

Research Article

Subject Multiplicities at LHC Energies and the QCD Color Factor Ratio C_A/C_F

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Subject multiplicity distributions of two jets with highest transverse momenta are simulated in proton-proton collisions at LHC energies of 7 TeV and 14 TeV. Jets are defined via the software package FastJet version 3.0.3 which includes the implementation of k_T sequential recombination algorithm with a jet size of $R = 0.6$. Subjects are resolved by rerunning the k_T algorithm on the jets and using the resolution cutoff of $y_{\text{cut}} = 10^{-3}$. The subject multiplicity distributions and their average values are measured as a function of the jet momenta and upto rapidities $|\eta| < 2$. The results are used to calculate the ratio $r = (\langle M_j \rangle - 1)/(\langle M_j \rangle - 1)$.

1. Introduction

One of the main motivations of studying highly energetic proton-proton (p-p) collisions at Large Hadron Collider (LHC) at CERN has been the discovery of Higgs Boson(s). The aim has recently been achieved with the discovery of a Higgs Boson. However, many more studies are needed to establish its properties. In addition, searches for new particles will continue for many more years.

The proton-proton collisions at the LHC are dominated by jet production which constitute a large background to potential signals of new physics. Quantum chromodynamics (QCD) describes well the dynamics of jet production in terms of partons. In QCD, quarks and gluons have different color charges and hence different coupling strengths. The values for the color factors originate directly from the symmetry group $SU(3)$ of QCD, calculated to be $C_A = 3$ for the gluon and $C_F = 4/3$ for the quark [1].

In hadron-hadron collisions, quarks and gluons fragment to produce collimated streams of particles conventionally called “jets.” A jet, characterized by its energy and momentum, is reconstructed according to a clustering prescription called a “jet algorithm” from the four vectors of constituents that may represent tracks, energy deposits in the calorimeter, reconstructed particle candidates, particles in a Monte Carlo

(MC) event generator, or partons of a theory calculation. In dijet events, the two jets leading in transverse momentum P_T can be associated with the two partons at leading order (LO) in perturbative QCD. The internal structure of these jets is then expected to depend mainly on the type of the primary parton, that is, either (anti-) quark or gluon, from which they originated. QCD predicts that gluons, because of their larger color factor, fragment more than quarks. Consequently, gluon-initiated jets become broader and exhibit a larger constituent multiplicity than quark jets. The ratio of the constituent multiplicity for gluon jets versus quark jets at LO is asymptotically given by the ratio of their color factor as $C_A/C_F = 9/4$. Effects of higher orders in the strong coupling constant α_s , however, could change this theoretical prediction.

In order to study the jet substructure, an experimental observable called subject multiplicity, M , is found to be very useful. It is defined as the number of subjects that can be resolved within a jet by reclustering the jet constituents with the same clustering algorithm. However, the spatial resolution is chosen to be finer than the one used in the jet reconstruction. In this way an infrared- and collinear-safe measure can be defined that is usable experimentally as well as in perturbative QCD. Various collinear and infrared safe jet algorithms exist [2].

2. Jet Algorithm and the Subject Multiplicity

The k_T algorithm [5] clusters all input objects i , $i = 1, \dots, n$, according to the following iterative steps.

TABLE 1: Average subject multiplicities for jets matched to gluons and quarks in the $|\eta|$ bins with $P_T^{\text{jet}} > 100$ GeV for k_T algorithm at $\sqrt{s} = 7$ TeV and $\sqrt{s} = 14$ TeV.

$ \eta $	7 TeV		14 TeV	
	Gluon jets (M)	Stat.	Quark jets (M)	Stat.
$ \eta < 1.0$	3.39	± 0.01	2.27	± 0.01
$1.0 \leq \eta < 2.0$	3.46	± 0.01	2.26	± 0.01
			3.45	± 0.01
			2.27	± 0.01

TABLE 2: Average subject multiplicities as a function of $|\eta|$ in different \hat{P}_T bins, for jets with $P_T^{\text{jet}} > 100$ GeV for k_T algorithm at $\sqrt{s} = 7$ TeV and $\sqrt{s} = 14$ TeV.

\hat{P}_T (GeV)	7 TeV		14 TeV	
	$ \eta $	(M)	Stat.	(M)
50–300	$ \eta < 0.5$	2.99	± 0.05	3.25
	$0.5 \leq \eta < 1.0$	2.90	± 0.07	3.06
	$1.0 \leq \eta < 1.5$	2.89	± 0.09	3.14
300–550	$1.5 \leq \eta < 2.0$	2.71	± 0.11	3.02
	$ \eta < 0.5$	2.11	± 0.01	2.21
	$0.5 \leq \eta < 1.0$	2.06	± 0.01	2.18
550–800	$1.0 \leq \eta < 1.5$	2.01	± 0.01	2.17
	$1.5 \leq \eta < 2.0$	1.95	± 0.02	2.10
	$ \eta < 0.5$	1.82	± 0.01	1.94
800–1050	$0.5 \leq \eta < 1.0$	1.77	± 0.01	1.90
	$1.0 \leq \eta < 1.5$	1.70	± 0.01	1.86
	$1.5 \leq \eta < 2.0$	1.65	± 0.04	1.80
	$ \eta < 0.5$	1.68	± 0.01	1.81
	$0.5 \leq \eta < 1.0$	1.63	± 0.01	1.77
	$1.0 \leq \eta < 1.5$	1.51	± 0.01	1.72
	$1.5 \leq \eta < 2.0$	1.49	± 0.08	1.64

