

# Advanced Programming Practice

## Autonomous Driving

### -Path Planning-

## 2023 Fall

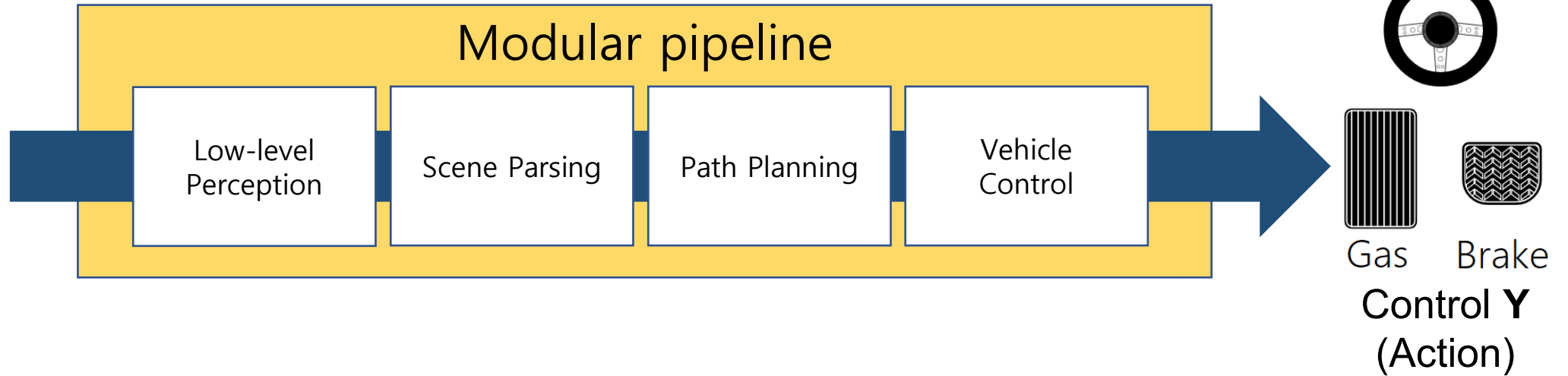
Sogang University



# Modular Pipeline



Sensor Input **X**



- Low-level Perception & Scene Parsing: Lecture 1
- **Path training: Lecture 2**
- Vehicle Control: Lecture 3

# Planning and Decision Making

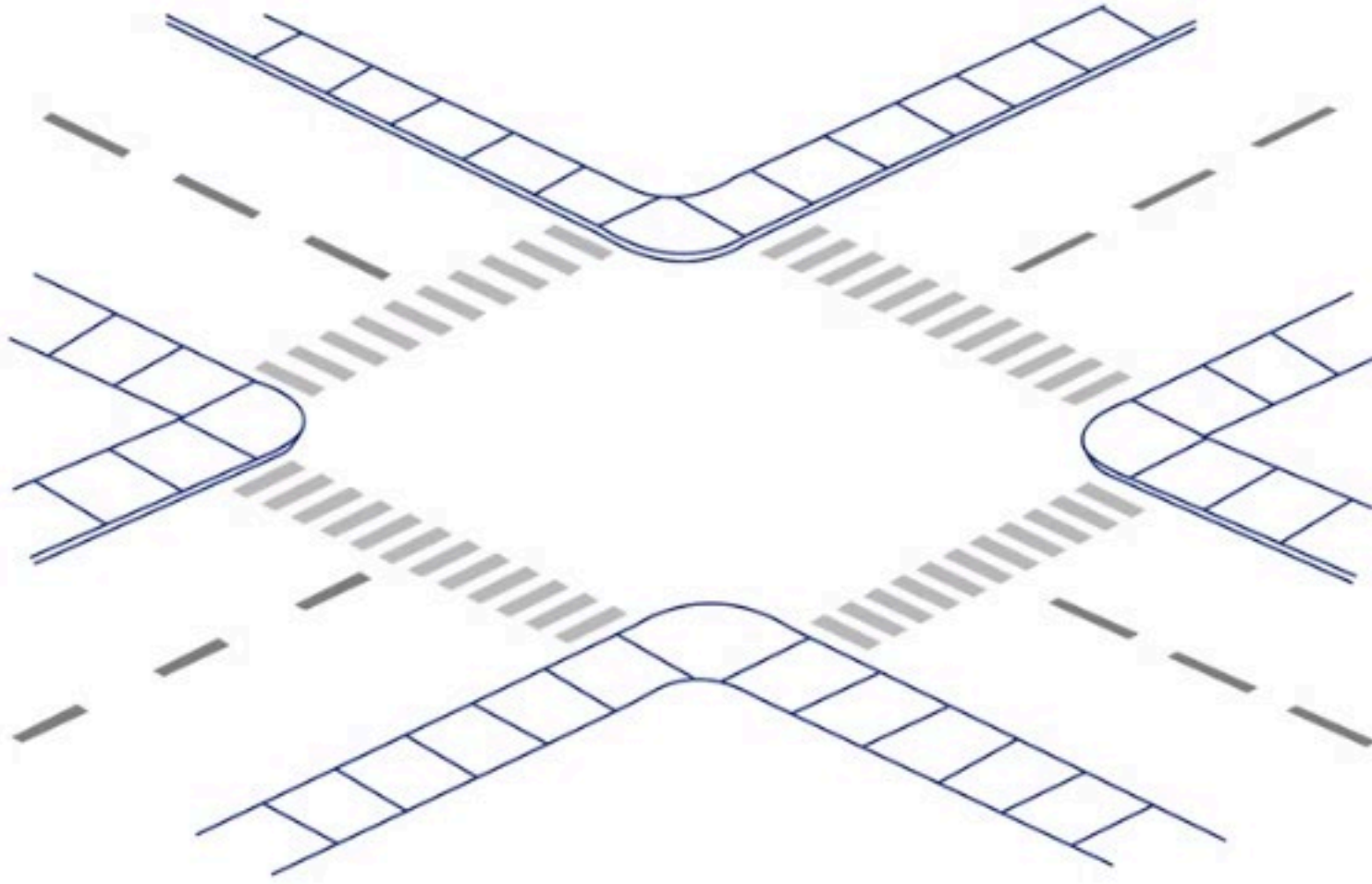
## **Problem definition:**

- Goal: Find and follow a path from here to destination
  - Need to think static infrastructure and dynamic objects
- Input: vehicle and sensed surrounding environment state
- Output: path or trajectory being passed to a vehicle controller

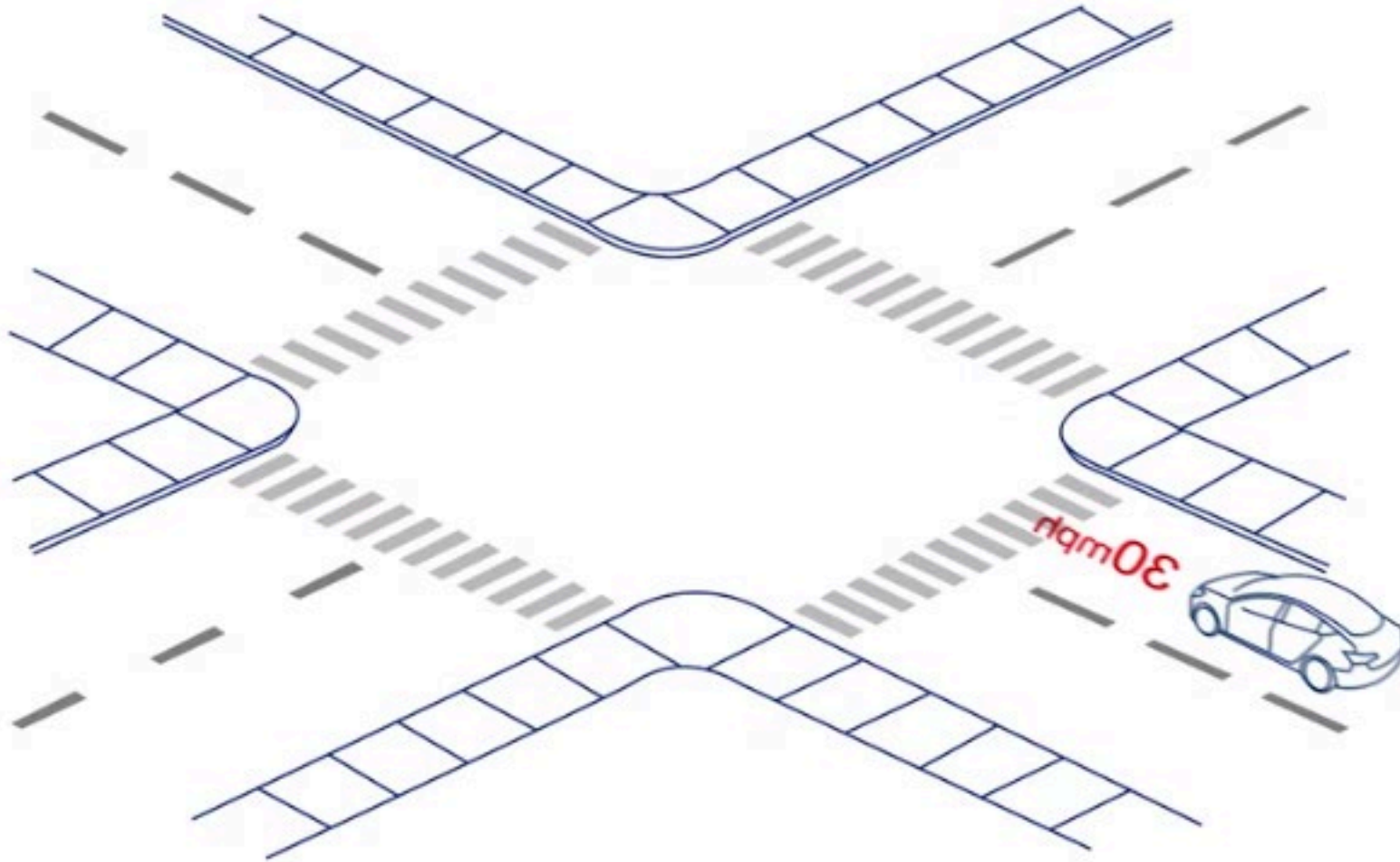
## **Challenges:**

- Driving situations and behaviors are very complex
- Thus difficult to model as a single optimization problem

