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# Chapter 2

## Theoretical Calculations

In an experiment, the measurements are validated by doing the comparison with the perturbative QCD (pQCD) theoretical calculations. The lowest order (LO) calculations describe well the shapes of the measured distributions but not the normalization due to the dependence on the unphysical renormalization ( $\mu_r$ ) and factorization ( $\mu_f$ ) scales. The next-to-leading order calculations (NLO) improves the precision by reducing the dependence on  $\mu_r$  and  $\mu_f$  scales and become an essential feature in the determination of fundamental parameters such as  $\alpha_s$  and the parton density distributions. In this chapter, the next-to-leading order pQCD calculations are described in details. NLO pQCD calculations are corrected for the multiparton interactions (MPI) and hadronization effects by applying non-perturbative (NP) corrections and also corrected for the electroweak interactions (EW).

### 2.1 Fixed Order NLO Calculations

The predictions of the inclusive differential jet event cross section at NLO accuracy in pQCD are computed with the NLOJET++ program version 4.1.3 [18, 19]. The results are provided within the framework of FASTNLO version 2.3 [20, 21] for use within fits. The parton distribution functions (PDFs) are accessed through the

LHAPDF6 library [22, 23]. The FASTNLO is preferred over the direct calculation with NLOJET++ as the calculations of the cross sections can be repeated several times with different PDFs as well as scale choices required for the calculating PDF and scale uncertainties. The renormalization and factorization scales are chosen equal to  $H_{T,2}/2$ , i.e.  $\mu_r = \mu_f = H_{T,2}/2$ .

In the current study, different PDF sets available for a series of different assumptions on  $\alpha_s(M_Z)$  are used for NLO calculations. In Table 2.1, already existing PDF sets in LHC Run 1 (upper rows) and newer ones for Run 2 (lower rows) are listed together with the corresponding number of flavours  $N_f$ , the assumed masses  $M_t$  and  $M_Z$  of the top quark and the  $Z$  boson, respectively, the default values of  $\alpha_s(M_Z)$ , and the range in  $\alpha_s(M_Z)$  variation available for fits. All sets employ a variable-flavour number scheme with at most five or six flavours apart from the ABM11 PDFs, which use a fixed-flavour number scheme with  $N_F = 5$ . Mainly CT10 PDF set is considered for comparison between data and theory predictions as well as for calculating theoretical uncertainties. Out of these eight PDF sets the following three are not considered further because of the below mentioned reasons :

- At NLO, predictions based on ABM11 do not describe LHC jet data at small jet rapidity [24–27].
- The HERAPDF2.0 set exclusively fits HERA DIS data with only weak constraints on the gluon PDF.
- The range in values available for  $\alpha_s(M_Z)$  is too limited for the NNPDF3.0 set.

### 2.1.1 NLO Correction Factors

The differences between LO predictions and NLO predictions give the impact of the higher-order contributions to the pQCD predictions. These are described by a NLO

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Table 2.1: NLO PDF sets are available via LHAPDF6 with various assumptions on the value of  $\alpha_s(M_Z)$ . The already existing sets in LHC Run 1 (upper rows) and newer ones for Run 2 (lower rows) are listed here with the corresponding number of flavours  $N_f$ , the assumed masses  $M_t$  and  $M_Z$  of the top quark and the  $Z$  boson, respectively, the default values of  $\alpha_s(M_Z)$ , and the range in  $\alpha_s(M_Z)$  variation available for fits. A \* behind the  $\alpha_s(M_Z)$  values signifies that the parameter was fixed, not fitted.

Base set	$N_F$	$M_t$ (GeV)	$M_Z$ (GeV)	$\alpha_s(M_Z)$	$\alpha_s(M_Z)$ range
ABM11 [28]	5	180	91.174	0.1180	0.110–0.130
CT10 [29]	$\leq 5$	172	91.188	0.1180*	0.112–0.127
MSTW2008 [30, 31]	$\leq 5$	$10^{10}$	91.1876	0.1202	0.110–0.130
NNPDF2.3 [32]	$\leq 6$	175	91.1876	0.1180*	0.114–0.124
CT14 [33]	$\leq 5$	172	91.1876	0.1180*	0.113–0.123
HERAPDF2.0 [34]	$\leq 5$	173	91.1876	0.1180*	0.110–0.130
MMHT2014 [35]	$\leq 5$	$10^{10}$	91.1876	0.1180*	0.108–0.128
NNPDF3.0 [36]	$\leq 5$	173	91.2	0.1180*	0.115–0.121

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correction factor, k-factor, which is defined as the ratio of cross sections at NLO accuracy to that at LO i.e.

$$\text{k-factor} = \frac{\sigma_{\text{NLO}}}{\sigma_{\text{LO}}} \quad (2.1)$$

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The size of k-factor determine the effect of the higher-order corrections. The small size of k-factor indicates that the cross section predictions are precisely described at the LO whereas the larger size hints the contributions from NLO. Figure 2.1 shows the k-factors of the NLOJET++ calculations, for inclusive 2-jet and 3-jet events cross sections and their ratio  $R_{32}$ , using five different PDF sets. k-factor for  $R_{32}$  is obtained by taking the ratio of k-factors for inclusive 3-jet events cross sections to that of inclusive 2-jet. The k-factors are similar for all the PDF sets in the lower region, but the differences increase in regions with larger  $H_{\text{T},2}/2$ . It is observed that for inclusive 3-jet events cross sections, k-factor jumps at lowest  $H_{\text{T},2}/2$ . This is because some jet configurations are kinematically forbidden near the  $p_{\text{T}}$  cut bin i.e. 150 GeV. Since the first few bins in  $H_{\text{T},2}/2$  (below 225 GeV) still suffer from these

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kinematical effects, the minimum value of  $H_{T,2}/2$  studied is 300 GeV.

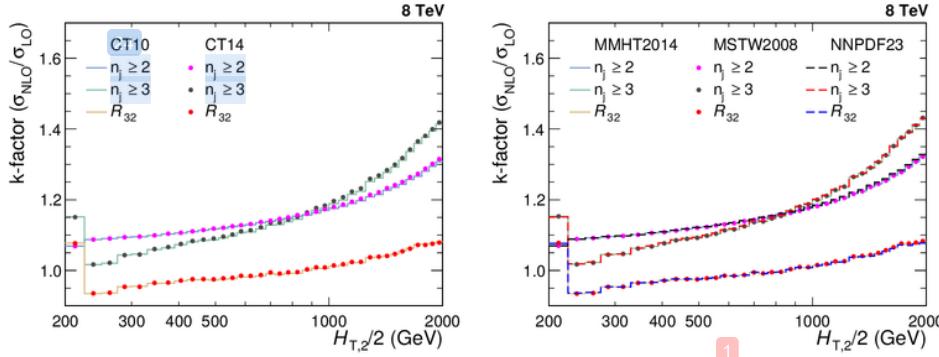


Figure 2.1: The k-factors of the NLOJET++ calculations, for inclusive 2-jet and 3-jet events cross sections and their ratio  $R_{32}$ , using five different PDF sets.

### 9 2.1.2 Non-Perturbative Corrections

The fixed-order pQCD calculations predict the parton-level cross section but lacks accuracy due to several effects. The partons which are emitted close to each other in phase space are not handled well in lower order perturbation theories and hence requires a parton shower (PS) correction. The scattering phenomena between partons within a colliding proton, other than the hard scattering, are known as multi-parton interactions (MPI). The partons of the hard scattering forms colorless bound states called hadrons through a process of hadronization (HAD). The MPI and hadronization cannot be modelled well within the perturbative framework. Since the fixed-order NLO calculations do not include these additional soft QCD effects, these calculations cannot be compared directly to unfolded data. So these calculations should be corrected for non-perturbative effects (NP). The cross section ratio between a nominal event generation interfaced to the simulation of UE contributions and a sample without hadronization and MPI effects are taken as correction factors and are defined as :

$$C^{\text{NP}} = \frac{\sigma^{\text{PS+HAD+MPI}}}{\sigma^{\text{PS}}} \quad (2.2)$$

In this analysis, the NP effects are evaluated by using samples obtained from different MC event generators with a simulation of parton shower and underlying-event (UE) contributions. The leading order (LO), HERWIG++ [37] with the default tune of version 2.3 and PYTHIA6 [2] with tune Z2\*, and the NLO, POWHEG [38–40], MC event generators are considered. The matrix-element calculation performed with POWHEG is interfaced to PYTHIA8 with tune CUETS1 [41] for the UE simulation. The ratio, defined in Eq. 2.2, is obtained for each MC generator and is fitted by a power-law function defined in Eq. 2.3. Since this ratio obtained from different MC generators have large differences, so the average of the envelope, which covers all the differences, is taken as the correction factor which is then applied as bin-by-bin multiplicative factor to the parton-level NLO cross section. The half of the envelope it is taken as the uncertainty on the NP correction factor.

$$f(H_{T,2}/2) = a \cdot (H_{T,2}/2)^b + c \quad (2.3)$$

The NP correction factors,  $C_{3\text{-jet}}^{\text{NP}}$  and  $C_{2\text{-jet}}^{\text{NP}}$  are calculated for  $n_j \geq 2$  and  $n_j \geq 3$  event cross sections respectively and then their ratio gives the correction factor for  $R_{32}$ . These are shown in Fig. 2.2 for the inclusive 2-jet (top left) and 3-jet event cross sections (top right), as well as for cross section ratio  $R_{32}$  (bottom). The NP corrections amount to  $\sim 4\text{--}5\%$  for inclusive 2-jet and 3-jet events cross section and  $\sim 1\%$  for ratio  $R_{32}$ , for  $H_{T,2}/2 \sim 300$  GeV and decrease rapidly for increasing  $H_{T,2}/2$ . On comparing the NP correction factors of cross section ratio with that for individual cross sections, it has been observed that the non-perturbative effects get reduced in the cross section ratio.

