**REPORT**

Group Members: Hanfei Qi, Anmol Singh, Wuraola Olawole, Ting Lian

**Abstract**

In the most recent years, America has seen an increase in the occurrences of hate crimes. These crimes are often based on biases such as religious, racial, sexual orientations etc. and these have become a source of concern. In the initial analysis published by FiveThirtyEight, it was shown that income inequality was the main predictor of hate crimes. We worked with a dataset containing details on hate crimes occurring in several states to explore and identify other variables that were associated with hate crimes and predict its outcome. We conducted a thorough analysis of all the predictors including performing multicollinearity analysis, stepwise regression procedures, and checking model diagnostics to come up with the best possible model to explain the incidence of these crimes. Our findings show that income inequality is not the only predictor that is pertinent in determining hate crime incidence and that other factors play a role as well.

**Introduction**

Hate crimes in the United States have become a severe problem and their occurrence has been rising in recent years [[1]](https://www.bbc.com/news/world-us-canada-54968498). According to the FBI, a hate crime is a “criminal offense against a person or property motivated in whole or in part by an offender’s bias against a race, religion, disability, sexual orientation, ethnicity, gender, or gender identity.”[[2]](https://www.fbi.gov/investigate/civil-rights/hate-crimes) These types of crimes can have lasting impact and cause devastating effects to people due to the horrific nature of the crimes, which is why they are the highest priority of the FBI’s civil rights program [[2]](https://www.fbi.gov/investigate/civil-rights/hate-crimes).

A previous study used data from FBI and a self-reported survey to analyze the association between hate crime rates (outcome) and different variables (potential predictors) [[3]](https://fivethirtyeight.com/features/higher-rates-of-hate-crimes-are-tied-to-income-inequality/). The author concluded that income inequality was the most significant predictor of hate crime [[3]](https://fivethirtyeight.com/features/higher-rates-of-hate-crimes-are-tied-to-income-inequality/). In this project, our goal is to use the author’s data to build our own model, check if the author’s conclusion is correct, as well as assess if any other factors may play a role in hate crime occurrence. Potential predictors include level of state unemployment (low/high), level of state urbanization (high/low), median household income per state, percentage of adults (>25 yrs.) with a high school degree, percentage of population that are not US citizens, percentage of population that are non-white, Gini index that measuring income inequality (range 0-100). Finding out what factors play a role in the occurrence of hate crimes may be able to help us curb the incidence of these horrible crimes in the United States.

**Methods**

**Data Exploration**

There are 8 variables in the dataset. Numerical variables are: hate\_crimes\_per\_100k\_splc, median\_household\_income, perc\_population\_with\_high\_school\_degree, perc\_non\_citizen, gini\_index, and perc\_non\_white, while categorical variables include: unemployment, and urbanization. Both categorical variables contain two levels: low, and high. All coding process was done by using RStudio.

First, we generated a descriptive statistics table (Table 1). This included the mean, standard deviation (SD), median, 25% quantile (Q1), 75% quantile (Q3), minimum value, maximum value, and count of missing values for each numerical variable. For categorical variables, we obtained counts of each level, and a count of missing values. Secondly, we generated a density plot of outcome to show its distribution by using the ggplot function (Figure 1). We, furthermore, used the boxcox function to find the optimal transformation of the outcome and then double-checked the distribution of transformed outcome (Figure 2,3). Finally, we generated a scatter plot of hate\_crimes\_per\_100k\_splc versus state, from low hate crime rate to high crime rate to observe any potential outliers (Figure 4).

**Testing Original Association**

We first wanted to check if the original association presented in the prior study on hate crimes [3] holds true. We thus performed a linear regression analysis with hate\_crimes\_per\_100k\_splc as the response variable and gini\_index as the predictor. For the original data we found that the association was significant at a threshold of 0.05. However, for the log transformed data we found that the significance decreased as the relationship was not significant at a threshold of 0.05. We thought this could be a problem with model diagnostics, so we checked them using graphical displays. Doing this we found definite outliers that are affecting the association from the leverage plots. We confirmed these outliers by using the standard formula with IQR (Interquartile Range). Doing this we confirmed that the District of Columbia and Oregon were outliers. We then removed the outliers and tested the original association again. The model assumptions were met when the outliers were deleted and thus, we proceeded to check for multicollinearity in the model.

