142342
422 500	0.0002092840146509655129045
435 600	0.0002029834820708866188923
448 900	0.0001969631714697324337597
462 400	0.0001912067106647736217729
476 100	0.0001856989058325603332323
490 000	0.0001804256411884740405029
504 100	0.0001753737884905988203842
518 400	0.0001705311252836056581882
532 900	0.0001658862609311393855807
547 600	0.0001614285696001663478875
562 500	0.0001571481294604796141143
577 600	0.0001571481254004750141145
592 900	0.0001330330074492370978270
608 400	0.0001450825050200830753634
624 100	0.0001416221268455244386003
640 000	0.0001381001545028978909747
656 100	0.0001347079156462604010872
672 400	0.0001314391167621441559521
688 900	0.0001282878413590495160661
705 600	0.0001252485231869791987851
722 500	0.0001223159216501877112162
739 600	0.0001194850992102538116335
756 900	0.0001167514005974571166318
774 400	0.0001141104336669543637750
792 100	0.0001115580517526962072395
810000	0.0001090903373866532848325
828 100	0.0001067035872639491652503
846 400	0.0001043942983461179058064
864 900	0.0001021591550050810198386
883 600	0.0000999950171197174287176
902 500	0.0000978989090452069146097
921600	0.0000958680093827736280533
940 900	0.0000938996414841383183755
960 400	0.0000919912646309915982091
980 100	0.0000901404658352006566497
1000000	0.0000883449522103245579091
1000000	1.1100000 1.00221002 10010001











# Run Cross Section $\alpha_s$ (s), 3 Loops

```
In[2135]:= g = 3;
        \alpha = 1/137;
        Conversion = 389 379;
        n = 3;
       C_F = \frac{n^2 - 1}{2 n};
       Born = \frac{4\pi\alpha^2}{3s};
In[2141]:= CrossBorn[s_] = Conversion * Born;
        CrossBorn50sq = CrossBorn[50<sup>2</sup>];
        CrossBorn60sq = CrossBorn[60<sup>2</sup>];
        CrossBorn70sq = CrossBorn[70<sup>2</sup>];
        CrossBorn80sq = CrossBorn[80<sup>2</sup>];
        CrossBorn90sq = CrossBorn[90<sup>2</sup>];
ln[2147] = CrossBorn100sq = CrossBorn[100<sup>2</sup>];
        CrossBorn110sq = CrossBorn[110<sup>2</sup>];
        CrossBorn120sq = CrossBorn[120<sup>2</sup>];
        CrossBorn130sq = CrossBorn[130<sup>2</sup>];
        CrossBorn140sq = CrossBorn[140<sup>2</sup>];
        CrossBorn150sq = CrossBorn[150<sup>2</sup>];
        CrossBorn160sq = CrossBorn[160<sup>2</sup>];
        CrossBorn170sq = CrossBorn[170<sup>2</sup>];
        CrossBorn180sq = CrossBorn[180<sup>2</sup>];
        CrossBorn190sq = CrossBorn[190<sup>2</sup>];
```

```
ln[2157] = CrossBorn200sq = CrossBorn[200<sup>2</sup>];
        CrossBorn210sq = CrossBorn[210<sup>2</sup>];
        CrossBorn220sq = CrossBorn[220<sup>2</sup>];
        CrossBorn230sq = CrossBorn[230<sup>2</sup>];
        CrossBorn240sg = CrossBorn[240<sup>2</sup>];
        CrossBorn250sq = CrossBorn[250<sup>2</sup>];
        CrossBorn260sq = CrossBorn[260<sup>2</sup>];
        CrossBorn270sq = CrossBorn[270<sup>2</sup>];
        CrossBorn280sq = CrossBorn[280<sup>2</sup>];
        CrossBorn290sq = CrossBorn[290<sup>2</sup>];
ln[2167]:= CrossBorn300sq = CrossBorn[300<sup>2</sup>];
        CrossBorn310sq = CrossBorn[310<sup>2</sup>];
        CrossBorn320sq = CrossBorn[320<sup>2</sup>];
        CrossBorn330sq = CrossBorn[330<sup>2</sup>];
        CrossBorn340sq = CrossBorn[340<sup>2</sup>];
        CrossBorn350sq = CrossBorn[350<sup>2</sup>];
        CrossBorn360sq = CrossBorn[360<sup>2</sup>];
        CrossBorn370sq = CrossBorn[370<sup>2</sup>];
        CrossBorn380sq = CrossBorn[380<sup>2</sup>];
        CrossBorn390sq = CrossBorn[390<sup>2</sup>];
ln[2177]:= CrossBorn400sq = CrossBorn[400<sup>2</sup>];
        CrossBorn410sq = CrossBorn[410<sup>2</sup>];
        CrossBorn420sq = CrossBorn [420<sup>2</sup>];
        CrossBorn430sq = CrossBorn [430<sup>2</sup>];
        CrossBorn440sq = CrossBorn [440<sup>2</sup>];
        CrossBorn450sq = CrossBorn[450<sup>2</sup>];
        CrossBorn460sq = CrossBorn [460<sup>2</sup>];
        CrossBorn470sq = CrossBorn [470<sup>2</sup>];
        CrossBorn480sq = CrossBorn [480<sup>2</sup>];
        CrossBorn490sq = CrossBorn[490<sup>2</sup>];
ln[2187] = CrossBorn500sq = CrossBorn[500<sup>2</sup>];
        CrossBorn510sq = CrossBorn[510<sup>2</sup>];
        CrossBorn520sq = CrossBorn[520<sup>2</sup>];
        CrossBorn530sq = CrossBorn[530<sup>2</sup>];
        CrossBorn540sq = CrossBorn[540<sup>2</sup>];
        CrossBorn550sq = CrossBorn[550<sup>2</sup>];
        CrossBorn560sq = CrossBorn[560<sup>2</sup>];
        CrossBorn570sq = CrossBorn[570<sup>2</sup>];
        CrossBorn580sq = CrossBorn[580<sup>2</sup>];
        CrossBorn590sq = CrossBorn[590<sup>2</sup>];
```

```
ln[2197] = CrossBorn600sq = CrossBorn[600<sup>2</sup>];
       CrossBorn610sq = CrossBorn[610<sup>2</sup>];
       CrossBorn620sq = CrossBorn[620<sup>2</sup>];
       CrossBorn630sq = CrossBorn[630<sup>2</sup>];
       CrossBorn640sq = CrossBorn[640<sup>2</sup>];
       CrossBorn650sq = CrossBorn[650<sup>2</sup>];
       CrossBorn660sq = CrossBorn[660<sup>2</sup>];
       CrossBorn670sq = CrossBorn[670<sup>2</sup>];
       CrossBorn680sq = CrossBorn[680<sup>2</sup>];
       CrossBorn690sq = CrossBorn[690<sup>2</sup>];
ln[2207]:= CrossBorn700sq = CrossBorn[700<sup>2</sup>];
       CrossBorn710sq = CrossBorn[710<sup>2</sup>];
       CrossBorn720sq = CrossBorn[720<sup>2</sup>];
       CrossBorn730sq = CrossBorn[730<sup>2</sup>];
       CrossBorn740sq = CrossBorn[740<sup>2</sup>];
       CrossBorn750sq = CrossBorn[750<sup>2</sup>];
       CrossBorn760sq = CrossBorn[760<sup>2</sup>];
       CrossBorn770sq = CrossBorn[770<sup>2</sup>];
       CrossBorn780sq = CrossBorn[780<sup>2</sup>];
       CrossBorn790sq = CrossBorn[790<sup>2</sup>];
ln[2217] = CrossBorn800sq = CrossBorn[800<sup>2</sup>];
       CrossBorn810sq = CrossBorn[810<sup>2</sup>];
       CrossBorn820sq = CrossBorn[820<sup>2</sup>];
       CrossBorn830sq = CrossBorn[830<sup>2</sup>];
       CrossBorn840sq = CrossBorn[840<sup>2</sup>];
       CrossBorn850sq = CrossBorn[850<sup>2</sup>];
       CrossBorn860sq = CrossBorn[860<sup>2</sup>];
       CrossBorn870sq = CrossBorn[870<sup>2</sup>];
       CrossBorn880sq = CrossBorn[880<sup>2</sup>];
       CrossBorn890sq = CrossBorn[890<sup>2</sup>];
```

```
ln[2227]:= CrossBorn900sq = CrossBorn[900<sup>2</sup>];
       CrossBorn910sq = CrossBorn[910<sup>2</sup>];
       CrossBorn920sq = CrossBorn[920<sup>2</sup>];
       CrossBorn930sq = CrossBorn[930<sup>2</sup>];
       CrossBorn940sq = CrossBorn[940<sup>2</sup>];
       CrossBorn950sq = CrossBorn[950<sup>2</sup>];
       CrossBorn960sq = CrossBorn[960<sup>2</sup>];
       CrossBorn970sq = CrossBorn[970<sup>2</sup>];
       CrossBorn980sq = CrossBorn[980<sup>2</sup>];
       CrossBorn990sq = CrossBorn[990<sup>2</sup>];
       CrossBorn1000sq = CrossBorn[1000<sup>2</sup>];
In[2238]:= As50sq = AsRunDec [asMz /. NumDef, Mz /. NumDef, 50<sup>2</sup>, g];
       As60sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 60<sup>2</sup>, g];
       As70sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 70<sup>2</sup>, g];
       As80sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 80<sup>2</sup>, g];
       As90sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 90<sup>2</sup>, g];
ln[2243]:= As100sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 100<sup>2</sup>, g];
       As110sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 110<sup>2</sup>, g];
       As120sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 120<sup>2</sup>, g];
       As130sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 130<sup>2</sup>, g];
       As140sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 140<sup>2</sup>, g];
       As150sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 150<sup>2</sup>, g];
       As160sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 160<sup>2</sup>, g];
       As170sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 170<sup>2</sup>, g];
       As180sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 180<sup>2</sup>, g];
       As190sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 190<sup>2</sup>, g];
ln[2253]:= As200sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 200<sup>2</sup>, g];
       As210sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 210<sup>2</sup>, g];
       As220sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 220<sup>2</sup>, g];
       As230sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 230<sup>2</sup>, g];
       As240sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 240<sup>2</sup>, g];
       As250sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 250<sup>2</sup>, g];
       As260sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 260<sup>2</sup>, g];
       As270sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 270<sup>2</sup>, g];
       As280sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 280<sup>2</sup>, g];
       As290sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 290<sup>2</sup>, g];
```

```
|n|_{2263}|_{=} As300sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 300<sup>2</sup>, g];
       As310sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 310<sup>2</sup>, g];
       As320sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 320<sup>2</sup>, g];
       As330sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 330<sup>2</sup>, g];
       As340sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 340<sup>2</sup>, g];
       As350sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 350<sup>2</sup>, g];
       As360sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 360<sup>2</sup>, g];
       As370sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 370<sup>2</sup>, g];
       As380sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 380<sup>2</sup>, g];
       As390sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 390<sup>2</sup>, g];
ln[2273] = As400sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 400<sup>2</sup>, g];
       As410sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 410<sup>2</sup>, g];
       As420sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 420<sup>2</sup>, g];
       As430sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 430<sup>2</sup>, g];
       As440sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 440<sup>2</sup>, g];
       As450sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 450<sup>2</sup>, g];
       As460sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 460<sup>2</sup>, g];
       As470sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 470<sup>2</sup>, g];
       As480sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 480<sup>2</sup>, g];
       As490sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 490<sup>2</sup>, g];
ln[2283] = As500sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 500<sup>2</sup>, g];
       As510sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 510<sup>2</sup>, g];
       As520sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 520<sup>2</sup>, g];
       As530sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 530<sup>2</sup>, g];
       As540sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 540<sup>2</sup>, g];
       As550sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 550<sup>2</sup>, g];
       As560sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 560<sup>2</sup>, g];
       As570sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 570<sup>2</sup>, g];
       As580sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 580<sup>2</sup>, g];
       As590sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5902, g];
ln[2293] = As600sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 600<sup>2</sup>, g];
       As610sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 610<sup>2</sup>, g];
       As620sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 620<sup>2</sup>, g];
       As630sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 630<sup>2</sup>, g];
       As640sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 640<sup>2</sup>, g];
       As650sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 650<sup>2</sup>, g];
       As660sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 660<sup>2</sup>, g];
       As670sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 670<sup>2</sup>, g];
       As680sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 680<sup>2</sup>, g];
       As690sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 690<sup>2</sup>, g];
```

```
ln[2303] = As700sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 700<sup>2</sup>, g];
       As710sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 710<sup>2</sup>, g];
       As720sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 720<sup>2</sup>, g];
       As730sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 730<sup>2</sup>, g];
       As740sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 740<sup>2</sup>, g];
       As750sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 750<sup>2</sup>, g];
       As760sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 760<sup>2</sup>, g];
       As770sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 770<sup>2</sup>, g];
       As780sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 780<sup>2</sup>, g];
       As790sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 790<sup>2</sup>, g];
ln[2313] = As800sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 800<sup>2</sup>, g];
       As810sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 810<sup>2</sup>, g];
       As820sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 820<sup>2</sup>, g];
       As830sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 830<sup>2</sup>, g];
       As840sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 840<sup>2</sup>, g];
       As850sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 850<sup>2</sup>, g];
       As860sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 860<sup>2</sup>, g];
       As870sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 870<sup>2</sup>, g];
       As880sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 880<sup>2</sup>, g];
       As890sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 890<sup>2</sup>, g];
ln[2323] = As900sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 900<sup>2</sup>, g];
       As910sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 910<sup>2</sup>, g];
       As920sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 920<sup>2</sup>, g];
       As930sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 930<sup>2</sup>, g];
       As940sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 940<sup>2</sup>, g];
       As950sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 950<sup>2</sup>, g];
       As960sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 960<sup>2</sup>, g];
       As970sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 970<sup>2</sup>, g];
       As980sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 980<sup>2</sup>, g];
       As990sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 990<sup>2</sup>, g];
       As1000sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1000<sup>2</sup>, g];
```