### 2.1.3 Electroweak Corrections

In LHC, the centre-of-mass energy of proton-proton collisions is well beyond the electroweak (EW) scale  $\sim O(100)$  GeV. At such a high energy, the impact of higher

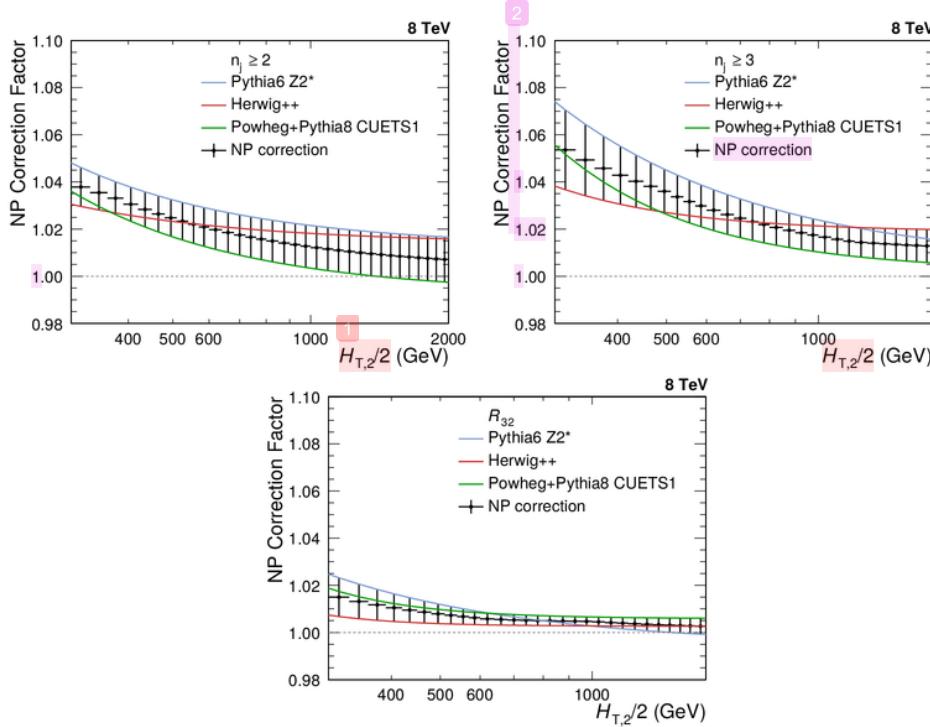


Figure 2.2: 1 The nonperturbative (NP) corrections are presented as a function of  $H_{T,2}/2$  for inclusive 2-jet (top left) and 3-jet (top right) event cross sections, as well as their ratio  $R_{32}$ . These corrections are calculated from the leading order HERWIG++ with the default tune of version 2.3 (red line) and PYTHIA6 with tune Z2\* (blue line); and the next-to-leading order POWHEG interfaced to PYTHIA8 with tune CUETS1 (green line) Monte Carlo event generators. The black solid circles give the average NP correction factor along with the uncertainty shown by the error bars.

order EW corrections is much more with respect to QCD effects [42] and affect jet cross sections at large jet  $p_T$ . The quark-quark scattering processes involving virtual exchanges of massive W and Z bosons contribute to electroweak (EW) corrections. The fixed-order QCD calculations do not include EW corrections and hence the NLO theory calculations are corrected for EW effects. The EW corrections have been calculated for inclusive 1-jet and 2-jet case, in Ref. [43] but are not available yet for inclusive 3-jet production. The EW correction factors in the phase space of the measurement are shown as a function of  $H_{T,2}/2$  in Fig. 2.3 for inclusive 2-jet

events cross sections. These correction factor increases up to 13% at high ends of  $H_{T,2}/2$  and significantly improves the agreement between data and prediction. Since the guess from theory side is that EW for inclusive 2-jet and 3-jet will be similar, so for  $R_{32}$ , it is assumed to be equal to the factor of 1. These corrections are applied as a bin-by-bin correction factor to the fixed-order calculation of NLOJET++ as well as to the Monte Carlo predictions .

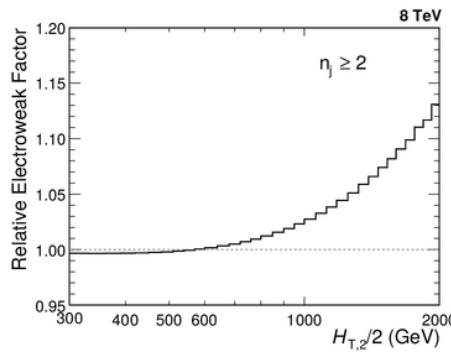


Figure 2.3: The electroweak (EW) corrections [43] in the phase space of the measurement are shown as a function of  $H_{T,2}/2$  for inclusive 2-jet events cross sections. These corrections are applied as a bin-by-bin correction factor to the fixed-order calculation of NLOJET++ as well as the MC predictions of MADGRAPH5+PYTHIA6. The EW correction factor increases up to 13% at high ends of  $H_{T,2}/2$  and significantly improves the agreement between data and prediction.

## 2.2 Theoretical Uncertainties

The measurements are not only sensitive to experimental uncertainties but also to the theoretical uncertainties. The various sources contributing to theoretical uncertainties are described below :

### 2.2.1 Scale Uncertainty

In perturbative QCD calculations of cross sections, one has to choose a renormalization ( $\mu_r$ ) and factorization ( $\mu_f$ ) scale. The dependence on scales is negligible

if these calculations are performed for all orders of the perturbative series. But the perturbative series is truncated at NLO, so there is a scale dependence of the measurement which is covered by systematic uncertainty known as scale uncertainty. The scale uncertainty is evaluated with the conventional recipe of varying the default scale  $H_{\text{T},2}/2$  chosen for  $\mu_r$  and  $\mu_f$  independently in the following six combinations:  $(\mu_r/H_{\text{T},2}/2, \mu_f/H_{\text{T},2}/2) = (1/2,1/2), (1/2,1), (1,1/2), (1,2), (2,1)$  and  $(2,2)$ . The maximal upwards and downwards deviations in cross section from the central prediction give the scale uncertainty. To calculate the scale uncertainty for cross section ratio  $R_{32}$ , first  $R_{32}$  is obtained for each above mentioned scale choice and then its difference from central  $R_{32}$  is taken. The scale uncertainty calculated using CT10-NLO PDF set ranges for inclusive 2-jet events from 5% to 13%, for inclusive 3-jet events from 11% to 17% and for  $R_{32}$  from 6% to 8%.

### 2.2.2 PDF Uncertainty

The calculation of the jet production cross sections in proton-proton collisions relies upon the knowledge of parton distribution functions (PDF). These PDF sets are best determined by global fits to all the available deep inelastic scattering (DIS) and related hard scattering data from different experiments. The various sources affect the PDFs such as theory model, input parameters like the strong coupling constant  $\alpha_s$ , the quark masses and the statistical and systematic uncertainty sources of the data included in the PDF fit. These sources contribute to PDF uncertainty which is evaluated according to the prescriptions given for each PDF set. The CT10 NLO PDF set [29, 44] employ the eigenvector method to evaluate the PDF uncertainties. The CT10 PDF set consists of  $N_{\text{ev}} = 26$  eigenvectors with two PDF members per eigenvector  $k$ , which are varied upwards and downwards to generate a set of eigenvector pairs. The asymmetric uncertainties,  $\Delta X^+$  and  $\Delta X^-$ , of a quantity  $X$  are given by Eq. 2.4 where  $X_0$  is the central prediction,  $X_k^+$  and  $X_k^-$  are

the predictions using the upwards and downwards variation of each eigenvector  $k$ .

$$\Delta X^+ = \sqrt{\sum_{k=1}^{N_{\text{ev}}} [\max(X_k^+ - X^0, X_k^- - X^0, 0)]^2} \quad (2.4)$$

$$\Delta X^- = \sqrt{\sum_{k=1}^{N_{\text{ev}}} [\min(X_k^+ - X^0, X_k^- - X^0, 0)]^2}$$

The symmetric uncertainty ( $\Delta X^\pm$ ) is given by half the difference of the upwards and downwards variations :

$$\Delta X^\pm = \sqrt{\sum_{k=1}^{N_{\text{ev}}} \left[ \frac{X_k^+ - X_k^-}{2} \right]^2} \quad (2.5)$$

6 The CT10 uncertainties are downscaled by a factor of 1.64 in order to have the uncertainties at the 68.3% confidence level CL( $1\sigma$ ) instead of 90% CL( $2\sigma$ ). The PDF uncertainty as derived with the CT10 PDF set is the dominant source of uncertainty and ranges from 3% to 30% for inclusive 2-jet and from 4% to 32% for 3-jet cross sections. For  $R_{32}$ , the ratio of predictions for inclusive 3-jet to that of 2-jet is taken for each eigen vector with upwards and downwards variations separately and then PDF uncertainty is calculated as done for individual cross sections. The PDF uncertainty ranges and from 2% to 10% for cross section ratio  $R_{32}$ .