# Planning and Decision Making

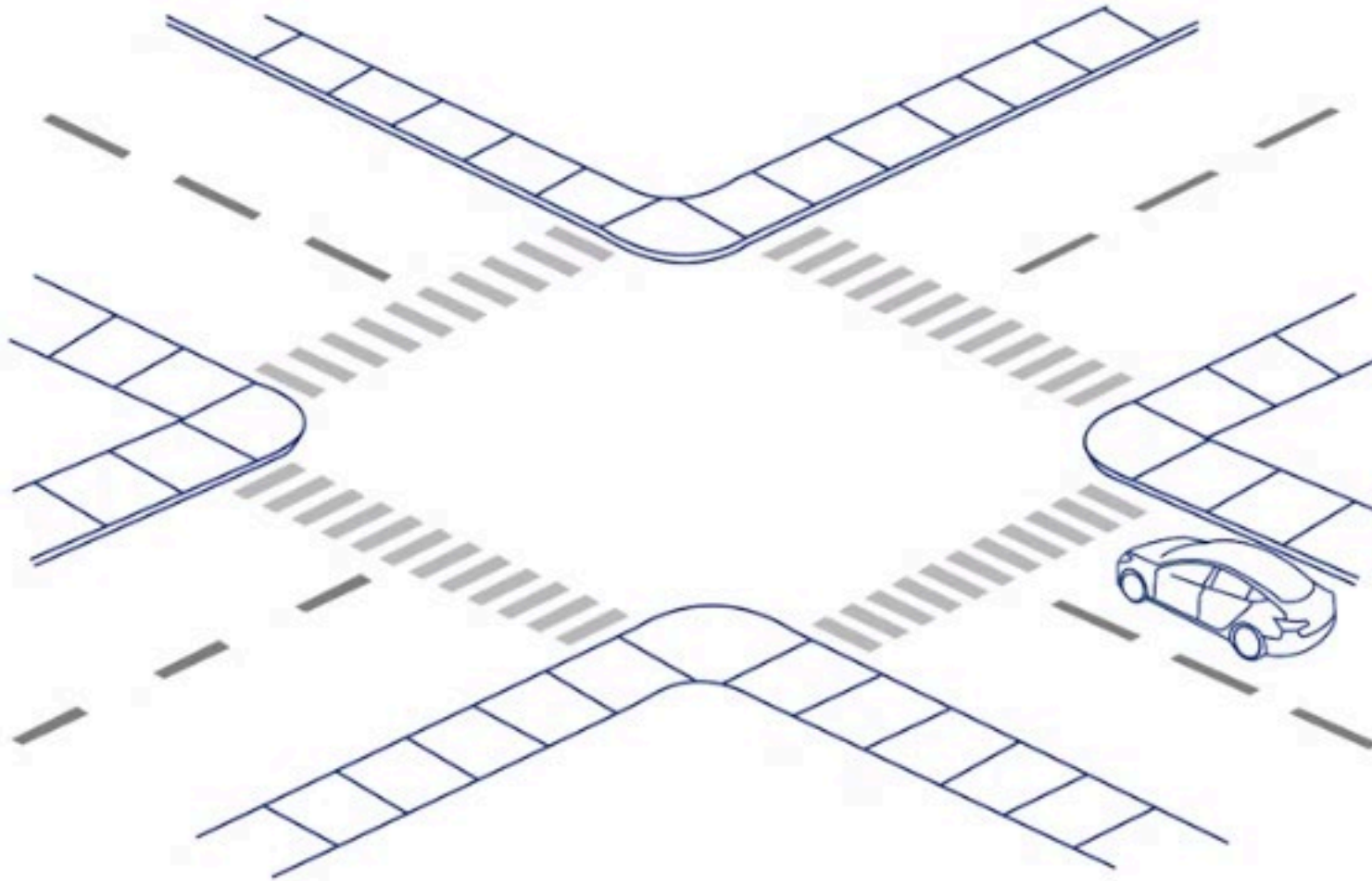


# Planning and Decision Making



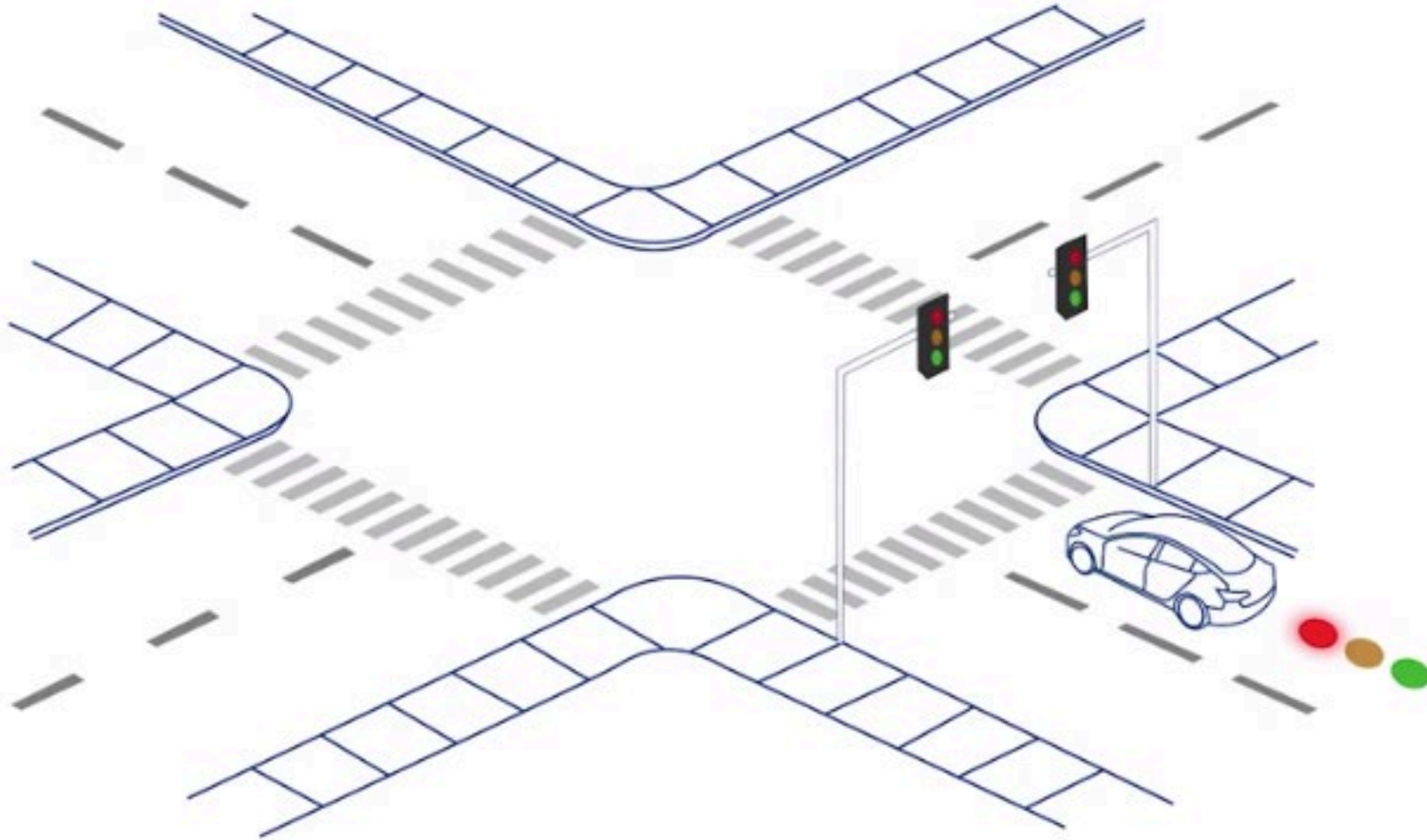
Speed tracking (30 mph)

