Fortcoders Code Library

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#pragma GCC optimize("-fdevirtualize") #pragma GCC optimize("-fcaller-saves") 17 Main template #pragma GCC optimize("-fcrossjumping") 19 #pragma GCC optimize("-fthread-jumps") #include <bits/stdc++.h> #pragma GCC optimize("-funroll-loops") 21 using namespace std; #pragma GCC optimize("-fwhole-program") #pragma GCC optimize("-freorder-blocks") 22 #define FOR(x,n) for(int x=0;x< n;x++)23 #pragma GCC optimize("-fschedule-insns") #define form(i, n) for (int i = 0; i < int(n); i++) #pragma GCC optimize("inline-functions") #define all(v) v.begin(), v.end() #pragma GCC optimize("-ftree-tail-merge") 26 using ll = long long; #pragma GCC optimize("-fschedule-insns2") using ld = long double; #pragma GCC optimize("-fstrict-aliasing") using pii = pair<int, int>; #pragma GCC optimize("-fstrict-overflow") const char nl = '\n'; #pragma GCC optimize("-falign-functions") 11 #pragma GCC optimize("-fcse-skip-blocks") 31 int main() { 12 #pragma GCC optimize("-fcse-follow-jumps") cin.tie(nullptr)->sync_with_stdio(false); #pragma GCC optimize("-fsched-interblock") cout << fixed << setprecision(20);</pre> 14 #pragma GCC optimize("-fpartial-inlining") // mt19937 #pragma GCC optimize("no-stack-protector") \hookrightarrow rng(chrono::steady_clock::now().time_since_epoch().count()); 35 #pragma GCC optimize("-freorder-functions") #pragma GCC optimize("-findirect-inlining") #pragma GCC optimize("-fhoist-adjacent-loads") Fast IO #pragma GCC optimize("-frerun-cse-after-loop") #pragma GCC optimize("inline-small-functions") 40 #pragma GCC optimize("-finline-small-functions") #pragma GCC optimize("-ftree-switch-conversion") namespace io { 41 constexpr int SIZE = 1 << 16;</pre> #pragma GCC optimize("-foptimize-sibling-calls") char buf[SIZE], *head, *tail; #pragma GCC optimize("-fexpensive-optimizations") char get char() { if (head == tail) tail = (head = buf) + fread(buf, 1, SIZE, #pragma GCC optimize("-funsafe-loop-optimizations") stdin); #pragma GCC optimize("inline-functions-called-once") 46 return *head++; #pragma GCC optimize("-fdelete-null-pointer-checks") 47 } #pragma GCC 11 read() { → target("sse,sse2,sse3,sse3,sse4.1,sse4.2,avx,avx2,popcnt,tune=nave 11 x = 0, f = 1;char c = get_char(); 10 for (; !isdigit(c); c = get_char()) (c == '-') && (f = -1); Data Structures 11 12 for (; isdigit(c); $c = get_char()) x = x * 10 + c - '0'$; return x * f; 13 Segment Tree 14 string read_s() { 15 Recursive 16 string str; char c = get_char(); 17 while $(c == ' ' | | c == ' n' | | c == ' r') c = get_char();$ • Implicit segment tree, range query + point update 18 while (c != ' ' && c != '\n' && c != '\r') str += c, c = 19 struct Node { get_char(); 2 int lc, rc, p; 20 return str; }; 21 } void print(int x) { 22 struct SegTree { if (x > 9) print(x / 10); 23 vector<Node> t = {{}}; putchar(x % 10 | '0'); 24 SegTree(int n) { t.reserve(n * 40); } int modify(int p, int l, int r, int x, int v) { void println(int x) { print(x), putchar('\n'); } 26 int u = p; 27 if (p == 0) { Read& operator>>(11& x) { return x = read(), *this; } t.push_back(t[p]); Read& operator>>(long double& x) { return x = 11 29 u = (int)t.size() - 1; stold(read_s()), *this; } } in; 13 30 if (r - l == 1) { 14 } // namespace io t[u].p = t[p].p + v;15 } else { 16 Pragmas (lol) int m = (1 + r) / 2;17 if (x < m) { 18 #pragma GCC optimize(2) t[u].lc = modify(t[p].lc, 1, m, x, v); 19 #pragma GCC optimize(3) 20 #pragma GCC optimize("Ofast") 21 t[u].rc = modify(t[p].rc, m, r, x, v); #pragma GCC optimize("inline") 22 #pragma GCC optimize("-fgcse") t[u].p = t[t[u].lc].p + t[t[u].rc].p;23 #pragma GCC optimize("-fgcse-lm") 24 #pragma GCC optimize("-fipa-sra") 25 return u; #pragma GCC optimize("-ftree-pre") #pragma GCC optimize("-ftree-vrp") 26 27 int query(int p, int l, int r, int x, int y) { #pragma GCC optimize("-fpeephole2") if (x <= 1 && r <= y) return t[p].p;</pre> 10 28 #pragma GCC optimize("-ffast-math") int m = (1 + r) / 2, res = 0;#pragma GCC optimize("-fsched-spec") if (x < m) res += query(t[p].lc, l, m, x, y);</pre> 12 30 #pragma GCC optimize("unroll-loops") 31 if (y > m) res += query(t[p].rc, m, r, x, y); 13 #pragma GCC optimize("-falign-jumps") 32 return res;