### 2.2.3 Non-perturbative Uncertainty

As discussed in 2.1.2, the differences in the non-perturbative (NP) corrections calculated from different Monte Carlo event generators introduce the NP uncertainty which is of the order of 1% and 1 to 2% for inclusive 2-jet and 3-jet events cross sections respectively, and < 1% for cross section ratio  $R_{32}$ .

### 2.2.4 Total Theoretical Uncertainty

The total systematic theoretical uncertainties are evaluated as the quadratic sum of the scale, PDF and NP uncertainties. Figure 2.4 presents the systematic theoretical uncertainties affecting the cross section measurement for inclusive 2-jet (top left) and 3-jet events (top right) and the cross section ratio  $R_{32}$  (bottom), using CT10 PDF set. The scale (red dashed line), PDF (green line) and NP (blue dashed line) uncertainties as well as total theoretical uncertainty (black dashed line) are shown. The total theoretical uncertainty is asymmetric and is dominated by PDF uncertainty. Table 2.2 quotes the values of the theoretical uncertainty from each source as well as total uncertainty affecting the measurements. The bin-wise values of uncertainties (in %) from each source as well as total uncertainty are shown in Tables A.5, A.6 and A.7 for  $n_j \geq 2$  and  $n_j \geq 3$  events cross sections and cross section ratio  $R_{32}$ , respectively. The computation of the NLO predictions with NLOJET++ is also subject to statistical fluctuations from the complex numerical integrations. For the inclusive 2-jet event cross sections this uncertainty is smaller than about a per mille, while for the inclusive 3-jet event cross section it amounts to 1-9 per mille. Hence the statistical uncertainty is not considered in the total theoretical uncertainty.

Table 2.2: Overview of all systematic theoretical uncertainties obtained using CT10-NLO PDF set, affecting the measurement of cross sections for inclusive 2-jet (left) and inclusive 3-jet events (middle) and cross section ratio  $R_{32}$  (right).

Uncertainty Source	Inclusive 2-jet	Inclusive 3-jet	$R_{32}$
Scale	5 to 13%	11 to 17%	6 to 8%
PDF	3 to 30%	4 to 32%	2 to 10%
Non-perturbative (NP)	1%	1 to 2%	< 1%
Total	3 to 30%	5 to 34%	3 to 11%

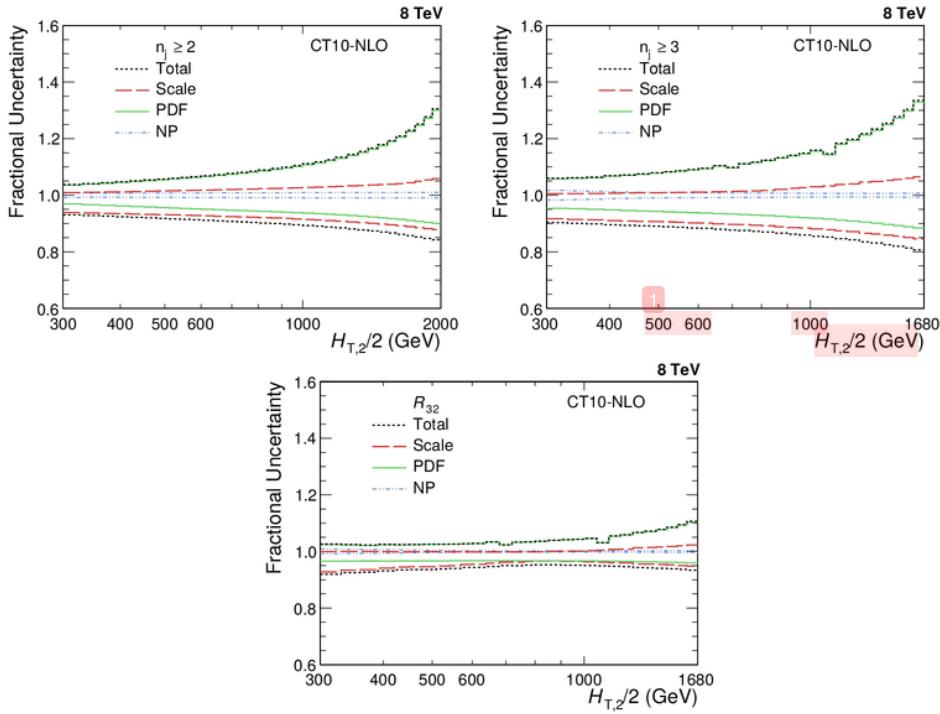


Figure 2.4: The systematic theoretical uncertainties affecting the cross section measurement for inclusive 2-jet (top left) and 3-jet events (top right) and their ratio  $R_{32}$  (bottom). The scale (red dashed line), PDF (green line) and NP (blue dashed line) uncertainties as well as total uncertainty (black dashed line) obtained using CT10-NLO PDF set are shown. The total theoretical uncertainty is asymmetric and is dominated by PDF uncertainty.

## 2.3 Comparison of theory to data

After correcting the measurement for detector effects as well as NLO pQCD calculations for non-perturbative (NP) and electroweak (EW) effects, it is now possible to compare the measured cross sections with the theory predictions. Figure 2.5 shows the measured differential inclusive 2-jet and 3-jet event cross sections as a function of  $H_{T,2}/2$  after unfolding for detector effects. On the left, the measurements (points) are compared to the NLOJET++ predictions using the CT10 PDF set (line), corrected for NP effects and in addition for EW effects in the 2-jet case. On the right, the comparison is made to the predictions from MADGRAPH5+PYTHIA6 (MG+P6)

with tune Z2<sup>\*</sup> (line), corrected for EW effects in the 2-jet case. The error bars [7] correspond to the total experimental uncertainty, for which the statistical and systematic uncertainties are added in quadrature. On a logarithmic scale, the data are [22] in agreement with the NLO predictions over the whole range of  $H_{T,2}/2$  from 300 GeV up to 2000 (2-jet) and 1680 GeV (3-jet) respectively.

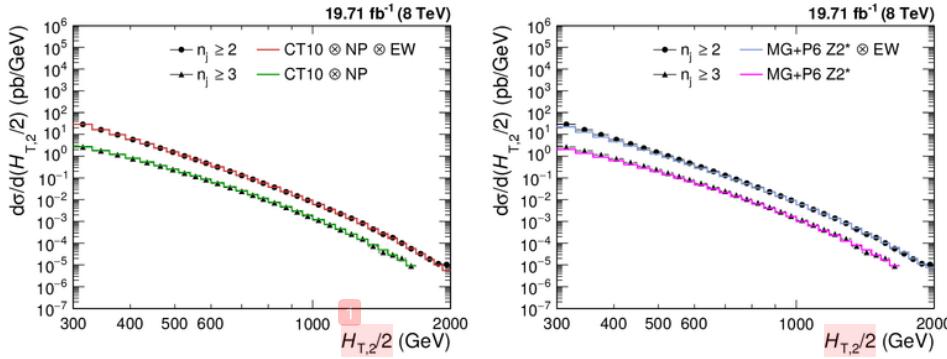


Figure 2.5: Comparison of the measured differential inclusive 2-jet and 3-jet event cross sections as a function of  $H_{T,2}/2$  to theoretical predictions. On the left, the data (points) are shown together with NLOJET++ predictions (line) using the CT10 PDF set, corrected for non-perturbative (NP) and electroweak (EW) effects (2-jet) or only NP effects (3-jet). On the right, the data (points) are compared to predictions from MADGRAPH5+PYTHIA6 (MG+P6) with tune Z2<sup>\*</sup> (line), corrected for EW effects in the 2-jet case. The error bars correspond to the total experimental uncertainty, for which the statistical and systematic uncertainties are added in quadrature.