**Multicollinearity**

To check for multicollinearity in the model we started by creating a correlation matrix of all the variables that could be used in the model and then isolating the pairs of variables that had a correlation above 0.6. Furthermore, we conducted some research to figure out why these variables are so highly correlated and found sources that support the relationships we saw. Now that we know that there are highly correlated variable pairs in the model, we need to perform a stepwise regression procedure to eliminate variables that do not contribute to our model.

**Stepwise Regression Procedure**

For this procedure we started out with a model with all possible predictor variables and used the R function step in the backward direction to eliminate non-essential predictors one by one based on their AIC value.

**Interactions**

After obtaining our final model we thought to check for interactions between the predictors in our model to see how that affects the associations between the predictors and the outcome. We performed a 2-way interaction among all variables, 3-way interaction (between our predictors) of interest and an ANOVA.

**Model Diagnostics**

For model diagnosis, we plotted four diagnosis plots of our final model to check the assumptions. We also checked the existence of outliers using the studentized residuals. Since there is no candidate for outlier, we did not further explore the existence of the influential point. Finally, the existence of multicollinearity was checked by the variance inflation factor (VIF).

**Results**

**Data Exploration**

Table 1 showed that there were 4 NA’s in the variable hate\_crimes\_per\_100k\_splc and 3 NA’s in the variable perc\_non\_citizen. The low level of unemployment and urbanization were similar, about 50% across 51 states. The distribution of the outcome variable was highly skewed to right (Figure 1). The box-cox transformation indicated that a natural logarithm transformation should be applied to the outcome variable (Figure 2). The distribution of transformed outcome variable was approximately normal (Figure 3). The scatter plot indicated that data from District of Columbia and Oregon could be potential outliers (Figure 4).

**Checking Original Association**

When checking the association between income inequality and hate crime rate using the original data, we found that there is a significant linear relationship exists with p-value equals 0.024 (Table 2). However, in the data exploration part, we found that the original data is heavily left skewed. So we also checked the association using the log transformed data. The p-value for the association using transformed data was 0.311 (Table 3) indicating that the linear association between income inequality and hate crime rate is not significant.

**Multicollinearity**

There were three pairs of variables that were highly correlated (correlation > 0.6) in this analysis (Table 4). We found that studies have shown that high income is correlated with increased education and thus it would make sense that the median income and percentage of high school diploma holders are highly correlated [[4]](https://budgetmodel.wharton.upenn.edu/issues/2016/2/22/education-and-income-growth). Furthermore, a study conducted by the pew research center found that only 17.7% of immigrants are white non-hispanic which makes sense why the percentage of non citizens and the percentage of white people are very highly correlated as well [[5]](https://www.pewresearch.org/hispanic/2020/08/20/facts-on-u-s-immigrants-current-data/). To address the problem of the high correlation between these variables as well as eliminate any other insignificant predictors we ran the model through a stepwise regression procedure which narrowed the final model down to unemployment, perc\_population\_with\_high\_school\_degree, and gini\_index as predictors.

**Interactions**

We explored all 2-way interactions among all the variables. Here, we observed that there were three different interactions (Figure 5). Next, we did a stratified analysis to further explore these interactions. From these we found that two of the interactions were not significant. The only significant interaction upon stratification was between urbanization and perc\_population\_with\_high\_school\_degree: high urbanization affects the percentage of the population with high school degree. We further carried out an ANOVA test and obtained that there was no statistical evidence of interaction . We also checked for 3-way interactions between our predictors of interest but found no significant interaction.

