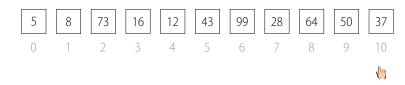
Integer Arrays



5	8	73	16	12	43	99	28	64	50	37
		2								



























Time Complexity



Time Complexity

Linear



Time Complexity

Linear Random



Time Complexity

Linear 11 Random



Time Complexity

Linear **n** Random



Time Complexity

Linear n Random 11



Time Complexity

Linear n
Random n

5	8	73	16	12	43	99	28	64	50	37
0	1	2	3	4	5	6	7	8	9	10







Where is 12?

Where is 12?

$$\frac{0+10}{2}=1$$

Where is 12?

$$\frac{0+10}{2}=1$$

Where is 12?

$$\frac{0+10}{2}=1$$

Where is 12?

$$\frac{0+4}{2} = 2$$



Where is 12?

$$\frac{0+4}{2} = 2$$



Where is 50?

Where is 50?

$$\frac{0+10}{2}=1$$

Where is 50?

$$\frac{0+10}{2}=5$$

Where is 50?

$$\frac{0+10}{2}=5$$

Where is 50?

$$\frac{6+10}{2}=8$$



Where is 50?

$$\frac{6+10}{2}=8$$

Where is 50?

$$\frac{6+10}{2}=8$$

Where is 50?

$$\frac{6+7}{2} = 6.5$$

Where is 50?

$$\frac{6+7}{2} = 6$$

Where is 50?

$$\frac{6+7}{2}=\epsilon$$



Where is 50?



Where is 25?

Where is 25?

$$\frac{0+10}{2}=5$$

Where is 25?

$$\frac{0+10}{2}=5$$

Where is 25?

$$\frac{0+10}{2}=5$$

Where is 25?

$$\frac{0+4}{2} = 2$$



Where is 25?

$$\frac{0+4}{2} = 2$$

Where is 25?

$$\frac{0+4}{2} = 1$$

Where is 25?

$$\frac{3+4}{2} = 3.5$$

Where is 25?

$$\frac{3+4}{2} = 4$$



Where is 25?

$$\frac{3+4}{2} = 4$$

Where is 25?

$$\frac{3+4}{2} = 4$$



Where is 25?

$$\frac{3+4}{2} = 4$$





Time Complexity



Time Complexity



Time Complexity

In each step, the number of elements becomes half.

n



Time Complexity

$$n \to \frac{n}{2}$$



Time Complexity

$$n \to \frac{n}{2} \to \frac{n}{2^2}$$



Time Complexity

$$n \to \frac{n}{2} \to \frac{n}{2^2} \to \frac{n}{2^3}$$



Time Complexity

$$n \to \frac{n}{2} \to \frac{n}{2^2} \to \frac{n}{2^3} \to \cdots$$



Time Complexity

$$n \to \frac{n}{2} \to \frac{n}{2^2} \to \frac{n}{2^3} \to \cdots \to 1$$



Time Complexity

$$n \to \frac{n}{2} \to \frac{n}{2^2} \to \frac{n}{2^3} \to \cdots \to 1 = \frac{n}{2^i} (i \text{ steps})$$



Time Complexity

$$\frac{n}{2i} = \frac{1}{2}$$



Time Complexity

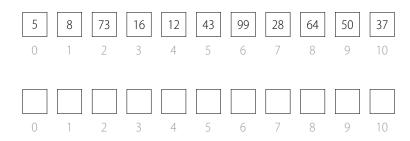
$$\frac{n}{2^i} = 1 \implies i = \log_2 n$$