Figure 2.6 presents the cross section ratio  $R_{32}$  as obtained from unfolded data [32] data (solid circles) in comparison to that from NLO pQCD predictions [4] obtained using the CT10 NLO PDF set corrected with NP corrections (line). The error bars [3] here correspond to the total experimental uncertainty derived as quadratic sum from all uncertainty sources. The deviations of measured  $R_{32}$  from the theoretical predicted value can be explained by the electroweak effects which are not considered yet because of their unavailability for inclusive 3-jet events cross sections.

For better visibility, the ratios of data over the theory at NLO are also studied [6] in details. In Fig. 2.7, the ratios of data over NLOJET++ predictions using the [2] CT10 PDF set are shown for inclusive 2-jet (top left) and 3-jet event cross sections [1].

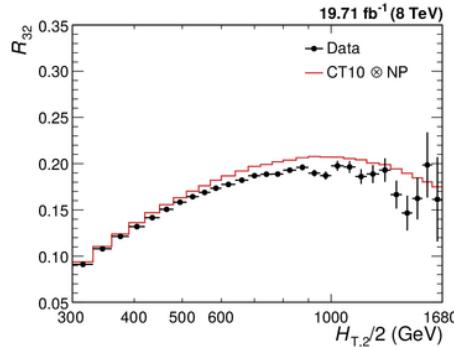


Figure 2.6: Cross section ratio  $R_{32}$  as a function of  $H_{T,2}/2$  calculated from data (solid circles) in comparison to that from NLO pQCD predictions obtained using the CT10 NLO PDF set corrected with non-perturbative (NP) corrections (line). The error bars correspond to the total experimental uncertainty derived as quadratic sum from all uncertainty sources.

(top right) as well as their ratio  $R_{32}$  (bottom). The data are well described by the predictions within their uncertainty, which is dominated at large  $H_{T,2}/2$  by PDF effects in the upwards and by scale variations in the downwards direction. A trend towards an increasing systematic excess of the 2-jet data with respect to theory, starting at about 1 TeV in  $H_{T,2}/2$ , is remedied by the inclusion of EWK corrections. In the 3-jet case the statistical precision of the data and the reach in  $H_{T,2}/2$  is insufficient to observe any effect. The alternative PDF sets MSTW2008 and NNPDF2.3 exhibit a small underestimation of the cross sections at high  $H_{T,2}/2$ .

The POWHEG framework providing a NLO dijet calculation matched to the parton showers of PYTHIA8 employed with the CUETS1 and CUETM1 tunes [41] is also used for a comparison. The ratios of data over theory from POWHEG+PYTHIA8 with tune CUETS1 are shown for inclusive 2-jet (top left) and 3-jet event cross sections (top right) as well as their ratio  $R_{32}$  (bottom) in Fig. 2.8. For comparison, the LO prediction from PYTHIA6 with tune Z2\*, the tree-level multi-leg improved prediction by MADGRAPH5+PYTHIA6 with tune Z2\*, and the matched NLO prediction from POWHEG+PYTHIA8 with tune CUETM1 are shown as well. EW corrections have been accounted for in this comparison in the 2-jet case only. Significant dis-

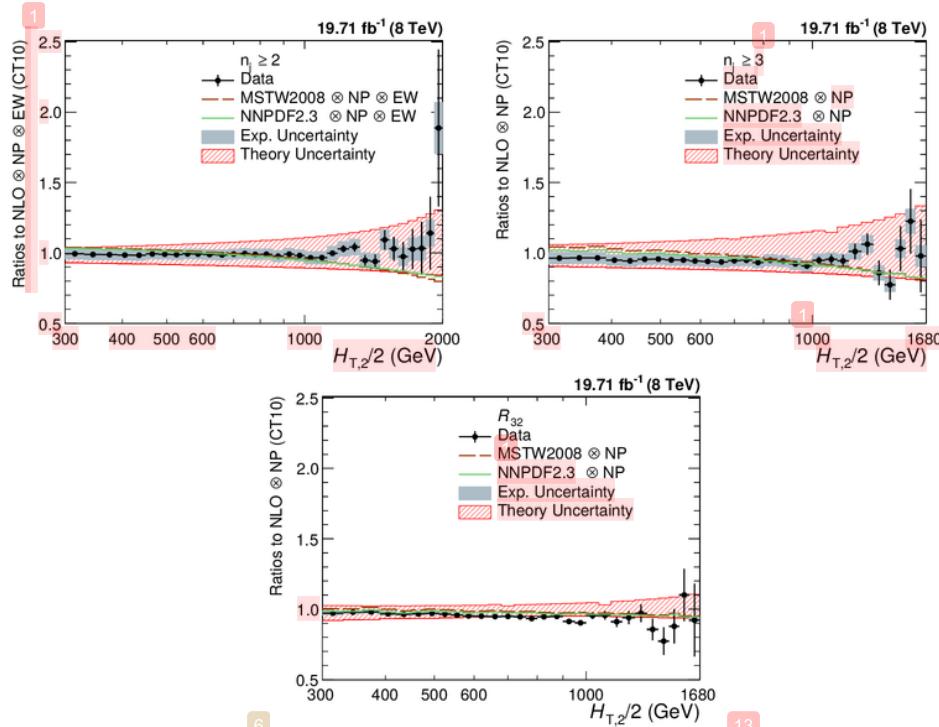


Figure 2.7: Ratio of data over theory using the CT10 PDF set for inclusive 2-jet (top left) and inclusive 3-jet event cross sections (top right) and their ratio  $R_{32}$  (bottom). For comparison predictions employing two other PDF sets, MSTW2008 and NNPDF2.3, are also shown. The error bars correspond to the statistical uncertainty of the data and the shaded rectangles to the total experimental systematic uncertainty. The shaded band around unity represents the total uncertainty of the theory.

crepancies, which are cancelled to a large extent in the ratio  $R_{32}$ , are visible in the comparison with the LO prediction from MADGRAPH5+PYTHIA6 with tune Z2\*, in particular for small  $H_{T,2}/2$ . In contrast, the employed dijet MC POWHEG+PYTHIA8 better describe the 2-jet event cross section, but fail for the 3-jet case.

The jet measurements at hadron colliders can be used to determine the strong coupling constant  $\alpha_S$ , which are discussed in the next chapter.

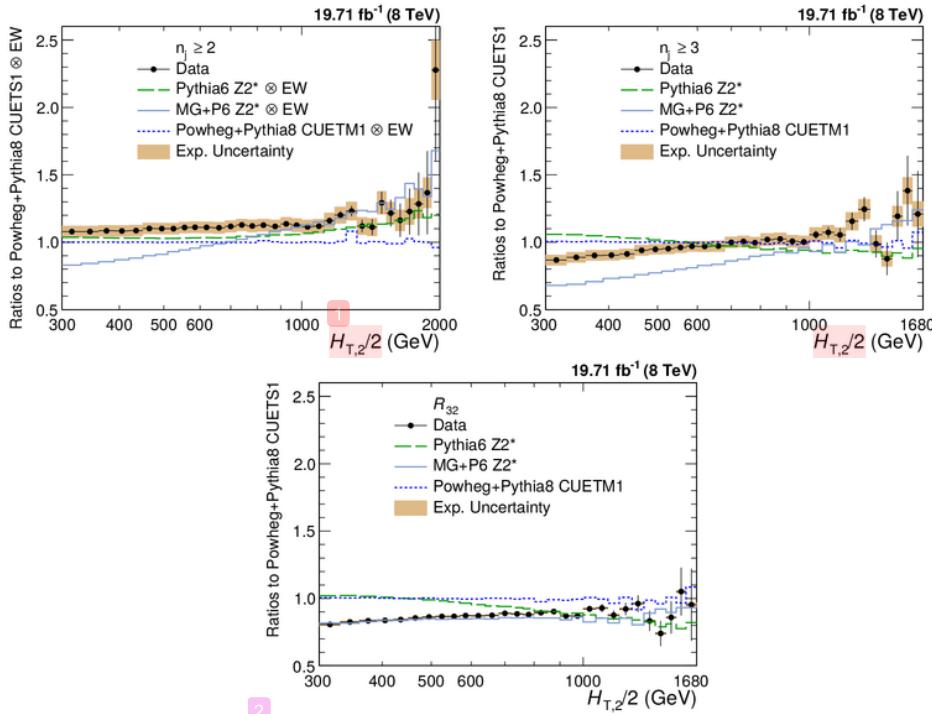


Figure 2.8: Ratio of data over the prediction from POWHEG+PYTHIA8 with tune CUETS1 are presented for inclusive 2-jet (top left) and 3-jet event cross sections (top right) as well as their ratio  $R_{32}$  (bottom). For comparison the alternative tune CUETM1 of POWHEG+PYTHIA8, the tree-level multi-leg improved prediction by MADGRAPH5+PYTHIA6 with tune  $Z2^*$ , and the the LO MC predictions from PYTHIA6 tune  $Z2^*$  are shown as well. The error bars correspond to the statistical uncertainty of the data and the shaded rectangles to the total experimental systematic uncertainty. EW corrections have been accounted for in this comparison in the 2-jet case only.



