

# Database Management Systems

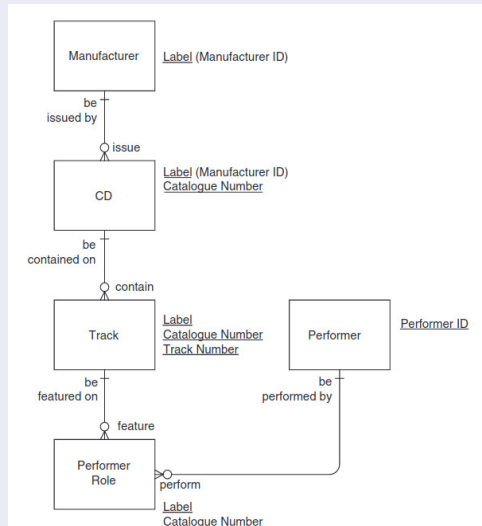
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Fri, 24<sup>th</sup> Jan 2020

# Structured Keys

## Keys made up of more than one attribute



# Weak Entity Sets - 01

## Definition

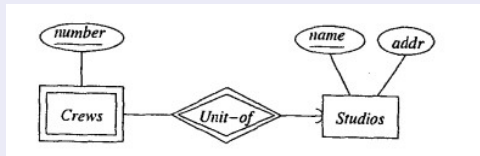
An entity set's key is composed of attributes some or all of which belong to another entity set.

## Causes

- When entity sets fall into a hierarchy based on classifications unrelated to the "isa hierarchy"
- Connecting entity sets as a way to eliminate multiway (d-ary) relationships. Entity sets have no attributes of their own

# Weak Entity Sets - 02

## Example



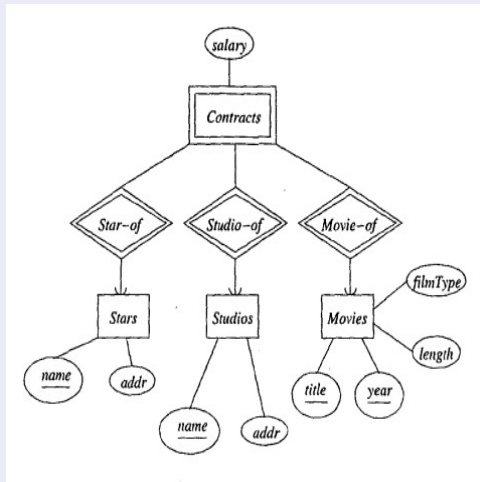
# Weak Entity Sets - 03

## Example

Studio		Crew
Studio name	Studio address	Number
ABC	123, XYZ1	1
ABC	123, XYZ1	2
ABC	123, XYZ1	3
EFG	124, XYZ2	1
EFG	124, XYZ2	2
EFG	124, XYZ2	3

# Weak Entity Sets - 04

## Example



# Weak Entity Sets - 05

## Requirements

- Cannot obtain key attributes for an entity set
- If  $E$  is a weak entity set then its key consists of
- Zero or more of its own attributes
- Key attributes from entity sets that are reached by certain **many-to-one** relationships from  $E$  to other entity sets.

# Weak Entity Sets - 06

## Requirements

- Let  $R : E \rightarrow F$
- $R$  must be a binary, many-to-one relationship from  $E$  to  $F$
- $R$  must have referential integrity from  $E$  to  $F$
- Attributes of  $F$  supplies for the key of  $E$  must be key attributes of  $F$
- If  $F$  itself is weak, then some or all of the key attributes of  $F$  supplied to  $E$  will be key attributes of one or more entity sets of  $G$  to which  $F$  is connected



# Functional Dependencies

## Overview

- Relational designs can be produced in multiple ways
- Regardless of how they are produced, it is possible to **improve designs** systematically
- Improvements are **based on certain types of constraints**
- Most important type of constraint is **unique-value constraint**
- Known as functional dependency (FD)
- Knowledge of this type of constraint is vital for **re-design of database schemas**
- **They eliminate redundancy**

# Functional Dependencies

## Definition - 01

A *functional dependency* (FD) on a relation  $R$  is a statement of the form:  
If two tuples of  $R$  agree on attributes  $A_1, A_2, \dots, A_n$  then they must agree on another attribute  $B$

# Functional Dependencies

what is agreeing?