(i) For each pair (i, j) of objects find

$$d_{ij} = \min \left(\frac{\Delta R_{ij}^2}{P_{Ti} P_{Tj}}, \frac{\Delta \phi_{ij}^2}{R^2} \right), \quad (1)$$

where $R = 0.6$ is the jet size in $y - \phi$ space

$$\Delta R_{ij} = \sqrt{(y_{ij})^2 + (\Delta \phi_{ij})^2}. \quad (2)$$

(ii) For each object calculate the beam distance

$$d_{\#} = P_{Tj}^2. \quad (3)$$

(iii) If the minimum d_{min} of all possible d_{ij} and $d_{\#}$ is d_{ij} , then merge objects i and j into a single object by 4-momentum vector addition. If it is $d_{\#}$, then remove object i from the list and define it to be a final jet.

(iv) Repeat the above steps until no clustering objects are left.

2.1. Subject Multiplicities. Subjects are resolved within a jet by repeating the application of k_T cluster algorithm described

above. The clustering is terminated when all d_{ij}, d_{ib} are above the quantity $d_{\text{cut}} = y_{\text{cut}} P_T^2(\text{jet})$. All remaining objects are called subjects. While the stopping parameter d_{cut} defines the hard scale of the process, the parameter y_{cut} is known as the resolution parameter. The subject structure depends upon the values chosen for the resolution parameter y_{cut} . The mean subject multiplicity $\langle M \rangle$ is defined as the average number of subjects in a jet at a given value of y_{cut} :

$$\langle M \rangle = \frac{1}{N_{\text{jet}}} \sum_{\text{jet}=1}^{N_{\text{jet}}} M(y_{\text{cut}}). \quad (4)$$

By definition $M(y_{\text{cut}}) \geq 1$ and $0 \leq y_{\text{cut}} \leq 1$. The mean subject multiplicity is measured for $y_{\text{cut}} = 10^{-3}$ and $R = 0.6$, where y_{cut} is the subject resolution parameter. A study to optimise the value of y_{cut} at 7 TeV was done in an earlier work, documented in [10, 11] and the same used here. This optimum value of y_{cut} matches with the one used for the definition of subjects in [12]. In addition two subjects within a jet are resolved if they are well separated in $\eta \times \phi$ space.

3. Determination of Ratio r

In the p-p collisions, the final state stable particles are arranged into jets by using a jet algorithm, as described above. These particles are produced in the hadronisation of hard partons. In a mixed sample of quark and gluon initiated particle jets, M is the subject multiplicity which can be written as a linear combination of subject multiplicity in gluon jets M_g and quark jets M_q :

$$M = f M_g + (1 - f) M_q \quad (5)$$

where f is the fraction of gluon jets and $(1 - f)$ is the fraction of quark jets in the mixed sample. The gluon jet fraction f is the number of outgoing gluons that pass the selection cuts divided by the total number of outgoing partons that pass the selection cuts. Considering the above equation for two similar samples of jets at \sqrt{s} (\sqrt{s} is the center of mass energy (c.m.)) = 7 TeV and 14 TeV and assuming M_g and M_q to be independent of \sqrt{s} , we get

$$\begin{aligned} M^7 &= f^7 M_g + (1 - f^7) M_q \\ M^{14} &= f^{14} M_g + (1 - f^{14}) M_q \end{aligned} \quad (6)$$

The solutions are

$$\begin{aligned} M_q &= \frac{f^{14} M^7 - f^7 M^{14}}{f^{14} - f^7}, \\ M_g &= \frac{(1 - f^7) M^{14} - (1 - f^{14}) M^7}{f^{14} - f^7}, \end{aligned} \quad (7)$$

where M^{14} and M^7 are extracted from the total subjects in mixed samples of quark and gluon initiated jets in the data at $\sqrt{s} = 14$ and 7 TeV, respectively, and f^{14} and f^7 are the gluon jet fractions at the two energies. This method relies

on the extraction of quark and gluon fractions from the Monte Carlo information, obtained by tagging the particle jets with partons. This way the knowledge of the two gluon jet fractions is obtained. The subject multiplicity distributions can be characterized by the mean values $\langle M \rangle$ such that $\langle M_q \rangle - 1$ and $\langle M_g \rangle - 1$ gives the average number of subjects in a gluon and quark jet, respectively. The gluon jets are compared to the quark jets by having a ratio:

$$r = \frac{\langle M_g \rangle - 1}{\langle M_q \rangle - 1}. \quad (8)$$

4. Event Samples and Jet Selection

To study the subject multiplicity in high P_T jets and to calculate the color factor ratio, events are generated using PYTHIA8 with CTEQ6L1 PDFs at $\sqrt{s} = 7$ TeV and 14 TeV. At each energy, 1 million events are generated in 4 bins of \hat{P}_T in the pseudorapidity range $|\eta| < 2$. The bins in \hat{P}_T are 50–300, 300–550, 550–800, and 800–1050 GeV. One million events are generated in each pseudorapidity range $|\eta| < 1$ and $1 \leq |\eta| < 2$. One million events are also generated separately in each bin of jet pseudorapidity $|\eta|$ which are 0.0–0.5, 0.5–1.0, 1.0–1.5, and 1.5–2.0 for leading jets. Thus in total we have generated 7 million events for each energy for the present study.