# Planning and Decision Making



**Decelerate to stop**

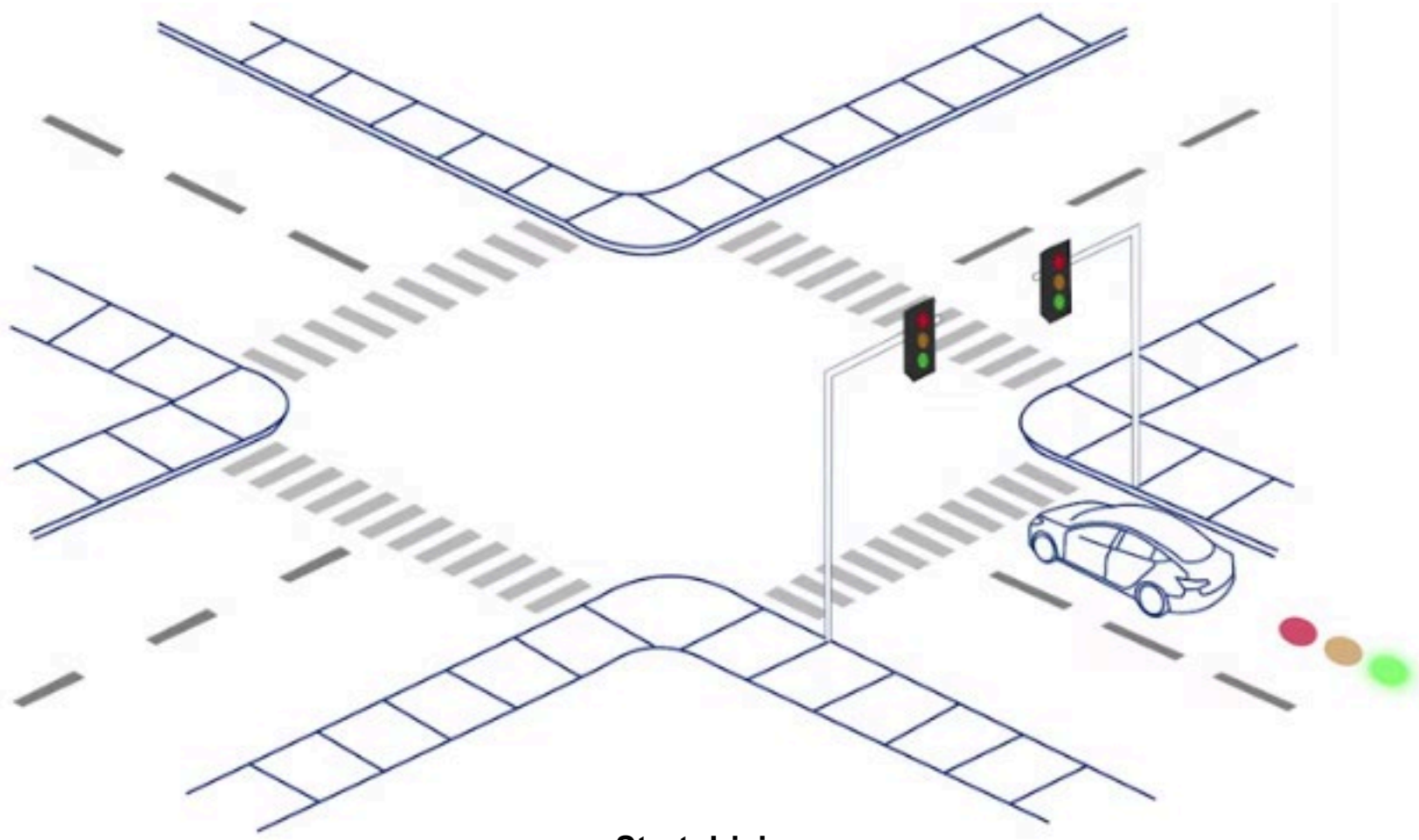
# Planning and Decision Making



**Stay stopped**



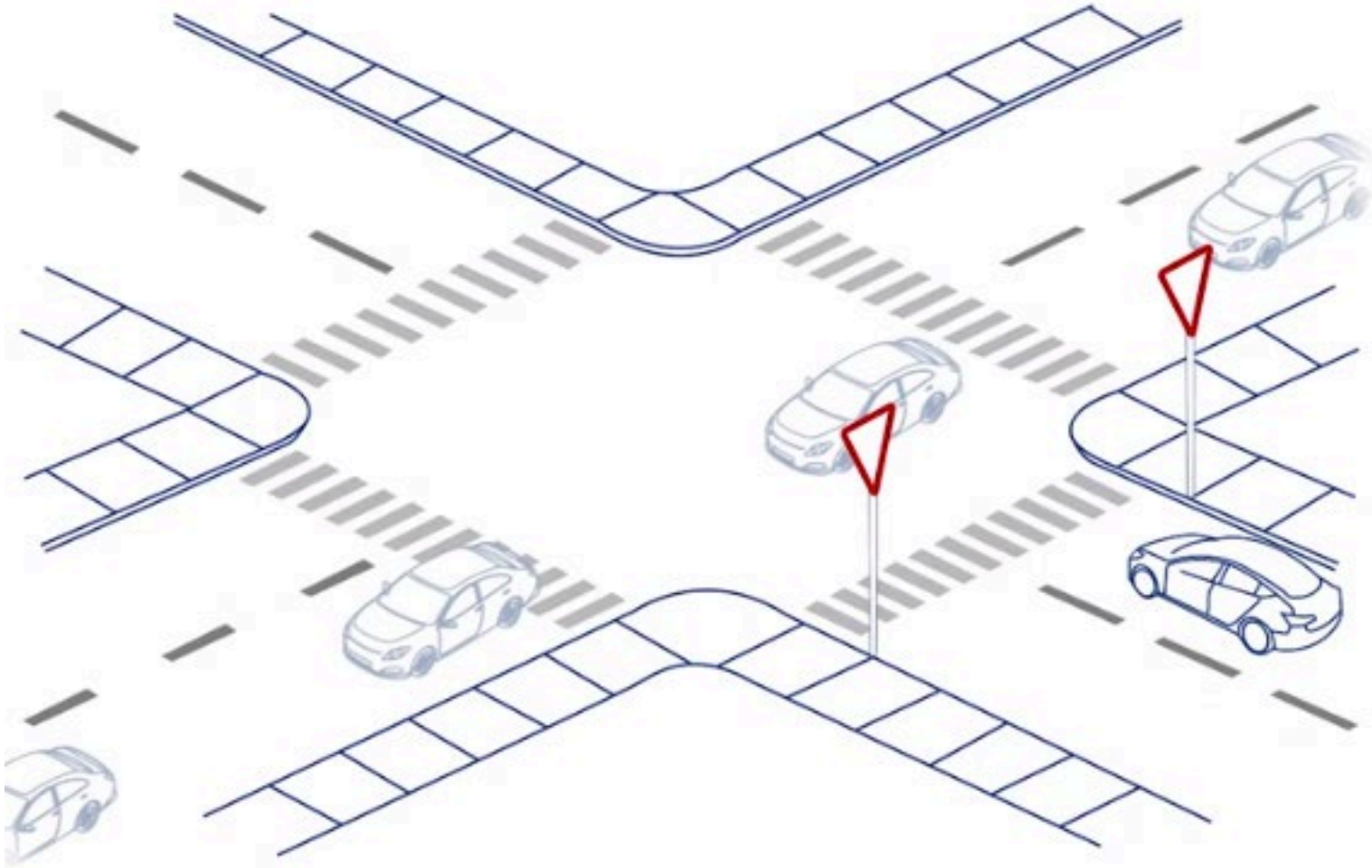
# Planning and Decision Making



**Start driving**

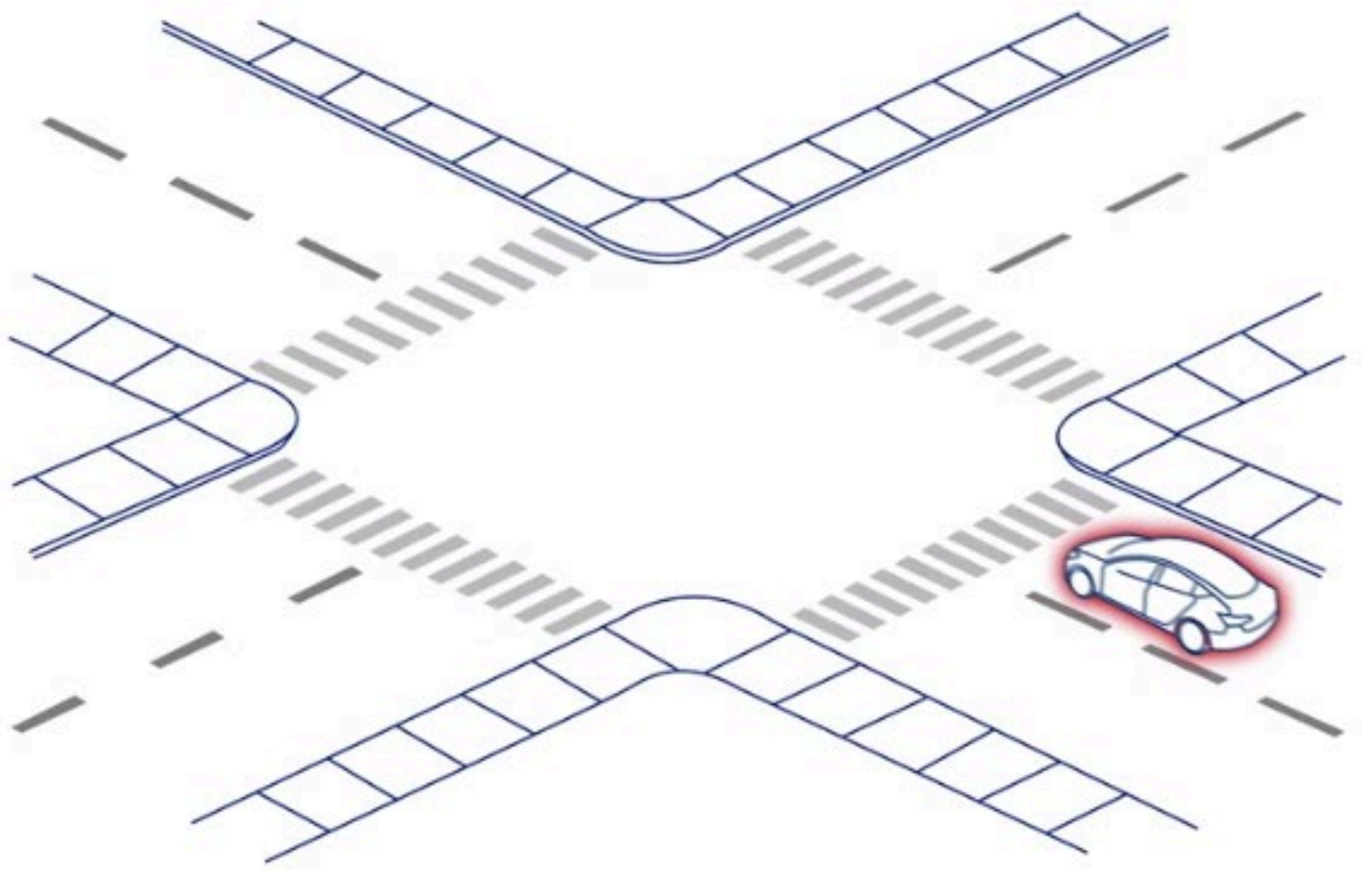


# Planning and Decision Making



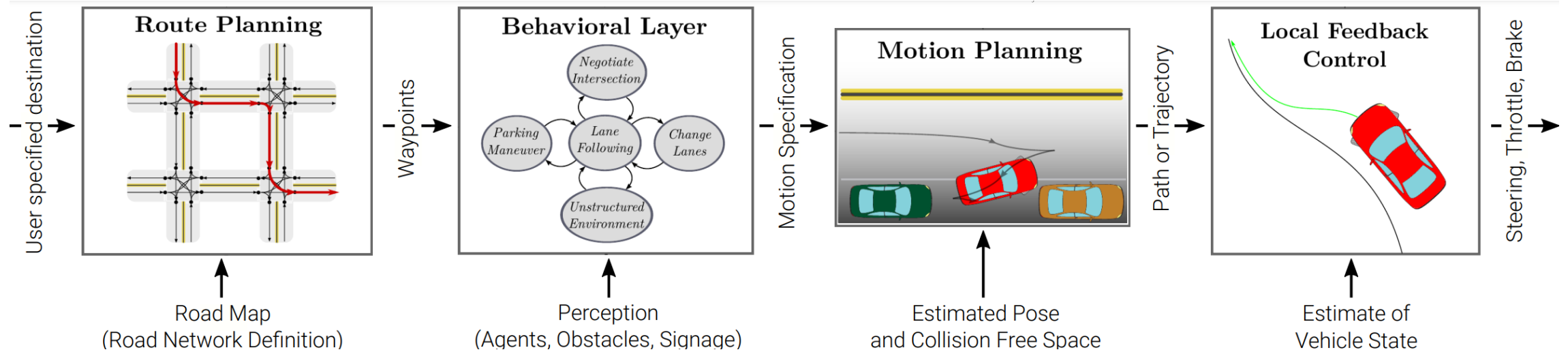
**Yield to traffic**

# Planning and Decision Making



**Emergency stop (and many more ...)**

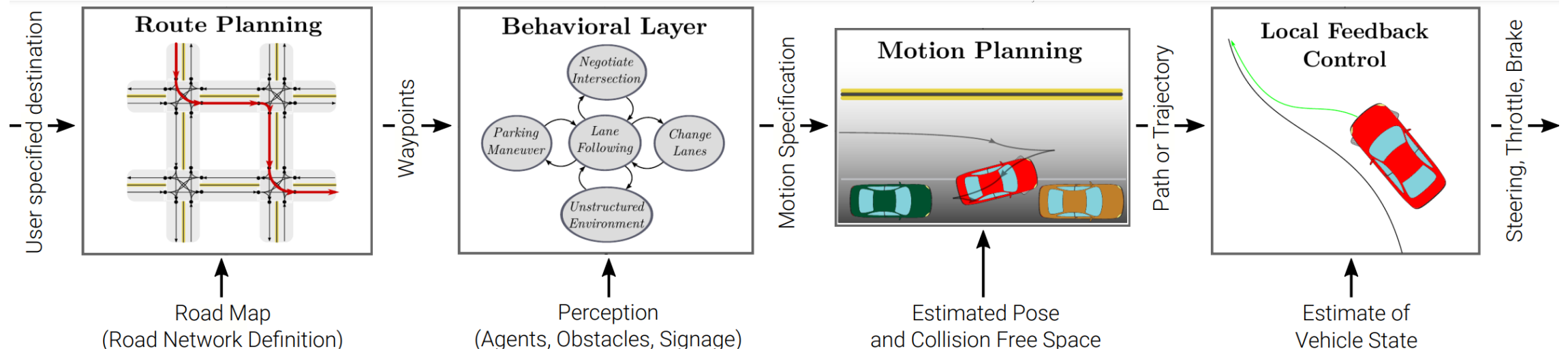
# Planning and Decision Making



Idea: Break planning problem into a **hierarchy of simpler problems**

- Each problem tailored to its scope and level of abstraction
- Earlier in this hierarchy means higher level of abstraction
- Each optimization problem will have constraints and objective functions

# Planning and Decision Making



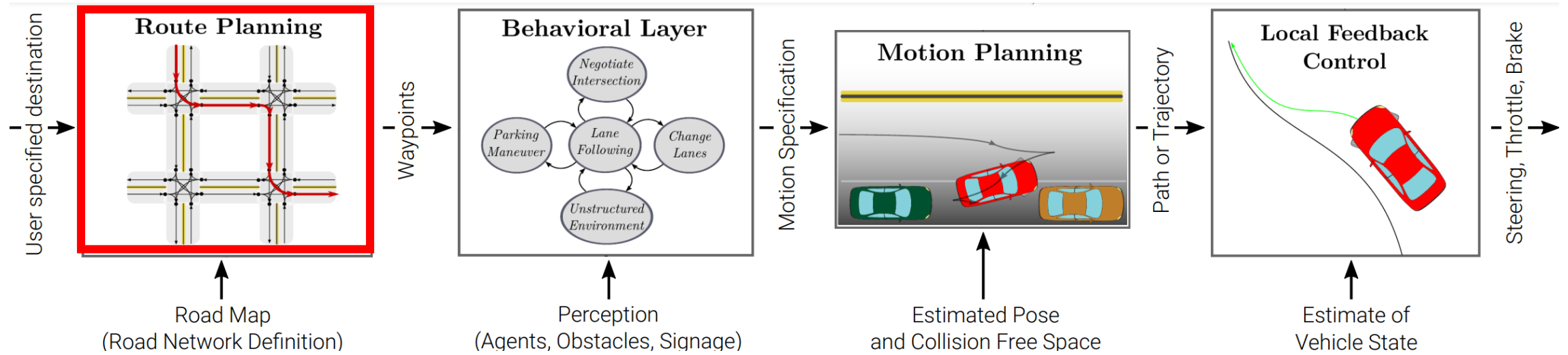
**Route planning:** a route through the road network

**Behavior layer:** motion specification responding to the environment

**Motion Planning:** solving a feasible path accomplishing the specification.

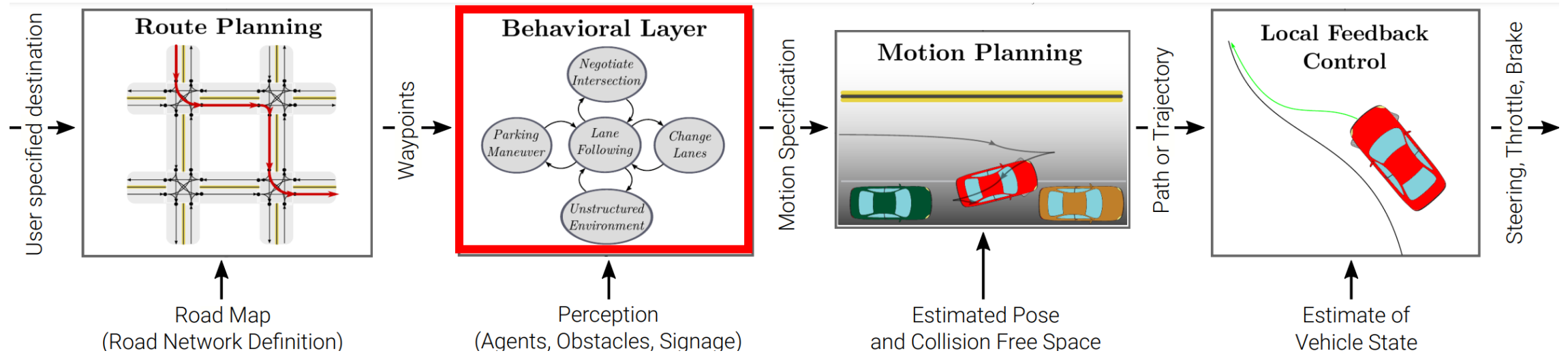
**Feedback Control:** adjusting actuation variables to correct errors in executing the path.

# Route Planning



- Represent road network as directed graph