Two tuples have same values in their respective components for each of the attributes.

# Functional Dependencies

what is agreeing?

- Let  $t_1$  and  $t_2$  be two tuples
- Let  $t_1[A_1]$  denote value of attribute  $A_1$  in tuple  $t_1$
- Then the following holds for agreeing  
 $t_1[A_1] = t_2[A_1], t_1[A_2] = t_2[A_2], \dots, t_1[A_n] = t_2[A_n]$
- This FD is written as:  $A_1 A_2 \dots A_n \rightarrow B$
- Pronounced as  $A_1 A_2 \dots A_n$  functionally determines  $B$

# Functional Dependencies

## Definition - 02

- Let  $R$  be a relational scheme
- Let  $X \subseteq R$  and  $Y \subseteq R$
- We say **relational instance**  $r(R)$  **satisfies** a functional dependency  $X \rightarrow Y$
- If for *every pair* of tuples  $t_1 \in r$  and  $t_2 \in r$ , if  $t_1[X] = t_2[X]$  then  $t_1[Y] = t_2[Y]$

# Legal instance

## Definition

An instance  $r$  of relational scheme  $R$  is a legal instance if it is a true reflection of the mini-world facts it represents.

That is  $r$  satisfies all constraints imposed on it in the real world

# Valid FD

## Definition

- Let  $R$  be a relational scheme
- Let  $X \subseteq R$  and  $Y \subseteq R$
- The FD:  $X \rightarrow Y$  is **valid** if every legal instance  $r(R)$  satisfies  $X \rightarrow Y$

# Armstrong's Axioms - 01

## Reflexivity

If  $Y \subseteq X$  then,  $X \rightarrow Y$ .



# Armstrong's Axioms - 01

## Reflexivity

That is: if  $A_1A_2 \cdots A_n \rightarrow B_1B_2 \cdots B_m$  then  $B$ 's are subset of the  $A$ 's

# Armstrong's Axioms - 02

## Augmentation

If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$

# Armstrong's Axioms - 03

## Transitivity

- If  $X \rightarrow Y$  and  $Y \rightarrow Z$  then
- $X \rightarrow Z$

# Armstrong's Axioms - 04

## Additional Rules of Inference - Union

If  $X \rightarrow Y$  and  $X \rightarrow Z$  then  $X \rightarrow YZ$

①  $X \rightarrow Y$  is given

# Armstrong's Axioms - 04

## Additional Rules of Inference - Union

If  $X \rightarrow Y$  and  $X \rightarrow Z$  then  $X \rightarrow YZ$

- 1  $X \rightarrow Y$  is given
- 2  $X \rightarrow Z$  is given

# Armstrong's Axioms - 04

## Additional Rules of Inference - Union

If  $X \rightarrow Y$  and  $X \rightarrow Z$  then  $X \rightarrow YZ$

- 1  $X \rightarrow Y$  is given
- 2  $X \rightarrow Z$  is given
- 3  $XZ \rightarrow YZ$  (Augment 1 by  $Z$ )

# Armstrong's Axioms - 04

## Additional Rules of Inference - Union

If  $X \rightarrow Y$  and  $X \rightarrow Z$  then  $X \rightarrow YZ$

- 1  $X \rightarrow Y$  is given
- 2  $X \rightarrow Z$  is given
- 3  $XZ \rightarrow YZ$  (Augment 1 by  $Z$ )
- 4  $X \rightarrow XZ$  (Trivial; Augment 2 by  $X$ )

# Armstrong's Axioms - 04

## Additional Rules of Inference - Union

If  $X \rightarrow Y$  and  $X \rightarrow Z$  then  $X \rightarrow YZ$

- 1  $X \rightarrow Y$  is given
- 2  $X \rightarrow Z$  is given
- 3  $XZ \rightarrow YZ$  (Augment 1 by  $Z$ )
- 4  $X \rightarrow XZ$  (Trivial; Augment 2 by  $X$ )
- 5  $X \rightarrow YZ$  (Transitivity using 4 and 3)