16

#pragma GCC optimize("-falign-labels")

Intro

#pragma GCC optimize("-falign-loops")

```
};
                                                                            struct Node {
                                                                        1
                                                                              11 v = 0;
                                                                        2
       • Persistent implicit, range query + point update
                                                                        3
                                                                            };
                                                                            struct Tag {
                                                                        4
                                                                              11 v = 0;
      int lc = 0, rc = 0, p = 0;
2
                                                                        6
                                                                            }:
                                                                            Node pull(const Node& a, const Node& b) { return {max(a.v,
                                                                             → b.v)}; }
    struct SegTree {
5
                                                                            Tag pull(const Tag& a, const Tag& b) { return {a.v + b.v}; }
      vector<Node> t = {{}}; // init all
                                                                            Node apply_tag(const Node& a, const Tag& b) { return {a.v +
      SegTree() = default;

    b.v}; }

      SegTree(int n) { t.reserve(n * 20); }
                                                                       10
      int modify(int p, int 1, int r, int x, int v) {
                                                                       11
                                                                            struct SegTree {
        // p: original node, update a[x] \rightarrow v
10
                                                                              11 n, h;
                                                                       12
        t.push_back(t[p]);
11
                                                                              vector<Node> t;
        int u = (int)t.size() - 1;
12
                                                                              vector<Tag> lazy;
                                                                       14
         if (r - l == 1) {
13
                                                                              SegTree(ll _n) : n(_n), h((ll)log2(n)), t(2 * _n), lazy(2 *
14
          t[u].p = v;
                                                                                _n) {}
15
         } else {
                                                                              void apply(ll x, const Tag& tag) {
                                                                       16
          int m = (1 + r) / 2;
16
                                                                                t[x] = apply_tag(t[x], tag);
                                                                       17
          if (x < m) {
17
                                                                                lazy[x] = pull(lazy[x], tag);
                                                                       18
            t[u].lc = modify(t[p].lc, 1, m, x, v);
18
                                                                       19
            t[u].rc = t[p].rc;
19
                                                                              void build(ll 1) {
                                                                       20
          } else {
20
                                                                                for (1 = (1 + n) / 2; 1 > 0; 1 /= 2) {
            t[u].lc = t[p].lc;
21
                                                                                  if (!lazy[1].v) t[1] = pull(t[1 * 2], t[2 * 1 + 1]);
                                                                       22
            t[u].rc = modify(t[p].rc, m, r, x, v);
22
                                                                       23
                                                                              }
                                                                       24
          t[u].p = t[t[u].lc].p + t[t[u].rc].p;
24
                                                                              void push(11 1) {
                                                                       25
25
                                                                                1 += n;
26
        return u;
                                                                       27
                                                                                for (ll s = h; s > 0; s--) {
27
                                                                                  ll i = 1 >> s;
                                                                       28
       int query(int p, int 1, int r, int x, int y) {
28
                                                                                  if (lazy[i].v) {
                                                                       29
        // query sum a[x]...a[y-1] rooted at p
29
                                                                                    apply(2 * i, lazy[i]);
                                                                       30
         // t[p] holds the info of [l, r)
                                                                       31
                                                                                    apply(2 * i + 1, lazy[i]);
        if (x <= 1 && r <= y) return t[p].p;
31
                                                                                  }
                                                                       32
        int m = (1 + r) / 2, res = 0;
32
                                                                                  lazy[i] = Tag();
                                                                       33
33
        if (x < m) res += query(t[p].lc, l, m, x, y);
                                                                                }
                                                                       34
        if (y > m) res += query(t[p].rc, m, r, x, y);
34
                                                                       35
35
        return res;
                                                                              void modify(ll l, ll r, const Tag& v) {
                                                                       36
      }
36
                                                                                push(1), push(r - 1);
                                                                       37
    };
                                                                       38
                                                                                11\ 10 = 1, r0 = r;
                                                                                for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
                                                                       39
                                                                                  if (1 & 1) apply(1++, v);
                                                                       40
    Iterating
                                                                                  if (r & 1) apply(--r, v);
                                                                       41
                                                                       42
       • Iterating, range query + point update
                                                                                build(10), build(r0 - 1);
                                                                       43
                                                                       44
    struct Node {
                                                                              Node query(ll 1, ll r) {
                                                                       45
      11 v = 0, init = 0;
2
                                                                       46
                                                                                push(1), push(r - 1);
3
                                                                                Node left, right;
                                                                       47
                                                                       48
                                                                                for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
    Node pull(const Node &a, const Node &b) {
                                                                                  if (1 & 1) left = pull(left, t[1++]);
                                                                       49
      if (!a.init) return b;
                                                                                   if (r \& 1) right = pull(t[--r], right);
      if (!b.init) return a;
                                                                       51
8
      Node c:
                                                                       52
                                                                                return pull(left, right);
9
      return c;
                                                                       53
10
                                                                            };
                                                                       54
    struct SegTree {
12
                                                                               • AtCoder Segment Tree (recursive structure but iterative)
13
14
      vector<Node> t;
                                                                            template <class T> struct PointSegmentTree {
      SegTree(ll _n) : n(_n), t(2 * n){};
15
                                                                              int size = 1;
      void modify(ll p, const Node &v) {
                                                                              vector<T> tree;
        t[p += n] = v;
17
                                                                              PointSegmentTree(int n) : PointSegmentTree(vector<T>(n)) {}
        for (p /= 2; p; p /= 2) t[p] = pull(t[p * 2], t[p * 2 +
                                                                              PointSegmentTree(vector<T>& arr) {

→ 1]);

                                                                                while(size < (int)arr.size())</pre>
19
                                                                                   size <<= 1;
      Node query(ll 1, ll r) {
20
                                                                                tree = vector<T>(size << 1);</pre>
        Node left, right;
21
                                                                                for(int i = size + arr.size() - 1; i >= 1; i--)
         for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
22
                                                                       10
                                                                                  if(i >= size) tree[i] = arr[i - size];
23
          if (1 & 1) left = pull(left, t[1++]);
                                                                                  else consume(i);
                                                                       11
          if (r \& 1) right = pull(t[--r], right);
24
                                                                       12
25
                                                                              void set(int i, T val) {
                                                                       13
        return pull(left, right);
26
                                                                                tree[i += size] = val;
                                                                       14
      }
27
                                                                                for(i >>= 1; i >= 1; i >>= 1)
                                                                       15
    };
28
                                                                                   consume(i);
                                                                       16
                                                                       17
       • Iterating, range query + range update
                                                                              T get(int i) { return tree[i + size]; }
```

```
int set(int p, int x, int v) { return seg.modify(p, 0, n, x,
      T query(int 1, int r) {
19
                                                                         44
         T resl, resr;
                                                                               \hookrightarrow v); }
20
         for(1 += size, r += size + 1; 1 < r; 1 >>= 1, r >>= 1) {
21
                                                                         45
                                                                                int find(int p, int x) {
           if(1 & 1) resl = resl * tree[1++];