- Edge weights correspond to road segment length or travel time
- Problem translates into a minimum-cost graph network problem
- Inference algorithms: Dijkstra,  $A^*$ , . . .

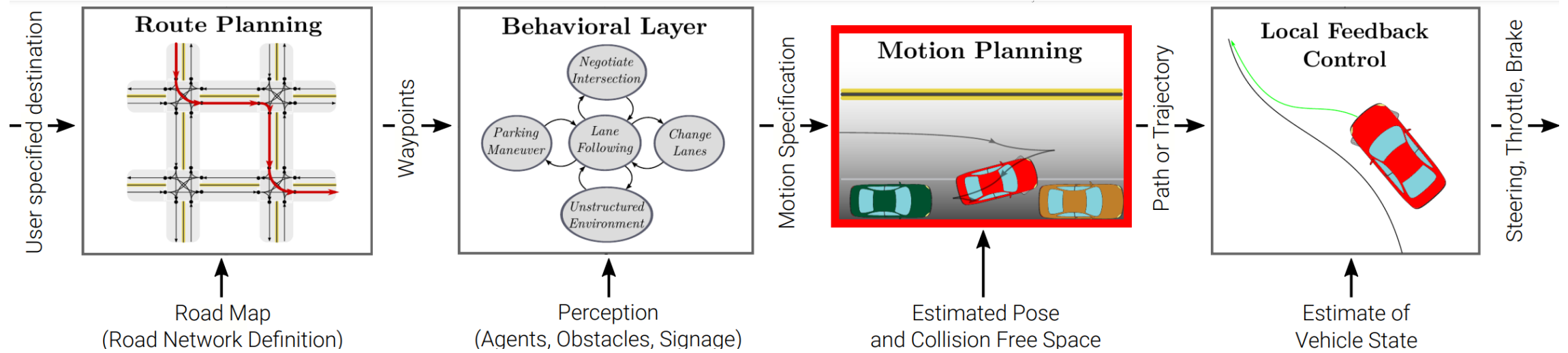
# Behavioral Layer



- Select driving behavior based on current vehicle/environment state
- E.g. at stop line: stop, observe other traffic participants, traverse
- Often modeled via finite state machines (transitions governed by perception)
- Can be modeled probabilistically, e.g., using Markov Decision Processes (MDPs)

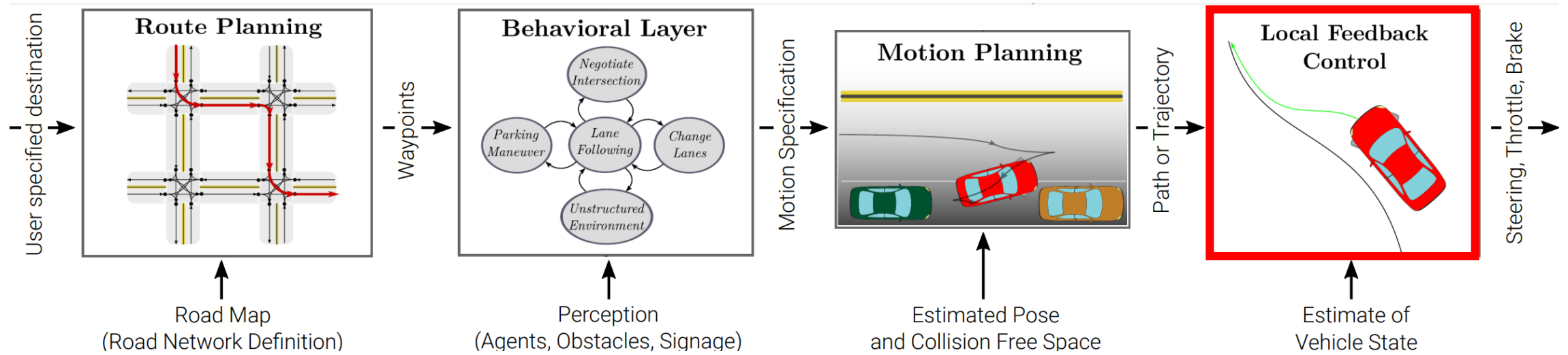


# Motion Planning



- Find feasible, comfortable, safe and fast vehicle path/trajectory
- Exact solutions in most cases computationally intractable
- Thus often numerical approximations are used
- Approaches: variational methods, graph search, incremental tree-based

# Local Feedback Control

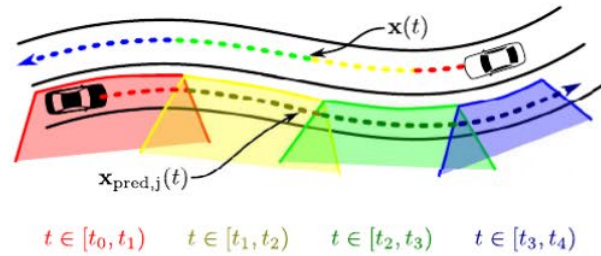


- Feedback controller executes the path/trajectory from the motion planner
- Corrects errors due to inaccuracies of the vehicle model
- Emphasis on robustness, stability and comfort
- Vehicle dynamics and control in Lecture 3