# Armstrong's Axioms - 05

## Additional Rules of Inference - Decomposition

If  $X \rightarrow YZ$  then  $X \rightarrow Y$  AND  $X \rightarrow Z$

- 1  $X \rightarrow YZ$  is given

# Armstrong's Axioms - 05

## Additional Rules of Inference - Decomposition

If  $X \rightarrow YZ$  then  $X \rightarrow Y$  AND  $X \rightarrow Z$

- ①  $X \rightarrow YZ$  is given
- ②  $YZ \rightarrow Y$  (Reflexivity)

# Armstrong's Axioms - 05

## Additional Rules of Inference - Decomposition

If  $X \rightarrow YZ$  then  $X \rightarrow Y$  AND  $X \rightarrow Z$

- 1  $X \rightarrow YZ$  is given
- 2  $YZ \rightarrow Y$  (Reflexivity)
- 3  $X \rightarrow Y$  (Transitivity)

# Armstrong's Axioms - 05

## Additional Rules of Inference - Decomposition

If  $X \rightarrow YZ$  then  $X \rightarrow Y$  AND  $X \rightarrow Z$

- ①  $X \rightarrow YZ$  is given
- ②  $YZ \rightarrow Y$  (Reflexivity)
- ③  $X \rightarrow Y$  (Transitivity)
- ①  $X \rightarrow YZ$  is given

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## Additional Rules of Inference - Decomposition

If  $X \rightarrow YZ$  then  $X \rightarrow Y$  AND  $X \rightarrow Z$

- ①  $X \rightarrow YZ$  is given
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- ②  $YZ \rightarrow Z$  (Reflexivity)

# Armstrong's Axioms - 05

## Additional Rules of Inference - Decomposition

If  $X \rightarrow YZ$  then  $X \rightarrow Y$  AND  $X \rightarrow Z$

- ①  $X \rightarrow YZ$  is given
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- ①  $X \rightarrow YZ$  is given
- ②  $YZ \rightarrow Z$  (Reflexivity)
- ③  $X \rightarrow Z$  (Transitivity)

# Armstrong's Axioms - 06

## Additional Rules of Inference - Composition

If  $X \rightarrow Y$  and  $A \rightarrow B$  then  $XA \rightarrow YB$

- 1  $X \rightarrow Y$  (given)

# Armstrong's Axioms - 06

## Additional Rules of Inference - Composition

If  $X \rightarrow Y$  and  $A \rightarrow B$  then  $XA \rightarrow YB$

- 1  $X \rightarrow Y$  (given)
- 2  $A \rightarrow B$  (given)



# Armstrong's Axioms - 06

## Additional Rules of Inference - Composition

If  $X \rightarrow Y$  and  $A \rightarrow B$  then  $XA \rightarrow YB$

- 1  $X \rightarrow Y$  (given)
- 2  $A \rightarrow B$  (given)
- 3  $XA \rightarrow YA$  (Augmentation of 1 with  $A$ )

# Armstrong's Axioms - 06

## Additional Rules of Inference - Composition

If  $X \rightarrow Y$  and  $A \rightarrow B$  then  $XA \rightarrow YB$

- ①  $X \rightarrow Y$  (given)
- ②  $A \rightarrow B$  (given)
- ③  $XA \rightarrow YA$  (Augmentation of 1 with  $A$ )
- ④  $XA \rightarrow Y$  Decomposition of 3 (and  $XA \rightarrow A$ )

# Armstrong's Axioms - 06

## Additional Rules of Inference - Composition

If  $X \rightarrow Y$  and  $A \rightarrow B$  then  $XA \rightarrow YB$

- ①  $X \rightarrow Y$  (given)
- ②  $A \rightarrow B$  (given)
- ③  $XA \rightarrow YA$  (Augmentation of 1 with  $A$ )
- ④  $XA \rightarrow Y$  Decomposition of 3 (and  $XA \rightarrow A$ )
- ⑤  $XA \rightarrow XB$  (Augmentation of 2 with  $X$ )

