

Name: Asjid Fahir
Roll no: 19p-0085
Section: B

Numerical Computing

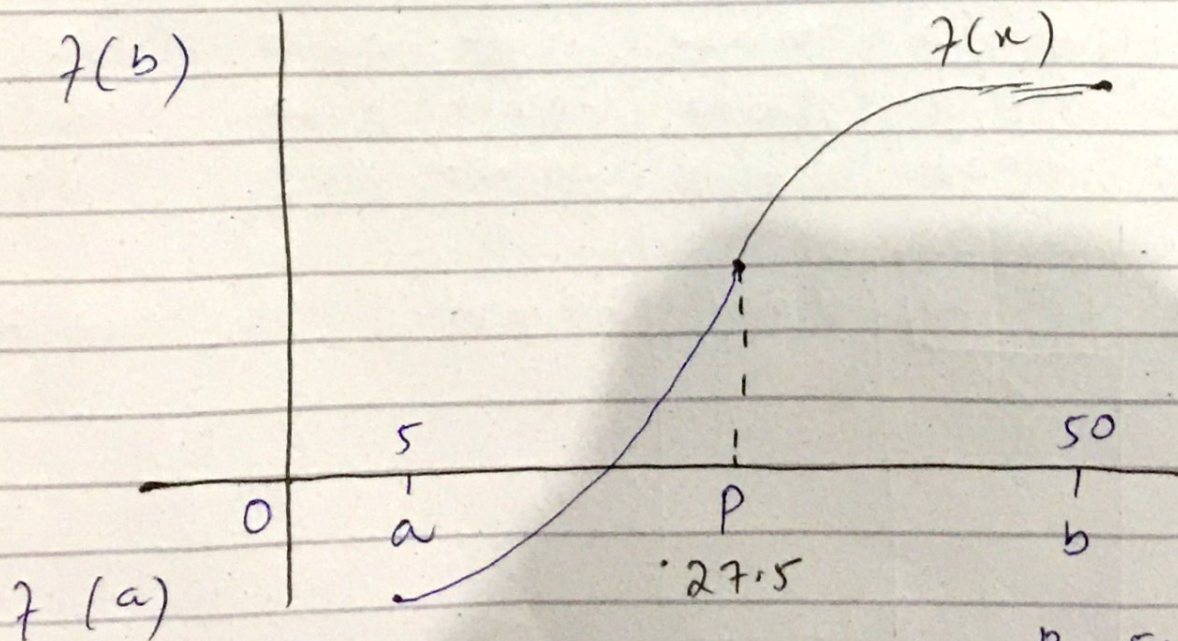
Assignment # 03:

Topic: Root Finding

1. $F(x) = x^2 - 81$

where, $a = 5, b = 50$

First, we understand diagrammatically,



$$f(a) = -56, f(b) = 2419$$

\therefore when we put value in eq!

$$p = \frac{5+50}{2}$$

$$p = 27.5$$

1st iteration:

$$f(a) = -56, \quad f(b) = 2419$$

$$P_1 = 27.5$$

$$F(P_1) = (27.5)^2 - 81 = 675.25$$

2nd iteration:

$$F(P_2) = ?$$

$$P_2 = \frac{5 + 27.5}{2} = 16.25$$

$$F(P_2) = (16.25)^2 - 81 = 183.0625$$

3rd iteration

$$P_3 = \frac{5 + 16.25}{2} = 10.625$$

$$F(P_3) = (10.625)^2 - 81 = 31.890$$

4th iteration

$$P_4 = \frac{5 + 10.625}{2} = 7.8125$$

$$F(P_4) = (7.8125)^2 - 81 = -19.964 < 0$$

And, that's how we go on doing the iterations!

Table (for iteration)

i	a_n	P_n	b_n	$f(a)$	$f(b)$	$f(p)$
1	5	27.5	50	-56	2419	675.25
2	5	16.25	27.5	-56	675.25	183.062
3	5	10.625	16.25	-56	183.062	31.890
4	5	7.8125	10.625	-56	31.890	-19.964
5	7.812	9.218	10.625	-19.964	31.890	3.985
6	7.812	8.515	9.218	-19.964	3.985	-8.484
7	8.515	8.867	9.218	-8.484	3.985	-2.372
8	8.867	9.042	9.218	-2.372	3.985	0.775
9	8.867	8.955	9.042	-2.372	0.775	-0.806
10	8.955	8.999	9.042	-0.806	0.775	-0.017
11	8.999	9.020	9.042	-0.017	0.775	0.378
12	8.999	9.010	9.020	-0.017	0.378	0.180
13	8.999	9.004	9.010	-0.017	0.180	0.081
14	8.999	9.001	9.004	-0.017	0.081	0.031
15	8.999	9.000	9.001	-0.017	0.031	0.007



$$P_n = 9.000$$