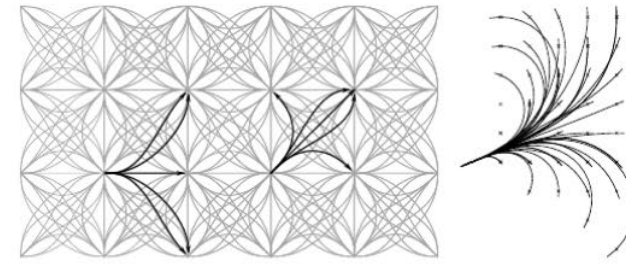
# Path Algorithms



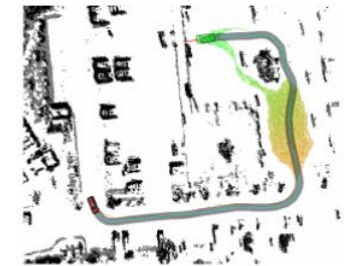
(a) Dijkstra [29]



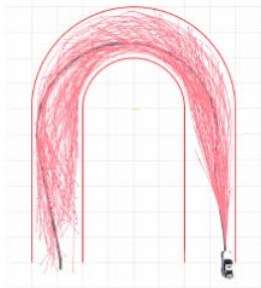
(b) FunctionOptimization [38]



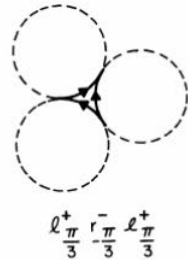
(c) Lattices [39]



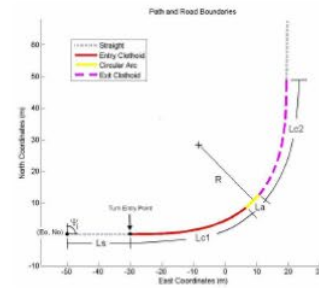
(d) A\* [36]



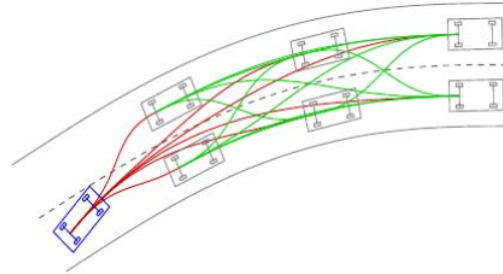
(e) RRT [40]



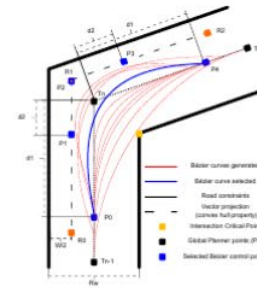
(f) Line&Circle [41]



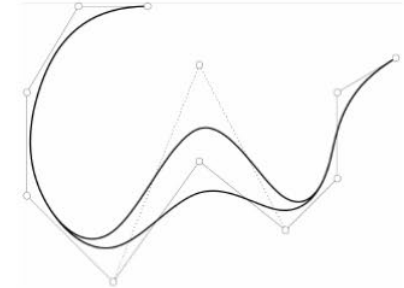
(g) Clothoid [42]



(h) Polynomial [43]



(i) Bezier [44]



(j) Spline [45]

- Planning algorithms used in the autonomous driving literature
- There are many of them – we will focus only on a few today