Quark and gluon jets are unambiguously defined only in the leading order QCD where there are only two jets, that is, two partons in the final state. So a sample of dijet events in hard QCD $2 \rightarrow 2$ scattering events is defined by selecting the two jets leading in P_T in each event with the following selection cuts:

- (i) $P_T^{\text{jet}} > 100$ GeV,
- (ii) $|\Delta\phi(j_1, j_2) - \pi| < 1.0$ (requiring the jets to be back-to-back in the azimuthal plane),
- (iii) $|\eta| < 2$.

For k_T algorithm, mean subject multiplicity is measured for cone radius, $R = 0.6$ and $y_{\text{cut}} = 10^{-3}$.

5. Discrimination between Quark and Gluons Jets

To determine the ratio of color factor, jet substructure of gluon and quark initiated jets is studied in terms of subject multiplicities. For the Monte Carlo PYTHIA8 events used here, the quark and gluon jets are identified using parton level information. The direction of each primary parton is determined after its perturbative evolution has terminated. The jet closest to the direction of the primary parton (quark/antiquark or gluon) tagged to be the quark/gluon jet, respectively. The two highest P_T jets are identified as quark or gluon initiated jets via the tagging in the spatial coordinates and the kinematical cuts. Thus we implement these cuts by allowing the maximum distance in $\eta \times \phi$ space as $\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} < 0.4$. The maximum relative

TABLE 3: Average subject multiplicities as a function of P_T^{jet} (GeV) for mixed jets and jets matched to gluons and quarks, for k_T algorithm at $\sqrt{s} = 7$ TeV and $\sqrt{s} = 14$ TeV.

P_T^{jet} (GeV)	$\langle M \rangle$	Stat.	$\langle M_g \rangle$	Stat.	$\langle M_q \rangle$	Stat.
7 TeV						
100–300	2.63	± 0.01	3.06	± 0.01	2.05	± 0.01
300–500	2.03	± 0.01	2.45	± 0.01	1.72	± 0.01
500–700	1.82	± 0.01	2.25	± 0.01	1.58	± 0.01
700–900	1.71	± 0.01	2.17	± 0.01	1.53	± 0.01
900–1100	1.64	± 0.01	2.11	± 0.01	1.49	± 0.01
14 TeV						
100–300	2.76	± 0.01	3.07	± 0.01	2.13	± 0.01
300–500	2.11	± 0.01	2.43	± 0.01	1.70	± 0.01
500–700	1.93	± 0.01	2.28	± 0.01	1.60	± 0.01
700–900	1.82	± 0.01	2.17	± 0.01	1.56	± 0.01
900–1100	1.75	± 0.01	2.11	± 0.01	1.52	± 0.01

TABLE 4: Fraction of gluon and quark jets in phase space $|\eta| < 2$ in different P_T^{jet} (GeV) bins for k_T algorithm.

P_T^{jet} (GeV)	7 TeV			14 TeV		
	Gluon jets	Quark jets		Gluon jets	Quark jets	
	f	$1 - f$	Stat.	f	$1 - f$	Stat.
100–300	0.57	0.43	± 0.01	0.68	0.32	± 0.01
300–500	0.44	0.56	± 0.01	0.56	0.44	± 0.01
500–700	0.33	0.67	± 0.01	0.48	0.52	± 0.01
700–900	0.27	0.73	± 0.01	0.42	0.58	± 0.01
900–1100	0.22	0.78	± 0.01	0.37	0.63	± 0.01

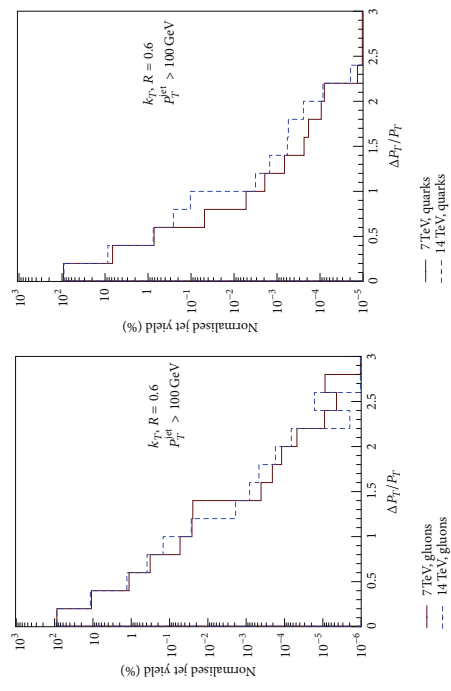


FIGURE 1: Distribution of $\Delta P_T/P_T$ for the matched quark and gluon jets with $P_T^{\text{jet}} > 100$ GeV at $\sqrt{s} = 7$ TeV compared to $\sqrt{s} = 14$ TeV for k_T algorithm.

