

AI1103-Assignment 1

Name: Asish sashank reddy, Roll Number: CS20BTECH11010

Download all python codes from

<https://github.com/asishcs2011010/demo/blob/main/assignment-1/assignment-1.py>

and latex-tikz codes from

[https://github.com/asishcs2011010/demo/blob/main/assignment-1/assignment-1\(8\).tex](https://github.com/asishcs2011010/demo/blob/main/assignment-1/assignment-1(8).tex)

QUESTION NO

prob - 1.15

QUESTION

Let $X \in \{0, 1\}$ and $Y \in \{0, 1\}$ be two independent binary random variables. if $P(X = 0) = p$ and $P(Y = 0) = q$, then $P(X + Y \geq 1)$ is equal to

- (A) $pq + (1 - p)(1 - q)$ (C) $p(1 - q)$
 (B) pq (D) $1 - pq$

SOLUTION

Given $\Pr(X=0) = p$, $\Pr(Y=0) = q$ and X and Y are independent binary random variables.

| X | $X = 0$ | $X = 1$ |
|----|---------|---------|
| Pr | p | $1 - p$ |

| Y | $Y = 0$ | $Y = 1$ |
|----|---------|---------|
| Pr | q | $1 - q$ |

$P(X + Y \geq 1) = 1 - P(X + Y < 1)$

$(X + Y < 1, \text{ implies } X=0, Y=0; \text{ as } X \in \{0, 1\} \text{ and } Y \in \{0, 1\})$

$P(X + Y \geq 1) = 1 - (P(X = 0)(Y = 0))$ (as they are independent events)

$P(X + Y \geq 1) = 1 - pq$