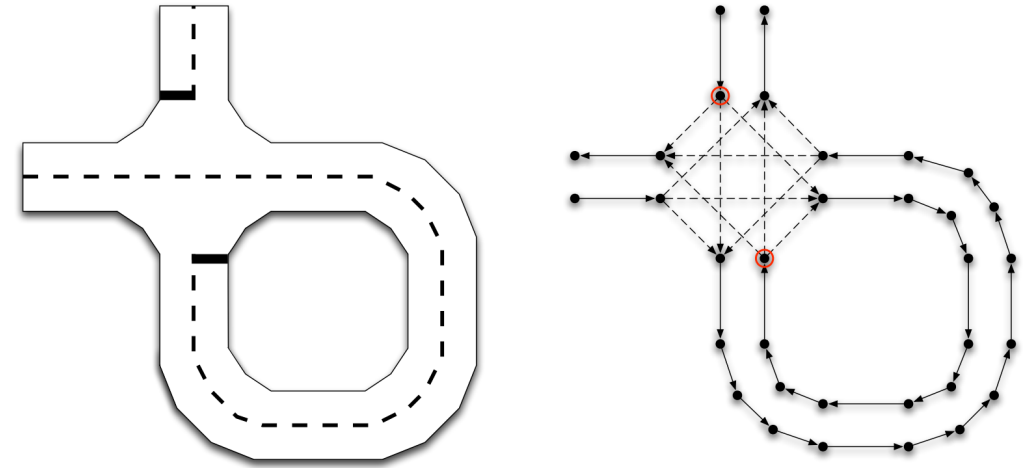
# Route Planning



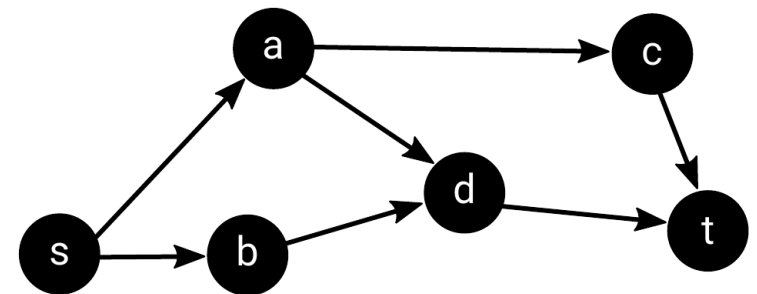
# Road Networks as Graphs



**Road Networks**



**How to interpret roads in graphs**



**A route network is a directional graph!**

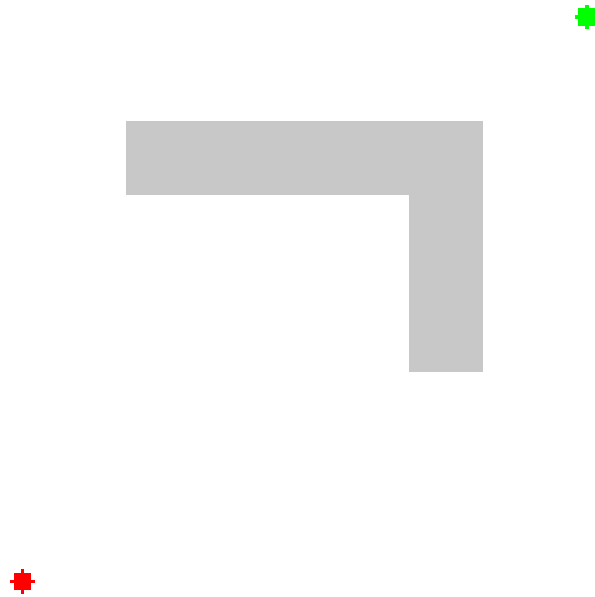
# Route Planning Algorithms

Breadth First Search

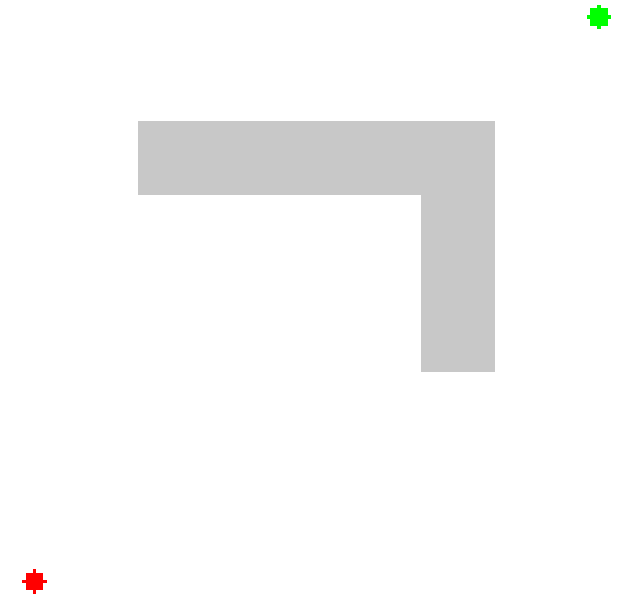
Dijkstra algorithm

A\* algorithm

Other heuristics



**Dijkstra Algorithm**



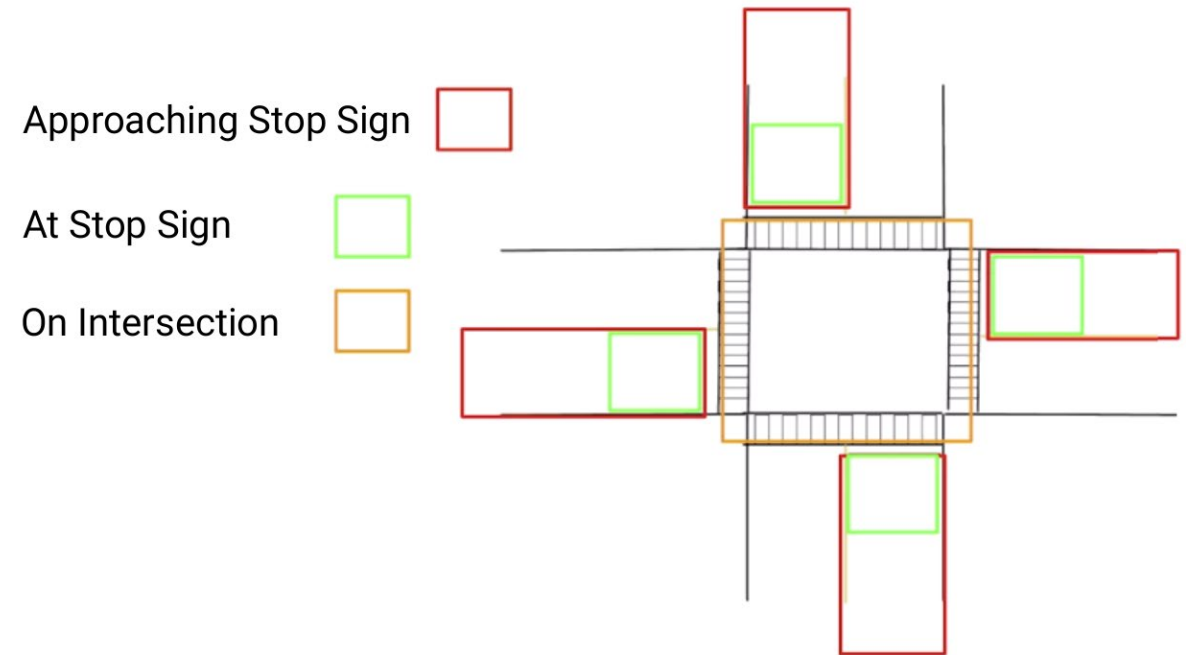
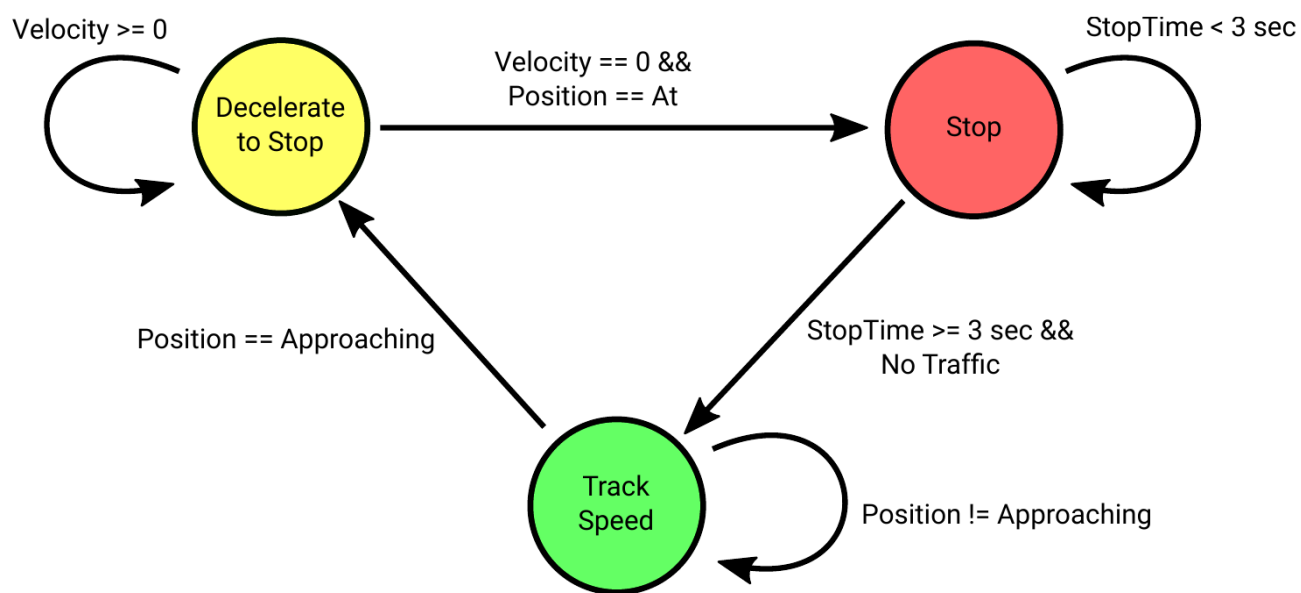
**A\* Algorithm**



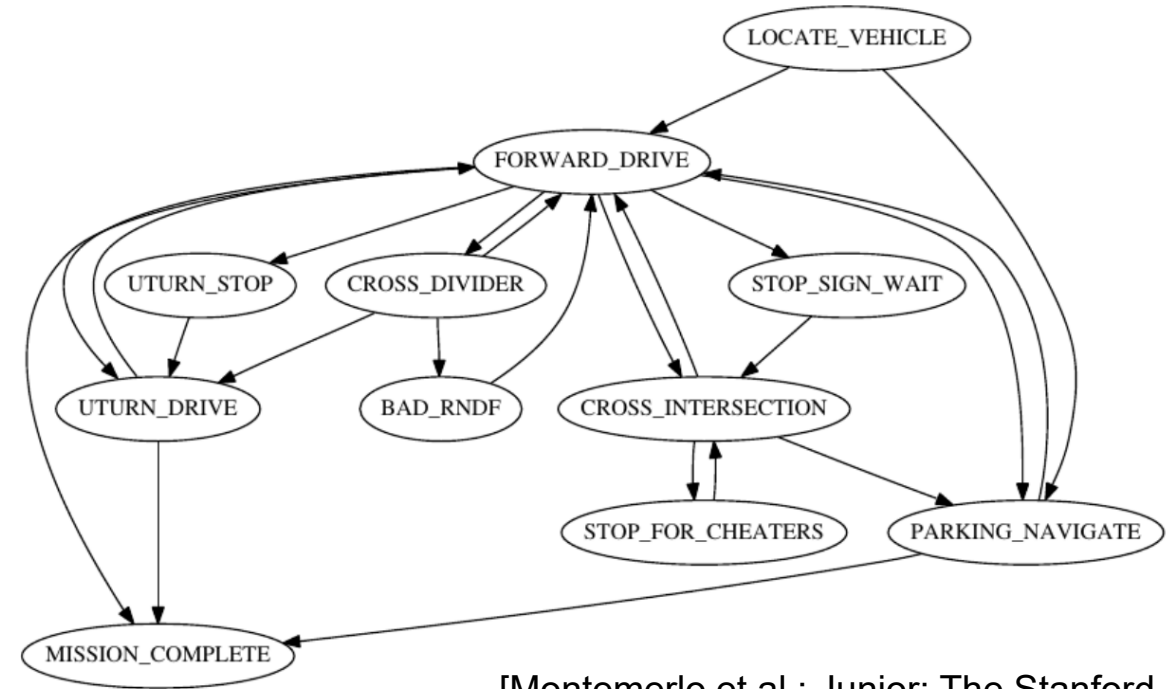
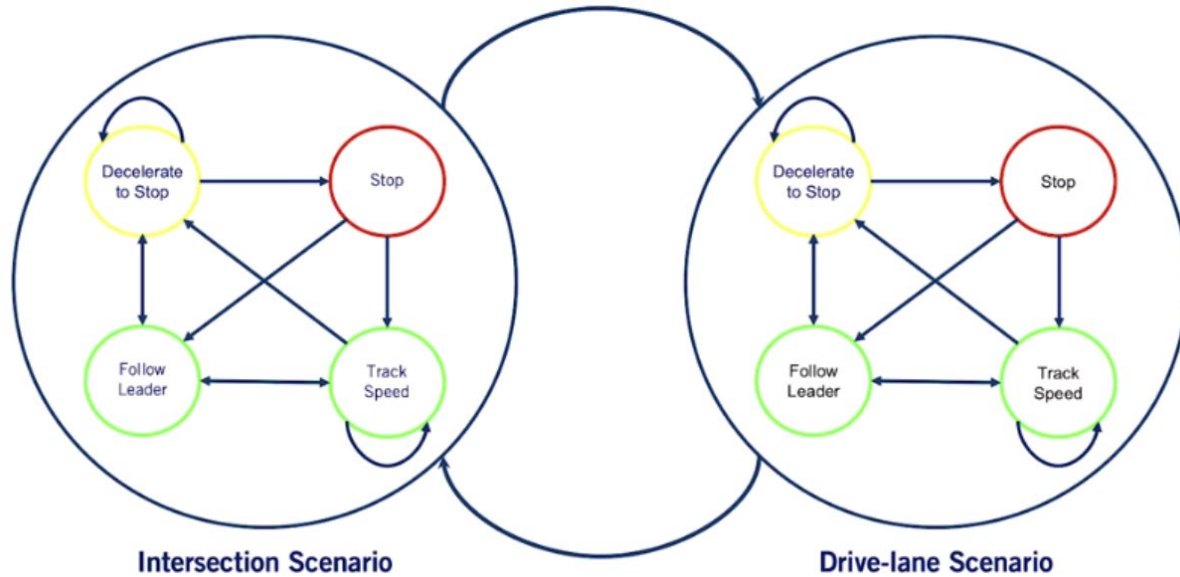
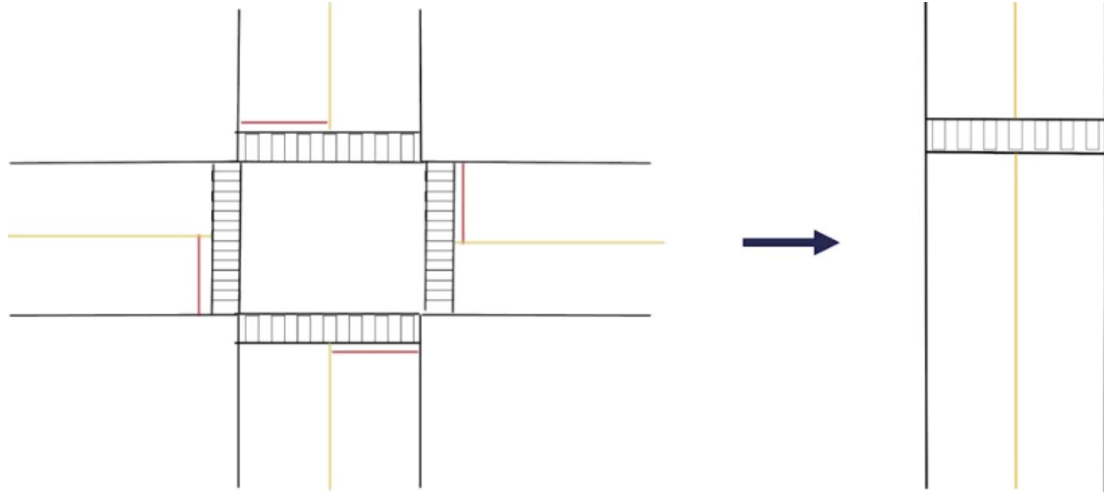
# Behavior Planning

# Finite State Machine for Simple Vehicle Behavior

- While driving, a car needs various maneuvers (decelerating, stop, follow the lane).
- Discretizing car behaviors into atomic maneuvers and the developer design a motion planner dedicated for each maneuver.