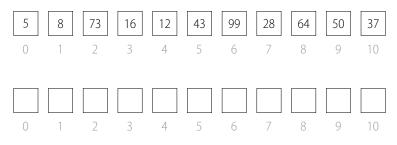


Time Complexity

Binary Search takes $\operatorname{atmost} \log_2 n$ steps

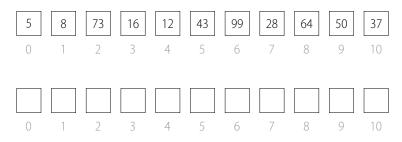






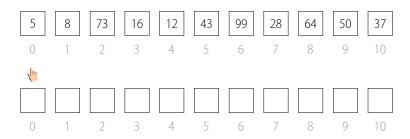
Strategy

Select the smallest element



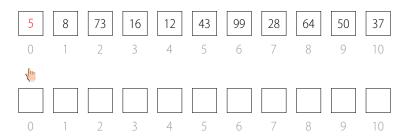
Strategy

Select the smallest element – Linear Search



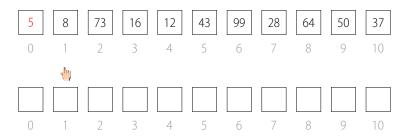
Strategy

Select the smallest element – Linear Search

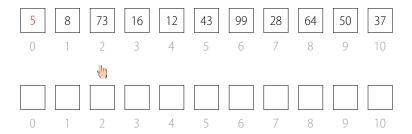


Strategy

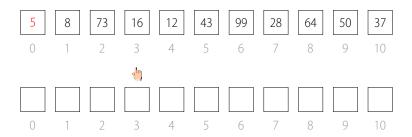
Select the smallest element – Linear Search