## **Appendix A**

## A.1 Cross Section Ratio, $R_{32}$

Table A.1: Differential cross sections and cross section ratio at detector level in each bin of  $H_{T,2}/2$ , along with statistical uncertainty (in %).

Bin	2-jet x-section (x $10^{-3}$ (pb/GeV))	Stat. unc.	3-jet x-section (x $10^{-3}$ (pb/GeV))	Stat. unc.	Ratio $R_{32}$	Stat. unc.
300 - 330	29772.726	0.211	2640.629	0.707	0.089	+0.665 -0.661
330 - 360	16792.917	0.231	1773.485	0.704	0.106	+0.523 -0.521
360 - 390	9889.326	0.182	1176.544	0.526	0.119	+0.485 -0.483
390 - 420	5976.777	0.179	778.034	0.492	0.130	+0.206 -0.206
420 - 450	3731.760	0.067	522.624	0.180	0.140	+0.167 -0.167
450 - 480	2398.741	0.084	357.622	0.217	0.149	+0.201 -0.200
480 - 510	1570.192	0.104	246.051	0.262	0.157	+0.241 -0.241
510 - 540	1048.665	0.127	171.080	0.314	0.163	+0.288 -0.287
540 - 570	713.042	0.154	119.566	0.376	0.168	+0.344 -0.343
570 - 600	490.776	0.186	84.798	0.447	0.173	+0.407 -0.406
600 - 640	325.046	0.198	57.463	0.470	0.177	+0.427 -0.426
640 - 680	205.727	0.248	37.282	0.583	0.181	+0.529 -0.527
680 - 720	133.674	0.308	24.859	0.714	0.186	+0.646 -0.643
720 - 760	87.911	0.380	16.560	0.875	0.188	+0.791 -0.786
760 - 800	58.657	0.465	11.056	1.071	0.188	+0.968 -0.961
800 - 850	38.106	0.516	7.318	1.178	0.192	+1.063 -1.054
850 - 900	23.587	0.656	4.600	1.485	0.195	+1.339 -1.326
900 - 950	15.130	0.819	2.896	1.872	0.191	+1.694 -1.672
950 - 1000	9.696	1.023	1.812	2.366	0.187	+2.151 -2.116
1000 - 1060	6.026	1.185	1.186	2.670	0.197	+2.414 -2.371
1060 - 1120	3.668	1.518	0.716	3.436	0.195	+3.118 -3.046
1120 - 1180	2.327	1.906	0.437	4.398	0.188	+4.024 -3.903
1180 - 1250	1.419	2.260	0.265	5.227	0.187	+4.798 -4.627
1250 - 1320	0.853	2.915	0.165	6.623	0.194	+6.080 -5.811
1320 - 1390	0.477	3.898	0.080	9.492	0.169	+8.951 -8.355
1390 - 1460	0.263	5.249	0.042	13.131	0.160	+12.619 -11.449
1460 - 1530	0.192	6.143	0.029	15.811	0.151	+15.437 -13.698
1530 - 1600	0.104	8.362	0.021	18.570	0.203	+17.571 -15.536
1600 - 1680	0.060	10.314	0.009	26.726	0.149	+27.132 -22.170

## A.2 Individual Sources of Jet Energy Correction Uncertainties

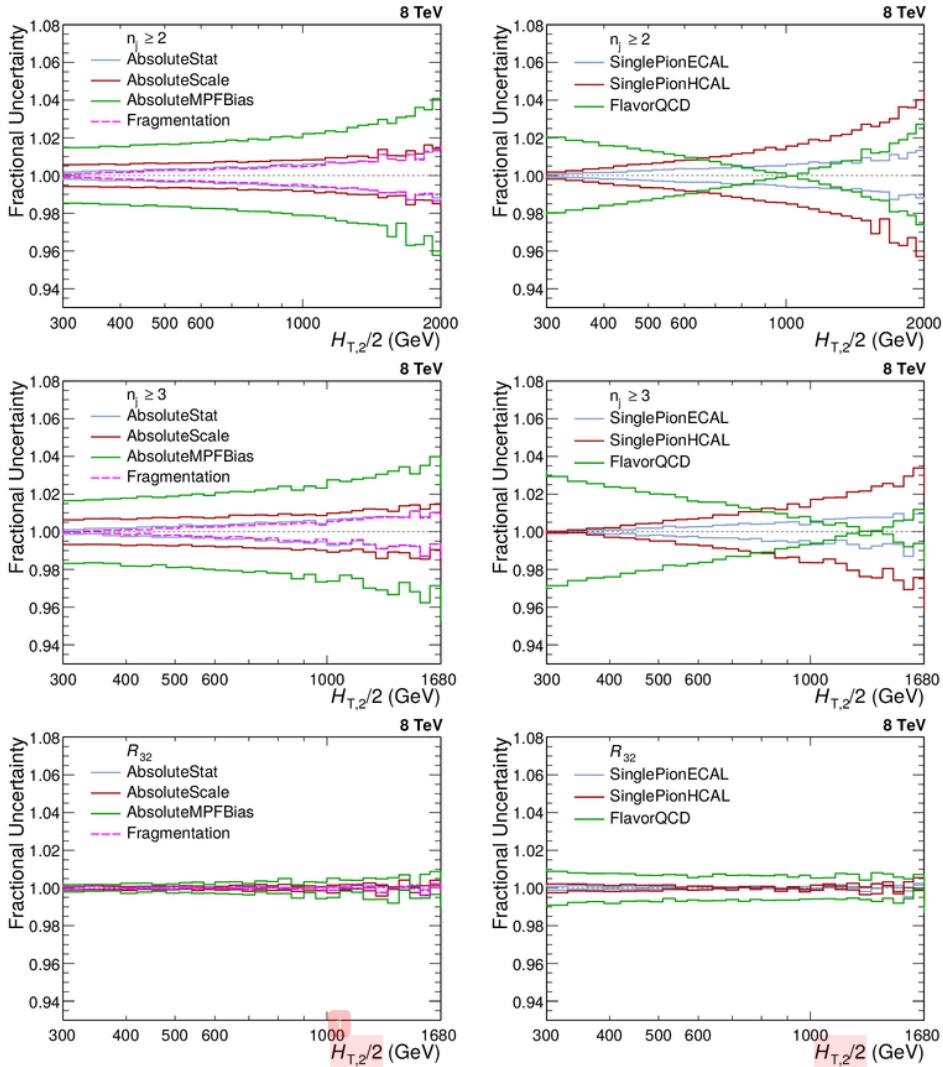


Figure A.1: The fractional jet energy correction (JEC) uncertainties from individual sources are shown for inclusive 2-jet (top) and 3-jet events (middle); and cross section ratio  $R_{32}$  (bottom). On left, JEC uncertainties are evaluated from AbsoluteStat (blue), AbsoluteScale (red), AbsoluteMPFBias (green) and Fragmentation (pink) sources whereas on right, these are evaluated from SinglePionECAL (blue), SinglePionHCAL (red) and FlavorQCD (green) sources.