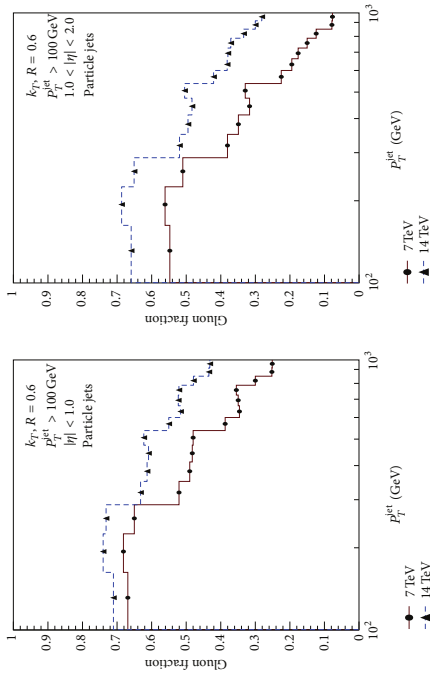


FIGURE 2: Fraction of gluon initiated jets differentiated via matching of the two partons leading jets to the hard partons of the leading-order process as a function of jet P_T from k_T algorithm at $\sqrt{s} = 7$ TeV compared to $\sqrt{s} = 14$ TeV in the pseudorapidity bins of $|\eta| < 1$ and $1 \leq |\eta| < 2$.

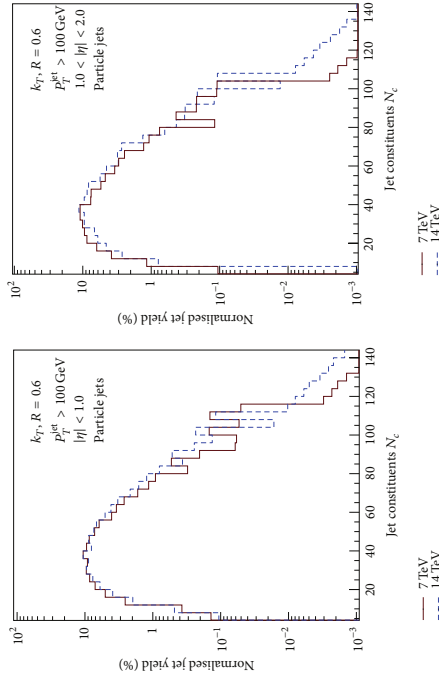


FIGURE 3: Distributions of the jet constituent multiplicity in particle jets having $P_T^{\text{jet}} > 100$ GeV from k_T algorithm at $\sqrt{s} = 7$ TeV compared to $\sqrt{s} = 14$ TeV in the pseudorapidity bins of $|\eta| < 1$ and $1 \leq |\eta| < 2$.

deviation in transverse momentum between the jet and the associated parton with respect to the jet transverse momentum is $\Delta P_T/P_T$. $\Delta P_T/P_T$ is abs(parton $P_T - \text{jet } P_T)/\text{jet } P_T < 3.0$. Figure 1 shows the ratio $\Delta P_T/P_T$ for quark and gluon jets matched, respectively, to partons for $\sqrt{s} = 7$ TeV

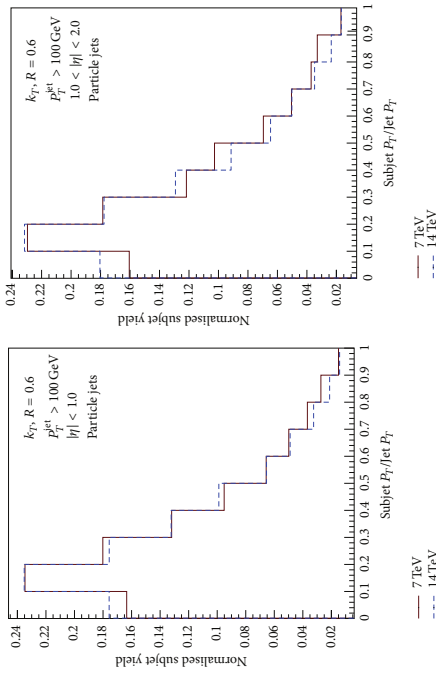


FIGURE 4: Distributions of the subject P_T fraction in particle jets having $P_T^{\text{jet}} > 100$ GeV from k_T algorithm at $\sqrt{s} = 7$ TeV compared to $\sqrt{s} = 14$ TeV in the pseudorapidity bins of $|\eta| < 1$ and $1 \leq |\eta| < 2$.

partons of the LO process as a function of jet P_T for the two different pseudorapidity bins, $|\eta| < 1$ and $1 \leq |\eta| < 2$. As expected the fraction of gluon jets decreases with increasing jet P_T in both the cases. Also, quark jets make up a dominant fraction of the jets only at high jet transverse momenta.

6. Systematic Uncertainties

The uncertainties in the subject multiplicities are of two categories:

- (i) statistical uncertainties,
- (ii) systematic uncertainties.

For the present analysis using Monte Carlo samples, the uncertainties are mainly on account of the statistics which are found to be negligibly small. The systematic uncertainties arise due to the change in gluon fraction due to minimum P_T imposed. This is measured as follows.

- (i) Gluon Jet fraction: The uncertainty in gluon jet fraction introduces a systematic error on the subject multiplicity. To calculate this, the gluon jet fraction is obtained as a function of minimum jet P_T (GeV) by varying minimum jet P_T from 90 to 100 GeV. This introduces an error of ± 0.02 on gluon fraction at $\sqrt{s} = 7$ TeV and ± 0.01 on gluon fraction at $\sqrt{s} = 14$ TeV. If the gluon fraction increases or decreases at both the energies, the change in ratio r is not much effective. But the increase in gluon jet fraction at one energy and decrease at other or vice versa introduces a largest change in ratio r , giving minimum and maximum

value of r . The difference of the calculated value r given in Table 5 from the minimum value and maximum value of r gives the systematic uncertainty due to gluon fraction as $+0.08$ -0.05 .