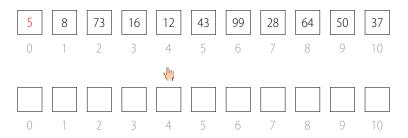
Strategy



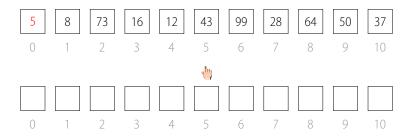
Strategy



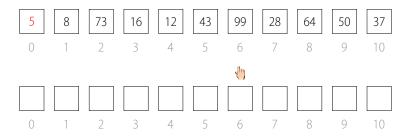
Strategy



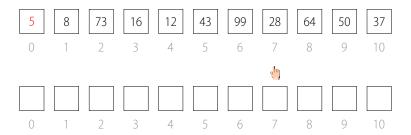
Strategy



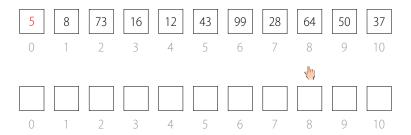
Strategy



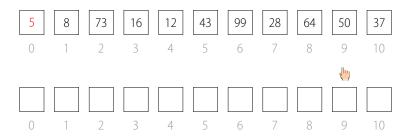
Strategy



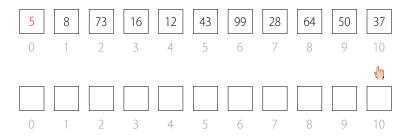
Strategy



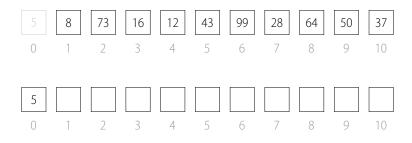
Strategy



Strategy

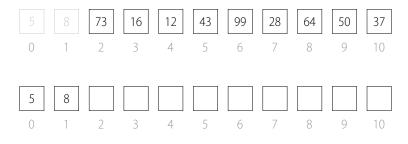


Strategy

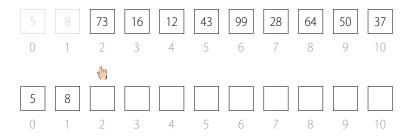


Select the smallest element – Linear Search

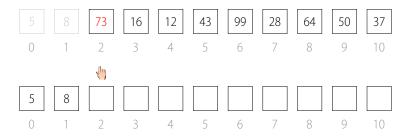
Strategy



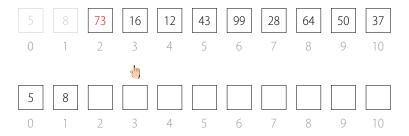
Strategy



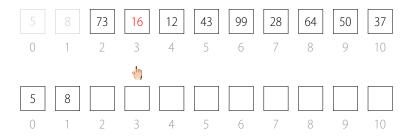
Strategy



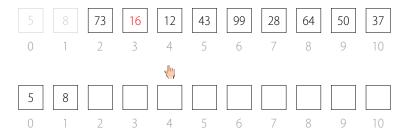
Strategy



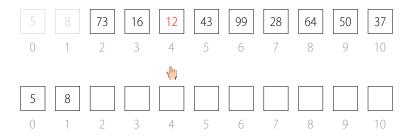
Strategy



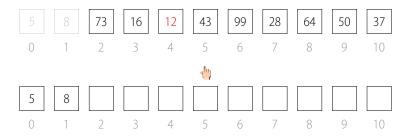
Strategy



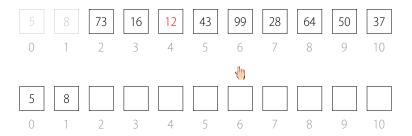
Strategy



Strategy

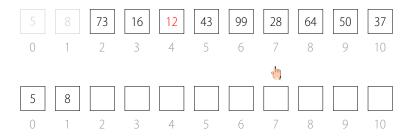


Strategy



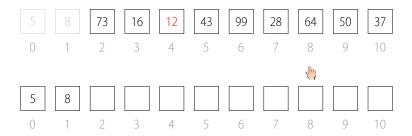
Select the smallest element – Linear Search

Strategy

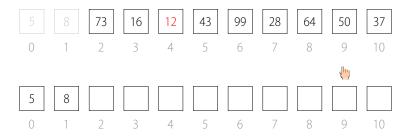


Select the smallest element – Linear Search

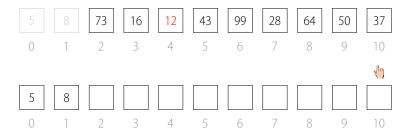
Strategy



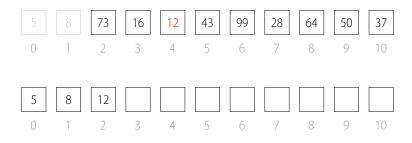
Strategy



Strategy

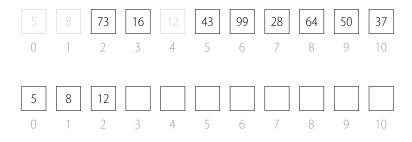


Strategy



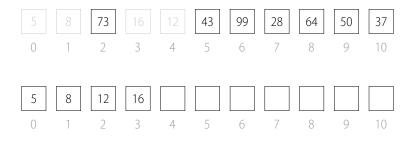
Select the smallest element – Linear Search

Strategy

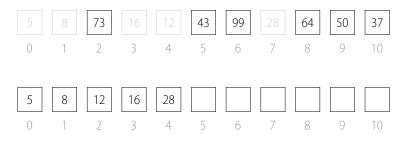


Select the smallest element – Linear Search

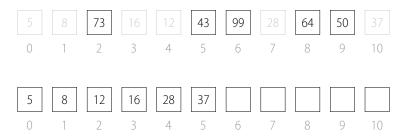
Strategy



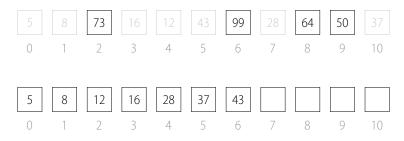
Strategy



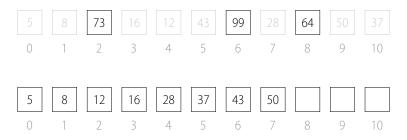
Strategy



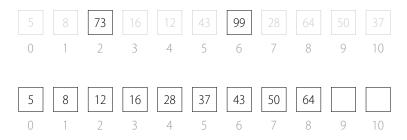
Strategy



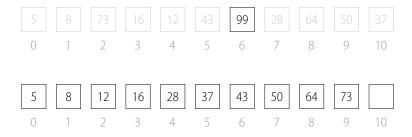
Strategy



Strategy



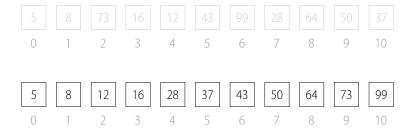
Strategy



Select the smallest element – Linear Search

Strategy





Time Complexity



n

Time Complexity



$$n + (n - 1)$$

Time Complexity

n + (n-1) + (n-2)