In[2334]:= Correction50sq = 
$$\left(1 + \frac{3 \text{ As50sq}}{4 \pi} C_F\right)$$
;

Correction60sq =  $\left(1 + \frac{3 \text{ As60sq}}{4 \pi} C_F\right)$ ;

Correction70sq =  $\left(1 + \frac{3 \text{ As70sq}}{4 \pi} C_F\right)$ ;

Correction80sq =  $\left(1 + \frac{3 \text{ As80sq}}{4 \pi} C_F\right)$ ;

Correction90sq =  $\left(1 + \frac{3 \text{ As90sq}}{4 \pi} C_F\right)$ ;

In[2339]:= Correction100sq = 
$$\left(1 + \frac{3 \text{ As100sq}}{4 \pi} C_F\right)$$
;

Correction110sq =  $\left(1 + \frac{3 \text{ As110sq}}{4 \pi} C_F\right)$ ;

Correction120sq =  $\left(1 + \frac{3 \text{ As120sq}}{4 \pi} C_F\right)$ ;

Correction130sq =  $\left(1 + \frac{3 \text{ As130sq}}{4 \pi} C_F\right)$ ;

Correction140sq =  $\left(1 + \frac{3 \text{ As140sq}}{4 \pi} C_F\right)$ ;

Correction150sq =  $\left(1 + \frac{3 \text{ As150sq}}{4 \pi} C_F\right)$ ;

Correction160sq =  $\left(1 + \frac{3 \text{ As160sq}}{4 \pi} C_F\right)$ ;

Correction170sq =  $\left(1 + \frac{3 \text{ As170sq}}{4 \pi} C_F\right)$ ;

Correction180sq =  $\left(1 + \frac{3 \text{ As180sq}}{4 \pi} C_F\right)$ ;

Correction190sq =  $\left(1 + \frac{3 \text{ As190sq}}{4 \pi} C_F\right)$ ;

In[2349]:= Correction200sq = 
$$\left(1 + \frac{3 \text{ As200sq}}{4 \pi} C_F\right)$$
;

Correction210sq =  $\left(1 + \frac{3 \text{ As210sq}}{4 \pi} C_F\right)$ ;

Correction220sq =  $\left(1 + \frac{3 \text{ As220sq}}{4 \pi} C_F\right)$ ;

Correction230sq =  $\left(1 + \frac{3 \text{ As230sq}}{4 \pi} C_F\right)$ ;

Correction240sq =  $\left(1 + \frac{3 \text{ As240sq}}{4 \pi} C_F\right)$ ;

Correction250sq =  $\left(1 + \frac{3 \text{ As250sq}}{4 \pi} C_F\right)$ ;

Correction260sq =  $\left(1 + \frac{3 \text{ As250sq}}{4 \pi} C_F\right)$ ;

Correction270sq =  $\left(1 + \frac{3 \text{ As260sq}}{4 \pi} C_F\right)$ ;

Correction280sq =  $\left(1 + \frac{3 \text{ As270sq}}{4 \pi} C_F\right)$ ;

Correction290sq =  $\left(1 + \frac{3 \text{ As280sq}}{4 \pi} C_F\right)$ ;

Correction290sq =  $\left(1 + \frac{3 \text{ As290sq}}{4 \pi} C_F\right)$ ;

In[2359]:= Correction300sq = 
$$\left(1 + \frac{3 \text{ As300sq}}{4 \pi} C_F\right)$$
;

Correction310sq =  $\left(1 + \frac{3 \text{ As310sq}}{4 \pi} C_F\right)$ ;

Correction320sq =  $\left(1 + \frac{3 \text{ As320sq}}{4 \pi} C_F\right)$ ;

Correction330sq =  $\left(1 + \frac{3 \text{ As330sq}}{4 \pi} C_F\right)$ ;

Correction340sq =  $\left(1 + \frac{3 \text{ As340sq}}{4 \pi} C_F\right)$ ;

Correction350sq =  $\left(1 + \frac{3 \text{ As350sq}}{4 \pi} C_F\right)$ ;

Correction360sq =  $\left(1 + \frac{3 \text{ As350sq}}{4 \pi} C_F\right)$ ;

Correction370sq =  $\left(1 + \frac{3 \text{ As370sq}}{4 \pi} C_F\right)$ ;

Correction380sq =  $\left(1 + \frac{3 \text{ As380sq}}{4 \pi} C_F\right)$ ;

Correction390sq =  $\left(1 + \frac{3 \text{ As380sq}}{4 \pi} C_F\right)$ ;

$$\label{eq:localization} \begin{split} &\text{In}[2369]\text{:=} \;\; \text{Correction400sq} = \left(1 + \frac{3 \, \text{As400sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction410sq} = \left(1 + \frac{3 \, \text{As410sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction420sq} = \left(1 + \frac{3 \, \text{As420sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction430sq} = \left(1 + \frac{3 \, \text{As430sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction440sq} = \left(1 + \frac{3 \, \text{As440sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction450sq} = \left(1 + \frac{3 \, \text{As450sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction460sq} = \left(1 + \frac{3 \, \text{As460sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction470sq} = \left(1 + \frac{3 \, \text{As480sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction490sq} = \left(1 + \frac{3 \, \text{As490sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction500sq} = \left(1 + \frac{3 \, \text{As500sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction520sq} = \left(1 + \frac{3 \, \text{As500sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction530sq} = \left(1 + \frac{3 \, \text{As520sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As530sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As530sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As530sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As530sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As530sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As530sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \, \text{C}_F\right); \\ &\text{Correction540sq} = \left(1 + \frac{3 \, \text{As540sq}}{4 \, \pi} \,$$