# Armstrong's Axioms - 06

## Additional Rules of Inference - Composition

If  $X \rightarrow Y$  and  $A \rightarrow B$  then  $XA \rightarrow YB$

- ①  $X \rightarrow Y$  (given)
- ②  $A \rightarrow B$  (given)
- ③  $XA \rightarrow YA$  (Augmentation of 1 with  $A$ )
- ④  $XA \rightarrow Y$  Decomposition of 3 (and  $XA \rightarrow A$ )
- ⑤  $XA \rightarrow XB$  (Augmentation of 2 with  $X$ )
- ⑥  $XA \rightarrow B$  Decomposition 5 (and  $XA \rightarrow X$ )

# Armstrong's Axioms - 06

## Additional Rules of Inference - Composition

If  $X \rightarrow Y$  and  $A \rightarrow B$  then  $XA \rightarrow YB$

- ①  $X \rightarrow Y$  (given)
- ②  $A \rightarrow B$  (given)
- ③  $XA \rightarrow YA$  (Augmentation of 1 with  $A$ )
- ④  $XA \rightarrow Y$  Decomposition of 3 (and  $XA \rightarrow A$ )
- ⑤  $XA \rightarrow XB$  (Augmentation of 2 with  $X$ )
- ⑥  $XA \rightarrow B$  Decomposition 5 (and  $XA \rightarrow X$ )
- ⑦  $XA \rightarrow YB$  (Union 4 and 6)

# Armstrong's Axioms - 07

## Additional Rules of Inference - Pseudo Transitivity

If  $X \rightarrow ZY$  and  $Y \rightarrow W$  then  $X \rightarrow ZW$

- 1  $X \rightarrow ZY$  (given)

# Armstrong's Axioms - 07

## Additional Rules of Inference - Pseudo Transitivity

If  $X \rightarrow ZY$  and  $Y \rightarrow W$  then  $X \rightarrow ZW$

- 1  $X \rightarrow ZY$  (given)
- 2  $Y \rightarrow W$  (given)

# Armstrong's Axioms - 07

## Additional Rules of Inference - Pseudo Transitivity

If  $X \rightarrow ZY$  and  $Y \rightarrow W$  then  $X \rightarrow ZW$

- 1  $X \rightarrow ZY$  (given)
- 2  $Y \rightarrow W$  (given)
- 3  $YZ \rightarrow ZW$  (Augmentation of 2 with  $Z$ )



# Armstrong's Axioms - 07

## Additional Rules of Inference - Pseudo Transitivity

If  $X \rightarrow ZY$  and  $Y \rightarrow W$  then  $X \rightarrow ZW$

- ①  $X \rightarrow ZY$  (given)
- ②  $Y \rightarrow W$  (given)
- ③  $YZ \rightarrow ZW$  (Augmentation of 2 with  $Z$ )
- ④  $X \rightarrow ZW$  (Transitivity of 1 and 3)

# Armstrong's Axioms - 08

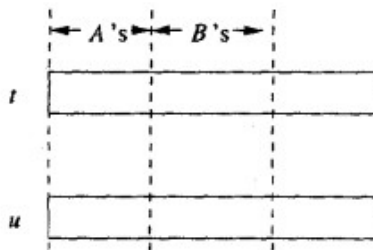
## Additional Rules of Inference - Union (Extended)

$$\begin{array}{cccccc} A_1 & A_2 & \cdots & A_n & \rightarrow & B_1 \\ A_1 & A_2 & \cdots & A_n & \rightarrow & B_2 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ A_1 & A_2 & \cdots & A_n & \rightarrow & B_m \end{array}$$