**Model Diagnostics**

We plotted the four diagnosis graphs after we got the final model (Figure 6). Points in the Residuals vs. Fitted plot show a random pattern and are evenly spread above and below the line of 0. The red line is approximately horizontal and is bouncing around the line of 0. This graph shows that this model fit the assumption of homoscedasiticity. Similar pattern also shows in the Scale-Location plot indicating that the variance of the model is equal. No point in the Residual vs. Leverage plot is beyond the boundary of Cook’s distance so we could assume that there is no significant influence point. In the Normal Q-Q Plot, all points align in an approximately straight line with no significant departure which indicates that the residuals are normal. Overall, these four graphs show that this fitted model is good for represent the data. There is no observation has absolute studentized residual value greater than 2.5. So we conlcude that there is no outlier in Y in the data and assume that there is no influential point. The VIF values for the three predictors are 1.335 for unemploymentlow, 1.806 for gini\_index and, 1.971 for perc\_population\_with\_high\_school\_degree (Table 5). None of the predictor has variance inflation factor (VIF) value greater than 5 indicating that there is no multicollinearity in the final model.

**Conclusion/Discussion**

The final model included unemployment, perc\_population\_with\_high\_school\_degree, and gini\_index as predictors, without any interactions. We concluded that gini\_index was not the only main predictor. Adjusting for other predictors made the association between gini\_index and hate crimes more significant than when gini\_index was the only predictor based on the comparison of p-values between the two models. Thus, from our analysis we conclude that it is important to account for unemployment, the percentage of population with a high school degree, and the income inequality of an area when assessing the incidence of hate crimes.

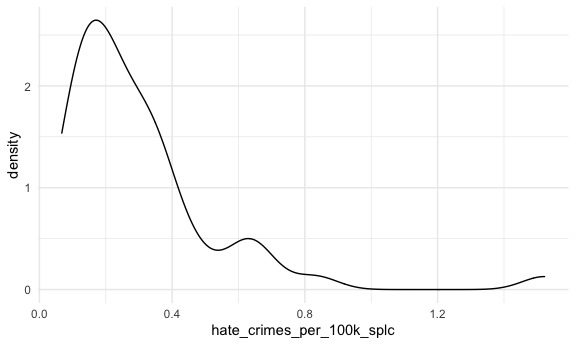
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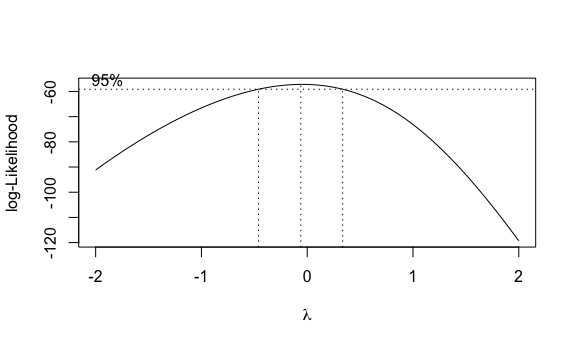
**Appendix:**