# Handling Multiple Scenarios



[Montemerlo et al.: Junior: The Stanford Entry in the Urban Challenge. JFR, 2008]

[Slide Credit: Steven Waslander<sup>23</sup>]

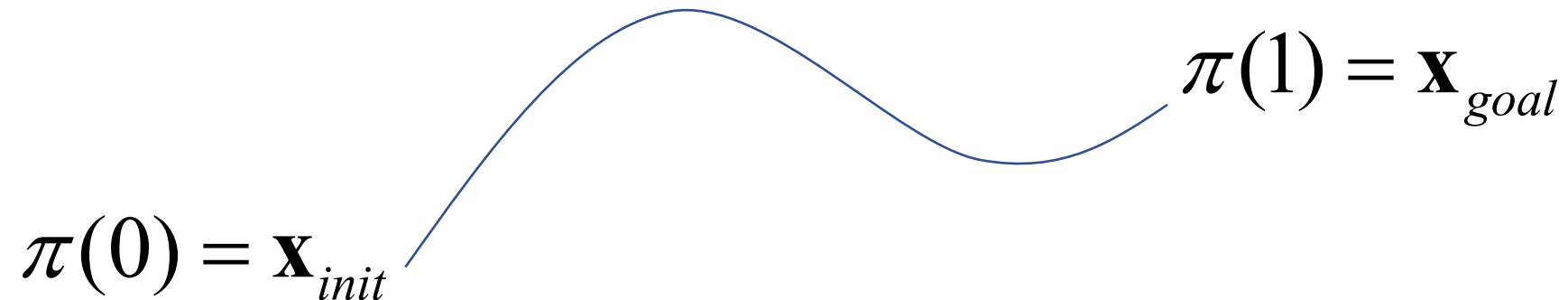
# Motion Planning

# Variational Optimization (함수 최적화)

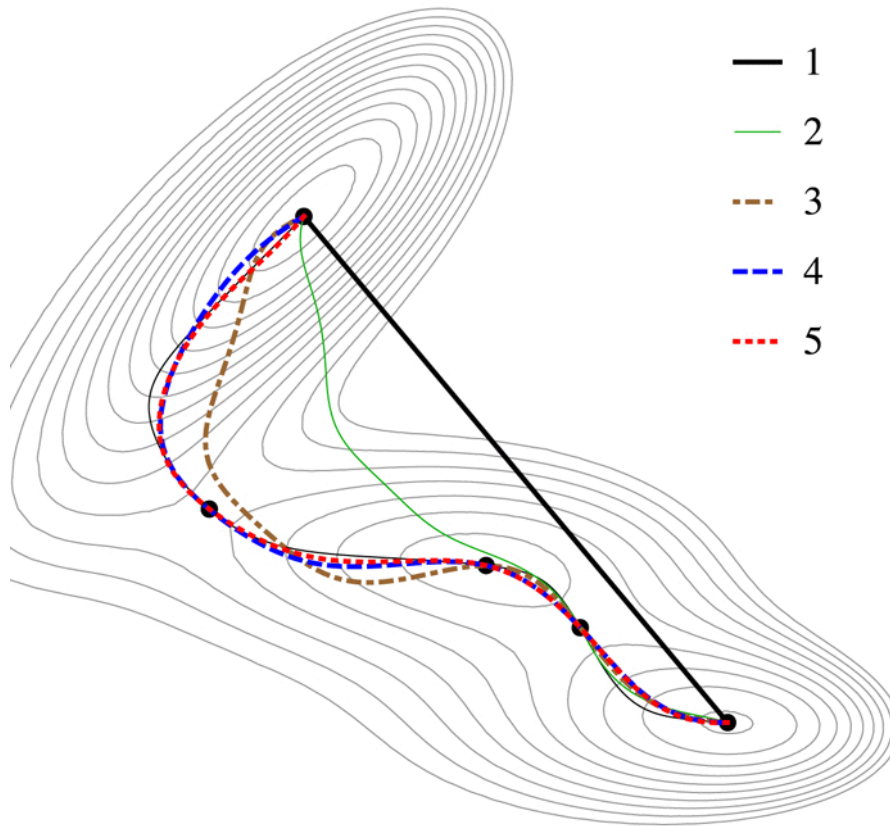
- Variational methods minimize a functional (a function that takes a function as input):

$$\operatorname{argmin}_{\pi} J(\pi) = \int_0^T f(\pi) dt$$

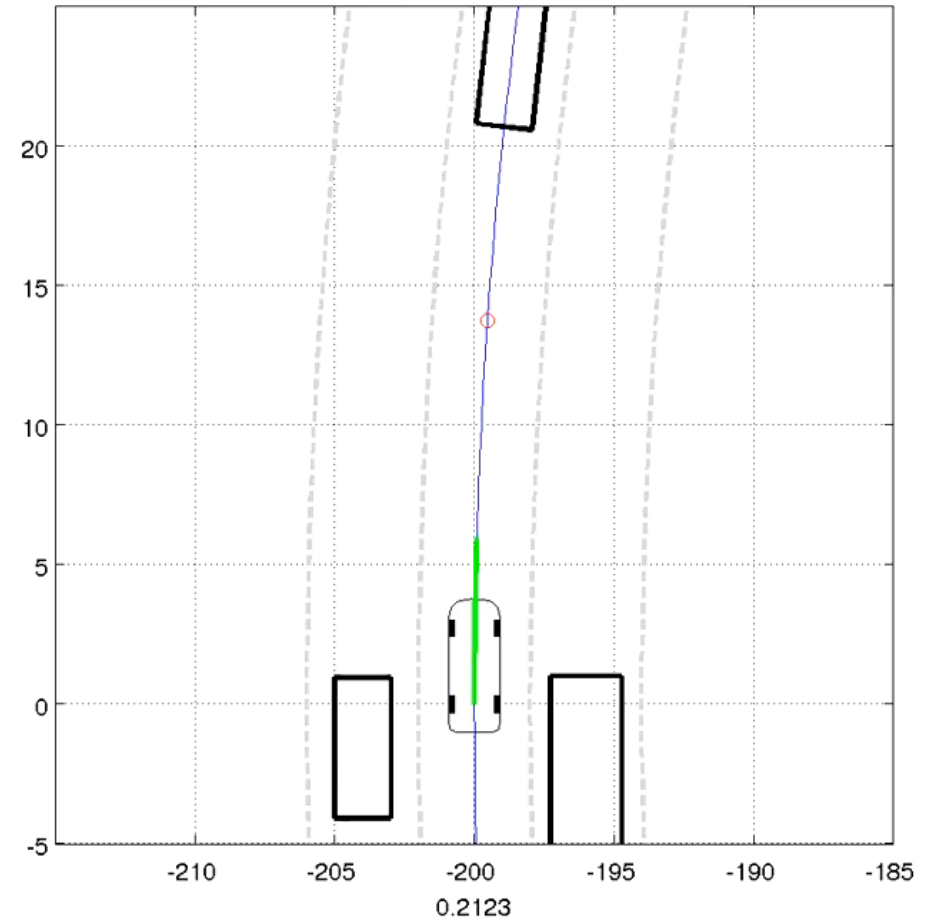
$$\text{s.t. } \pi(0) = \mathbf{x}_{init} \wedge \pi(T) \in \mathbf{x}_{goal}$$



# Variational Optimization examples



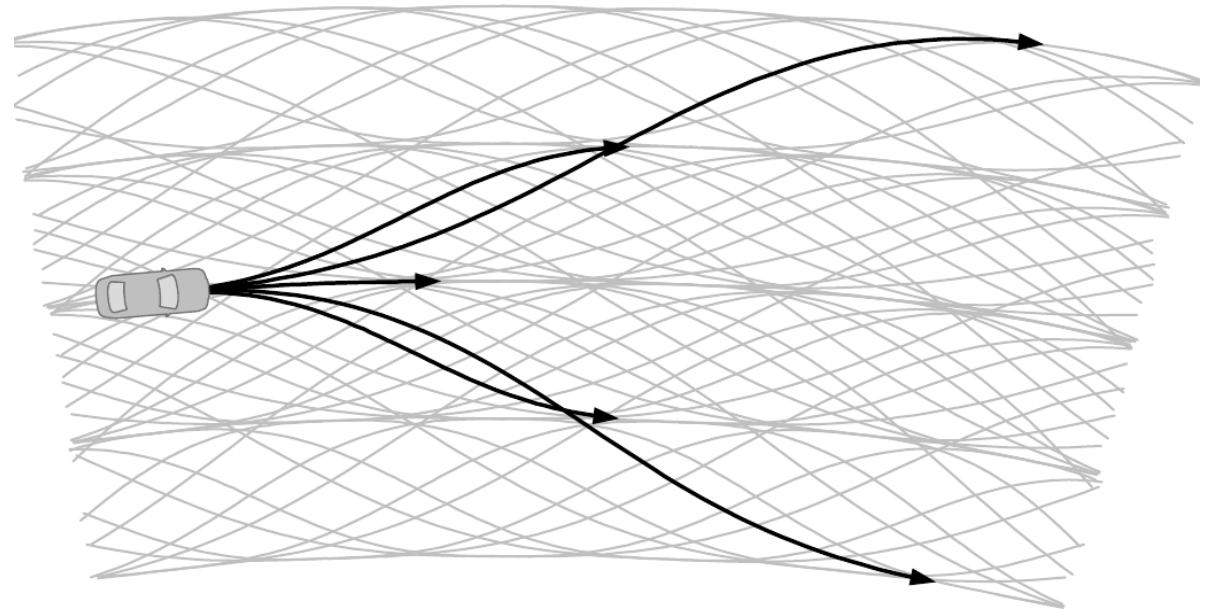
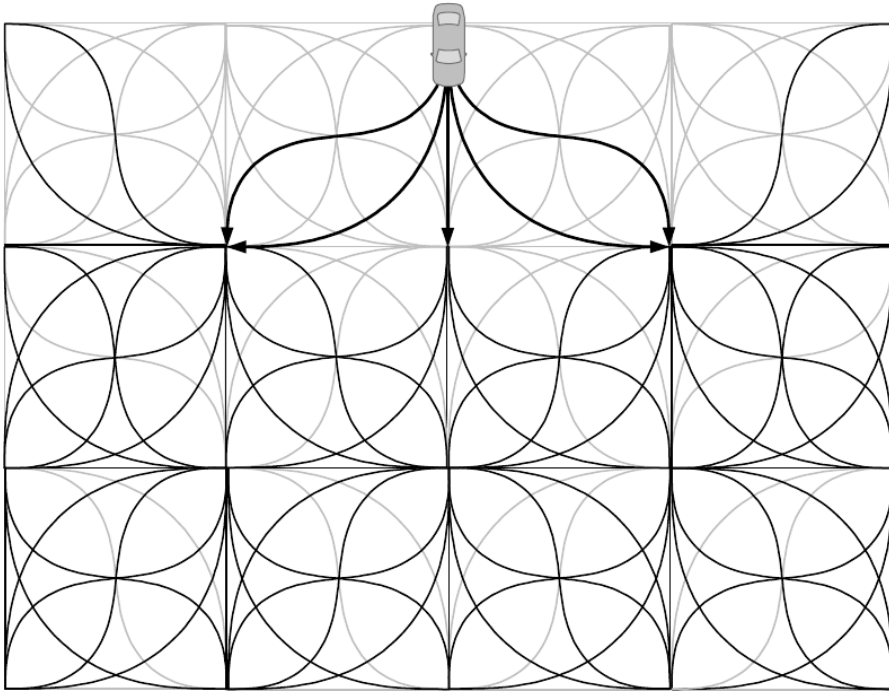
Minimizing the 1<sup>st</sup> derivative of a track



