1

AI1103-Assignment 3

Name: Asish sashank reddy, Roll Number: CS20BTECH11010

Download all python codes from

https://github.com/asishcs2011010/demo/blob/main/assignment-3/assignment-3.py

and latex-tikz codes from

https://github.com/asishcs2011010/demo/blob/main/assignment-3/assignment-3(3).tex

QUESTION NO

GATE 2019 (IN), Q.3 (IN Engg. section)

QUESTION

A box has 8 red balls and 8 green balls. Two balls are drawn randomly in succession from the box without replacement. The probability that the first ball drawn is red and the second ball drawn is green is

- 1) $\frac{4}{15}$
- 2) $\frac{7}{16}$
- 3) $\frac{1}{2}$
- 4) $\frac{8}{15}$

SOLUTION

let $X \in \{0,1\}$ and $Y \in \{0,1\}$ be the random variable which denotes whether the picked up ball is red or green in the first draw and second draw respectively.

- 1 represents picking up of red ball
- 0 represent picking up of green ball

The probability that the second ball drawn is green

given that first ball drawn is red is = $Pr(Y = 0|X = 1) = \frac{8}{15}$

$$Pr(Y = 0|X = 1) = \frac{8}{15}$$
 (0.0.2)

We know that

$$Pr(X = x | Y = y) = \frac{Pr(X = x, Y = y)}{Pr(Y = y)}$$
(0.0.3)

The probability that the first ball drawn is red and the second ball drawn is green = Pr(X = 1, Y = 0)

$$Pr(X = 1, Y = 0) = Pr(X = 1) \times Pr(Y = 0 | X = 1)$$

$$(0.0.4)$$

$$Pr(X = 1, Y = 0) = \frac{8}{16} \times \frac{8}{15} = \frac{4}{15}$$