

## PROBLEMS

Answers to problems marked with \* appear at the end of the book.

- 2.1** Demonstrate the validity of the following identities by means of truth tables:
- (a) DeMorgan's theorem for three variables:  $(x + y + z)' = x'y'z'$  and  $(xyz)' = x' + y' + z'$
  - (b) The distributive law:  $x + yz = (x + y)(x + z)$
  - (c) The distributive law:  $x(y + z) = xy + xz$
  - (d) The associative law:  $x + (y + z) = (x + y) + z$
  - (e) The associative law and  $x(yz) = (xy)z$
- 2.2** Simplify the following Boolean expressions to a minimum number of literals:
- (a)\*  $xy + xy'$
  - (b)\*  $(x + y)(x + y')$
  - (c)\*  $xyz + x'y + xyz'$
  - (d)\*  $(A + B)'(A' + B)'$
  - (e)  $xyz' + x'yz + xyz + x'yz'$
  - (f)  $(x + y + z')(x' + y' + z)$
- 2.3** Simplify the following Boolean expressions to a minimum number of literals:
- (a)\*  $ABC + A'B + ABC'$
  - (b)\*  $x'yz + xz$
  - (c)\*  $(x + y)(x' + y')$
  - (d)\*  $xy + x(wz + wz')$
  - (e)\*  $(BC' + A'D)(AB' + CD')$
  - (f)  $(x + y' + z')(x' + z')$
- 2.4** Reduce the following Boolean expressions to the indicated number of literals:
- (a)\*  $A'C' + ABC + AC'$  to three literals
  - (b)\*  $(x'y' + z)' + z + xy + wz$  to three literals
  - (c)\*  $A'B(D' + C'D) + B(A + A'CD)$  to one literal
  - (d)\*  $(A' + C)(A' + C')(A + B + C'D)$  to four literals
  - (e)  $ABCD + A'BD + ABC'D$  to two literals
- 2.5** Draw logic diagrams of the circuits that implement the original and simplified expressions in Problem 2.2.
- 2.6** Draw logic diagrams of the circuits that implement the original and simplified expressions in Problem 2.3.
- 2.7** Draw logic diagrams of the circuits that implement the original and simplified expressions in Problem 2.4.
- 2.8** Find the complement of  $F = wx + yz$ ; then show that  $FF' = 0$  and  $F + F' = 1$ .
- 2.9** Find the complement of the following expressions:
- (a)\*  $xy' + x'y$
  - (b)  $(A'B + CD)E' + E$
  - (c)  $(x' + y + z')(x + y')(x + z)$
- 2.10** Given the Boolean functions  $F_1$  and  $F_2$ , show that
- (a) The Boolean function  $E = F_1 + F_2$  contains the sum of the minterms of  $F_1$  and  $F_2$ .
  - (b) The Boolean function  $G = F_1F_2$  contains only the minterms that are common to  $F_1$  and  $F_2$ .
- 2.11** List the truth table of the function:
- (a)\*  $F = xy + xy' + y'z$
  - (b)  $F = x'z' + yz$
- 2.12** We can perform logical operations on strings of bits by considering each pair of corresponding bits separately (called bitwise operation). Given two eight-bit strings  $A = 10110001$  and  $B = 10101100$ , evaluate the eight-bit result after the following logical operations: (a)\* AND, (b) OR, (c)\* XOR, (d)\* NOT A, (e) NOT B.

**2.13** Draw logic diagrams to implement the following Boolean expressions:

- (a)  $Y = A + B + B'(A + C')$
- (b)  $Y = A(B \oplus D) + C'$
- (c)  $Y = A + CD + ABC$
- (d)  $Y = (A \oplus C)' + B$
- (e)  $Y = (A' + B')(C + D')$
- (f)  $Y = [(A + B')(C' + D)]$

**2.14** Implement the Boolean function

$$F = xy + x'y' + y'z$$

- (a) with AND, OR, and inverter gates,
- (b)\* with OR and inverter gates,
- (c) with AND and inverter gates,
- (d) with NAND and inverter gates, and
- (e) with NOR and inverter gates.

**2.15\*** Simplify the following Boolean functions  $T_1$  and  $T_2$  to a minimum number of literals:

<b>A</b>	<b>B</b>	<b>C</b>	<b><math>T_1</math></b>	<b><math>T_2</math></b>
0	0	0	1	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	0	1
1	0	1	0	1
1	1	0	0	1
1	1	1	0	1

**2.16** The logical sum of all minterms of a Boolean function of  $n$  variables is 1.

- (a) Prove the previous statement for  $n = 3$ .
- (b) Suggest a procedure for a general proof.

**2.17** Obtain the truth table of the following functions, and express each function in sum-of-minterms and product-of-maxterms form:

- (a)\*  $(xy + z)(y + xz)$
- (b)  $(x + y')(y' + z)$
- (c)  $x'z + wx'y + wyz' + w'y'$
- (d)  $(xy + yz' + x'z)(x + z)$

**2.18** For the Boolean function

$$F = xy'z + x'y'z + w'xy + wx'y + wxy$$

- (a) Obtain the truth table of  $F$ .
- (b) Draw the logic diagram, using the original Boolean expression.
- (c)\* Use Boolean algebra to simplify the function to a minimum number of literals.
- (d) Obtain the truth table of the function from the simplified expression and show that it is the same as the one in part (a).
- (e) Draw the logic diagram from the simplified expression, and compare the total number of gates with the diagram of part (b).

**2.19\*** Express the following function as a sum of minterms and as a product of maxterms:

$$F(A, B, C, D) = B'D + A'D + BD$$

**2.20** Express the complement of the following functions in sum-of-minterms form:

(a)  $F(A, B, C, D) = \Sigma(3, 5, 9, 11, 15)$       (b)  $F(x, y, z) = \Pi(2, 4, 5, 7)$

**2.21** Convert each of the following to the other canonical form:

(a)  $F(x, y, z) = \Sigma(2, 5, 6)$       (b)  $F(A, B, C, D) = \Pi(0, 1, 2, 4, 7, 9, 12)$

**2.22\*** Convert each of the following expressions into sum of products and product of sums:

(a)  $(AB + C)(B + C'D)$       (b)  $x' + x(x + y')(y + z')$

**2.23** Draw the logic diagram corresponding to the following Boolean expressions without simplifying them:

(a)  $BC' + AB + ACD$       (b)  $(A + B)(C + D)(A' + B + D)$   
 (c)  $(AB + A'B')(CD' + C'D)$       (d)  $A + CD + (A + D')(C' + D)$

**2.24** Show that the dual of the exclusive-OR is equal to its complement.

**2.25** By substituting the Boolean expression equivalent of the binary operations as defined in Table 2.8, show the following:

- (a) The inhibition operation is neither commutative nor associative.  
 (b) The exclusive-OR operation is commutative and associative.

**2.26** Show that a positive logic NAND gate is a negative logic NOR gate and vice versa.

**2.27** Write the Boolean equations and draw the logic diagram of the circuit whose outputs are defined by the following truth table:

$f_1$	$f_2$	$a$	$b$	$c$
1	0	0	0	0
0	0	0	0	1
0	1	0	1	0
1	1	0	1	1
0	1	1	0	0
0	1	1	0	1
1	1	1	1	0
1	0	1	1	1

**2.28** Write Boolean expressions and construct the truth tables describing the outputs of the circuits described by the following logic diagrams:

