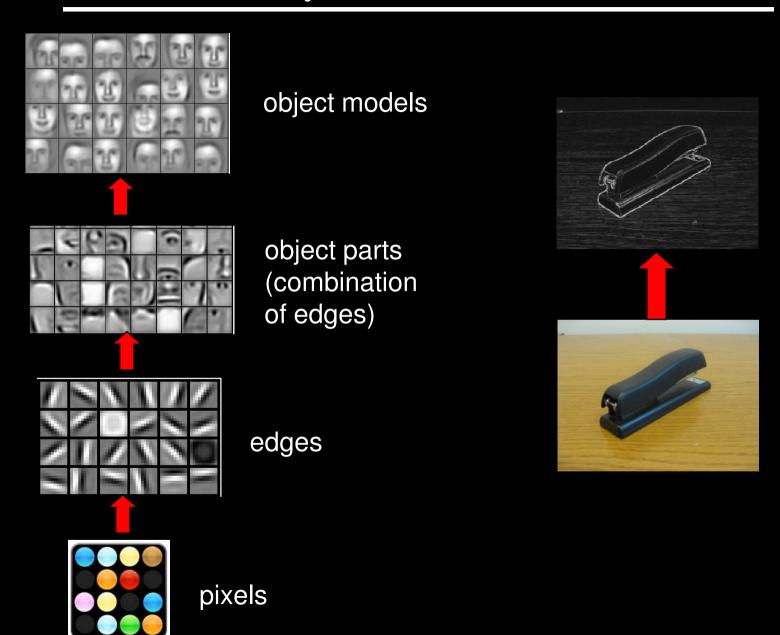
Some slides were adated/taken from various sources, including Andrew Ng's Coursera Lectures, CS231n: Convolutional Neural Networks for Visual Recognition lectures, Stanford University CS Waterloo Canada lectures, Aykut Erdem, et.al. tutorial on Deep Learning in Computer Vision, Ismini Lourentzou's lecture slide on "Introduction to Deep Learning", Ramprasaath's lecture slides, and many more. We thankfully acknowledge them. Students are requested to use this material for their study only and NOT to distribute it.

# Learning feature hierarchies/Deep learning

# Why feature hierarchies



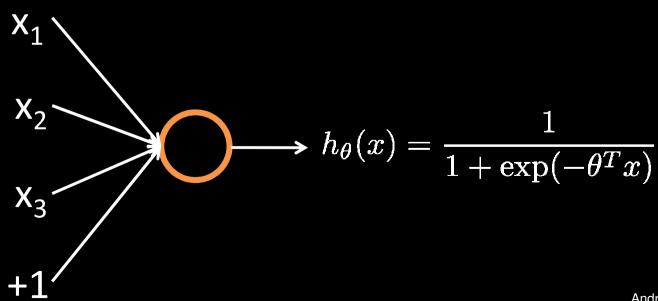
#### Logistic regression

Logistic regression has a learned parameter vector  $\theta$ . On input x, it outputs:

$$h_{ heta}(x) = \sigma( heta^T x) = rac{1}{1 + \exp(- heta^T x)}$$

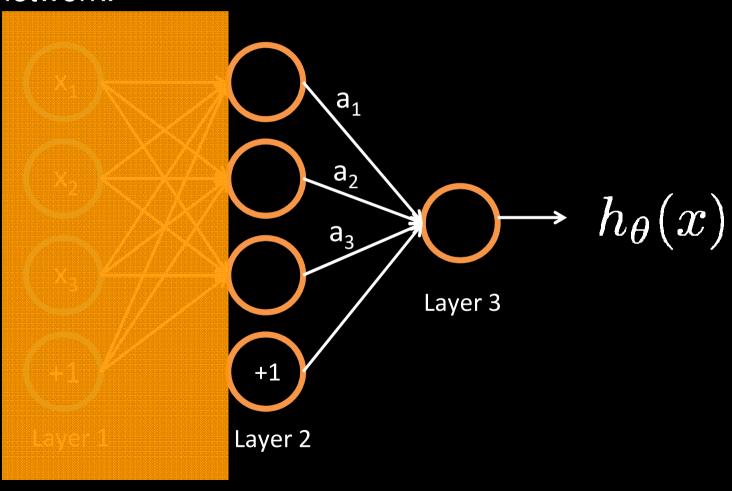
where 
$$\sigma(z) = 1/(1 + \exp(-z))$$

Draw a logistic regression unit as:



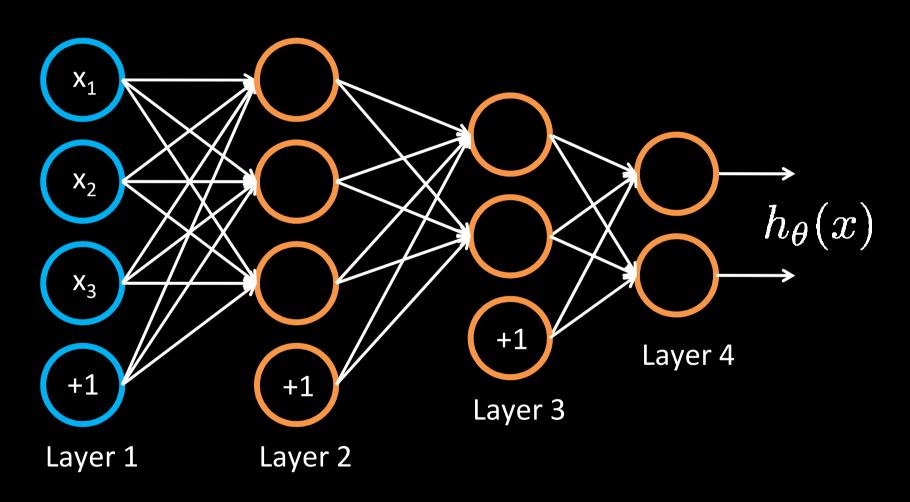
#### **Neural Network**

String a lot of logistic units together. Example 3 layer network:

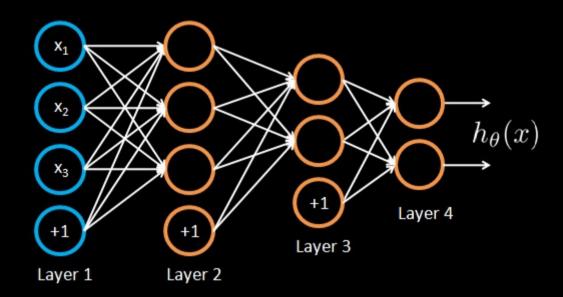


#### **Neural Network**

Example 4 layer network with 2 output units:



#### Training a neural network

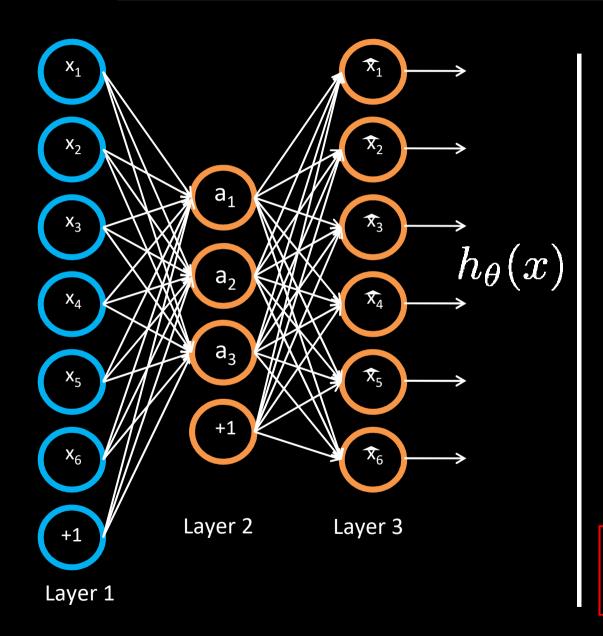


Given training set  $(x_1, y_1), (x_2, y_2), (x_3, y_3), \dots$ 

Adjust parameters  $\theta$  (for every node) to make:

$$h_{\theta}(x_i) \approx y_i$$

(Use gradient descent. "Backpropagation" algorithm. Susceptible to local optima.)



Autoencoder.