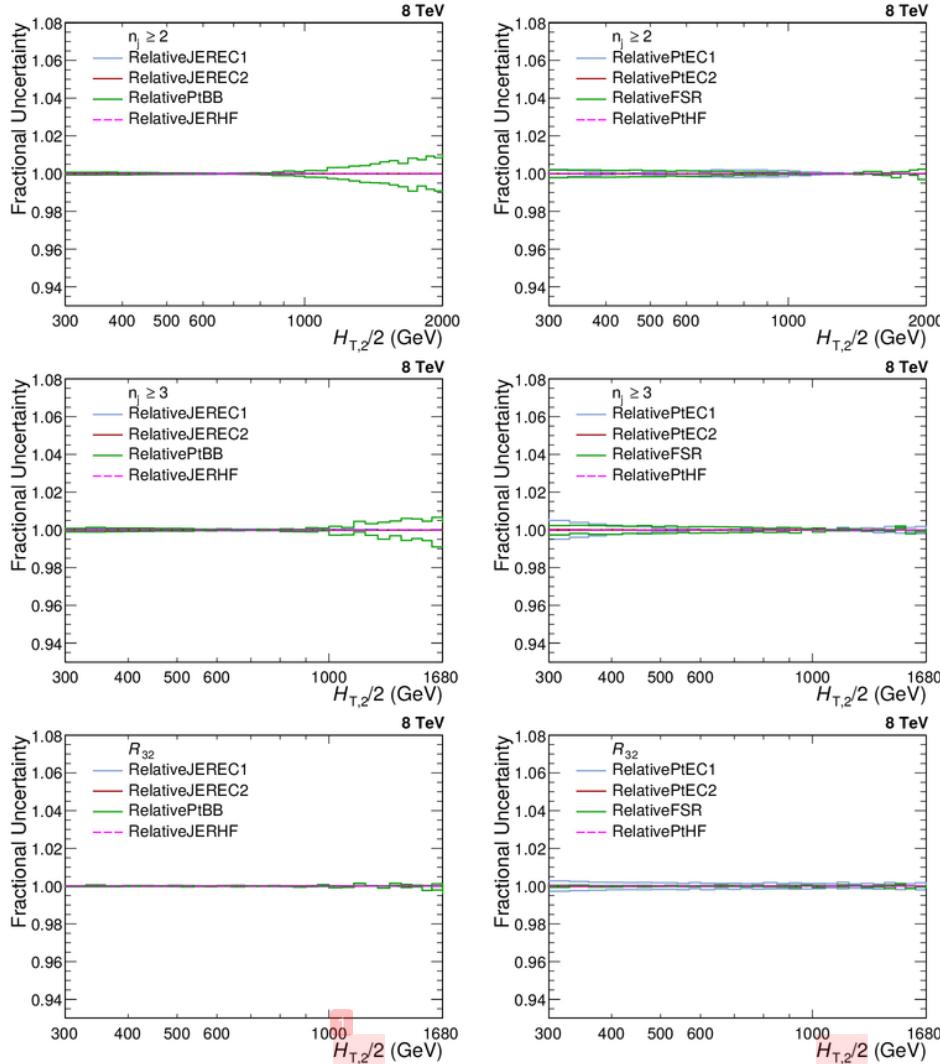


Figure A.2: The fractional jet energy correction (JEC) uncertainties from individual sources are shown for inclusive 2-jet (top) and 3-jet events cross sections (middle); and cross section ratio  $R_{32}$  (bottom). On left, JEC uncertainties are evaluated from RelativeJEREC1 (blue), RelativeJEREC2 (red), RelativePtBB (green) and RelativeJERHF (pink) sources whereas on right, these are evaluated from RelativePtEC1 (blue), RelativePtEC2 (red), RelativePFSR (green) and RelativePtHF (pink) sources.

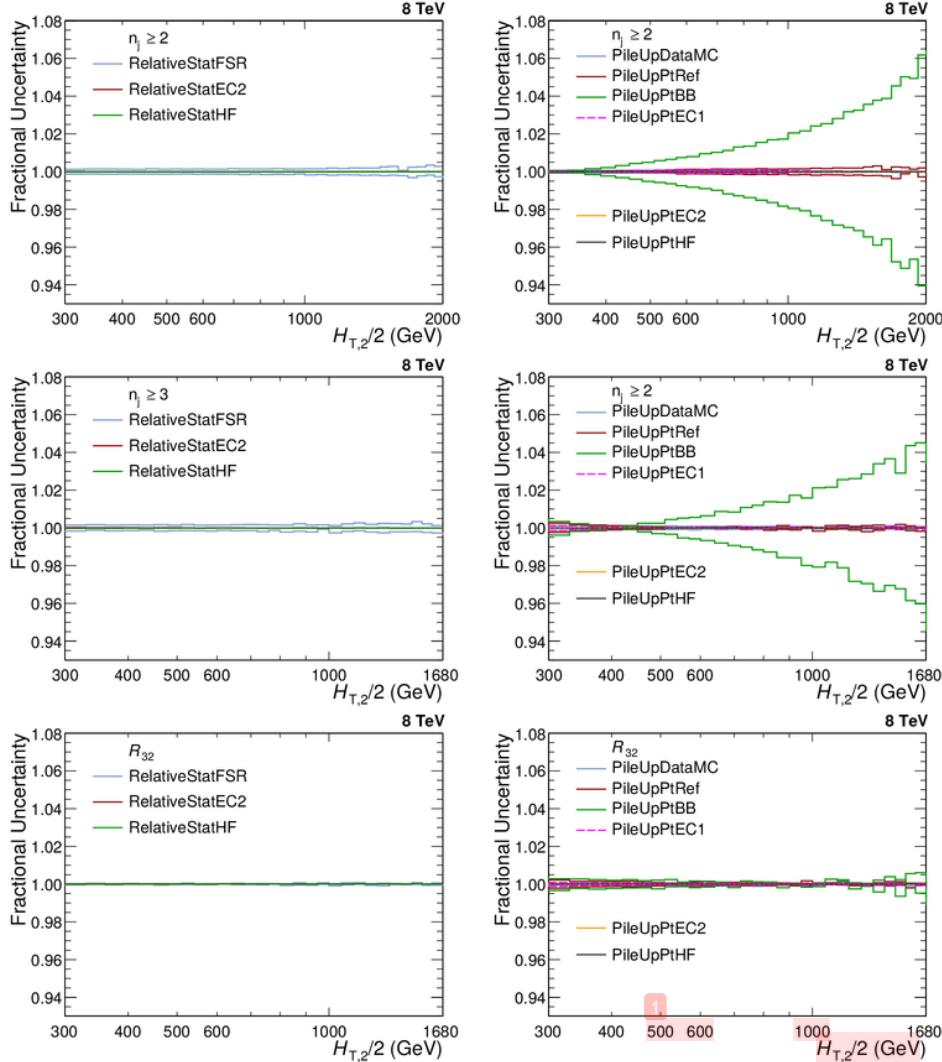


Figure A.3: The fractional jet energy correction (JEC) uncertainties from individual sources are shown for inclusive 2-jet (top) and 3-jet events (middle); and cross section ratio  $R_{32}$  (bottom). On left, JEC uncertainties are evaluated from RelativeStatFSR (blue), RelativeStatEC2 (red) and RelativeStatHF (green) sources whereas on right, these are evaluated from PileUpDataMC (blue), PileUpPtRef (red), PileUpPtBB (green), PileUpPtEC1 (pink), PileUpPtEC2 (orange) and PileUpPtHF (black) sources.

### A.3 Experimental Uncertainties

Table A.2: Experimental uncertainties (in %), from all sources as well as the total uncertainty, affecting the cross section measurement in each bin of  $H_{\text{T},2}/2$  for inclusive 2-jet events.

Bin	Statistical	JEC	Unfolding	Lumi	Residual	Total
300 - 330	0.242	+2.612 -2.565	+0.948 -0.928	2.6	1.0	+3.942 -3.906
330 - 360	0.258	+2.507 -2.473	+0.976 -0.969	2.6	1.0	+3.882 -3.858
360 - 390	0.202	+2.504 -2.465	+0.779 -0.783	2.6	1.0	+3.831 -3.807
390 - 420	0.193	+2.363 -2.381	+0.905 -0.904	2.6	1.0	+3.768 -3.780
420 - 450	0.084	+2.448 -2.422	+0.904 -0.895	2.6	1.0	+3.818 -3.799
450 - 480	0.096	+2.440 -2.352	+0.797 -0.795	2.6	1.0	+3.789 -3.733
480 - 510	0.107	+2.427 -2.406	+0.728 -0.715	2.6	1.0	+3.767 -3.751
510 - 540	0.128	+2.425 -2.395	+0.835 -0.862	2.6	1.0	+3.789 -3.775
540 - 570	0.154	+2.425 -2.376	+0.687 -0.674	2.6	1.0	+3.760 -3.726
570 - 600	0.180	+2.497 -2.474	+0.839 -0.827	2.6	1.0	+3.838 -3.820
600 - 640	0.209	+2.495 -2.491	+0.744 -0.743	2.6	1.0	+3.819 -3.816
640 - 680	0.264	+2.582 -2.545	+0.912 -0.912	2.6	1.0	+3.915 -3.891
680 - 720	0.320	+2.691 -2.574	+0.763 -0.756	2.6	1.0	+3.961 -3.880
720 - 760	0.387	+2.690 -2.755	+0.705 -0.712	2.6	1.0	+3.955 -4.001
760 - 800	0.465	+2.858 -2.846	+0.859 -0.846	2.6	1.0	+4.109 -4.098
800 - 850	0.548	+2.889 -2.913	+0.783 -0.787	2.6	1.0	+4.126 -4.143
850 - 900	0.698	+3.145 -3.102	+0.961 -0.958	2.6	1.0	+4.366 -4.334
900 - 950	0.847	+3.298 -3.233	+0.828 -0.829	2.6	1.0	+4.476 -4.429
950 - 1000	1.041	+3.291 -3.330	+0.895 -0.872	2.6	1.0	+4.525 -4.549
1000 - 1060	1.268	+3.598 -3.569	+0.945 -0.956	2.6	1.0	+4.817 -4.798
1060 - 1120	1.611	+3.759 -3.756	+0.970 -0.967	2.6	1.0	+5.043 -5.040
1120 - 1180	1.985	+4.154 -4.053	+1.089 -1.080	2.6	1.0	+5.490 -5.413
1180 - 1250	2.406	+4.251 -4.313	+1.062 -1.070	2.6	1.0	+5.722 -5.770
1250 - 1320	3.101	+4.696 -4.624	+1.151 -1.144	2.6	1.0	+6.384 -6.330
1320 - 1390	4.157	+4.934 -4.979	+1.343 -1.341	2.6	1.0	+7.155 -7.186
1390 - 1460	5.270	+5.148 -5.104	+1.185 -1.177	2.6	1.0	+7.965 -7.936
1460 - 1530	6.360	+5.890 -5.652	+1.405 -1.406	2.6	1.0	+9.213 -9.063
1530 - 1600	8.183	+5.924 -6.311	+1.598 -1.590	2.6	1.0	+10.601 -10.821
1600 - 1680	10.630	+5.969 -5.655	+1.607 -1.592	2.6	1.0	+12.608 -12.461
1680 - 1760	13.864	+7.245 -7.603	+1.821 -1.839	2.6	1.0	+15.993 -16.161
1760 - 1840	18.192	+7.781 -7.820	+1.902 -1.906	2.6	1.0	+20.071 -20.087
1840 - 1920	22.612	+7.647 -7.537	+1.588 -1.590	2.6	1.0	+24.085 -24.050
1920 - 2000	29.530	+9.199 -9.469	+1.511 -1.505	2.6	1.0	+31.092 -31.172

Table A.3: Experimental uncertainties (in %), from all sources as well as the total uncertainty, affecting the cross section measurement in each bin of  $H_{\mathrm{T},2}/2$  for inclusive 3-jet events.