The same analysis for measuring r , when performed on the data from a detector such as CMS at LHC, would involve the following systematic errors also. In one such measurement with 36 pb^{-1} data used for measuring the subject multiplicity at $\sqrt{s} = 7$ TeV energy [10], we estimated the following uncertainties.

- (ii) Jet-Energy calibration: The maximum systematic uncertainty in jet-Energy calibration was estimated to be 5% depending upon jet P_T and jet η . This introduces an error of about 2% on the subject multiplicity average value.
- (iii) Jet-Energy resolution (JER): The uncertainty on the jet P_T resolution (JER) was estimated to be less than 10% and this results in less than 0.25% uncertainty in the subject multiplicity distributions.

- (iv) Uncertainties due to the different physics models employed for the simulations: The uncertainty due to different physics models implemented in the Monte Carlo generators is estimated to be less than 3%.

Compounding these systematic errors (ii)–(iv), the maximum uncertainty in the subject multiplicity of 3.28 at 7 TeV was estimated to be 0.10. The details can be found in [10]. We use the same percent value of each of the above mentioned systematic uncertainties in subject multiplicities at the two energies which will be reflected in ratio r . The systematic errors on ratio r are given in Table 6 and added in quadrature

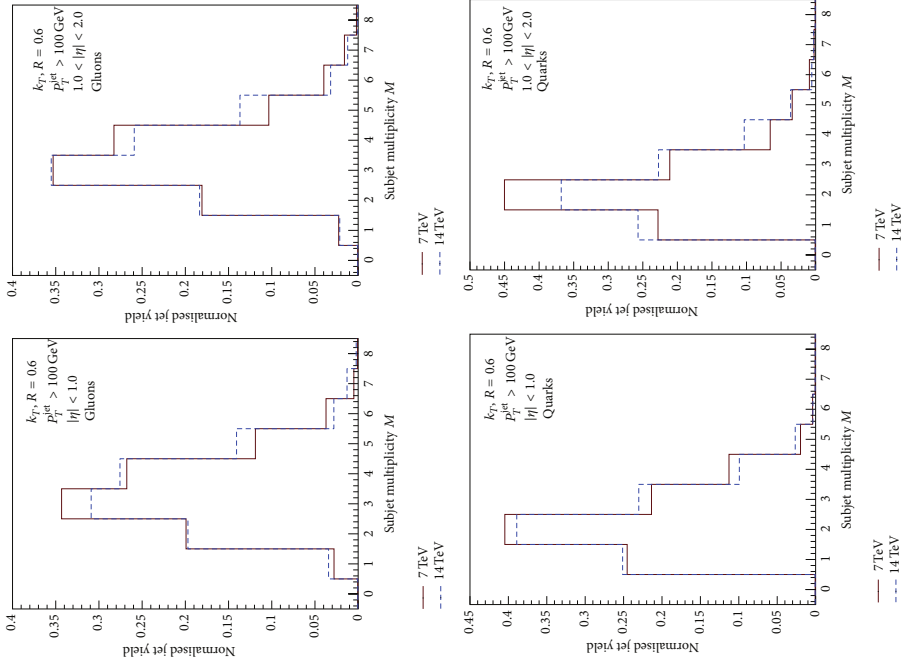


FIGURE 3: Subject multiplicity distributions for jets matched to gluons (top) and quarks (bottom), having $p_T^{\text{jet}} > 100$ GeV, in the pseudorapidity bins of $|\eta| < 1$ (left) and $1 \leq |\eta| < 2$ (right) at $\sqrt{s} = 7$ TeV and $\sqrt{s} = 14$ TeV from k_T algorithm.

to have the total systematic uncertainty in the calculated value of the ratio r .

7. Results and Discussions

Figure 3 shows jet constituent multiplicity distributions for k_T algorithm at $\sqrt{s} = 7$ TeV and at $\sqrt{s} = 14$ TeV in the two pseudorapidity bins, $|\eta| < 1$ and $1 \leq |\eta| < 2$. It