Network is trained to output the input (learn identify function).

$$h_{\theta}(x) \approx x$$

Trivial solution unless:

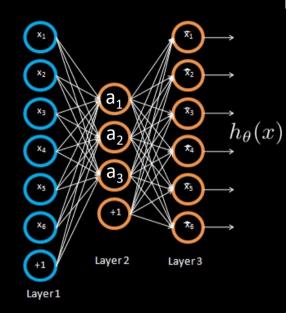
- Constrain number of units in Layer 2 (learn compressed representation), or
- Constrain Layer 2 to be **sparse**.

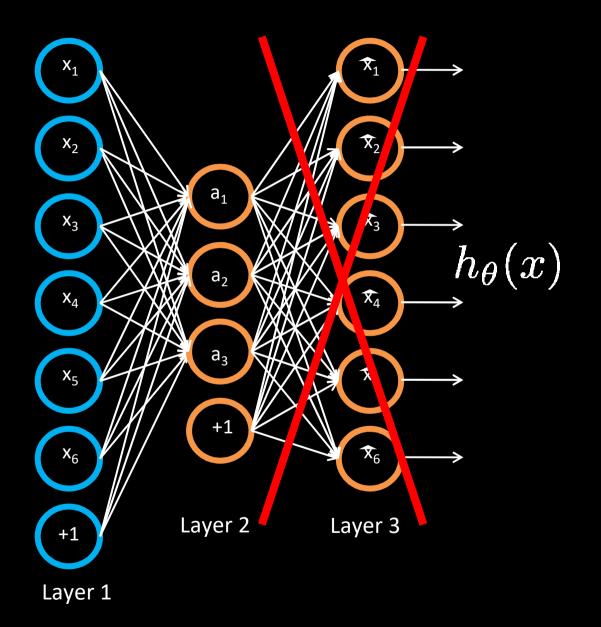
Training a sparse autoencoder.

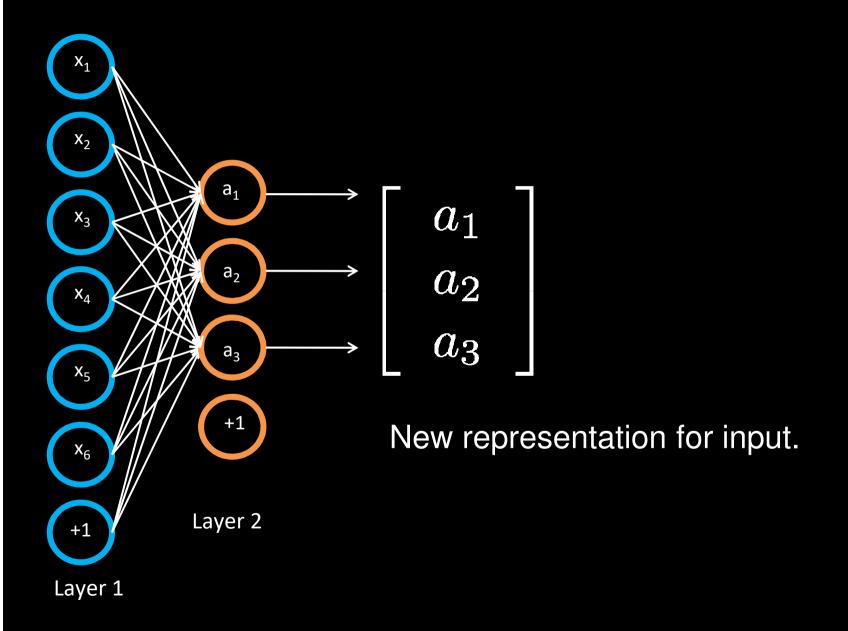
error term

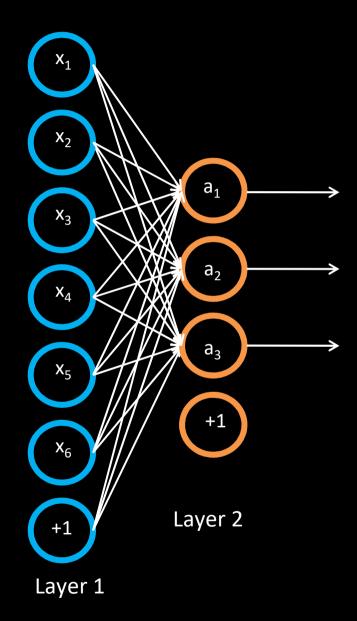
Given unlabeled training set x<sub>1</sub>, x<sub>2</sub>, ...

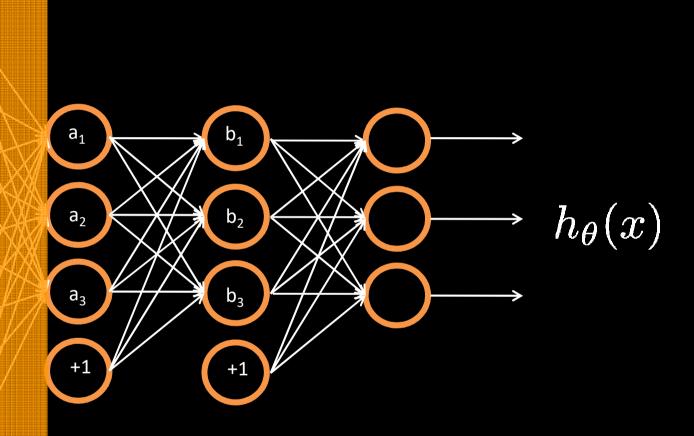
$$\min_{\theta} \left\| h_{\theta}(x) - x \right\|^2 + \lambda \sum_{i} |a_i|$$
Reconstruction L<sub>1</sub> sparsity term



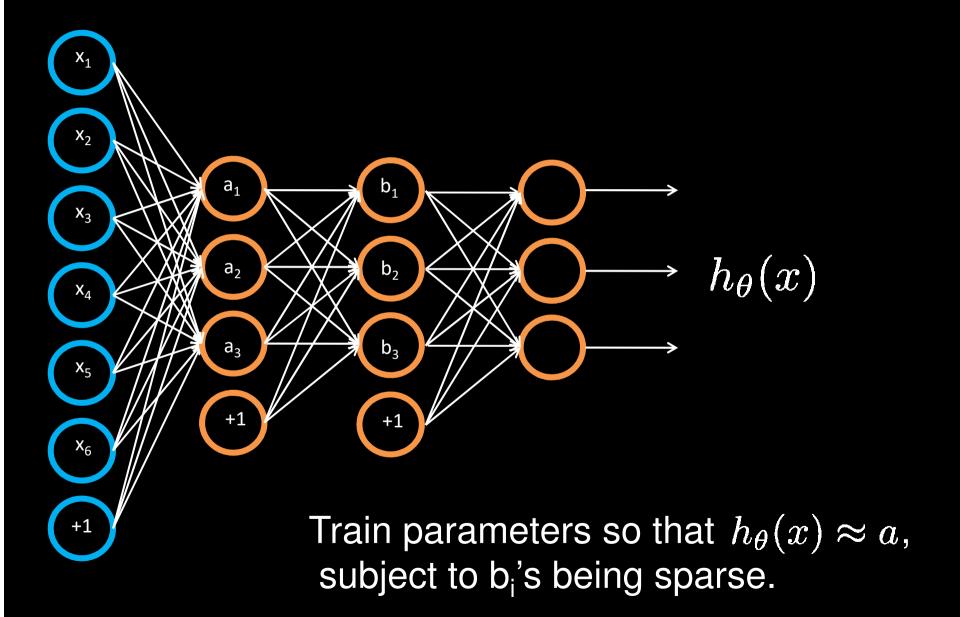


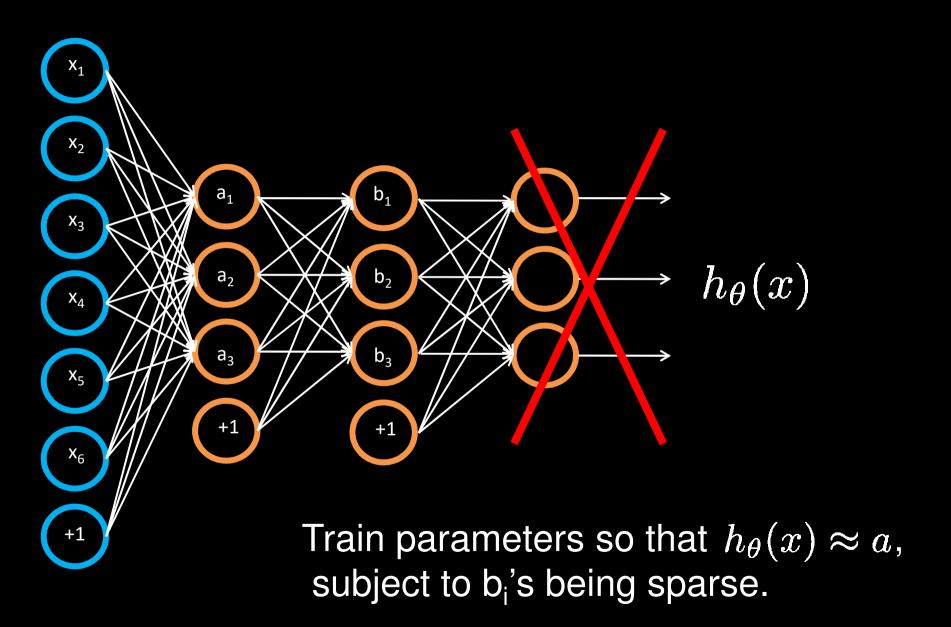


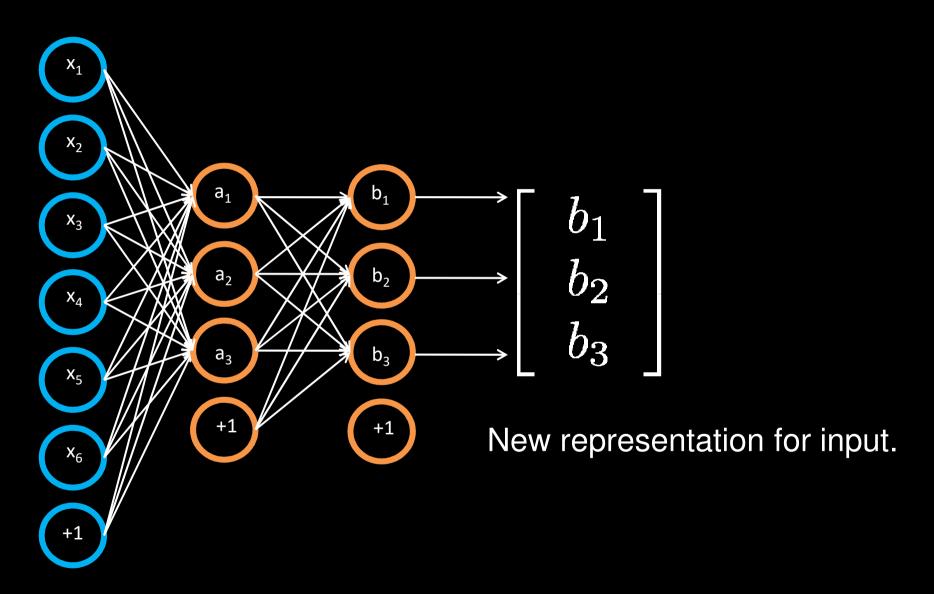


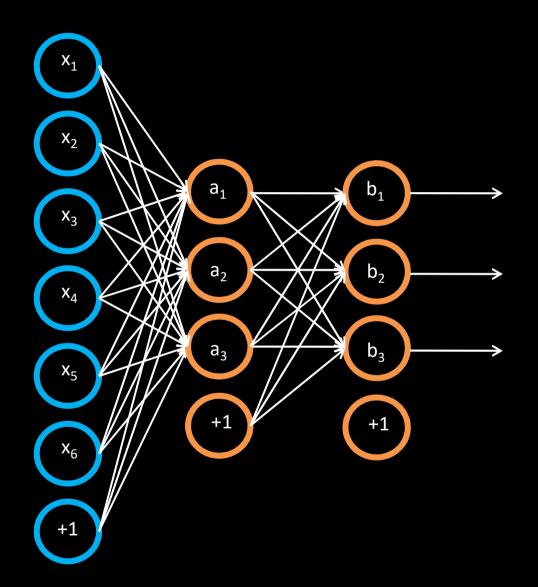


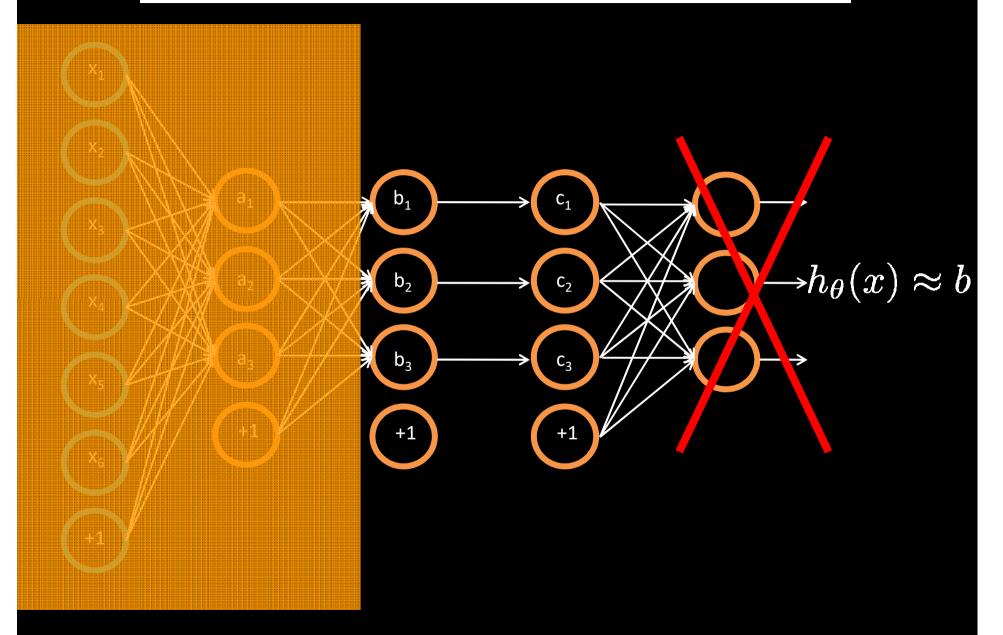
