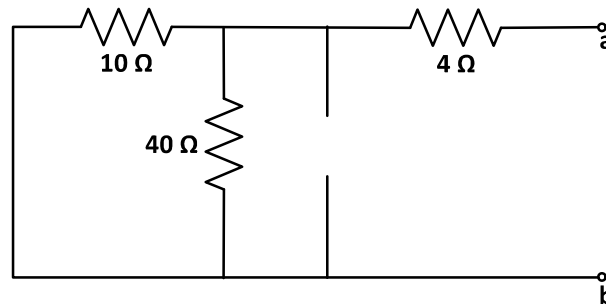


# Solutions

1. Deactivate the independent sources. The equivalent circuit looks as shown in Fig. 1.

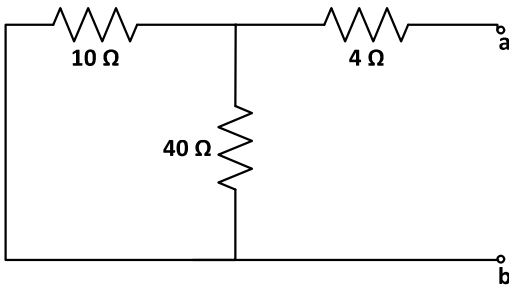


**Fig. 1** Thevenin's equivalent circuit after deactivating the independent source.

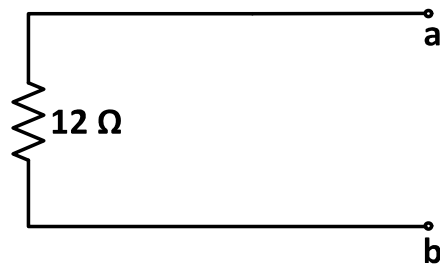
The network shown in Fig. 1 can be simplified (Fig. 2a) and the equivalent resistance, as seen from nodes a-b, is determined (Fig. 2b). The equivalent resistance shown in Fig. 2b is the Thevenin's resistance:

$$Z_{th} = 12\ \Omega \quad (1)$$

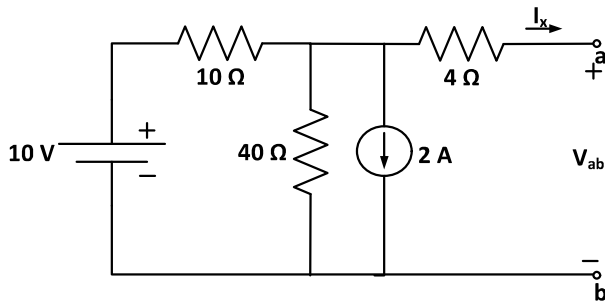
Next we determine the open circuit voltage across a-b. The current is  $I_x = 0$  because the terminals a-b are open (Fig. 3a). Hence, there is no voltage drop across the  $4\ \Omega$  resistance and this resistance can be ignored (Fig. 3b).



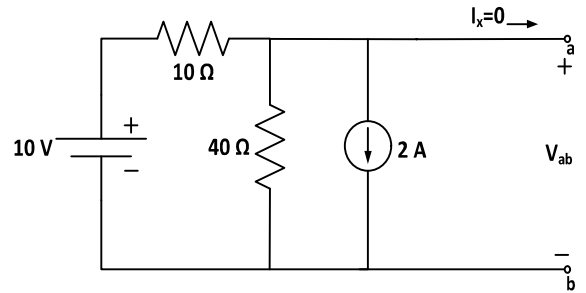
**Fig. 2a** Simplified circuit



**Fig. 2b** Equivalent resistance



**Fig. 3a** Current  $I_x=0$

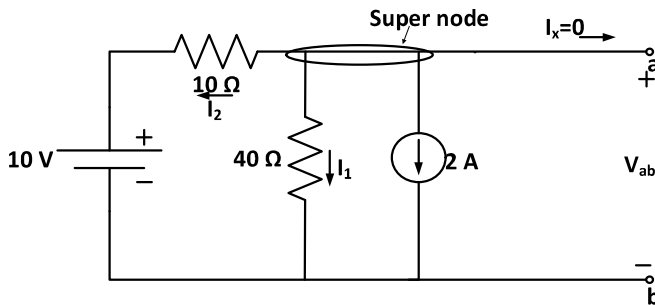


**Fig. 3b** Simplified circuit

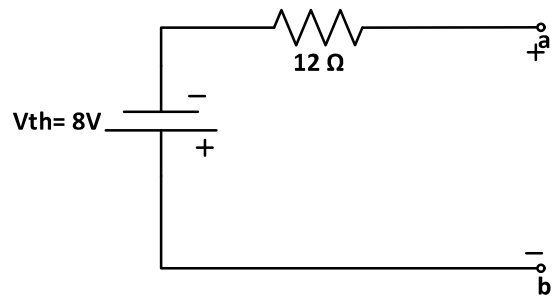
Using a super node and applying KCL (Fig. 4) gives