                                                                                   int parent = get(p, x);
22
                                                                         46
           if(r & 1) resr = tree[--r] * resr;
                                                                                   if (parent < 0) return x;</pre>
23
                                                                          47
                                                                                   return find(p, parent);
24
                                                                         48
25
        return resl * resr;
                                                                          49
                                                                                int is_same(int p, int x, int y) { return find(p, x) ==
26
                                                                          50
      T query_all() { return tree[1]; }

    find(p, y); }

27
      void consume(int i) { tree[i] = tree[i << 1] * tree[i << 1 |</pre>
                                                                                int merge(int p, int x, int y) {
                                                                                   int rx = find(p, x), ry = find(p, y);
     };
                                                                                   if (rx == ry) return -1;
29
                                                                          53
30
                                                                         54
                                                                                   int rank_x = -get(p, rx), rank_y = -get(p, ry);
                                                                                   if (rank_x < rank_y) {</pre>
                                                                         55
31
    struct SegInfo {
                                                                                    p = set(p, rx, ry);
32
                                                                          56
      11 v:
                                                                                   } else if (rank_x > rank_y) {
                                                                         57
33
34
       SegInfo() : SegInfo(0) {}
                                                                         58
                                                                                    p = set(p, ry, rx);
       SegInfo(ll val) : v(val) {}
35
                                                                         59
                                                                                   } else {
       SegInfo operator*(SegInfo b) {
                                                                                    p = set(p, ry, rx);
36
                                                                         60
                                                                                     p = set(p, rx, -rx - 1);
37
         return SegInfo(v + b.v);
                                                                         61
38
                                                                         62
    };
39
                                                                         63
                                                                                   return p;
                                                                                }
                                                                         64
                                                                              };
    Union Find
                                                                              Fenwick Tree
    vector<int> p(n);
    iota(p.begin(), p.end(), 0);
                                                                              template <typename T> struct FenwickTree {
    function \langle int(int) \rangle find = [&](int x) { return p[x] == x ? x :
                                                                                int size = 1, high_bit = 1;
     \leftrightarrow (p[x] = find(p[x])); \};
                                                                                vector<T> tree;
    auto merge = [\&](int x, int y) { p[find(x)] = find(y); };
                                                                                 FenwickTree(int _size) : size(_size) {
                                                                                   tree.resize(size + 1);

    Persistent version

                                                                                   while((high_bit << 1) <= size) high_bit <<= 1;</pre>
                                                                          6
    struct Node {
                                                                                FenwickTree(vector<T>& arr) : FenwickTree(arr.size()) {
2
      int lc, rc, p;
                                                                                   for(int i = 0; i < size; i++) update(i, arr[i]);</pre>
3
                                                                          10
                                                                                 int lower_bound(T x) {
    struct SegTree {
                                                                          11
5
       vector<Node> t = \{\{0, 0, -1\}\}; // init all
                                                                                   int res = 0; T cur = 0;
                                                                         12
      SegTree() = default;
                                                                                   for(int bit = high_bit; bit > 0; bit >>= 1) {
                                                                         13
                                                                                     if((res|bit) <= size && cur + tree[res|bit] < x) {</pre>
       SegTree(int n) { t.reserve(n * 20); }
                                                                                       res |= bit; cur += tree[res];
       int modify(int p, int 1, int r, int x, int v) {
                                                                         15
         // p: original node, update a[x] \rightarrow v
                                                                          16
10
                                                                                  }
         t.push_back(t[p]);
                                                                         17
         int u = (int)t.size() - 1;
                                                                                  return res;
12
                                                                         18
```