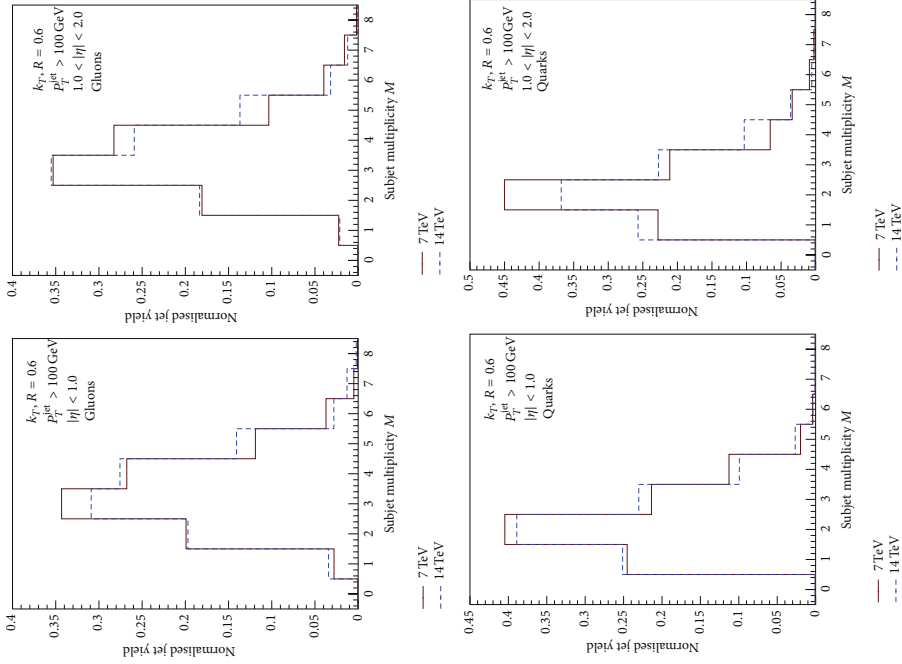


FIGURE 5: Subject multiplicity distributions for jets matched to gluons (top) and quarks (bottom), having $p_T^{\text{jet}} > 100$ GeV, in the pseudorapidity bins of $|\eta| < 1$ (left) and $1 \leq |\eta| < 2$ (right) at $\sqrt{s} = 7$ TeV and $\sqrt{s} = 14$ TeV from k_T algorithm.

may be observed that the average number of jet constituents is larger at 14 TeV. The subject P_T fractions for the two pseudorapidity regions and for the two energies are shown in Figure 4. In k_T algorithm, the procedure to resolve subjects is dependent on P_T of jet and the P_T of subjects in a particular jet is distributed in such a way that there is no sudden decrease. Thus as shown in Figure 4, we get monotonically decreasing values for subject P_T fraction.

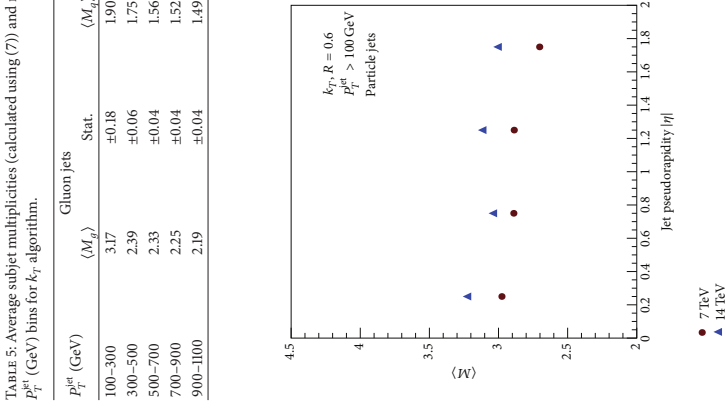


FIGURE 6: Average subject multiplicity $\langle M \rangle$ as a function of absolute jet pseudorapidity $|\eta|$ for the whole range in P_T at $\sqrt{s} = 7$ TeV and $\sqrt{s} = 14$ TeV for k_T algorithm.

Figure 5 shows the subject multiplicity distributions for jets matched to gluons in the two pseudorapidity bins and jets matched to quarks in the two pseudorapidity bins $|\eta| < 1$ and for $1 \leq |\eta| < 2$. The mean values are given in Table 1. Average number of subjects in gluon jets is found to be larger than in the quark jets indicating a higher degree of collimation in quark jets.

Average subject multiplicity, $\langle M \rangle$ dependence on absolute jet pseudorapidity for $\sqrt{s} = 7$ TeV and at $\sqrt{s} = 14$ TeV for the whole P_T range, is shown in Figure 6. Figure 7 shows the subject multiplicity distributions of jets as a function of the pseudorapidity bins (0.0–0.5, 0.5–1.0, 1.0–1.5, and 1.5–2.0) for four P_T intervals 50–300, 300–550, 550–800, and 800–1050 GeV. The values are given in Table 2. We observe that from inner to outer rapidities windows, with same rapidity

TABLE 5: Average subject multiplicities (calculated using (7)) and ratio of subject multiplicities (from (8)) in the phase space $|\eta| < 2$ in different p_T^{jet} (GeV) bins for k_T algorithm.

p_T^{jet} (GeV)	Gluon jets $\langle M_g \rangle$	Stat.	Quark jets $\langle M_q \rangle$	Stat.	$r = \langle M_g \rangle - 1 / \langle M_q \rangle - 1$	Stat.
100–300	3.17	± 0.18	1.90	± 0.17	2.42	± 0.25
300–500	2.39	± 0.06	1.75	± 0.05	1.87	± 0.07
500–700	2.33	± 0.04	1.56	± 0.03	2.36	± 0.06
700–900	2.25	± 0.04	1.52	± 0.03	2.42	± 0.06
900–1100	2.19	± 0.04	1.49	± 0.02	2.43	± 0.06

TABLE 6: Systematic uncertainties on ratio of subject multiplicities from different sources.

Source	δr
Gluon jet fraction	(+0.08) (−0.05)
Jet-energy calibration	± 0.15
Jet-energy resolution	± 0.02
Different physical model	± 0.22
Total	(+0.28) (−0.27)

window size, the subject multiplicity tends to get smaller very slightly.

Figure 8 shows the jet P_T versus $\langle M \rangle$ for pseudorapidity $|\eta| < 2$ for quarks, gluons, and matched jets for the two energies under study. The mean values are given in Table 3.

The selected dijet sample consists of mixture of gluon and quark initiated jets as in the LO hard QCD $2 \rightarrow 2$ processes. Following the recipe from Section 3, we use (7) to separate these two types and obtain the average subject multiplicities $\langle M \rangle$ for gluon jets and quark jets in the five bins of jet P_T . The results are given in Table 5 (the weighted mean \bar{M} and the uncertainties are calculated by using $\bar{M} = (\sum M_i / \text{error}_i^2) / (\sum 1 / \text{error}_i^2)$ and $\text{error}_{\bar{M}}^2 = 1 / (\sum 1 / \text{error}_i^2)$). These values are then used to calculate the ratio r from (8) as given in Table 5.

8. Summary

The subject multiplicities in proton-proton collisions at $\sqrt{s} = 7$ TeV and at $\sqrt{s} = 14$ TeV are estimated in 14 million proton-proton collisions by selecting dijet samples simulated using PYTHIA8.

The jets and subjects have been resolved with the k_T jet algorithm for a jet size of $R = 0.6$ and a subject resolution cutoff $y_{\text{cut}} = 10^{-3}$. The subject multiplicity distribution and its average $\langle M \rangle$ have been determined in the jet P_T range of 100–1100 GeV for jet pseudorapidity $|\eta| < 2$. In the whole pseudorapidity range $|\eta| < 2$, the average subject multiplicity $\langle M \rangle$ for particle jets is found to decrease from 2.63 ± 0.01 (stat.) down to 1.64 ± 0.01 (stat.) for 7 TeV and from 2.76 ± 0.01 (stat.) down to 1.75 ± 0.01 (stat.) at 14 TeV with increasing jet P_T . The average subject multiplicity for jets

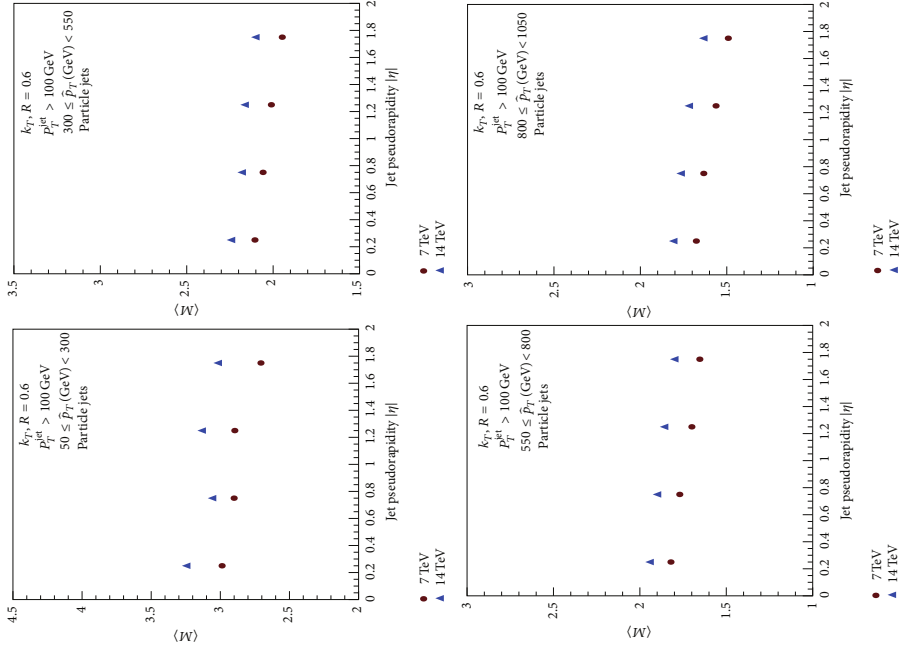


FIGURE 7: Average subject multiplicity $\langle M \rangle$ as a function of absolute jet pseudorapidity $| \eta |$ in the four \hat{p}_T bins at $\sqrt{s} = 7 \text{ TeV}$ and $\sqrt{s} = 14 \text{ TeV}$ for k_T algorithm.

matched to gluons, $\langle M_g \rangle$, is also found to decrease from 3.06 ± 0.01 (stat.) down to 2.11 ± 0.01 (stat.) for 7 TeV and from 3.07 ± 0.01 (stat.) down to 2.11 ± 0.01 (stat.) at 14 TeV with increase in jet \hat{p}_T from 100 GeV to 1100 GeV. The average subject multiplicity for jets matched to quarks, $\langle M_q \rangle$, is also found to decrease from 2.05 ± 0.01 (stat.) down to 1.49 ± 0.01 (stat.) for 7 TeV and from 2.13 ± 0.01 (stat.) down to 1.52 ± 0.01 (stat.) at 14 TeV with increase in jet \hat{p}_T .

This is a clear indication of a higher degree of collimation with rising jet \hat{p}_T . In Table 2, we can observe that from inner to outer rapidities the subject multiplicity tends to get slightly smaller as well. Evidently, a direct conclusion on the gluon-quark fraction cannot be drawn since the subject multiplicity not only depends on this fraction but also on details of the Multiple Parton Interactions (MPI), parton shower, and hadronization models. Exploiting data at two

TABLE 7: Color factor ratio for different experiments.