$$\frac{V_{ab} - 10}{10} + \frac{V_{ab}}{40} + 2 = 0 \quad (2)$$

$$V_{ab} = -8V = V_{th} \quad (3)$$



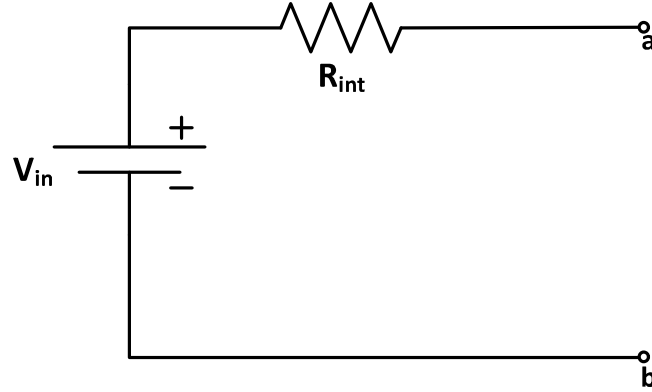
**Fig. 4** KCL at Supernode



**Fig. 5** Thevenin's equivalent circuit

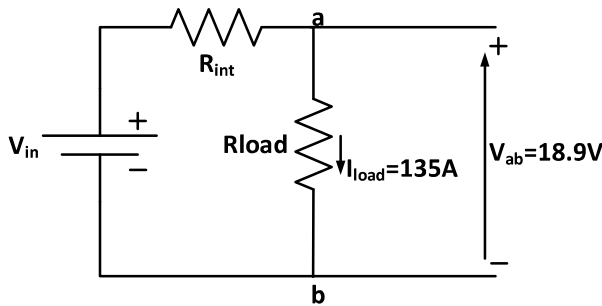
The Thevenin's equivalent circuit is shown in Fig. 5.

2. The equivalent circuit the arc welding system is shown in Fig.6. In this figure  $V_{in}$  is the internal voltage of the source and  $R_{int}$  is the internal resistance of the source. The welding stick is connected across the terminals **a-b**.

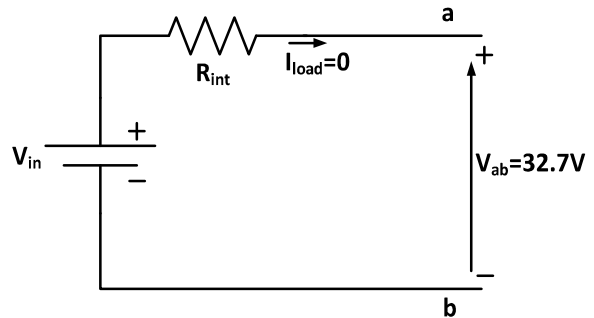


**Fig. 6** Thevenin's equivalent circuit of the arc welding system

When the arc welder is loaded, the equivalent circuit is as shown in Fig. 7 and when it is under no load, its equivalent circuit is shown in Fig. 8.



**Fig. 7** Thevenin's equivalent circuit under load condition



**Fig. 8** Thevenin's equivalent circuit under no load condition

From the Fig.7 and 8 we can determine the open circuit voltage and it is:

$$V_{in} = V_{oc} = V_{th} = 32.7V \quad (4)$$

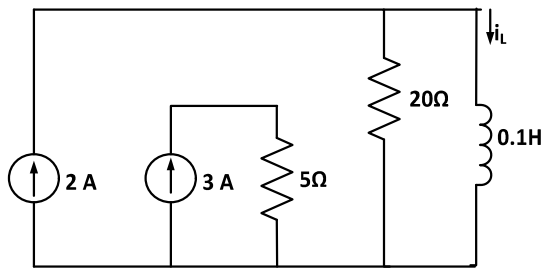
The internal resistance  $R_{int}$  is given by

$$R_{int} = \frac{V_{in} - V_{ab} \text{ (during load condition)}}{I_{load} \text{ (during load condition)}} = \frac{32.7 - 18.9}{135} = 0.102 = R_{th} \quad (5)$$

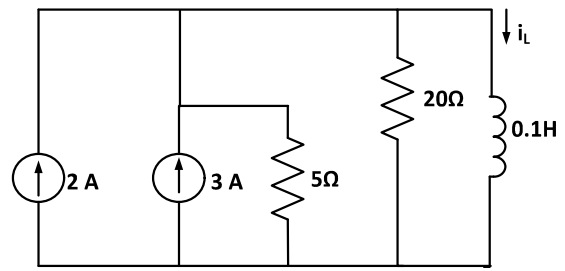
The Norton's current is given by

$$I_{Norton} = \frac{V_{th}}{R_{th}} = \frac{32.7}{0.102} = 320.5A \quad (6)$$

3.