if (r - 1 == 1) {

if (x < m) {

} else {

return u;

return res;

int m = (1 + r) / 2;

t[u].rc = t[p].rc;

t[u].lc = t[p].lc;

t[u].lc = modify(t[p].lc, l, m, x, v);

t[u].rc = modify(t[p].rc, m, r, x, v);

t[u].p = t[t[u].lc].p + t[t[u].rc].p;

int query(int p, int l, int r, int x, int y) {

if (x < m) res += query(t[p].lc, l, m, x, y);

if (y > m) res += query(t[p].rc, m, r, x, y);

int get(int p, int x) { return seg.query(p, 0, n, x, x + 1);

// query sum a[x]...a[y-1] rooted at p

// t[p] holds the info of [l, r)if (x <= 1 && r <= y) return t[p].p;

int m = (1 + r) / 2, res = 0;

DSU(int _n) : n(_n), seg(n) {}

t[u].p = v;

} else {

13

14

15

16

17

19

20

21

22

23

24 25

26

27

28

29

31

32

33

34

35

36

38

39

40

41

42

}

struct DSU {

SegTree seg;

int n;

37 };

Fenwick2D Tree

-i)) tree[i] += delta; }

T prefix_sum(int i) {

return ret;

7

7

19

20

21

22

23

24

25

26

27 }:

```
struct Fenwick2D {
 ll n, m;
  vector<vector<ll>> a:
 Fenwick2D(11 _n, 11 _m) : n(_n), m(_m), a(n, vector<11>(m))
→ {}
  void add(ll x, ll y, ll v) {
    for (int i = x + 1; i \le n; i += i \& -i) {
      for (int j = y + 1; j \le m; j += j & -j) {
        (a[i - 1][j - 1] += v) \%= MOD;
   }
 }
  void add(ll x1, ll x2, ll y1, ll y2, ll v) {
    // [(x1, y1), (x2, y2))
    add(x1, y1, v);
    add(x1, y2, MOD - v), add(x2, y1, MOD - v);
    add(x2, y2, v);
```

for(i++; i > 0; i -= (i & -i)) ret += tree[i];

T range_sum(int l, int r) { return (l > r) ? 0 :