Bin	Statistical	JEC	Unfolding	Lumi	Residual	Total
300 - 330	0.796	+3.503 -3.475	+0.564 -0.552	2.6	1.0	+4.581 -4.558
330 - 360	0.781	+3.303 -3.186	+0.640 -0.633	2.6	1.0	+4.437 -4.350
360 - 390	0.583	+3.221 -3.094	+0.490 -0.496	2.6	1.0	+4.326 -4.233
390 - 420	0.531	+3.092 -3.149	+0.584 -0.584	2.6	1.0	+4.236 -4.278
420 - 450	0.224	+3.125 -2.996	+0.604 -0.592	2.6	1.0	+4.236 -4.140
450 - 480	0.248	+2.984 -2.890	+0.531 -0.528	2.6	1.0	+4.124 -4.056
480 - 510	0.269	+2.937 -2.963	+0.511 -0.512	2.6	1.0	+4.089 -4.108
510 - 540	0.318	+3.021 -2.797	+0.592 -0.612	2.6	1.0	+4.164 -4.007
540 - 570	0.375	+2.999 -2.935	+0.506 -0.500	2.6	1.0	+4.141 -4.094
570 - 600	0.434	+2.824 -2.906	+0.646 -0.620	2.6	1.0	+4.042 -4.096
600 - 640	0.497	+2.952 -2.956	+0.598 -0.604	2.6	1.0	+4.133 -4.136
640 - 680	0.617	+3.111 -3.001	+0.777 -0.786	2.6	1.0	+4.292 -4.215
680 - 720	0.739	+3.067 -2.984	+0.642 -0.611	2.6	1.0	+4.257 -4.194
720 - 760	0.895	+3.185 -3.111	+0.595 -0.607	2.6	1.0	+4.366 -4.313
760 - 800	1.068	+3.231 -3.166	+0.763 -0.774	2.6	1.0	+4.464 -4.419
800 - 850	1.250	+3.427 -3.295	+0.674 -0.687	2.6	1.0	+4.639 -4.544
850 - 900	1.578	+3.364 -3.540	+0.903 -0.898	2.6	1.0	+4.731 -4.857
900 - 950	1.961	+3.594 -3.524	+0.792 -0.793	2.6	1.0	+5.015 -4.965
950 - 1000	2.420	+3.603 -3.783	+0.846 -0.843	2.6	1.0	+5.226 -5.351
1000 - 1060	2.844	+4.164 -4.116	+0.916 -0.940	2.6	1.0	+5.834 -5.803
1060 - 1120	3.647	+4.038 -3.815	+0.963 -0.957	2.6	1.0	+6.188 -6.044
1120 - 1180	4.607	+4.278 -4.183	+1.084 -1.087	2.6	1.0	+6.961 -6.904
1180 - 1250	5.532	+4.894 -4.771	+1.074 -1.069	2.6	1.0	+7.967 -7.891
1250 - 1320	7.141	+5.144 -5.273	+1.222 -1.217	2.6	1.0	+9.312 -9.383
1320 - 1390	10.207	+5.542 -5.642	+1.414 -1.428	2.6	1.0	+12.027 -12.076
1390 - 1460	13.831	+5.630 -5.265	+1.257 -1.256	2.6	1.0	+15.242 -15.111
1460 - 1530	15.578	+5.576 -5.491	+1.546 -1.551	2.6	1.0	+16.850 -16.822
1530 - 1600	18.729	+6.409 -7.019	+1.718 -1.716	2.6	1.0	+20.063 -20.266
1600 - 1680	26.465	+7.017 -6.255	+1.775 -1.765	2.6	1.0	+27.578 -27.393

Table A.4: Experimental uncertainties (in %), from all sources as well as the total uncertainty, affecting the measurement of cross section ratio  $R_{32}$ , in each bin of  $H_{T,2}/2$ .

Bin	Statistical	JEC	Unfolding	Total
300 - 330	0.741	+1.059 -1.097	+0.754 -0.751	+1.496 -1.522
330 - 360	0.587	+0.954 -0.923	+0.685 -0.689	+1.313 -1.292
360 - 390	0.519	+0.902 -0.855	+0.594 -0.593	+1.199 -1.163
390 - 420	0.236	+0.907 -0.952	+0.439 -0.438	+1.035 -1.074
420 - 450	0.192	+0.900 -0.835	+0.360 -0.361	+0.988 -0.930
450 - 480	0.209	+0.788 -0.802	+0.307 -0.308	+0.872 -0.884
480 - 510	0.245	+0.795 -0.867	+0.254 -0.235	+0.870 -0.931
510 - 540	0.287	+0.852 -0.682	+0.264 -0.268	+0.937 -0.787
540 - 570	0.326	+0.807 -0.803	+0.193 -0.189	+0.891 -0.887
570 - 600	0.397	+0.656 -0.774	+0.199 -0.219	+0.792 -0.898
600 - 640	0.447	+0.763 -0.797	+0.150 -0.154	+0.897 -0.926
640 - 680	0.573	+0.861 -0.781	+0.153 -0.140	+1.045 -0.979
680 - 720	0.663	+0.766 -0.787	+0.147 -0.164	+1.024 -1.042
720 - 760	0.774	+0.842 -0.769	+0.118 -0.118	+1.149 -1.097
760 - 800	0.970	+0.800 -0.729	+0.115 -0.096	+1.263 -1.218
800 - 850	1.116	+0.873 -0.775	+0.115 -0.104	+1.422 -1.363
850 - 900	1.436	+0.770 -0.896	+0.069 -0.069	+1.631 -1.694
900 - 950	1.716	+0.704 -0.752	+0.050 -0.051	+1.855 -1.874
950 - 1000	2.156	+0.824 -0.897	+0.089 -0.045	+2.310 -2.336
1000 - 1060	2.554	+0.812 -0.870	+0.045 -0.040	+2.680 -2.698
1060 - 1120	3.244	+0.792 -0.658	+0.018 -0.027	+3.339 -3.310
1120 - 1180	4.121	+0.985 -0.757	+0.025 -0.043	+4.237 -4.191
1180 - 1250	4.990	+1.031 -0.848	+0.023 -0.041	+5.095 -5.062
1250 - 1320	6.456	+0.750 -1.087	+0.079 -0.079	+6.500 -6.548
1320 - 1390	8.990	+1.112 -1.144	+0.080 -0.099	+9.059 -9.063
1390 - 1460	12.699	+1.157 -0.815	+0.076 -0.078	+12.751 -12.725
1460 - 1530	13.926	+0.768 -1.235	+0.143 -0.145	+13.948 -13.981
1530 - 1600	16.903	+1.050 -1.258	+0.120 -0.127	+16.936 -16.950
1600 - 1680	28.070	+1.471 -0.859	+0.178 -0.177	+28.109 -28.084

## A.4 Theoretical Uncertainties

Table A.5: Theoretical uncertainties (in %) calculating using CT10-NLO PDF set from all sources as well as the total uncertainty, affecting the cross section measurement in each bin of  $H_{T,2}/2$  for inclusive 2-jet events.