**Fig. 9**



**Fig. 10**

Inductor behaves as a short circuit to D.C. source

$$\therefore i_L = 2A. \quad \text{for } t < 0 \text{ (Fig. 9)}$$

For  $t > 0$  the circuit becomes as shown in Fig. 10

$$i_L(t) = i_f + i_n$$

$i_f$  = forced response

$i_n$  = natural response

Inductor behaves as a short circuit to D.C. sources.

$$\therefore i_f = 2A + 3A = 5A.$$

$$i_n = A e^{-t/\tau}$$

$$\tau = \text{time constant} = \frac{L}{R_{eq}}$$

$$R_{eq} = 20 \parallel 5 = 4\Omega.$$

$$\therefore \tau = \frac{0.1}{4} = 0.025 \text{ sec}$$

$$\therefore i_n = A e^{-t/0.025} = A e^{-40t}$$

$$\therefore \text{Total response for } t > 0 \text{ is, } i_L(t) = 5 + A e^{-40t}$$

putting initial condition,  $i_L(0^-) = i_L(0^+)$

since the inductor cannot change the current through it instantaneously

$$i_L(0^-) = 2A$$

$$\therefore 2 = 5 + A \text{ (put } t = 0)$$

$$\therefore A = -3$$

$$\therefore i_L(t) = 5 - 3 e^{-40t} \quad \text{for } t > 0$$

For all time  $t$ ,

$$i_L(t) = 2 + (3 - 3 e^{-40t}) u(t) \quad \text{for all } t. \quad [u(t) \text{ is the unit step function}].$$

4.

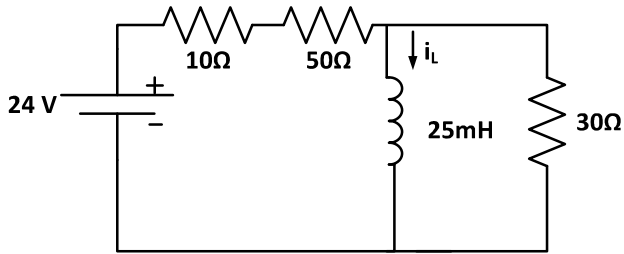


Fig. 11

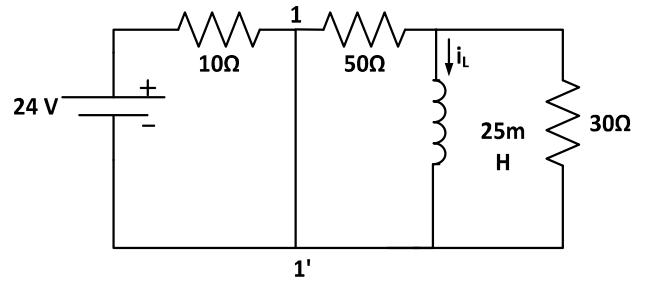


Fig. 12

For  $t < 0$ , the circuit is shown in Fig. 11.

Inductor will be short circuiting to D.C. source,

$$\therefore i_L = \frac{24}{10+50} = 0.4 \text{ A} \quad \text{for } t < 0.$$

For  $t > 0$ , the circuit is shown in Fig. 12

$$i_L(t) = i_f + i_n$$

$i_f$  = forced response = 0 (since current will follow short circuit path 11')

$i_n$  = natural response =  $A e^{-t/\tau}$

$$\tau = \text{time constant} = \frac{L}{R_{eq}} = \frac{L}{R_{eq}} = \frac{25 \times 10^{-3}}{R_{eq}},$$

$$R_{eq} = 30 \parallel 50 = 18.75 \Omega$$

$$\therefore \tau = \frac{25 \times 10^{-3}}{18.75} \text{ sec},$$

$$\text{Now, } i_n = A e^{-\frac{25 \times 10^{-3}}{18.75}} = A e^{-750t}$$

$$\therefore i_L(t) = A e^{-750t} \quad \text{for } t > 0$$

$$i_L(0^-) = i_L(0^+)$$

$$\therefore 0.4 = A e^{-750 \times 0} = A \quad \text{for } t = 0$$

$$\therefore i_L(t) = 0.4 e^{-750t} \quad \text{for } t > 0$$

5.