Then we can say:  $A_1 A_2 \cdots A_n \rightarrow B_1 B_2 \cdots B_m$

# Armstrong's Axioms - 08

## Additional Rules of Inference - Union (Extended)



If  $t$  and  $u$  agree here, Then they must agree here

# Example - 01

## Movies relation

- Let  $R$  be: `Movies(title, year, filmType, studioName, startName)`
- Let  $r(R)$  be

title	year	length	filmType	studioName	starName
Star wars	1977	124	color	Fox	Carrie Fisher
Star wars	1977	124	color	Fox	Mark Hamill
Star wars	1977	124	color	Fox	Harrison Ford
Mighty Ducks	1991	104	color	Disney	Emilio Estevez
Wayne's world	1992	95	color	Paramount	Data Carvey
Wayne's world	1992	95	color	Paramount	Mike Meyers

## Example - 02

### Movies relation

The three FDs for the Movies relation are

- `title year`  $\rightarrow$  `length`
- `title year`  $\rightarrow$  `filmType`
- `title year`  $\rightarrow$  `studioName`
- These three FDs satisfies every pair of  $r(R)$
- `title year`  $\rightarrow$  `length filmType studioName`

## Example - 03

Movies relation

FD that do not satisfy every pair of tuples in  $r(R)$  is `title year`  $\rightarrow$  `startName`

# Keys of Relations

## Properties

Set of one or more attributes  $\{A_1, A_2, \dots, A_n\}$  is a **key** for relation  $R$  if the following holds

- 1  $A_1$  to  $A_n$  functionally determine all the **other** attributes of  $R$
- 2 No proper subset of  $\{A_1, A_2, \dots, A_n\}$  functionally determines **all other attributes** of  $R$ . Satisfying **minimal** clause

# Keys of Relations

## Example Movies Relation

(title, year, starName) forms a key

- ① Argue for functionally determines all other attributes
  - That is two tuples agrees on (title, year, starName), those tuples agree on (length, fileType, studioName)
  - title year  $\rightarrow$  (length, fileType, studioName)



# Keys of Relations

## Example Movies Relation

(title, year, starName) forms a key

① Argue for No proper subset ... Point

- (title, year) do not determine starName
- (year, starName) is not a key (first point violation)
- (title, starName) is not a key (first point violation)

# Super Keys

## Definition

A set of attributes that contains a key is called a **super key** (super set of a key)

## Discussion

- Every key is a super key
- However, some super keys are not (minimal) keys
- That is super key need not satisfy minimality

# Discovering Keys for Relations

## Thumb Rules

- If entity set is translated to a relation then key attributes of entity set are the key for the relation. **Example:** students
- (For binary relationships) If  $R$  is **many-to-many**, then keys of both connected entity sets are the key attributes of  $R$ . **Example:** `grades(roll_number, cid, grd)`
- If  $R$  is **many-to-one** from  $E_1$  to  $E_2$  then key attribute of  $E_2$  are key attributes of  $R$ . **Example:** Employees works for department
- If  $R$  is **one-to-one** then the key attributes for either of the entity are key attributes of  $R$

# Rules About FD's - 01

## Splitting & Combining

Given an FD of the form:  $A_1A_2 \cdots A_n \rightarrow B_1B_2 \cdots B_m$

- Split the attributes on the right side so that only one attribute appears on right of every FD

$$\begin{array}{cccccc}
 A_1 & A_2 & \cdots & A_n & \rightarrow & B_1 \\
 A_1 & A_2 & \cdots & A_n & \rightarrow & B_2 \\
 \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\
 A_1 & A_2 & \cdots & A_n & \rightarrow & B_m
 \end{array}$$

- Likewise, replace a collection of FD's with common LHS by single FD

## Rules About FD's - 02

### Splitting & Combining - concise form

**Splitting Rule** Replace an FD of the form:  $A_1A_2 \cdots A_n \rightarrow B_1B_2 \cdots B_m$  by  $A_1A_2 \cdots A_n \rightarrow B_i$  for  $i = 1, 2, \cdots m$

## Rules About FD's - 02

### Splitting & Combining - concise form

**Splitting Rule** Replace an FD of the form:  $A_1A_2 \cdots A_n \rightarrow B_1B_2 \cdots B_m$  by  $A_1A_2 \cdots A_n \rightarrow B_i$  for  $i = 1, 2, \cdots m$

