

CSCI361 Assignment 1

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Part 2

1.

a)

$$1 \leq a < 14$$

$$0 \leq b < 14$$

$\gcd(a, m)$, where $m = 14$ = size of the alphabet must be 1. a and m need to be coprime

$$\gcd(a, 14) = 1$$

If the key is a multiple of the size of the alphabet, one to one mappings will not be possible

b)

The possible values of a are (6)

1, 3, 5, 9, 11, 13

The possible values of b are 0, 1 .. 13 (14 values)

$$14 * 6 = 84 \text{ distinct keys for the cipher}$$

c)

$$a = \text{"B"} = 11$$

$$b = 3$$

Plaintext	4	9	7	0	5	1	2
$a(X)$	44	99	77	0	55	11	22
$+ b$	47	102	80	3	58	14	25
$\text{mod}(14)$	5	4	A	3	2	0	B
Ciphertext	5	4	A	3	2	0	B

2)

X (P)	$x^2 + x + 1$	$\text{mod } 15 == y$
0	1	1
1	3	3
2	7	7
3	13	13
4	21	6
5	31	1
6	43	13
7	57	12
8	73	13
9	91	1
10	111	6
11	133	13
12	157	7
13	183	3
14	211	1

The mapping is not valid, as the function is not a one to one mapping. The duplicate values of y are highlighted in the same color.