Select MUX					Output					
↓										
					S3	S2	S1	S0	y	
Select MUX 1	0	0	0	0	I <sub>0</sub>	I <sub>0</sub>				
	0	0	0	1	I <sub>1</sub>	I <sub>1</sub>				
	0	0	1	0	I <sub>2</sub>	I <sub>2</sub>				
	0	0	1	1	I <sub>3</sub>	I <sub>3</sub>				
	0	1	0	0	I <sub>4</sub>	I <sub>4</sub>				
	0	1	0	1	I <sub>5</sub>	I <sub>5</sub>				
	0	1	1	0	I <sub>6</sub>	I <sub>6</sub>				
	0	1	1	1	I <sub>7</sub>	I <sub>7</sub>				
Select MUX 2	1	0	0	0	I <sub>8</sub>	I <sub>0</sub>				
	1	0	0	1	I <sub>9</sub>	I <sub>1</sub>				
	1	0	1	0	I <sub>10</sub>	I <sub>2</sub>				
	1	0	1	1	I <sub>11</sub>	I <sub>3</sub>				
	1	1	0	0	I <sub>12</sub>	I <sub>4</sub>				
	1	1	0	1	I <sub>13</sub>	I <sub>5</sub>				
	1	1	1	0	I <sub>14</sub>	I <sub>6</sub>				
	1	1	1	1	I <sub>15</sub>	I <sub>7</sub>				

Fig. 13

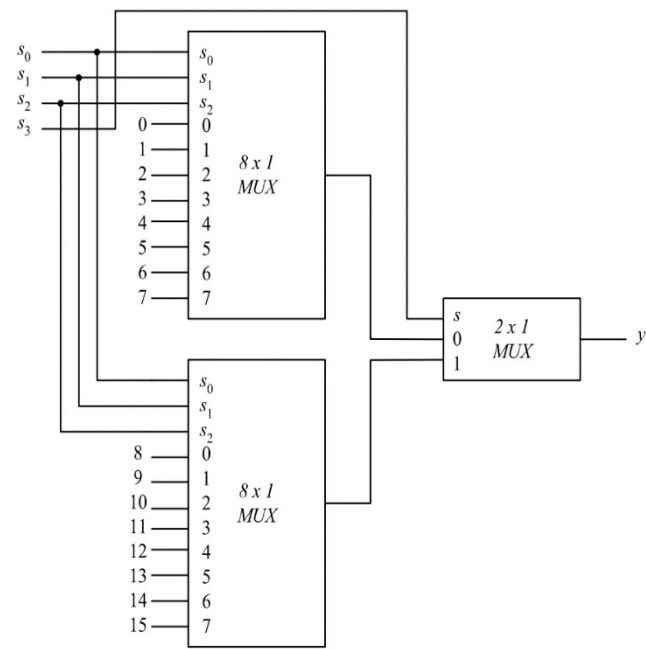


Fig. 14

6.

Fig. 15 shows Full-adder truth table. Where, Sum  $S = \sum(1,2,4,7)$  and carry  $C = \sum(3,5,6,7)$

X	Y	Z	S	C
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

**Fig. 15** Truth Table of Full adder

YZ X	I <sub>0</sub> 00	I <sub>1</sub> 01	I <sub>3</sub> 11	I <sub>2</sub> 10
0	0	1	0	1
1	1	0	1	0

**Fig. 16** Truth table for Sum

I <sub>0</sub>	I <sub>1</sub>	I <sub>2</sub>	I <sub>3</sub>
X	$\overline{X}$	$\overline{X}$	X

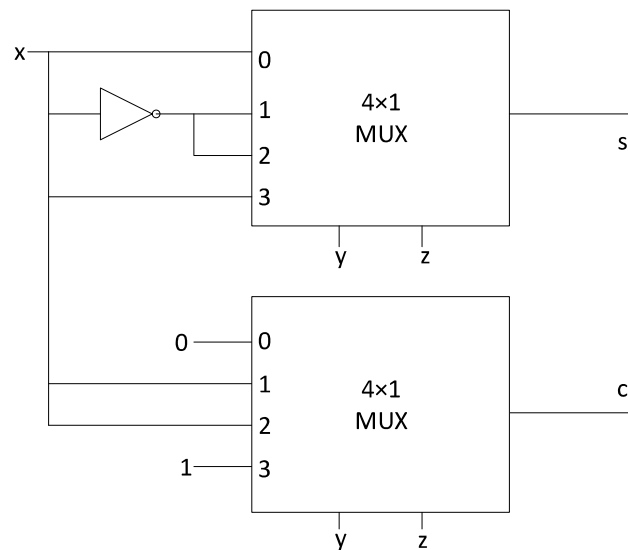
**Fig. 17** Inputs of Sum MUX in terms of X

YZ X	I <sub>0</sub> 00	I <sub>1</sub> 01	I <sub>3</sub> 11	I <sub>2</sub> 10
0	0	0	1	0
1	0	1	1	1

**Fig. 18** Truth table for Carry

I <sub>0</sub>	I <sub>1</sub>	I <sub>2</sub>	I <sub>3</sub>
0	X	X	1

**Fig. 19** Inputs of Carry MUX in terms of X



**Fig. 20** Full adder using two  $4 \times 1$  multiplexers