**Descriptive Statistics**

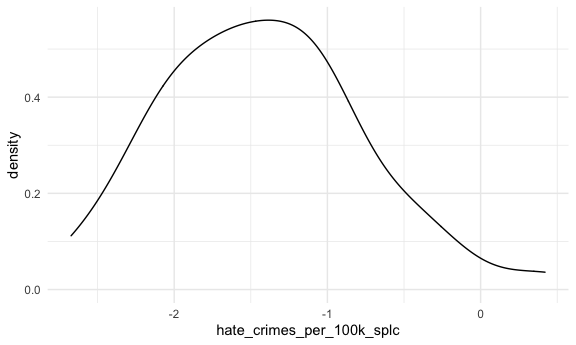
**Table 1: Descriptive Statistics**

|  |  |
| --- | --- |
|  | Overall (N=51) |
| hate\_crimes\_per\_100k\_splc |  |
| -Mean (SD) | 0.304 (0.253) |
| -Median (Q1, Q3) | 0.226 (0.143, 0.357) |
| - Min - Max | 0.067 - 1.522 |
| - Missing | 4 |
| unemployment |  |
| - high | 24 (47.1%) |
| - low | 27 (52.9%) |
| - Missing | 0 |
| urbanization |  |
| - high | 24 (47.1%) |
| - low | 27 (52.9%) |
| - Missing | 0 |
| median\_household\_income |  |
| - Mean (SD) | 55223.608 (9208.478) |
| - Median (Q1, Q3) | 54916.000 (48657.000, 60719.000) |
| - Min - Max | 35521.000 - 76165.000 |
| - Missing | 0 |
| perc\_population\_with\_high\_school\_degree |  |
| - Mean (SD) | 0.869 (0.034) |
| - Median (Q1, Q3) | 0.874 (0.841, 0.898) |
| - Min - Max | 0.799 - 0.918 |
| - Missing | 0 |
| perc\_non\_citizen |  |
| - Mean (SD) | 0.055 (0.031) |
| - Median (Q1, Q3) | 0.045 (0.030, 0.080) |
| - Min - Max | 0.010 - 0.130 |
| - Missing | 3 |
| gini\_index |  |
| - Mean (SD) | 0.454 (0.021) |
| - Median (Q1, Q3) | 0.454 (0.440, 0.467) |
| - Min - Max | 0.419 - 0.532 |
| - Missing | 0 |
| perc\_non\_white |  |
| - Mean (SD) | 0.316 (0.165) |
| - Median (Q1, Q3) | 0.280 (0.195, 0.420) |
| - Min - Max | 0.060 - 0.810 |
| - Missing | 0 |

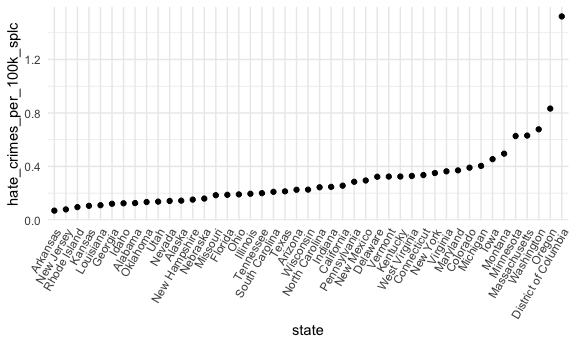


**Figure 1: Distribution of hate\_crimes\_per\_100k\_splc.**

**Figure 2: Box-Cox transformation.**



**Figure 3: Distribution of hate\_crimes\_per\_100k\_splc after applied logarithm transformation.**



**Figure 4: Scatter plot of hate\_crimes\_per\_100k\_splc of each state, from lowest hate crime rate to highest crime rate.**

**Modeling**

**Table 2: Testing Association Between Income Inequality & Hate Crime Rate Using Original Data**

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Term | Estimate | std.error | Statistic | p.value |
| (Intercept) | -1.527463 | 0.7833043 | -1.950025 | 0.0574197 |
| gini\_index | 4.020510 | 1.7177215 | 2.340606 | 0.0237445 |

**Table 3: Testing Association Between Income Inequality & Hate Crime Rate Using Transformed Data.**

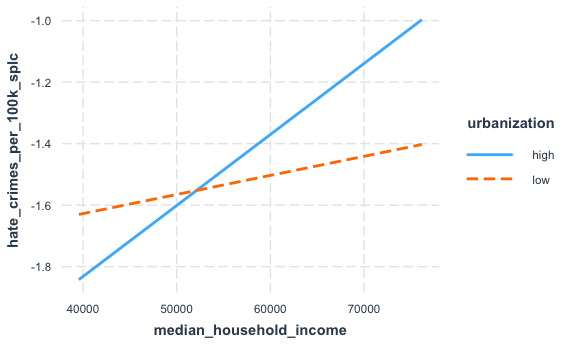
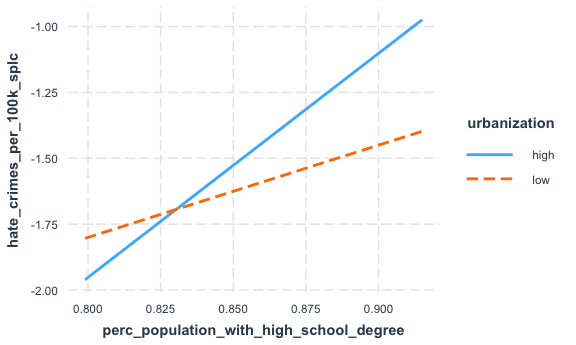
|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Term | Estimate | std.error | Statistic | p.value |
| (Intercept) | -3.675547 | 2.195289 | -1.674288 | 0.1010115 |
| gini\_index | 4.931538 | 4.814087 | 1.024398 | 0.3111231 |