Correction550sq =  $\left(1 + \frac{3 \text{ As550sq}}{4 \pi} C_F\right)$ ;

Correction560sq =  $\left(1 + \frac{3 \text{ As560sq}}{4 \pi} C_F\right)$ ;

Correction570sq =  $\left(1 + \frac{3 \text{ As570sq}}{4 \pi} C_F\right)$ ;

Correction580sq =  $\left(1 + \frac{3 \text{ As580sq}}{4 \pi} C_F\right)$ ;

Correction590sq =  $\left(1 + \frac{3 \text{ As590sq}}{4 \pi} C_F\right)$ ;

In[2389]:= Correction600sq = 
$$\left(1 + \frac{3 \text{ As600sq}}{4 \pi} \text{ C}_F\right)$$
;

Correction610sq =  $\left(1 + \frac{3 \text{ As610sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction620sq =  $\left(1 + \frac{3 \text{ As620sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction630sq =  $\left(1 + \frac{3 \text{ As630sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction640sq =  $\left(1 + \frac{3 \text{ As640sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction650sq =  $\left(1 + \frac{3 \text{ As650sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction660sq =  $\left(1 + \frac{3 \text{ As660sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction670sq =  $\left(1 + \frac{3 \text{ As660sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction680sq =  $\left(1 + \frac{3 \text{ As680sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction690sq =  $\left(1 + \frac{3 \text{ As680sq}}{4 \pi} \text{ C}_F\right)$ ;

$$\begin{array}{l} \text{In} \ [2399] \coloneqq \ \ \text{Correction700sq} = \left(1 + \frac{3 \ \text{As700sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction710sq} = \left(1 + \frac{3 \ \text{As710sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction720sq} = \left(1 + \frac{3 \ \text{As720sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction730sq} = \left(1 + \frac{3 \ \text{As730sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction740sq} = \left(1 + \frac{3 \ \text{As740sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction750sq} = \left(1 + \frac{3 \ \text{As750sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction760sq} = \left(1 + \frac{3 \ \text{As760sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction770sq} = \left(1 + \frac{3 \ \text{As770sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction780sq} = \left(1 + \frac{3 \ \text{As780sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As790sq}}{4 \ \pi} \ \text{C}_F\right); \\ \text{Correction790sq} = \left(1 + \frac{3 \ \text{As$$

Correction1000sq =  $\left(1 + \frac{3 \text{ As1000sq}}{4 \pi} C_F\right)$ ;

```
In[2430]:= PlotCross50sq = CrossBorn50sq * Correction50sq;
      PlotCross60sq = CrossBorn60sq * Correction60sq;
      PlotCross70sq = CrossBorn70sq * Correction70sq;
      PlotCross80sq = CrossBorn80sq * Correction80sq;
      PlotCross90sq = CrossBorn90sq * Correction90sq;
In[2435]:= PlotCross100sq = CrossBorn100sq * Correction100sq;
      PlotCross110sq = CrossBorn110sq * Correction110sq;
      PlotCross120sq = CrossBorn120sq * Correction120sq;
      PlotCross130sq = CrossBorn130sq * Correction130sq;
      PlotCross140sq = CrossBorn140sq * Correction140sq;
      PlotCross150sq = CrossBorn150sq * Correction150sq;
      PlotCross160sq = CrossBorn160sq * Correction160sq;
      PlotCross170sq = CrossBorn170sq * Correction170sq;
      PlotCross180sq = CrossBorn180sq * Correction180sq;
      PlotCross190sq = CrossBorn190sq * Correction190sq;
In[2445]:= PlotCross200sq = CrossBorn200sq * Correction200sq;
      PlotCross210sq = CrossBorn210sq * Correction210sq;
      PlotCross220sq = CrossBorn220sq * Correction220sq;
      PlotCross230sq = CrossBorn230sq * Correction230sq;
      PlotCross240sq = CrossBorn240sq * Correction240sq;
      PlotCross250sq = CrossBorn250sq * Correction250sq;
      PlotCross260sq = CrossBorn260sq * Correction260sq;
      PlotCross270sq = CrossBorn270sq * Correction270sq;
      PlotCross280sq = CrossBorn280sq * Correction280sq;
      PlotCross290sq = CrossBorn290sq * Correction290sq;
In[2455]:= PlotCross300sq = CrossBorn300sq * Correction300sq;
      PlotCross310sq = CrossBorn310sq * Correction310sq;
      PlotCross320sq = CrossBorn320sq * Correction320sq;
      PlotCross330sq = CrossBorn330sq * Correction330sq;
      PlotCross340sq = CrossBorn340sq * Correction340sq;
      PlotCross350sq = CrossBorn350sq * Correction350sq;
      PlotCross360sq = CrossBorn360sq * Correction360sq;
      PlotCross370sq = CrossBorn370sq * Correction370sq;
      PlotCross380sq = CrossBorn380sq * Correction380sq;
      PlotCross390sq = CrossBorn390sq * Correction390sq;
```

```
In[2465]:= PlotCross400sq = CrossBorn400sq * Correction400sq;
      PlotCross410sq = CrossBorn410sq * Correction410sq;
      PlotCross420sq = CrossBorn420sq * Correction420sq;
      PlotCross430sq = CrossBorn430sq * Correction430sq;
      PlotCross440sq = CrossBorn440sq * Correction440sq;
      PlotCross450sq = CrossBorn450sq * Correction450sq;
      PlotCross460sq = CrossBorn460sq * Correction460sq;
      PlotCross470sq = CrossBorn470sq * Correction470sq;
      PlotCross480sq = CrossBorn480sq * Correction480sq;
      PlotCross490sq = CrossBorn490sq * Correction490sq;
In[2475]:= PlotCross500sq = CrossBorn500sq * Correction500sq;
     PlotCross510sq = CrossBorn510sq * Correction510sq;
     PlotCross520sq = CrossBorn520sq * Correction520sq;
      PlotCross530sq = CrossBorn530sq * Correction530sq;
      PlotCross540sq = CrossBorn540sq * Correction540sq;
      PlotCross550sq = CrossBorn550sq * Correction550sq;
      PlotCross560sq = CrossBorn560sq * Correction560sq;
      PlotCross570sq = CrossBorn570sq * Correction570sq;
      PlotCross580sq = CrossBorn580sq * Correction580sq;
      PlotCross590sq = CrossBorn590sq * Correction590sq;
In[2485]:= PlotCross600sq = CrossBorn600sq * Correction600sq;
     PlotCross610sq = CrossBorn610sq * Correction610sq;
      PlotCross620sq = CrossBorn620sq * Correction620sq;
     PlotCross630sq = CrossBorn630sq * Correction630sq;
      PlotCross640sq = CrossBorn640sq * Correction640sq;
     PlotCross650sq = CrossBorn650sq * Correction650sq;
      PlotCross660sq = CrossBorn660sq * Correction660sq;
      PlotCross670sq = CrossBorn670sq * Correction670sq;
      PlotCross680sq = CrossBorn680sq * Correction680sq;
```

PlotCross690sq = CrossBorn690sq \* Correction690sq;

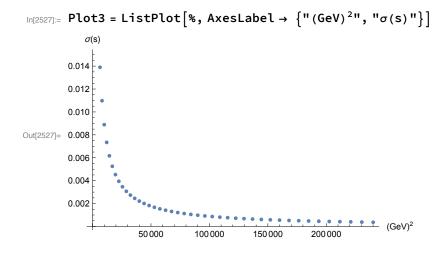
```
In[2495]:= PlotCross700sq = CrossBorn700sq * Correction700sq;
     PlotCross710sq = CrossBorn710sq * Correction710sq;
     PlotCross720sq = CrossBorn720sq * Correction720sq;
     PlotCross730sq = CrossBorn730sq * Correction730sq;
      PlotCross740sq = CrossBorn740sq * Correction740sq;
      PlotCross750sq = CrossBorn750sq * Correction750sq;
      PlotCross760sq = CrossBorn760sq * Correction760sq;
     PlotCross770sq = CrossBorn770sq * Correction770sq;
     PlotCross780sq = CrossBorn780sq * Correction780sq;
      PlotCross790sq = CrossBorn790sq * Correction790sq;
In[2505]:= PlotCross800sq = CrossBorn800sq * Correction800sq;
     PlotCross810sq = CrossBorn810sq * Correction810sq;
     PlotCross820sq = CrossBorn820sq * Correction820sq;
     PlotCross830sq = CrossBorn830sq * Correction830sq;
     PlotCross840sq = CrossBorn840sq * Correction840sq;
      PlotCross850sq = CrossBorn850sq * Correction850sq;
     PlotCross860sq = CrossBorn860sq * Correction860sq;
      PlotCross870sq = CrossBorn870sq * Correction870sq;
      PlotCross880sq = CrossBorn880sq * Correction880sq;
      PlotCross890sq = CrossBorn890sq * Correction890sq;
In[2515]:= PlotCross900sq = CrossBorn900sq * Correction900sq;
     PlotCross910sq = CrossBorn910sq * Correction910sq;
     PlotCross920sq = CrossBorn920sq * Correction920sq;
     PlotCross930sq = CrossBorn930sq * Correction930sq;
      PlotCross940sq = CrossBorn940sq * Correction940sq;
     PlotCross950sq = CrossBorn950sq * Correction950sq;
      PlotCross960sg = CrossBorn960sg * Correction960sg;
      PlotCross970sq = CrossBorn970sq * Correction970sq;
      PlotCross980sq = CrossBorn980sq * Correction980sq;
      PlotCross990sq = CrossBorn990sq * Correction990sq;
     PlotCross1000sq = CrossBorn1000sq * Correction1000sq;
```