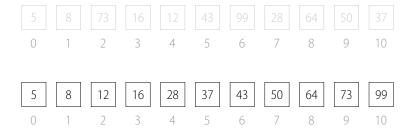
Time Complexity

n + (n-1) + (n-2) + (n-3)

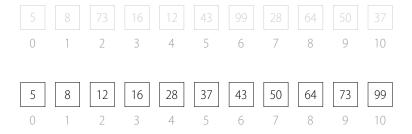
$$n + (n-1) + (n-2) + (n-3) + \dots$$

n + (n-1) + (n-2) + (n-3) + ... + 1

$$n + (n-1) + (n-2) + (n-3) + ... + 1 = n(n+1)/2$$

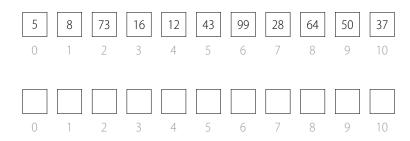


Space Complexity



 \mathfrak{n}

Space Complexity







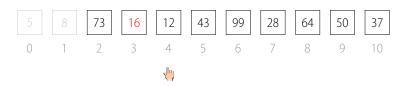


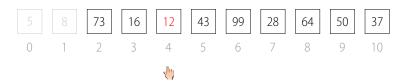














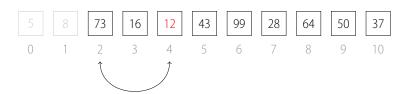












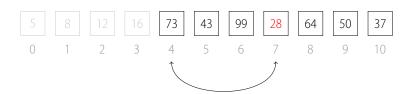






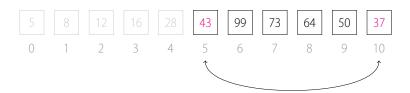


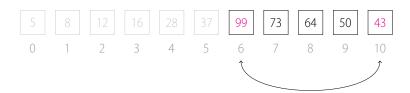
















Sorting Integer Arrays



Sorting Integer Arrays



Space Complexity

Constant

Sorting Integer Arrays - Selection Sort



Time Complexity

Sorting Integer Arrays - Selection Sort



Time Complexity

Does it change?

Sorting Integer Arrays - Selection Sort



Time Complexity

Does it change? - Thought Experiment

Sorting Integer Arrays









































Round 1 complete .'



Any guess as to how many rounds are required?

































Round 2 complete . !



Any guess as to how many rounds are required?





























Round 3 complete . !



Any guess as to how many rounds are required?

























Round 4 complete . !



Any guess as to how many rounds are required?



Any guess as to how many rounds are required?

$$n-1$$

























Round 5 complete . !























Nothing changed .'



Nothing changed .'





Complexity



Space Complexity



Space Complexity

Constant





$$(n-1)$$

$$(n-1) + (n-2)$$

$$(n-1) + (n-2) + (n-3)$$

$$(n-1) + (n-2) + (n-3) + \dots$$

$$(n-1) + (n-2) + (n-3) + \dots + 1$$

$$(n-1)+(n-2)+(n-3)+\ldots +1 \leq \frac{n(n+1)}{2}$$

Sorting Integer Arrays - Radix Sort

5	8	73	16	12	43	99	28	64	50	37
0	1	2	3	4	5	6	7	8	9	10

Sorting Integer Arrays - Radix Sort



0 1 2 3 4 5 6 7 8 9



0	1	2	3	4	5	6	7	8	9



0	1	2	3	4	5	6	7	8	9



Round 1



5 8











0	1	2	3	4	5	6	7	8	9
		12	73		5	16		8	











0	1	2	3	4	5	6	7	8	9
		12	73		5	16		8	99
			43					28	



0	1	2	3	4	5	6	7	8	9
		12	73	64	5	16		8	99
			43					28	



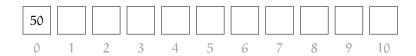
0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16		8	99
			43					28	



