

# AI1103-Assignment 4

Name: Asish sashank reddy, Roll Number: CS20BTECH11010

Download all python codes from

<https://github.com/asishcs2011010/demo/blob/main/assignment-4/assignment-4.py>

and latex-tikz codes from

[https://github.com/asishcs2011010/demo/blob/main/assignment-4/assignment-4\(2\).tex](https://github.com/asishcs2011010/demo/blob/main/assignment-4/assignment-4(2).tex)

QUESTION NO

gov/stats/2015/statistics-I(1), Q.1(C)

QUESTION

1)(c) Let X have pdf

$$f(x) = \begin{cases} \frac{1}{3} & -1 \leq x < 2 \\ 0 & \text{otherwise} \end{cases}$$

SOLUTION

CDF of X is defined as,

$$F_X(x) = \Pr(X \leq x) \quad (0.0.1)$$

The cdf of  $Y = X^2$  is given by  $G(y)$

$$G(y) = F_X(y) = \Pr(X^2 \leq y) = \Pr(X \leq \sqrt{y}) = F_X(\sqrt{y}) \quad (0.0.2)$$

$$G(y) = \int_{\max(-1, -\sqrt{y})}^{\min(2, \sqrt{y})} \frac{1}{3} dx \quad (0.0.3)$$

As bounds of integral should also remain within the support of the random variable X.

so when  $0 \leq y < 1$ , we have

$\max(-1, -\sqrt{y}) = -\sqrt{y}$ , and when  $1 \leq y$  it is -1. similarly the upper limit is  $\sqrt{y}$  when  $y < 9$  and 3 otherwise

$$G(y) = \begin{cases} 0 & y < 0 \\ \frac{2\sqrt{y}}{3} & 0 \leq y < 1 \\ \frac{\sqrt{y}+1}{3} & 1 \leq y < 4 \\ 1 & y \geq 4 \end{cases}$$

The plot of CDF is given in the Figure 0

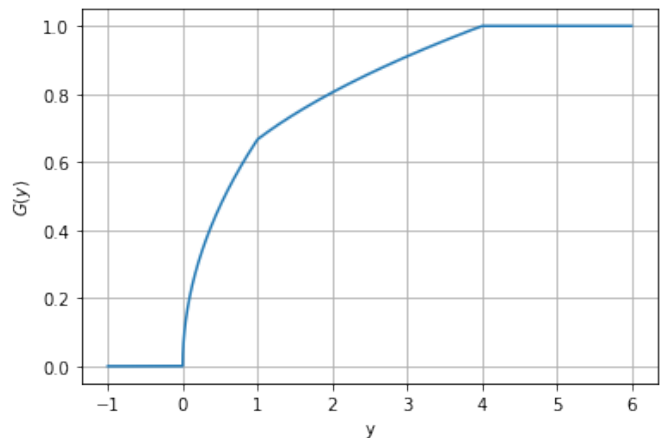


Fig. 0: CDF of X