## Plot Cross Section $\alpha_s$ (s), 3 Loops

```
In[2526]:= Table1 = TableForm[{{50^2, PlotCross50sq}, {60^2, PlotCross60sq}, {70^2, PlotCross70sq},
             {80<sup>2</sup>, PlotCross80sq}, {90<sup>2</sup>, PlotCross90sq}, {100<sup>2</sup>, PlotCross100sq},
             {110<sup>2</sup>, PlotCross110sq}, {120<sup>2</sup>, PlotCross120sq}, {130<sup>2</sup>, PlotCross130sq},
             {140<sup>2</sup>, PlotCross140sq}, {150<sup>2</sup>, PlotCross150sq}, {160<sup>2</sup>, PlotCross160sq},
             {170<sup>2</sup>, PlotCross170sq}, {180<sup>2</sup>, PlotCross180sq}, {190<sup>2</sup>, PlotCross190sq},
             {200<sup>2</sup>, PlotCross200sq}, {210<sup>2</sup>, PlotCross210sq}, {220<sup>2</sup>, PlotCross220sq},
             {230<sup>2</sup>, PlotCross230sq}, {240<sup>2</sup>, PlotCross240sq}, {250<sup>2</sup>, PlotCross250sq},
             {260<sup>2</sup>, PlotCross260sq}, {270<sup>2</sup>, PlotCross270sq}, {280<sup>2</sup>, PlotCross280sq},
             {290<sup>2</sup>, PlotCross290sq}, {300<sup>2</sup>, PlotCross300sq}, {310<sup>2</sup>, PlotCross310sq},
             {320<sup>2</sup>, PlotCross320sq}, {330<sup>2</sup>, PlotCross330sq}, {340<sup>2</sup>, PlotCross340sq},
             {350<sup>2</sup>, PlotCross350sq}, {360<sup>2</sup>, PlotCross360sq}, {370<sup>2</sup>, PlotCross370sq},
             {380<sup>2</sup>, PlotCross380sq}, {390<sup>2</sup>, PlotCross390sq}, {400<sup>2</sup>, PlotCross400sq},
             {410<sup>2</sup>, PlotCross410sq}, {420<sup>2</sup>, PlotCross420sq}, {430<sup>2</sup>, PlotCross430sq},
             {440<sup>2</sup>, PlotCross440sq}, {450<sup>2</sup>, PlotCross450sq}, {460<sup>2</sup>, PlotCross460sq},
             {470<sup>2</sup>, PlotCross470sq}, {480<sup>2</sup>, PlotCross480sq}, {490<sup>2</sup>, PlotCross490sq}},
           TableHeadings \rightarrow {None, {"(GeV)<sup>2</sup>", "\sigma(s)"}}]
```

Out[2526]//TableForm=

(GeV) <sup>2</sup>	$\sigma(s)$
2500	0.03565671302751665790763
3600	0.02474130956468746203983
4900	0.01816542668209675686974
6400	0.01390042631466346142361
8100	0.01097806116102646613988
10000	0.00888874601573238322258
12 100	0.00734355173280952224709
14 400	0.00616874717240972417844
16 900	0.00525477888392967986269
19 600	0.004529790859495364859039
22 500	0.003945066572935471237004
25 600	0.003466631267678222976450
28 900	0.003070206025653607050561
32 400	0.002738067569172633497094
36 100	0.002457033524078538956945
40 000	0.002217134702868581889569
44 100	0.002010719159025669517043
48 400	0.001831834696666137055973
52 900	0.001675795151844756069402
57 600	0.001538870499347579057818
62 500	0.001418061972403092783899
67 600	0.001310936551157115374944
72 900	0.001215503560904974806912
78 400	0.001130121566958504773577
84 100	0.001053427354478339610114
90 000	0.000984281203189459285952
96 100	0.000921724320277779611879
102 400	0.000864945439741205178909
108 900	0.000813254399858956691665
115 600	0.000766061081088426365820
122 500	0.000722858496674753091454
129 600	0.000683209125959625749412
136 900	0.000646733798720295054356
144 400	0.000613102600520709975385
152 100	0.000582027389795798215877
160 000	0.000553255608324971959058
168 100	0.0005265651357792106439285
176 400	0.0005017599918158475931761
184 900	0.0004786667298516439319395
193 600	0.0004571313981663919859853
202 500	0.0004370169685840822723616
211600	0.0004182011522848898197531
220 900	0.0004005745375433968594687
230 400	0.0003840389962881753395121
240 100	0.0003685063160333350154203

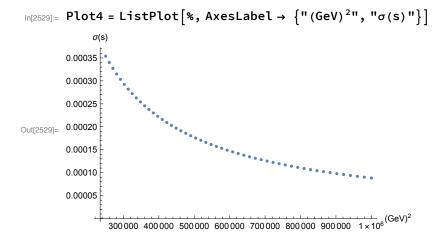


# In[2528]:= **Table2** =

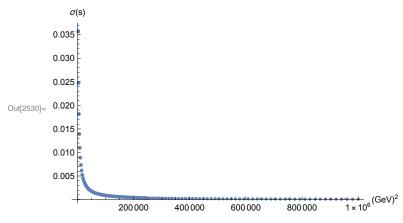
```
TableForm[\{\{500^2, PlotCross500sq\}, \{510^2, PlotCross510sq\}, \{520^2, PlotCross520sq\}, \{510^2, PlotCross520sq\}, \{510^2, PlotCross510sq\}, \{510^2, PlotCross520sq\}, \{510^2, PlotCross510sq\}, \{510^2, 
       {530<sup>2</sup>, PlotCross530sq}, {540<sup>2</sup>, PlotCross540sq}, {550<sup>2</sup>, PlotCross550sq},
       {560<sup>2</sup>, PlotCross560sq}, {570<sup>2</sup>, PlotCross570sq}, {580<sup>2</sup>, PlotCross580sq},
       {590<sup>2</sup>, PlotCross590sq}, {600<sup>2</sup>, PlotCross600sq}, {610<sup>2</sup>, PlotCross610sq},
       {620<sup>2</sup>, PlotCross620sq}, {630<sup>2</sup>, PlotCross630sq}, {640<sup>2</sup>, PlotCross640sq},
       {650<sup>2</sup>, PlotCross650sq}, {660<sup>2</sup>, PlotCross660sq}, {670<sup>2</sup>, PlotCross670sq},
       {680<sup>2</sup>, PlotCross680sq}, {690<sup>2</sup>, PlotCross690sq}, {700<sup>2</sup>, PlotCross700sq},
       {710<sup>2</sup>, PlotCross710sq}, {720<sup>2</sup>, PlotCross720sq}, {730<sup>2</sup>, PlotCross730sq},
       {740<sup>2</sup>, PlotCross740sq}, {750<sup>2</sup>, PlotCross750sq}, {760<sup>2</sup>, PlotCross760sq},
       {770<sup>2</sup>, PlotCross770sq}, {780<sup>2</sup>, PlotCross780sq}, {790<sup>2</sup>, PlotCross790sq},
       {800<sup>2</sup>, PlotCross800sq}, {810<sup>2</sup>, PlotCross810sq}, {820<sup>2</sup>, PlotCross820sq},
       {830<sup>2</sup>, PlotCross830sq}, {840<sup>2</sup>, PlotCross840sq}, {850<sup>2</sup>, PlotCross850sq},
       {860<sup>2</sup>, PlotCross860sq}, {870<sup>2</sup>, PlotCross870sq}, {880<sup>2</sup>, PlotCross880sq},
       {890<sup>2</sup>, PlotCross890sq}, {900<sup>2</sup>, PlotCross900sq}, {910<sup>2</sup>, PlotCross910sq},
       {920<sup>2</sup>, PlotCross920sq}, {930<sup>2</sup>, PlotCross930sq}, {940<sup>2</sup>, PlotCross940sq},
       {950<sup>2</sup>, PlotCross950sq}, {960<sup>2</sup>, PlotCross960sq}, {970<sup>2</sup>, PlotCross970sq},
       {980<sup>2</sup>, PlotCross980sq}, {990<sup>2</sup>, PlotCross990sq}, {1000<sup>2</sup>, PlotCross1000sq}},
   TableHeadings \rightarrow {None, {"(GeV)<sup>2</sup>", "\sigma(s)"}}]
```