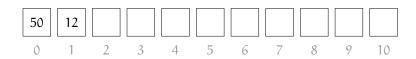
0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



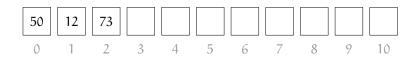
0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



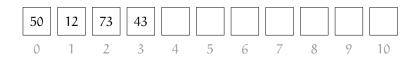
0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



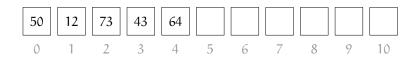
0	1	2	3	4	5	6	7	8	9
50		12		64					
			43					28	



0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



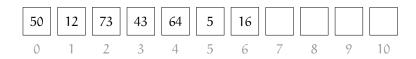
0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



0	1	2	3	4	5	6	7	8	9
50		12	73	64	5	16	37	8	99
			43					28	



0	1	2	3	4	5	6	7	8	9



Round 2

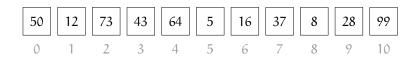
0 1 2 3 4 5 6 7 8 9



Round 2

0	1	2	3	4	5	6	7	8	9

12 50



0	1	2	3	4	5	6	7	8	9
	12				50		73		



0	1	2	3	4	5	6	7	8	9
	12			43	50		73		



0	1	2	3	4	5	6	7	8	9
	12			43	50	64	73		



0	1	2	3	4	5	6	7	8	9
5	12			43	50	64	73		



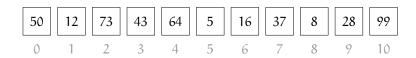
0	1	2	3	4	5	6	7	8	9
5	12 16			43	50	64	73		



0	1	2	3	4	5	6	7	8	9
	12 16		37	43	50	64	73		



0	1	2	3	4	5	6	7	8	9
5	12		37	43	50	64	73		
8	16								



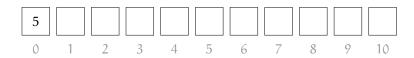
0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		
8	16								



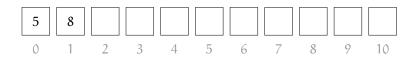
5 12 8 16		43	50	64	73	99



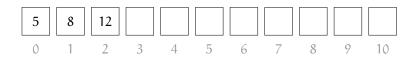
0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



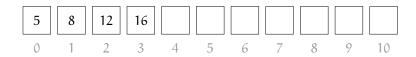
0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



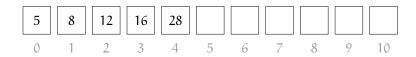
0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



0	1	2	3	4	5	6	7	8	9
5	12	28	37	43	50	64	73		99
8	16								



5 12 28 37 43 50 64 73	0	1	2	3	4	5	6	7	8	9
8 16					43	50	64	73		99

a < b

$$a = a_1 a_2 a_3 a_4$$

$$a = a_1 a_2 a_3 a_4$$

$$b = b_1 b_2 b_3 b_4$$

$$a = a_1 a_2 a_3 a_4$$

$$b = b_1 b_2 b_3 b_4$$

$$\alpha \ = \ \alpha_1 \ \alpha_2 \ \alpha_3 \ \alpha_4$$

$$b = b_1 b_2 b_3 b_4$$

$$\alpha_2 < b_2$$

$$a < b$$
 $a = a_1 a_2 a_3 a_4$
 $b = b_1 b_2 b_3 b_4$
 $a = a_2 < b_2$
 $a_1 == b_1$

Can we do it from the other end?

$$a = a_1 a_2 a_3 a_4$$

$$b = b_1 b_2 b_3 b_4$$

$$a_2 < b_2$$

$$a_1 == b_1$$



5 12 28 37 43 50 64 73	0	1	2	3	4	5	6	7	8	9
8 16					43	50	64	73		99

Round 2

Time Complexity



Round 2

Time Complexity

Number of rounds



Round 2

Time Complexity

Number of rounds * Time for each round

Round 2

Time Complexity



Round 2

Space Complexity

Round 2

Space Complexity