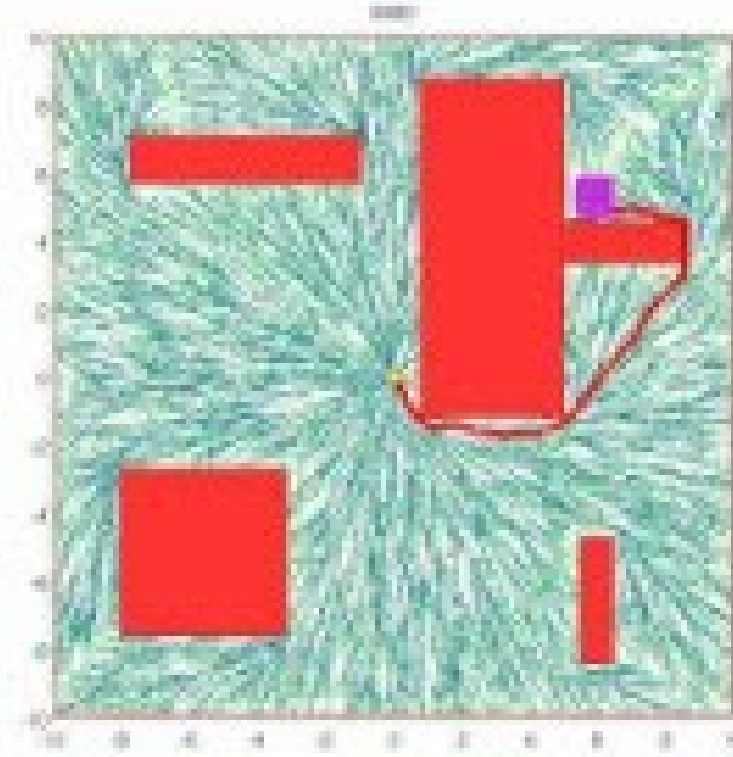


# Graph Search Methods

- Discretize the action space to detour variational optimization.

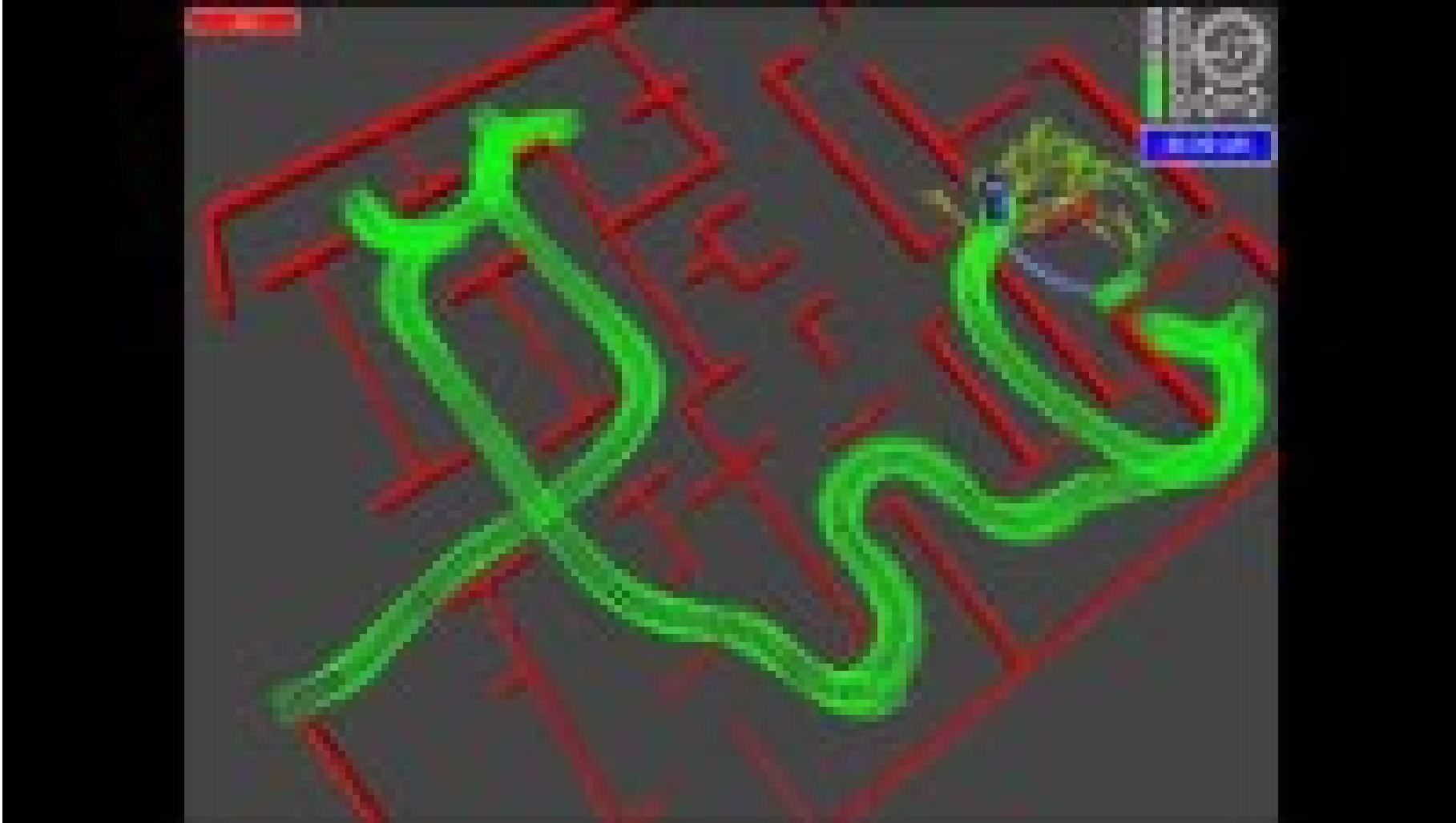


# Incremental Search Techniques



- Incrementally build increasing finer discretization of configuration space.
- Rapidly exploring random trees (RRT) and RRT\*
- <https://www.youtube.com/watch?v=YKiQTJpPFkA>

# RRT meets A\* algorithm



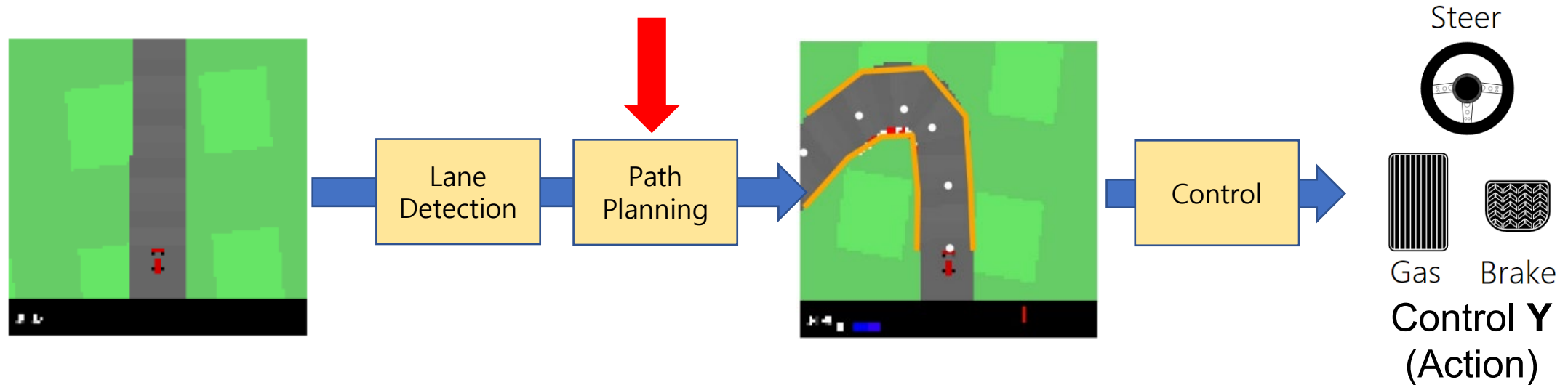
<https://blog.habrador.com/2015/11/explaining-hybrid-star-pathfinding.html>

CS4010

Dolgov et al.: Practical Search Techniques in Path Planning for Autonomous Driving. STAIR, 2008.

# Experiment

# Modular Pipeline Overview



- Implement simplified version of modular pipeline.
- You will understand basic concepts and get experiences of developing a simple self-driving application.

# Path Planning

- Template
  - waypoint\_prediction.py
  - Test\_waypoint\_prediction.py for testing

## a) **Road Center:**

- Use the lane boundary splines and derive lane boundary points for 6 equidistant spline parameter values
  - waypoint\_prediction()
- Determine the center between lane boundary points with the same spline parameter
  - waypoint\_prediction()



# Path Planning

## b) Path Smoothing:

- Improve the path by minimizing the following objective regarding the waypoints  $\mathbf{x}$  given the center waypoints  $\mathbf{y}$

$$\operatorname{argmin}_{x_1, \dots, x_N} \sum_i |\mathbf{y}_i - \mathbf{x}_i|^2 - \beta \sum_n \frac{(\mathbf{x}_{n+1} - \mathbf{x}_n) \cdot (\mathbf{x}_n - \mathbf{x}_{n-1})}{\|\mathbf{x}_{n+1} - \mathbf{x}_n\| \|\mathbf{x}_n - \mathbf{x}_{n-1}\|}$$

- Explain the effect of the second term
- Implement second term  
→ `curvature()`

# Path Planning

## c) Target Speed Prediction:

- Implement a function that outputs the target speed for the predicted path in the state image, using

$$v_{\text{target}}(\mathbf{x}_1, \dots, \mathbf{x}_N) = (v_{\text{max}} - v_{\text{min}}) \exp \left[ -K_v \cdot \left| N - 2 - \sum_n \frac{(\mathbf{x}_{n+1} - \mathbf{x}_n) \cdot (\mathbf{x}_n - \mathbf{x}_{n-1})}{\|\mathbf{x}_{n+1} - \mathbf{x}_n\| \|\mathbf{x}_n - \mathbf{x}_{n-1}\|} \right| \right] + v_{\text{min}}$$

As initial parameters use:  $v_{\text{max}} = 60$ ,  $v_{\text{min}} = 30$ , and  $K_v = 4.5$

→ `target_speed_prediction()`