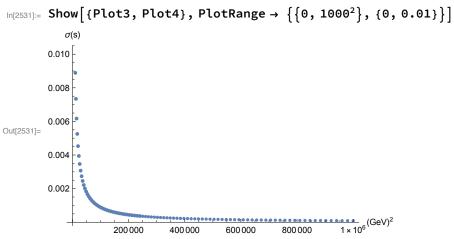
Out[2528]//TableForm=

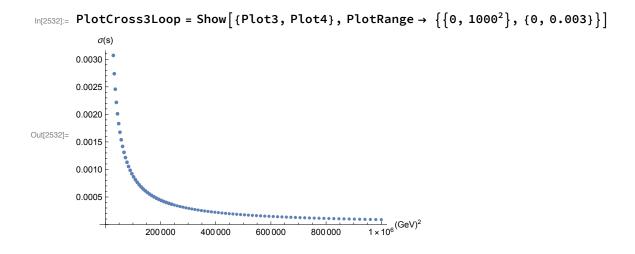
/TableForm=	
(GeV) <sup>2</sup>	$\sigma(s)$
250 000	0.0003538970214762437586441
260 100	0.0003401393562956701631282
270 400	0.0003271684007360875464398
280 900	0.0003149253046711735352162
291600	0.0003033566191931996332459
302 500	0.0002924137125243944696719
313 600	0.0002820522583091238406480
324 900	0.0002722317862149534370417
336 400	0.0002629152863203436561455
348 100	0.0002540688600559445250348
360 000	0.0002456614115425709065205
372 100	0.0002376643740700600907878
384 400	0.0002300514672181459539058
396 900	0.0002227984807582037078852
409 600	0.0002158830820135591028883
422 500	0.0002092846438126224275427
435 600	0.0002029840905570101436581
448 900	0.0001969637602572466946725
462 400	0.0001912072806708251120033
476 100	0.0001856994579189840508575
490 000	0.0001804261761658673096588
504 100	0.0001753743071220422641083
518 400	0.0001705316282880663281575
532 900	0.0001658867489865871539568
547 600	0.0001614290433464312463284
562 500	0.0001571485895018747986891
577 600	0.0001530361143569900781676
592 900	0.0001490829433404713150214
608 400	0.0001452809546422341464506
624 100	0.0001416225374806833693970
640 000	0.0001381005539999879100030
656 100	0.0001347083044409556232171
672 400	0.0001314394952679893172216
688 900	0.0001282882099688359510123
705 600 722 500	0.0001252488822740199772271 0.0001223162715695004178630
739 600	0.0001223102713093004178030
756 900	0.0001194834402996386483212
774 400	0.0001107317331783972880331
792 100	0.00011115583682222079509580
810 000	0.00011133838822222073383388
828 100	0.0001030300402243347733737
846 400	0.0001043945927072824263944
864 900	0.0001021594424969496848807
883 600	0.0000999952979739294770235
902 500	0.0000978991834832399751635
921600	0.0000958682776164903589042
940 900	0.0000938999037162983282464
960 400	0.0000919915210557311859808
980 100	0.0000901407166384826952705
1000000	0.0000883451975703606595103











## Run Cross Section $\alpha_s$ (s), 4 Loops

```
In[2533] := g = 4;
        \alpha = 1/137;
        Conversion = 389 379;
        n = 3;
       C_F = \frac{n^2 - 1}{2 n};
       Born = \frac{4\pi\alpha^2}{3s};
In[2539]:= CrossBorn[s_] = Conversion * Born;
        CrossBorn50sq = CrossBorn[50<sup>2</sup>];
        CrossBorn60sq = CrossBorn[60<sup>2</sup>];
        CrossBorn70sq = CrossBorn[70<sup>2</sup>];
        CrossBorn80sq = CrossBorn[80<sup>2</sup>];
        CrossBorn90sq = CrossBorn[90<sup>2</sup>];
ln[2545] = CrossBorn100sq = CrossBorn[100<sup>2</sup>];
        CrossBorn110sq = CrossBorn[110<sup>2</sup>];
        CrossBorn120sq = CrossBorn[120<sup>2</sup>];
        CrossBorn130sq = CrossBorn[130<sup>2</sup>];
        CrossBorn140sq = CrossBorn[140<sup>2</sup>];
        CrossBorn150sq = CrossBorn[150<sup>2</sup>];
        CrossBorn160sq = CrossBorn[160<sup>2</sup>];
        CrossBorn170sq = CrossBorn[170<sup>2</sup>];
        CrossBorn180sq = CrossBorn[180<sup>2</sup>];
        CrossBorn190sq = CrossBorn[190<sup>2</sup>];
```

```
ln[2555]:= CrossBorn200sq = CrossBorn[200<sup>2</sup>];
       CrossBorn210sq = CrossBorn[210<sup>2</sup>];
       CrossBorn220sq = CrossBorn[220<sup>2</sup>];
       CrossBorn230sq = CrossBorn[230<sup>2</sup>];
       CrossBorn240sq = CrossBorn[240<sup>2</sup>];
       CrossBorn250sq = CrossBorn[250<sup>2</sup>];
       CrossBorn260sq = CrossBorn[260<sup>2</sup>];
       CrossBorn270sq = CrossBorn[270<sup>2</sup>];
       CrossBorn280sq = CrossBorn[280<sup>2</sup>];
       CrossBorn290sq = CrossBorn[290<sup>2</sup>];
ln[2565]:= CrossBorn300sq = CrossBorn[300<sup>2</sup>];
       CrossBorn310sq = CrossBorn[310<sup>2</sup>];
       CrossBorn320sq = CrossBorn[320<sup>2</sup>];
       CrossBorn330sq = CrossBorn[330<sup>2</sup>];
       CrossBorn340sq = CrossBorn[340<sup>2</sup>];
       CrossBorn350sq = CrossBorn[350<sup>2</sup>];
       CrossBorn360sq = CrossBorn[360<sup>2</sup>];
       CrossBorn370sq = CrossBorn[370<sup>2</sup>];
       CrossBorn380sq = CrossBorn[380<sup>2</sup>];
       CrossBorn390sq = CrossBorn[390<sup>2</sup>];
ln[2575]:= CrossBorn400sq = CrossBorn[400<sup>2</sup>];
       CrossBorn410sq = CrossBorn[410<sup>2</sup>];
       CrossBorn420sq = CrossBorn [420<sup>2</sup>];
       CrossBorn430sq = CrossBorn [430<sup>2</sup>];
       CrossBorn440sq = CrossBorn [440<sup>2</sup>];
       CrossBorn450sq = CrossBorn[450<sup>2</sup>];
       CrossBorn460sq = CrossBorn [460<sup>2</sup>];
       CrossBorn470sq = CrossBorn[470<sup>2</sup>];
       CrossBorn480sq = CrossBorn [480<sup>2</sup>];
       CrossBorn490sq = CrossBorn[490<sup>2</sup>];
ln[2585] = CrossBorn500sq = CrossBorn[500<sup>2</sup>];
       CrossBorn510sq = CrossBorn[510<sup>2</sup>];
       CrossBorn520sq = CrossBorn[520<sup>2</sup>];
       CrossBorn530sq = CrossBorn[530<sup>2</sup>];
       CrossBorn540sq = CrossBorn[540<sup>2</sup>];
       CrossBorn550sq = CrossBorn[550<sup>2</sup>];
       CrossBorn560sq = CrossBorn[560<sup>2</sup>];
       CrossBorn570sq = CrossBorn[570<sup>2</sup>];
       CrossBorn580sq = CrossBorn[580<sup>2</sup>];
       CrossBorn590sq = CrossBorn[590<sup>2</sup>];
```

```
ln[2595] := CrossBorn600sq = CrossBorn[600<sup>2</sup>];
       CrossBorn610sq = CrossBorn[610<sup>2</sup>];
       CrossBorn620sq = CrossBorn[620<sup>2</sup>];
       CrossBorn630sq = CrossBorn[630<sup>2</sup>];
       CrossBorn640sq = CrossBorn[640<sup>2</sup>];
       CrossBorn650sq = CrossBorn[650<sup>2</sup>];
       CrossBorn660sq = CrossBorn[660<sup>2</sup>];
       CrossBorn670sq = CrossBorn[670<sup>2</sup>];
       CrossBorn680sq = CrossBorn[680<sup>2</sup>];
       CrossBorn690sq = CrossBorn[690<sup>2</sup>];
ln[2605]:= CrossBorn700sq = CrossBorn[700<sup>2</sup>];
       CrossBorn710sq = CrossBorn[710<sup>2</sup>];
       CrossBorn720sq = CrossBorn[720<sup>2</sup>];
       CrossBorn730sq = CrossBorn[730<sup>2</sup>];
       CrossBorn740sq = CrossBorn[740<sup>2</sup>];
       CrossBorn750sq = CrossBorn[750<sup>2</sup>];
       CrossBorn760sq = CrossBorn[760<sup>2</sup>];
       CrossBorn770sq = CrossBorn[770<sup>2</sup>];
       CrossBorn780sq = CrossBorn[780<sup>2</sup>];
       CrossBorn790sq = CrossBorn[790<sup>2</sup>];
ln[2615]:= CrossBorn800sq = CrossBorn[800<sup>2</sup>];
       CrossBorn810sq = CrossBorn[810<sup>2</sup>];
       CrossBorn820sq = CrossBorn[820<sup>2</sup>];
       CrossBorn830sq = CrossBorn[830<sup>2</sup>];
       CrossBorn840sq = CrossBorn[840<sup>2</sup>];
       CrossBorn850sq = CrossBorn[850<sup>2</sup>];
       CrossBorn860sq = CrossBorn[860<sup>2</sup>];
       CrossBorn870sq = CrossBorn[870<sup>2</sup>];
       CrossBorn880sq = CrossBorn[880<sup>2</sup>];
       CrossBorn890sq = CrossBorn[890<sup>2</sup>];
```

```
ln[2625]:= CrossBorn900sq = CrossBorn[900<sup>2</sup>];
       CrossBorn910sq = CrossBorn[910<sup>2</sup>];
       CrossBorn920sq = CrossBorn[920<sup>2</sup>];
       CrossBorn930sq = CrossBorn[930<sup>2</sup>];
       CrossBorn940sg = CrossBorn[940<sup>2</sup>];
       CrossBorn950sq = CrossBorn[950<sup>2</sup>];
       CrossBorn960sq = CrossBorn[960<sup>2</sup>];
       CrossBorn970sq = CrossBorn[970<sup>2</sup>];
       CrossBorn980sq = CrossBorn[980<sup>2</sup>];
       CrossBorn990sq = CrossBorn[990<sup>2</sup>];
       CrossBorn1000sq = CrossBorn[1000<sup>2</sup>];
In[2636]:= As50sq = AsRunDec [asMz /. NumDef, Mz /. NumDef, 50<sup>2</sup>, g];
       As60sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 60<sup>2</sup>, g];
       As70sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 70<sup>2</sup>, g];
       As80sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 80<sup>2</sup>, g];
       As90sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 90<sup>2</sup>, g];
ln[2641]:= As100sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 100<sup>2</sup>, g];
       As110sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 110<sup>2</sup>, g];
       As120sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 120<sup>2</sup>, g];
       As130sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 130<sup>2</sup>, g];
       As140sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 140<sup>2</sup>, g];
       As150sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 150<sup>2</sup>, g];
       As160sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 160<sup>2</sup>, g];
       As170sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 170<sup>2</sup>, g];
       As180sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 180<sup>2</sup>, g];
       As190sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 190<sup>2</sup>, g];
ln[2651]:= As200sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 200<sup>2</sup>, g];
       As210sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 210<sup>2</sup>, g];
       As220sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 220<sup>2</sup>, g];
       As230sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 230<sup>2</sup>, g];
       As240sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 240<sup>2</sup>, g];
       As250sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 250<sup>2</sup>, g];
       As260sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 260<sup>2</sup>, g];
       As270sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 270<sup>2</sup>, g];
       As280sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 280<sup>2</sup>, g];
       As290sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 290<sup>2</sup>, g];
```

```
ln(2661) = As300sq = AsRunDec[asMz/.NumDef, Mz/.NumDef, 300^2, g];
       As310sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 310<sup>2</sup>, g];
       As320sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 320<sup>2</sup>, g];
       As330sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 330<sup>2</sup>, g];
       As340sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 340<sup>2</sup>, g];
       As350sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 350<sup>2</sup>, g];
       As360sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 360<sup>2</sup>, g];
       As370sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 370<sup>2</sup>, g];
       As380sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 380<sup>2</sup>, g];
       As390sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 390<sup>2</sup>, g];
ln[2671] = As400sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 400<sup>2</sup>, g];
       As410sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 410<sup>2</sup>, g];
       As420sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 420<sup>2</sup>, g];
       As430sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 430<sup>2</sup>, g];
       As440sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 440<sup>2</sup>, g];
       As450sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 450<sup>2</sup>, g];
       As460sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 460<sup>2</sup>, g];
       As470sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 470<sup>2</sup>, g];
       As480sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 480<sup>2</sup>, g];
       As490sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 490<sup>2</sup>, g];
ln[2681] = As500sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 500<sup>2</sup>, g];
       As510sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 510<sup>2</sup>, g];
       As520sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 520<sup>2</sup>, g];
       As530sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 530<sup>2</sup>, g];
       As540sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 540<sup>2</sup>, g];
       As550sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 550<sup>2</sup>, g];
       As560sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 560<sup>2</sup>, g];
       As570sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 570<sup>2</sup>, g];
       As580sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 580<sup>2</sup>, g];
       As590sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 5902, g];
ln[2691] = As600sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 600<sup>2</sup>, g];
       As610sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 610<sup>2</sup>, g];
       As620sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 620<sup>2</sup>, g];
       As630sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 630<sup>2</sup>, g];
       As640sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 640<sup>2</sup>, g];
       As650sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 650<sup>2</sup>, g];
       As660sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 660<sup>2</sup>, g];
       As670sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 670<sup>2</sup>, g];
       As680sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 680<sup>2</sup>, g];
       As690sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 690<sup>2</sup>, g];
```

```
ln[2701] = As700sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 700<sup>2</sup>, g];
       As710sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 710<sup>2</sup>, g];
       As720sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 720<sup>2</sup>, g];
       As730sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 730<sup>2</sup>, g];
       As740sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 740<sup>2</sup>, g];
       As750sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 750<sup>2</sup>, g];
       As760sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 760<sup>2</sup>, g];
       As770sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 770<sup>2</sup>, g];
       As780sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 780<sup>2</sup>, g];
       As790sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 790<sup>2</sup>, g];
ln[2711] = As800sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 800<sup>2</sup>, g];
       As810sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 810<sup>2</sup>, g];
       As820sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 820<sup>2</sup>, g];
       As830sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 830<sup>2</sup>, g];
       As840sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 840<sup>2</sup>, g];
       As850sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 850<sup>2</sup>, g];
       As860sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 860<sup>2</sup>, g];
       As870sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 870<sup>2</sup>, g];
       As880sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 880<sup>2</sup>, g];
       As890sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 890<sup>2</sup>, g];
ln[2721] = As900sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 900<sup>2</sup>, g];
       As910sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 910<sup>2</sup>, g];
       As920sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 920<sup>2</sup>, g];
       As930sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 930<sup>2</sup>, g];
       As940sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 940<sup>2</sup>, g];
       As950sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 950<sup>2</sup>, g];
       As960sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 960<sup>2</sup>, g];
       As970sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 970<sup>2</sup>, g];
       As980sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 980<sup>2</sup>, g];
       As990sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 990<sup>2</sup>, g];
       As1000sq = AsRunDec[asMz /. NumDef, Mz /. NumDef, 1000<sup>2</sup>, g];
```