Bin	Scale	PDF	NP	Total
300 - 330	+0.942 -6.149	+3.566 -3.090	0.825	+3.780 -6.931
330 - 360	+1.035 -6.289	+3.906 -3.342	0.736	+4.107 -7.159
360 - 390	+1.159 -6.438	+4.232 -3.573	0.696	+4.442 -7.396
390 - 420	+1.220 -6.536	+4.551 -3.794	0.723	+4.767 -7.592
420 - 450	+1.326 -6.660	+4.857 -3.997	0.745	+5.089 -7.802
450 - 480	+1.421 -6.776	+5.153 -4.186	0.765	+5.399 -8.001
480 - 510	+1.512 -6.888	+5.444 -4.365	0.782	+5.704 -8.192
510 - 540	+1.566 -6.967	+5.721 -4.527	0.797	+5.984 -8.347
540 - 570	+1.666 -7.082	+6.000 -4.682	0.810	+6.279 -8.528
570 - 600	+1.731 -7.172	+6.269 -4.825	0.822	+6.555 -8.683
600 - 640	+1.805 -7.271	+6.597 -4.979	0.833	+6.890 -8.852
640 - 680	+1.930 -7.416	+6.978 -5.143	0.845	+7.289 -9.064
680 - 720	+2.007 -7.527	+7.364 -5.295	0.856	+7.680 -9.243
720 - 760	+2.113 -7.663	+7.749 -5.437	0.865	+8.078 -9.436
760 - 800	+2.196 -7.781	+8.140 -5.569	0.873	+8.476 -9.609
800 - 850	+2.323 -7.945	+8.573 -5.706	0.881	+8.926 -9.822
850 - 900	+2.389 -8.062	+9.082 -5.863	0.889	+9.433 -10.008
900 - 950	+2.499 -8.227	+9.600 -6.018	0.896	+9.961 -10.232
950 - 1000	+2.631 -8.402	+10.134 -6.166	0.902	+10.509 -10.460
1000 - 1060	+2.738 -8.569	+10.747 -6.343	0.908	+11.127 -10.700
1060 - 1120	+2.853 -8.751	+11.431 -6.526	0.914	+11.817 -10.955
1120 - 1180	+2.992 -8.970	+12.183 -6.727	0.919	+12.579 -11.250
1180 - 1250	+3.135 -9.194	+13.019 -6.944	0.924	+13.423 -11.558
1250 - 1320	+3.324 -9.469	+14.004 -7.189	0.929	+14.423 -11.925
1320 - 1390	+3.434 -9.677	+15.080 -7.444	0.933	+15.494 -12.244
1390 - 1460	+3.629 -9.976	+16.223 -7.700	0.937	+16.650 -12.637
1460 - 1530	+3.760 -10.224	+17.505 -7.980	0.940	+17.929 -13.004
1530 - 1600	+3.894 -10.471	+18.891 -8.258	0.943	+19.311 -13.368
1600 - 1680	+4.107 -10.813	+20.496 -8.560	0.946	+20.925 -13.824
1680 - 1760	+4.421 -11.101	+22.481 -8.905	0.949	+22.931 -14.263
1760 - 1840	+4.921 -11.461	+24.654 -9.251	0.951	+25.158 -14.760
1840 - 1920	+5.404 -11.813	+27.143 -9.607	0.953	+27.692 -15.256
1920 - 2000	+5.867 -12.154	+29.986 -9.973	0.955	+30.570 -15.751

Table A.6: Theoretical uncertainties (in %) calculating using CT10-NLO PDF set from all sources as well as the total uncertainty, affecting the cross section measurement in each bin of  $H_{T,2}/2$  for inclusive 3-jet events.

Bin	Scale	PDF	NP	Total
300 - 330	+0.539 -8.294	+5.716 -4.657	1.692	+5.986 -9.662
330 - 360	+0.550 -8.577	+5.977 -4.779	1.516	+6.191 -9.935
360 - 390	+0.599 -8.709	+6.187 -4.987	1.363	+6.363 -10.128
390 - 420	+0.719 -8.948	+6.751 -5.223	1.228	+6.900 -10.433
420 - 450	+0.799 -9.145	+7.031 -5.395	1.110	+7.162 -10.676
450 - 480	+0.847 -9.247	+7.404 -5.578	1.005	+7.520 -10.845
480 - 510	+0.847 -9.294	+7.837 -5.717	0.937	+7.938 -10.951
510 - 540	+0.922 -9.436	+8.198 -5.884	0.921	+8.301 -11.158
540 - 570	+0.974 -9.566	+8.529 -6.000	0.904	+8.632 -11.328
570 - 600	+1.086 -9.786	+8.970 -6.156	0.886	+9.079 -11.595
600 - 640	+1.107 -9.852	+9.402 -6.297	0.866	+9.506 -11.724
640 - 680	+1.278 -10.101	+10.310 -6.526	0.842	+10.423 -12.055
680 - 720	+1.384 -10.342	+9.682 -6.618	0.820	+9.815 -12.305
720 - 760	+1.415 -10.404	+11.051 -6.826	0.798	+11.170 -12.469
760 - 800	+1.547 -10.615	+11.565 -7.009	0.777	+11.694 -12.744
800 - 850	+1.679 -10.804	+12.242 -7.185	0.755	+12.379 -12.997
850 - 900	+2.085 -11.134	+13.097 -7.461	0.731	+13.282 -13.422
900 - 950	+2.475 -11.432	+13.889 -7.703	0.709	+14.125 -13.804
950 - 1000	+2.655 -11.608	+14.614 -7.915	0.688	+14.869 -14.066
1000 - 1060	+3.025 -11.926	+15.576 -8.173	0.667	+15.881 -14.473
1060 - 1120	+3.299 -12.189	+14.250 -8.441	0.645	+14.641 -14.840
1120 - 1180	+3.741 -12.584	+17.984 -8.787	0.625	+18.380 -15.361
1180 - 1250	+3.969 -12.843	+19.324 -9.127	0.625	+19.737 -15.768
1250 - 1320	+4.663 -13.452	+21.246 -9.517	0.642	+21.761 -16.490
1320 - 1390	+4.878 -13.702	+22.884 -9.899	0.657	+23.407 -16.916
1390 - 1460	+5.242 -14.095	+24.854 -10.332	0.670	+25.410 -17.489
1460 - 1530	+5.582 -14.464	+27.170 -10.733	0.682	+27.746 -18.024
1530 - 1600	+6.003 -14.907	+29.741 -11.165	0.692	+30.349 -18.637
1600 - 1680	+6.503 -15.418	+32.855 -11.617	0.702	+33.500 -19.317

Table A.7: Theoretical uncertainties (in %) calculating using CT10-NLO PDF set from all sources as well as the total uncertainty, affecting the measurement of cross section ratio  $R_{32}$ , in each bin of  $H_{\mathrm{T},2}/2$ .

<b>Bin</b>	<b>Scale</b>	<b>PDF</b>	<b>NP</b>	<b>Total</b>
300 - 330	+0.038 -7.203	+2.458 -3.463	0.822	+2.592 -8.035
330 - 360	+0.027 -6.626	+2.317 -3.378	0.734	+2.431 -7.474
360 - 390	+0.024 -6.449	+2.149 -3.367	0.656	+2.247 -7.304
390 - 420	+0.084 -5.894	+2.411 -3.383	0.586	+2.482 -6.821
420 - 450	+0.113 -5.532	+2.345 -3.362	0.523	+2.405 -6.494
450 - 480	+0.109 -5.409	+2.390 -3.357	0.467	+2.438 -6.383
480 - 510	+0.073 -5.442	+2.506 -3.327	0.416	+2.541 -6.392
510 - 540	+0.107 -5.168	+2.559 -3.326	0.371	+2.588 -6.157
540 - 570	+0.112 -5.010	+2.586 -3.292	0.330	+2.609 -6.004
570 - 600	+0.163 -4.576	+2.729 -3.292	0.292	+2.750 -5.645
600 - 640	+0.146 -4.565	+2.824 -3.270	0.253	+2.839 -5.621
640 - 680	+0.198 -4.163	+3.368 -3.298	0.236	+3.382 -5.316
680 - 720	+0.155 -3.754	+2.352 -3.247	0.227	+2.368 -4.968
720 - 760	+0.196 -3.842	+3.267 -3.268	0.219	+3.280 -5.049
760 - 800	+0.126 -3.523	+3.366 -3.272	0.212	+3.375 -4.813
800 - 850	+0.110 -3.368	+3.596 -3.261	0.206	+3.604 -4.693
850 - 900	+0.048 -3.351	+3.909 -3.309	0.200	+3.915 -4.714
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1000 - 1060	+0.282 -3.683	+4.604 -3.357	0.204	+4.617 -4.988
1060 - 1120	+0.436 -3.779	+3.079 -3.375	0.224	+3.118 -5.071
1120 - 1180	+0.732 -3.982	+5.430 -3.452	0.241	+5.485 -5.276
1180 - 1250	+0.813 -4.031	+5.835 -3.511	0.258	+5.897 -5.352
1250 - 1320	+1.303 -4.414	+6.626 -3.591	0.275	+6.759 -5.697
1320 - 1390	+1.403 -4.471	+7.036 -3.659	0.290	+7.180 -5.785
1390 - 1460	+1.564 -4.590	+7.657 -3.778	0.304	+7.822 -5.953
1460 - 1530	+1.765 -4.738	+8.438 -3.853	0.316	+8.626 -6.115
1530 - 1600	+2.040 -4.972	+9.306 -3.962	0.328	+9.532 -6.366
1600 - 1680	+2.313 -5.179	+10.381 -4.075	0.339	+10.641 -6.599



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