Source Code

First, I generate a 3x3 matrix of random numbers. To create it, I use a function **randi** that generates an integer or a matrix of integers between a given range, which in my case is [-1000,1000]. In order to keep the numbers between -0.1 and 0.1, I multiply the matrix by 0.0001. Then, I make a matrix A that is a sum of matrix r with random numbers, and coordinates given in the exercise. Each row of the matrix A represents a point and columns stand for respectively x, y, z coordinate.

Second, I want to find the equation of the plane that the three points lie on. Because of the choice of constant coordinates and the range of random numbers that are added to it, the plane will not pass through the origin. Therefore, the equation of the plane can be written as:

$$ax + by + cz = 1$$

To find numbers a, b, c I want to solve the equation:

$$\begin{pmatrix} x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \\ x_3 & y_3 & z_3 \end{pmatrix} \times \begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$$

Where x_i, y_i, z_i stand for coordinates of given points. The equation can be written as:

$$AX = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$$

I find matrix X using Gaussian elimination operator \ I get:

$$X = A \setminus \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$$

Where $X = \begin{pmatrix} a \\ b \\ c \end{pmatrix}$, which is the solution.

Output