**Combining Rule** Replace set of FD's of the form  $A_1A_2 \cdots A_n \rightarrow B_i$  for  $i = 1, 2, \cdots m$  by  $A_1A_2 \cdots A_n \rightarrow B_1B_2 \cdots B_m$

## Rules About FD's - 03

### Classification

An FD  $A_1A_2 \cdots A_n \rightarrow B_1B_2 \cdots B_m$  is

Trivial if  $B$ 's are a subset of  $A$ 's.  $\text{title year} \rightarrow \text{title}$

# Rules About FD's - 03

## Classification

An FD  $A_1A_2 \cdots A_n \rightarrow B_1B_2 \cdots B_m$  is

Trivial if  $B$ 's are a subset of  $A$ 's.  $\text{title year} \rightarrow \text{title}$

Non-trivial if **at least** one of the  $B$ 's is not among the  $A$ 's.  $\text{title year} \rightarrow \text{year length}$



# Rules About FD's - 03

## Classification

An FD  $A_1A_2 \cdots A_n \rightarrow B_1B_2 \cdots B_m$  is

Trivial if  $B$ 's are a subset of  $A$ 's.  $\text{title year} \rightarrow \text{title}$

Non-trivial if **at least** one of the  $B$ 's is not among the  $A$ 's.  $\text{title year} \rightarrow \text{year length}$

Completely non-trivial if **none of the**  $B$ 's is also one of the  $A$ 's.  $\text{title year} \rightarrow \text{length}$

# Closure of Attributes

## Definition

A general principle from which **all rules follow**

# Closure of Attributes

## Definition

- Let  $\{A_1, A_2, \dots, A_n\}$  be set of attributes
- S be a set of FD's
- closure of  $\{A_1, A_2, \dots, A_n\}$  denoted as  $\{A_1, A_2, \dots, A_n\}^+$  under FD's in S is
  - set of attributes B such that
  - every relation that satisfies all the FDs in S also satisfies  $A_1 A_2 \dots A_n \rightarrow B$

# Closure of Attributes

## Definition

That is  $A_1A_2 \cdots A_n \rightarrow B$  follows from the FDs of  $S$

# Closure of Attributes

## Computation

Closure of  $\{A_1, A_2, \dots, A_n\}$  w.r.t. set of FD's  $S$

- 1 Let  $X$  be set of attributes that will become the closure. Initialize  $X = \{A_1, A_2, \dots, A_n\}$
- 2 Repeatedly search for some FD  $B_1 B_2 \dots B_m \rightarrow C$  such that all of  $B_1 B_2 \dots B_m$  are in  $X$  and  $C \notin X$ .  $X = X \cup \{C\}$
- 3 Repeat step 2 until no more attributes can be added to  $X$
- 4 The resulting set  $X$  is the  $\{A_1, A_2, \dots, A_n\}^+$

# Closure of Attributes

## Computation

- 1 Let  $R(A, B, C, D, E, F)$  be a relation
- 2  $R$  satisfies the set of FDs  
 $\{AB \rightarrow C, BC \rightarrow AD,$   
 $D \rightarrow E, CF \rightarrow B\}$
- 3 Compute  $\{A, B\}^+$

# Closure of Attributes

## Computation

- ①  $X = \{A, B\}$
- ②  $\{AB \rightarrow C\}$  satisfies step 2
- ③ Therefore add C to X. That is  $X = \{A, B, C\}$
- ④  $\{BC \rightarrow AD\}$  satisfies step 2
- ⑤ Therefore add D to X.  $X = \{A, B, C, D\}$  (A is already present in X)
- ⑥  $\{D \rightarrow E\}$  satisfies step 2
- ⑦ Therefore add E to X.  $X = \{A, B, C, D, E\}$
- ⑧  $\{CF \rightarrow F\}$  **does not** satisfies step 2
- ⑨  $\{A, B\}^+ = \{A, B, C, D, E\}$