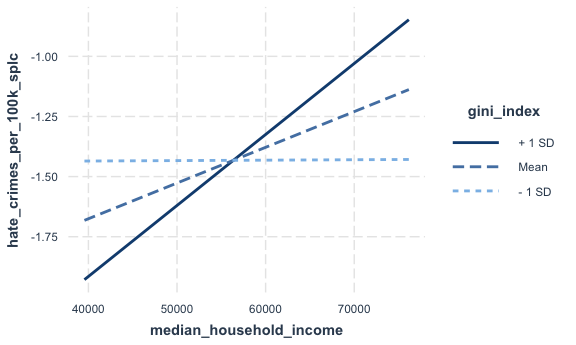
**Table 4: Variables that are Highly Correlated from Correlation Matrix (Correlation ≥ |0.6|)**

Table

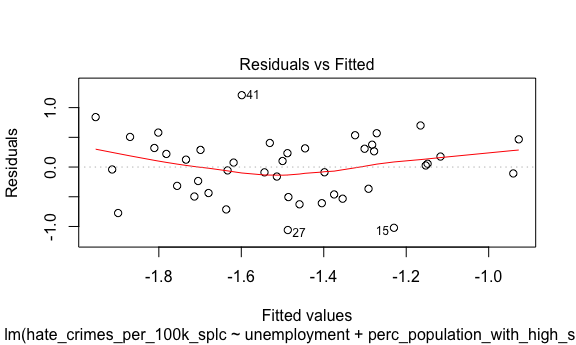
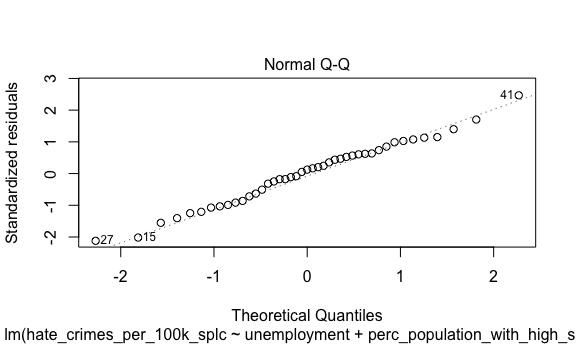
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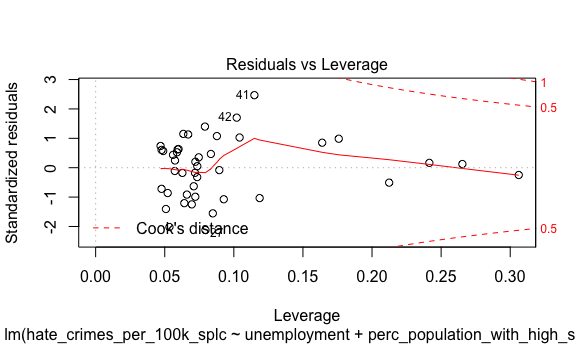
**Interactions**

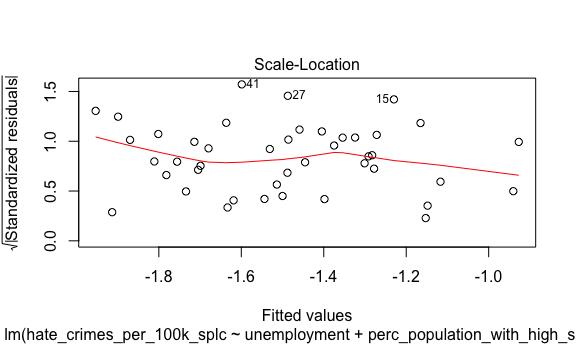




**Figure 5: Two-way Interactions Among All Predictors**

**Model Diagnostics**





**Figure 6: Four Diagnosis Graphs for the Final Model**

**Table 5: The variance inflation factor Values for the Final Model**

|  |  |
| --- | --- |
|  | x |
| unemploymentlow | 1.335118 |
| perc\_population\_with\_high\_school\_degree | 1.970627 |
| gini\_index | 1.806199 |