Experiment	Ratio C_s/C_F	Stat.	Sys.
Do (2 jet events) [12]	1.91	± 0.04	± 0.21
DELPHI (3 jet events) [13]	1.74	± 0.03	± 0.10
OPAL (4 jet events) [14]	2.11	± 0.16	± 0.28
DELPHI (4 jet events) [15]	2.12	± 0.35	± 0.11
ALEPH (4 jet events) [16]	2.20	± 0.09	± 0.13

good agreement with the value predicted from the symmetry group $SU(3)$ of QCD and also with the values measured at previous experiments listed in Table 7.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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References

- [1] R. K. Ellis, W. J. Stirling, and B. R. Webber, *QCD and Collider Physics*, Cambridge University Press, Cambridge, UK, 1996.
- [2] G. P. Salam, "Towards Jetography," *The European Physical Journal C*, vol. 67, no. 3-4, pp. 637–686, 2010.
- [3] S. Catani, Y. L. Dokshitzer, M. Olsson, G. Turnock, and B. R. Webber, "New clustering algorithm for multijet cross sections in e^+e^- annihilation," *Physics Letters B*, vol. 269, no. 3-4, pp. 432–438, 1991.
- [4] S. Catani, Y. L. Dokshitzer, and B. R. Webber, "The k_s -clustering algorithm for jets in deep inelastic scattering and hadron collisions," *Physics Letters B*, vol. 285, no. 3, pp. 291–299, 1992.
- [5] S. D. Ellis and D. E. Soper, "Successive combination jet algorithm for hadron collisions," *Physical Review D*, vol. 48, no. 7, pp. 3160–3166, 1993.
- [6] M. Cacciari, G. P. Salam, and G. Soyez, "Fastjet user manual," *The European Physical Journal C*, vol. 72, 2012.
- [7] M. Cacciari, G. P. Salam, and G. Soyez, "Fastjet homepage," <http://www.hepforge.org/fastjet/>.
- [8] M. Cacciari and G. P. Salam, "Dispelling the N^3 myth for the k_T jet-finder," *Physics Letters B*, vol. 641, no. 1, pp. 57–61, 2006.
- [9] T. Sjostrand, S. Mrenna, and P. Z. Skands, "A brief introduction to PYTHIA 8.1," *Computer Physics Communications*, vol. 178, no. 11, pp. 852–867, 2008.
- [10] The CMS Collaboration, "Measurement of the Subject Multiplicity in DiJet Events from proton-proton collisions at $\sqrt{s} = 7 \text{ TeV}$," CMS PAS QCD-10-041, 2012.
- [11] M. Zubin Mehra, M. Kaur, K. Rabbertz et al., "Measurement of the Subject Multiplicity in DiJet Events from proton-proton collisions at $\sqrt{s} = 7 \text{ TeV}$," CMS AN-2010-252, 2011.

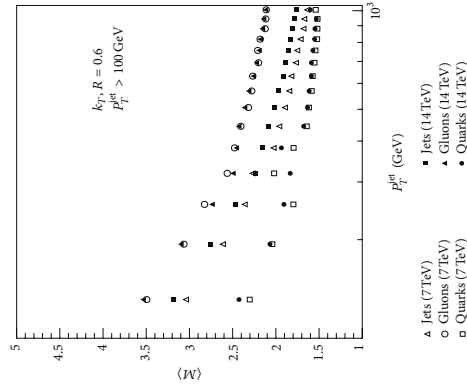


FIGURE 8: Average subject multiplicity $\langle M \rangle$ as a function of jet \hat{p}_T in the pseudorapidity range of $| \eta | < 2$ at $\sqrt{s} = 7 \text{ TeV}$ and $\sqrt{s} = 14 \text{ TeV}$ for k_T algorithm.

different center-of-mass energies, the model dependence can be potentially eliminated. This technique was applied for data at two center-of-mass energies at Tevatron, as described in [12] to measure the ratio r . This method has been exploited for present and future LHC energies to predict the value of ratio r . The values of average subject multiplicities in quark and gluon jets in different jet \hat{p}_T bins are calculated from (7) using the values given in Tables 3 and 4 and the ratio from (8). The results are given in Table 5. The mean value of ratio r is calculated by using maximum likelihood estimator of the subject distributions as $r = 2.30 \pm 0.03$ (stat.). The total systematic uncertainty from different sources comes out to be $^{+0.28}_{-0.27}$ given in Table 6. So the extracted value of ratio of subject multiplicities of gluon jets and quark jets is $r = 2.30 \pm 0.03$ (stat.) $^{+0.28}_{-0.27}$ (sys.). This value converges to the ratio of the color factors, $C_s/C_F = 9/4$. In [17], it is shown that the ratio of the multiplicities from quark and gluon jets should converge to the color factor ratio. The extracted value is in

- [12] D0 Collaboration, "Subjet multiplicity of gluon and quark jets reconstructed with the k_t algorithm in $p\bar{p}$ collisions," *Physical Review D*, vol. 65, no. 5, Article ID 052008, 20 pages, 2002.
- [13] J. William Gary, "Determination of the QCD color factor ratio C_A/C_F from the scale dependence of multiplicity in three jet events," *Physical Review D*, vol. 61, no. 11, Article ID 114007, 8 pages, 2000.
- [14] R. Akers, G. Alexander, J. Allison et al., "A measurement of the QCD colour factor ratios C_A/C_F and T_F/C_F from angular correlations in four-jet events," *Zeitschrift für Physik C*, vol. 65, no. 3, pp. 367–377, 1995.
- [15] P. Abreu, W. Adam, T. Aäbe et al., "Measurement of the triple-gluon vertex from 4-jet events at LEP," *Zeitschrift für Physik C*, vol. 59, no. 3, pp. 357–368, 1993.
- [16] The ALEPH Collaboration, "A measurement of the QCD colour factors and a limit on the light gluino," *Zeitschrift für Physik C*, vol. 76, pp. 1–14, 1997.
- [17] E. D. Malaza, "Multiplicity distributions in quark and gluon jets to $O(\alpha_s)$," *Zeitschrift für Physik C*, vol. 31, no. 1, pp. 143–150, 1986.