In[2732]:= Correction50sq = 
$$\left(1 + \frac{3 \text{ As50sq}}{4 \pi} C_F\right)$$
;

Correction60sq =  $\left(1 + \frac{3 \text{ As60sq}}{4 \pi} C_F\right)$ ;

Correction70sq =  $\left(1 + \frac{3 \text{ As70sq}}{4 \pi} C_F\right)$ ;

Correction80sq =  $\left(1 + \frac{3 \text{ As80sq}}{4 \pi} C_F\right)$ ;

Correction90sq =  $\left(1 + \frac{3 \text{ As90sq}}{4 \pi} C_F\right)$ ;

In[2737]:= Correction100sq = 
$$\left(1 + \frac{3 \text{ As100sq}}{4 \pi} C_F\right)$$
;

Correction110sq =  $\left(1 + \frac{3 \text{ As110sq}}{4 \pi} C_F\right)$ ;

Correction120sq =  $\left(1 + \frac{3 \text{ As120sq}}{4 \pi} C_F\right)$ ;

Correction130sq =  $\left(1 + \frac{3 \text{ As130sq}}{4 \pi} C_F\right)$ ;

Correction140sq =  $\left(1 + \frac{3 \text{ As140sq}}{4 \pi} C_F\right)$ ;

Correction150sq =  $\left(1 + \frac{3 \text{ As150sq}}{4 \pi} C_F\right)$ ;

Correction160sq =  $\left(1 + \frac{3 \text{ As160sq}}{4 \pi} C_F\right)$ ;

Correction170sq =  $\left(1 + \frac{3 \text{ As170sq}}{4 \pi} C_F\right)$ ;

Correction180sq =  $\left(1 + \frac{3 \text{ As180sq}}{4 \pi} C_F\right)$ ;

Correction190sq =  $\left(1 + \frac{3 \text{ As190sq}}{4 \pi} C_F\right)$ ;

Correction390sq =  $\left(1 + \frac{3 \text{ As390sq}}{4 \pi} C_F\right)$ ;

In[2767]:= Correction400sq = 
$$\left(1 + \frac{3 \text{ As400sq}}{4 \pi} \text{ C}_F\right)$$
;

Correction410sq =  $\left(1 + \frac{3 \text{ As410sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction420sq =  $\left(1 + \frac{3 \text{ As420sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction430sq =  $\left(1 + \frac{3 \text{ As430sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction440sq =  $\left(1 + \frac{3 \text{ As440sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction450sq =  $\left(1 + \frac{3 \text{ As450sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction460sq =  $\left(1 + \frac{3 \text{ As460sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction470sq =  $\left(1 + \frac{3 \text{ As470sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction480sq =  $\left(1 + \frac{3 \text{ As480sq}}{4 \pi} \text{ C}_F\right)$ ;

Correction490sq =  $\left(1 + \frac{3 \text{ As480sq}}{4 \pi} \text{ C}_F\right)$ ;

$$\begin{array}{l} \text{In} [2777] \coloneqq \text{ Correction500sq} = \left(1 + \frac{3 \text{ As500sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction510sq} = \left(1 + \frac{3 \text{ As510sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction520sq} = \left(1 + \frac{3 \text{ As530sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction530sq} = \left(1 + \frac{3 \text{ As530sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction540sq} = \left(1 + \frac{3 \text{ As540sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction550sq} = \left(1 + \frac{3 \text{ As550sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction560sq} = \left(1 + \frac{3 \text{ As560sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction570sq} = \left(1 + \frac{3 \text{ As570sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction580sq} = \left(1 + \frac{3 \text{ As580sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Correction590sq} = \left(1 + \frac{3 \text{ As590sq}}{4 \, \pi} \text{ C}_F\right); \\ \text{ Corre$$

$$\text{Im}[2787] = \text{Correction} 600 \text{sq} = \left(1 + \frac{3 \text{ As} 600 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 610 \text{sq} = \left(1 + \frac{3 \text{ As} 610 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 620 \text{sq} = \left(1 + \frac{3 \text{ As} 620 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 630 \text{sq} = \left(1 + \frac{3 \text{ As} 630 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 640 \text{sq} = \left(1 + \frac{3 \text{ As} 640 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 660 \text{sq} = \left(1 + \frac{3 \text{ As} 660 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 670 \text{sq} = \left(1 + \frac{3 \text{ As} 680 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 680 \text{sq} = \left(1 + \frac{3 \text{ As} 680 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 690 \text{sq} = \left(1 + \frac{3 \text{ As} 690 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 700 \text{sq} = \left(1 + \frac{3 \text{ As} 700 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 720 \text{sq} = \left(1 + \frac{3 \text{ As} 710 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 730 \text{sq} = \left(1 + \frac{3 \text{ As} 720 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 730 \text{sq} = \left(1 + \frac{3 \text{ As} 730 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 740 \text{sq} = \left(1 + \frac{3 \text{ As} 730 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 740 \text{sq} = \left(1 + \frac{3 \text{ As} 730 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

$$\text{Correction} 750 \text{sq} = \left(1 + \frac{3 \text{ As} 730 \text{ sq}}{4 \pi} \text{ C}_F\right);$$