Train parameters so that  $h_{\theta}(x) \approx a$ , subject to b<sub>i</sub>'s being sparse.

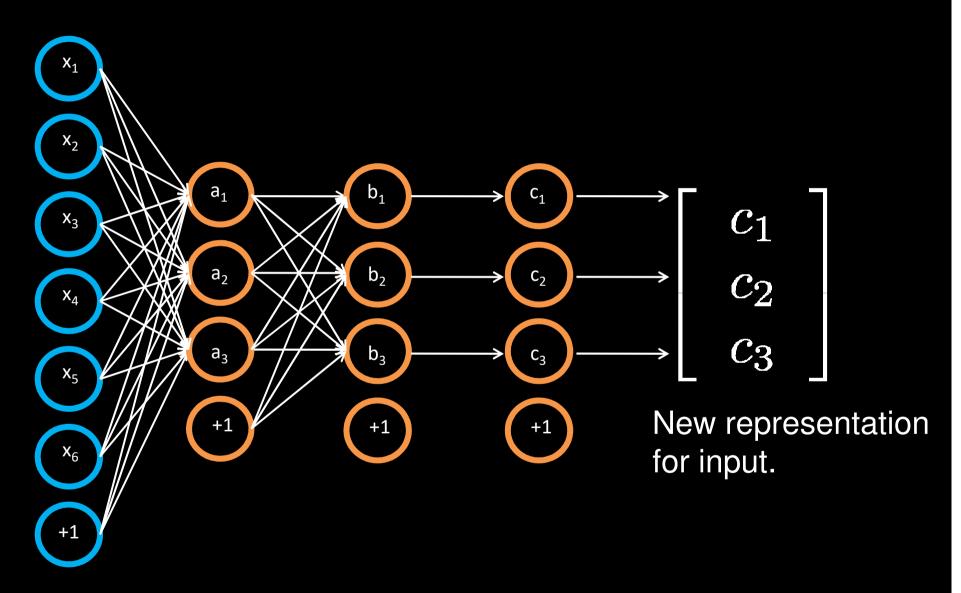












Use  $[c_1, c_3, c_3]$  as representation to feed to learning algorithm.