Correction760sq =  $\left(1 + \frac{3 \text{ As760sq}}{4 \pi} C_F\right)$ ;

Correction770sq =  $\left(1 + \frac{3 \text{ As770sq}}{4 \pi} C_F\right)$ ;

Correction780sq =  $\left(1 + \frac{3 \text{ As780sq}}{4 \pi} C_F\right)$ ;

Correction790sq =  $\left(1 + \frac{3 \text{ As790sq}}{4 \pi} C_F\right)$ ;

```
In[2828]:= PlotCross50sq = CrossBorn50sq * Correction50sq;
      PlotCross60sq = CrossBorn60sq * Correction60sq;
      PlotCross70sq = CrossBorn70sq * Correction70sq;
      PlotCross80sg = CrossBorn80sg * Correction80sg;
      PlotCross90sq = CrossBorn90sq * Correction90sq;
In[2833]:= PlotCross100sq = CrossBorn100sq * Correction100sq;
      PlotCross110sq = CrossBorn110sq * Correction110sq;
      PlotCross120sq = CrossBorn120sq * Correction120sq;
      PlotCross130sq = CrossBorn130sq * Correction130sq;
      PlotCross140sq = CrossBorn140sq * Correction140sq;
      PlotCross150sq = CrossBorn150sq * Correction150sq;
      PlotCross160sq = CrossBorn160sq * Correction160sq;
      PlotCross170sq = CrossBorn170sq * Correction170sq;
      PlotCross180sq = CrossBorn180sq * Correction180sq;
      PlotCross190sq = CrossBorn190sq * Correction190sq;
In[2843]:= PlotCross200sq = CrossBorn200sq * Correction200sq;
      PlotCross210sq = CrossBorn210sq * Correction210sq;
      PlotCross220sq = CrossBorn220sq * Correction220sq;
      PlotCross230sq = CrossBorn230sq * Correction230sq;
      PlotCross240sq = CrossBorn240sq * Correction240sq;
      PlotCross250sq = CrossBorn250sq * Correction250sq;
      PlotCross260sq = CrossBorn260sq * Correction260sq;
      PlotCross270sq = CrossBorn270sq * Correction270sq;
      PlotCross280sg = CrossBorn280sg * Correction280sg;
      PlotCross290sq = CrossBorn290sq * Correction290sq;
In[2853]:= PlotCross300sq = CrossBorn300sq * Correction300sq;
      PlotCross310sg = CrossBorn310sg * Correction310sg;
      PlotCross320sq = CrossBorn320sq * Correction320sq;
      PlotCross330sq = CrossBorn330sq * Correction330sq;
      PlotCross340sq = CrossBorn340sq * Correction340sq;
      PlotCross350sq = CrossBorn350sq * Correction350sq;
      PlotCross360sq = CrossBorn360sq * Correction360sq;
```

PlotCross370sq = CrossBorn370sq \* Correction370sq; PlotCross380sq = CrossBorn380sq \* Correction380sq; PlotCross390sq = CrossBorn390sq \* Correction390sq;

```
In[2863]:= PlotCross400sq = CrossBorn400sq * Correction400sq;
      PlotCross410sq = CrossBorn410sq * Correction410sq;
      PlotCross420sq = CrossBorn420sq * Correction420sq;
      PlotCross430sq = CrossBorn430sq * Correction430sq;
      PlotCross440sq = CrossBorn440sq * Correction440sq;
      PlotCross450sq = CrossBorn450sq * Correction450sq;
      PlotCross460sq = CrossBorn460sq * Correction460sq;
      PlotCross470sq = CrossBorn470sq * Correction470sq;
      PlotCross480sq = CrossBorn480sq * Correction480sq;
      PlotCross490sq = CrossBorn490sq * Correction490sq;
In[2873]:= PlotCross500sq = CrossBorn500sq * Correction500sq;
     PlotCross510sq = CrossBorn510sq * Correction510sq;
     PlotCross520sq = CrossBorn520sq * Correction520sq;
      PlotCross530sq = CrossBorn530sq * Correction530sq;
      PlotCross540sq = CrossBorn540sq * Correction540sq;
      PlotCross550sq = CrossBorn550sq * Correction550sq;
      PlotCross560sq = CrossBorn560sq * Correction560sq;
      PlotCross570sq = CrossBorn570sq * Correction570sq;
      PlotCross580sq = CrossBorn580sq * Correction580sq;
      PlotCross590sq = CrossBorn590sq * Correction590sq;
In[2883]:= PlotCross600sq = CrossBorn600sq * Correction600sq;
     PlotCross610sq = CrossBorn610sq * Correction610sq;
      PlotCross620sq = CrossBorn620sq * Correction620sq;
      PlotCross630sq = CrossBorn630sq * Correction630sq;
      PlotCross640sq = CrossBorn640sq * Correction640sq;
     PlotCross650sq = CrossBorn650sq * Correction650sq;
      PlotCross660sq = CrossBorn660sq * Correction660sq;
      PlotCross670sq = CrossBorn670sq * Correction670sq;
      PlotCross680sq = CrossBorn680sq * Correction680sq;
      PlotCross690sq = CrossBorn690sq * Correction690sq;
```

```
In[2893]:= PlotCross700sq = CrossBorn700sq * Correction700sq;
     PlotCross710sq = CrossBorn710sq * Correction710sq;
     PlotCross720sq = CrossBorn720sq * Correction720sq;
     PlotCross730sq = CrossBorn730sq * Correction730sq;
      PlotCross740sq = CrossBorn740sq * Correction740sq;
      PlotCross750sq = CrossBorn750sq * Correction750sq;
      PlotCross760sq = CrossBorn760sq * Correction760sq;
     PlotCross770sq = CrossBorn770sq * Correction770sq;
     PlotCross780sq = CrossBorn780sq * Correction780sq;
      PlotCross790sq = CrossBorn790sq * Correction790sq;
In[2903]:= PlotCross800sq = CrossBorn800sq * Correction800sq;
     PlotCross810sq = CrossBorn810sq * Correction810sq;
     PlotCross820sq = CrossBorn820sq * Correction820sq;
     PlotCross830sq = CrossBorn830sq * Correction830sq;
     PlotCross840sq = CrossBorn840sq * Correction840sq;
      PlotCross850sq = CrossBorn850sq * Correction850sq;
     PlotCross860sq = CrossBorn860sq * Correction860sq;
      PlotCross870sq = CrossBorn870sq * Correction870sq;
      PlotCross880sq = CrossBorn880sq * Correction880sq;
      PlotCross890sq = CrossBorn890sq * Correction890sq;
In[2913]:= PlotCross900sq = CrossBorn900sq * Correction900sq;
     PlotCross910sq = CrossBorn910sq * Correction910sq;
     PlotCross920sq = CrossBorn920sq * Correction920sq;
     PlotCross930sq = CrossBorn930sq * Correction930sq;
      PlotCross940sq = CrossBorn940sq * Correction940sq;
     PlotCross950sq = CrossBorn950sq * Correction950sq;
      PlotCross960sq = CrossBorn960sq * Correction960sq;
      PlotCross970sq = CrossBorn970sq * Correction970sq;
     PlotCross980sq = CrossBorn980sq * Correction980sq;
     PlotCross990sq = CrossBorn990sq * Correction990sq;
     PlotCross1000sq = CrossBorn1000sq * Correction1000sq;
```

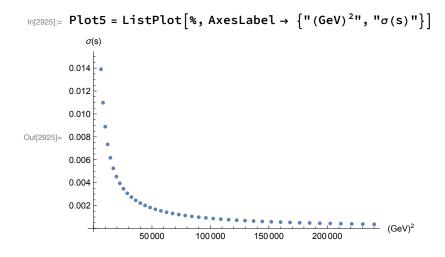
## Plot Cross Section $\alpha_s$ (s), 4 Loops

```
ln[2924]:= Table1 = TableForm[{{50<sup>2</sup>, PlotCross50sq}, {60<sup>2</sup>, PlotCross60sq}, {70<sup>2</sup>, PlotCross70sq},
             {80<sup>2</sup>, PlotCross80sq}, {90<sup>2</sup>, PlotCross90sq}, {100<sup>2</sup>, PlotCross100sq},
             {110<sup>2</sup>, PlotCross110sq}, {120<sup>2</sup>, PlotCross120sq}, {130<sup>2</sup>, PlotCross130sq},
             {140<sup>2</sup>, PlotCross140sq}, {150<sup>2</sup>, PlotCross150sq}, {160<sup>2</sup>, PlotCross160sq},
             \{170^2, PlotCross170sq\}, \{180^2, PlotCross180sq\}, \{190^2, PlotCross190sq\},
             {200<sup>2</sup>, PlotCross200sq}, {210<sup>2</sup>, PlotCross210sq}, {220<sup>2</sup>, PlotCross220sq},
             {230<sup>2</sup>, PlotCross230sq}, {240<sup>2</sup>, PlotCross240sq}, {250<sup>2</sup>, PlotCross250sq},
             {260<sup>2</sup>, PlotCross260sq}, {270<sup>2</sup>, PlotCross270sq}, {280<sup>2</sup>, PlotCross280sq},
             {290<sup>2</sup>, PlotCross290sq}, {300<sup>2</sup>, PlotCross300sq}, {310<sup>2</sup>, PlotCross310sq},
             {320<sup>2</sup>, PlotCross320sq}, {330<sup>2</sup>, PlotCross330sq}, {340<sup>2</sup>, PlotCross340sq},
             \{350^2, PlotCross350sq\}, \{360^2, PlotCross360sq\}, \{370^2, PlotCross370sq\},
             {380<sup>2</sup>, PlotCross380sq}, {390<sup>2</sup>, PlotCross390sq}, {400<sup>2</sup>, PlotCross400sq},
             {410<sup>2</sup>, PlotCross410sq}, {420<sup>2</sup>, PlotCross420sq}, {430<sup>2</sup>, PlotCross430sq},
             {440<sup>2</sup>, PlotCross440sq}, {450<sup>2</sup>, PlotCross450sq}, {460<sup>2</sup>, PlotCross460sq},
             {470<sup>2</sup>, PlotCross470sq}, {480<sup>2</sup>, PlotCross480sq}, {490<sup>2</sup>, PlotCross490sq}},
           TableHeadings \rightarrow {None, {"(GeV)<sup>2</sup>", "\sigma(s)"}}]
```

Out[2924]//TableForm=

// Tablet offile	
(GeV) <sup>2</sup>	$\sigma(s)$
2500	0.03565676390122235360000
3600	0.02474134087367976361476
4900	0.01816544752552721655933
6400	0.01390044100357860887621
8100	0.01097807196868900795719
10000	0.00888875424074629777463
12 100	0.00734355816459758547545
14 400	0.00616875231533417395774
16 900	0.00525478307361363522813
19 600	0.004529794326984266048348
22 500	0.003945069481917735903162
25 600	0.003466633737014075230701
28 900	0.003070208143515123849575
32 400	0.002738069402201427592628
36 100	0.002457035123481369620941
40 000	0.002217136108573879064137
44 100	0.002217130108373879004137
48 400	
52 900	0.001831835803287320848076
	0.001675796141912246857275
57 600	0.001538871389489429392770
62 500	0.001418062776308107455590
67 600	0.001310937280186564995212
72 900	0.001215504224559280116468
78 400	0.001130122173237172319830
84 100	0.001053427910160368407377
90 000	0.000984281714053831095741
96 100	0.000921724791278338466432
102 400	0.000864945875146480078157
108 900	0.000813254803364796346002
115 600	0.000766061455909371054356
122 500	0.000722858845618646424232
129 600	0.000683209451488917857987
136 900	0.000646734103002704610194
144 400	0.000613102885471322072868
152 100	0.000582027657112227243832
160 000	0.000553255859516875953290
168 100	0.0005265653721931795441131
176 400	0.0005017602146564829732766
184 900	0.0004786669401994877110466
193 600	0.0004571315969932358209445
202 500	0.0004370171567660898435589
211600	0.0004182013306138850902223
220 900	0.0004005747067366081191798
230 400	0.0003840391569966739846251
240 100	0.0003685064688493669322069

In[2926]:= Table2 =

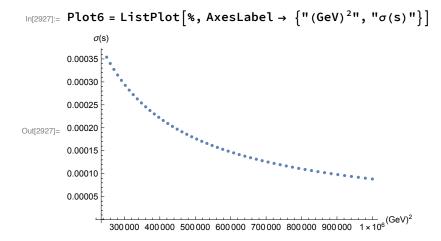


```
TableForm[\{\{500^2, PlotCross500sq\}, \{510^2, PlotCross510sq\}, \{520^2, PlotCross520sq\},
   {530<sup>2</sup>, PlotCross530sq}, {540<sup>2</sup>, PlotCross540sq}, {550<sup>2</sup>, PlotCross550sq},
```

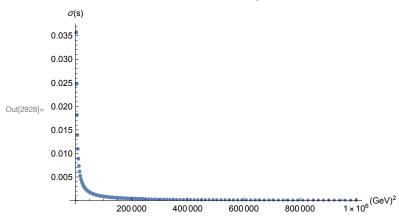
```
{560<sup>2</sup>, PlotCross560sq}, {570<sup>2</sup>, PlotCross570sq}, {580<sup>2</sup>, PlotCross580sq},
{590<sup>2</sup>, PlotCross590sq}, {600<sup>2</sup>, PlotCross600sq}, {610<sup>2</sup>, PlotCross610sq},
{620<sup>2</sup>, PlotCross620sq}, {630<sup>2</sup>, PlotCross630sq}, {640<sup>2</sup>, PlotCross640sq},
{650<sup>2</sup>, PlotCross650sq}, {660<sup>2</sup>, PlotCross660sq}, {670<sup>2</sup>, PlotCross670sq},
{680<sup>2</sup>, PlotCross680sq}, {690<sup>2</sup>, PlotCross690sq}, {700<sup>2</sup>, PlotCross700sq},
{710<sup>2</sup>, PlotCross710sq}, {720<sup>2</sup>, PlotCross720sq}, {730<sup>2</sup>, PlotCross730sq},
{740<sup>2</sup>, PlotCross740sq}, {750<sup>2</sup>, PlotCross750sq}, {760<sup>2</sup>, PlotCross760sq},
{770<sup>2</sup>, PlotCross770sq}, {780<sup>2</sup>, PlotCross780sq}, {790<sup>2</sup>, PlotCross790sq},
{800<sup>2</sup>, PlotCross800sq}, {810<sup>2</sup>, PlotCross810sq}, {820<sup>2</sup>, PlotCross820sq},
{830<sup>2</sup>, PlotCross830sq}, {840<sup>2</sup>, PlotCross840sq}, {850<sup>2</sup>, PlotCross850sq},
{860<sup>2</sup>, PlotCross860sq}, {870<sup>2</sup>, PlotCross870sq}, {880<sup>2</sup>, PlotCross880sq},
{890<sup>2</sup>, PlotCross890sq}, {900<sup>2</sup>, PlotCross900sq}, {910<sup>2</sup>, PlotCross910sq},
{920<sup>2</sup>, PlotCross920sq}, {930<sup>2</sup>, PlotCross930sq}, {940<sup>2</sup>, PlotCross940sq},
{950<sup>2</sup>, PlotCross950sq}, {960<sup>2</sup>, PlotCross960sq}, {970<sup>2</sup>, PlotCross970sq},
{980^2, PlotCross980sq}, {990^2, PlotCross990sq}, {1000^2, PlotCross1000sq}},
```

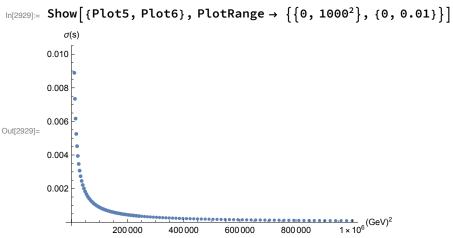
Out[2926]//TableForm=

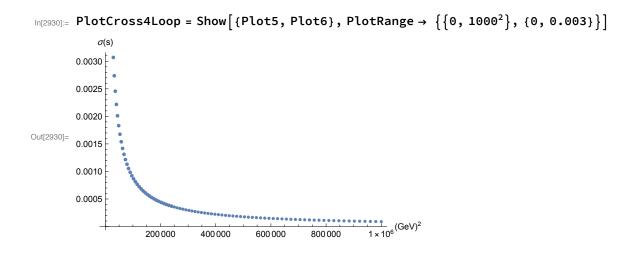
(GeV) <sup>2</sup>	$\sigma(s)$
250 000	0.0003538971669396178393236
260 100	0.0003401394948993412991316
270 400	0.0003271685329310491871401
280 900	0.0003149254308707566018393
291600	0.0003033567397768594683011
302 500	0.0002924138278410549929743
313 600	0.0002820523686801376596090
324 900	0.0002722318919367279846955
336 400	0.0002629153876666761417158
348 100	0.0002540689572801023756842
360 000	0.0002456615048791492216773
372 100	0.0002376644637366432759129
384 400	0.0002300515534167970050672
396 900	0.0002227985636768014781074
409 600	0.0002158831618270012029291
422 500	0.0002092847206839091232494
435 600	0.0002029841646382226501288
448 900	0.0001969638316904315808315
462 400	0.0001912073495887950776927
476 100	0.0001856995244460440804949
490 000	0.0001804262404184741287890
504 100	0.0001753743692094040781135
518 400	0.0001705316883126890063045
532 900	0.0001658868070447723111368
547 600	0.0001614290995287310545646
562 500	0.0001571486438935078128165
577 600	0.0001530361670382218898999
592 900	0.0001490829943869634285782
608 400	0.0001452810041253641033996
624 100	0.0001416225854678388273281
640 000	0.0001381006005548370942452
656 100	0.0001347083496236963163623
672 400	0.0001314395391355783368205
688 900	0.0001282882525752008560909
705 600	0.0001252489236702545788804
722 500	0.0001223163118040455090031
739 600	0.0001194854794184692288104
756 900	0.0001167517712252974398203
774 400	0.0001141107950622715161130
792 100	0.0001115584042469432770660
810 000	0.0001090906812958311001744
828 100	0.0001067039228894884468440
846 400	0.0001043946259757020304606
864 900	0.0001021594749134139908865
883 600	0.0000999953295692412400972
902 500	0.0000978992142867721454327
921600	0.0000958683076562667674334
940 900	0.0000938999330190690308052
960 400	0.0000919915496470428688032
980 100	0.0000901407445427445134901
1000000	0.0000883452248109058473987



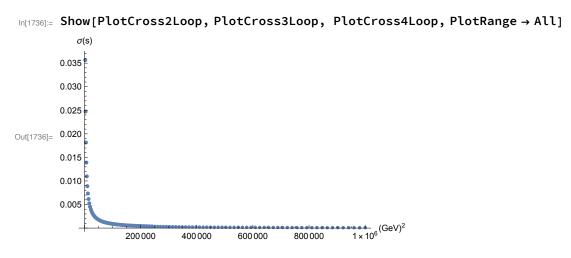








# Overlay



#### Load RunDec

```
In[541]:= << ~/Desktop/Software/CRunDec3/RunDec.m
     RunDec: a Mathematica package for running and decoupling of the
             strong coupling and quark masses
     by K.G. Chetyrkin, J.H. K\"uhn and M. Steinhauser (January 2000)
     by F. Herren and M. Steinhauser (February 2017, v3.0)
```

## Scratch