void update(int i, T delta) { for(i++; i <= size; i += (i &</pre>

→ prefix_sum(r) - prefix_sum(l - 1); }

9

10

11

12

13

```
}
                                                                                } else {
17
                                                                         30
       ll sum(ll x, ll y) { // [(0, 0), (x, y))
                                                                                   auto [x, y] = split(t->1, v);
18
                                                                         31
                                                                                  t->1 = y;
19
         11 \text{ ans} = 0;
                                                                         32
         for (int i = x; i > 0; i -= i & -i) {
                                                                                  t->pull();
20
                                                                         33
           for (int j = y; j > 0; j -= j & -j) {
                                                                                   return {x, t};
21
             (ans += a[i - 1][j - 1]) \% = MOD;
22
                                                                         35
23
                                                                         36
         }
24
                                                                         37
                                                                              Node *merge(Node *p, Node *q) {
25
         return ans;
                                                                         38
26
      }
                                                                                if (p == nullptr) return q;
                                                                                if (q == nullptr) return p;
    }:
                                                                         40
                                                                                if (p->w < q->w) swap(p, q);
                                                                         41
                                                                                auto [x, y] = split(q, p->s + rng() \% 2);
                                                                         42
    PBDS
                                                                                p->push();
                                                                         43
                                                                                p->1 = merge(p->1, x);
    #include <bits/stdc++.h>
                                                                                p->r = merge(p->r, y);
                                                                         45
    #include <ext/pb_ds/assoc_container.hpp>
                                                                                p->pull();
    using namespace std;
                                                                         47
                                                                                return p;
    using namespace __gnu_pbds;
                                                                         48
    template<typename T>
                                                                         49
    using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
                                                                              Node *insert(Node *t, int v) {
                                                                         50

→ tree order statistics node update>;

                                                                                auto [x, y] = split(t, v);
    template<typename T, typename X>
                                                                                return merge(merge(x, new Node(v)), y);
                                                                         52
    using ordered_map = tree<T, X, less<T>, rb_tree_tag,

→ tree_order_statistics_node_update>;

                                                                         54
    template<typename T, typename X>
                                                                              Node *erase(Node *t, int v) {
                                                                         55
    using fast_map = cc_hash_table<T, X>;
                                                                                auto [x, y] = split(t, v);
                                                                         56
                                                                                auto [p, q] = split(y, v + 1);
    template<typename T, typename X>
                                                                         57
    using ht = gp_hash_table<T, X>;
12
                                                                                return merge(merge(x, merge(p->1, p->r)), q);
    mt19937 64
     \leftrightarrow rng(chrono::steady_clock::now().time_since_epoch().count()); _{60}
14
                                                                              int get_rank(Node *&t, int v) {
    struct splitmix64 {
15
                                                                                auto [x, y] = split(t, v);
         size_t operator()(size_t x) const {
16
                                                                                int res = (x ? x->sz : 0) + 1;
             static const size_t fixed =
                                                                                t = merge(x, y);
                                                                         64
         chrono::steady_clock::now().time_since_epoch().count();
                                                                                return res;
                                                                         65
             x += 0x9e3779b97f4a7c15 + fixed;
18
                                                                         66
             x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;

x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
19
                                                                         67
20
                                                                              Node *kth(Node *t, int k) {
             return x \hat{} (x >> 31);
21
                                                                         69
22
                                                                                while (true) {
                                                                         70
    };
                                                                                  int left_sz = t->1 ? t->1->sz : 0;
                                                                         71
                                                                                  if (k < left_sz) {</pre>
                                                                         72
                                                                                    t = t->1;
     Treap
                                                                                  } else if (k == left_sz) {
                                                                         74
                                                                                    return t;
       • (No rotation version)
                                                                                  } else {
                                                                         76
                                                                         77
                                                                                    k -= left_sz + 1, t = t->r;
    struct Node {
                                                                         78
       Node *1, *r;
                                                                                }
                                                                         79
       int s, sz;
                                                                              }
                                                                         80
       // int t = 0, a = 0, g = 0; // for lazy propagation
                                                                         81
                                                                              Node *get_prev(Node *&t, int v) {
                                                                                auto [x, y] = split(t, v);
                                                                         83
      Node(int _s) : l(nullptr), r(nullptr), s(_s), sz(1),
                                                                                Node *res = kth(x, x->sz);
                                                                         84
     \rightarrow w(rng()) {}
                                                                                t = merge(x, y);
                                                                         85
       void apply(int vt, int vg) {
                                                                         86
                                                                                return res;
         // for lazy propagation
         // s -= vt;
10
                                                                         88
         // t += vt, a += vg, g += vg;
11
                                                                         89
                                                                              Node *get_next(Node *&t, int v) {
12
                                                                         90
                                                                                auto [x, y] = split(t, v + 1);
       void push() {
                                                                                Node *res = kth(y, 1);
                                                                         91
        // for lazy propagation
14
                                                                                t = merge(x, y);
         // if (l != nullptr) l->apply(t, g);
15
                                                                         93
                                                                                return res:
         // if (r != nullptr) r->apply(t, g);
16
                                                                         94
         // t = g = 0;
17

    USAGE

      void pull() { sz = 1 + (1 ? 1->sz : 0) + (r ? r->sz : 0); }
19
                                                                              int main() {
20
21
                                                                                cin.tie(nullptr)->sync_with_stdio(false);
    std::pair<Node *, Node *> split(Node *t, int v) {
                                                                                int n;
22
23
       if (t == nullptr) return {nullptr, nullptr};
                                                                                cin >> n;
                                                                                Node *t = nullptr;
       t->push();
24
       if (t->s < v) {
                                                                                for (int op, x; n--;) {
         auto [x, y] = split(t->r, v);
                                                                                  cin >> op >> x;
26
         t->r = x;
                                                                                  if (op == 1) {
27
         t->pull();
                                                                                   t = insert(t, x);
28
                                                                          9
         return {t, y};
                                                                                  } else if (op == 2) {
                                                                          10
```

```
t = erase(t, x);
11
         } else if (op == 3) {
12
           cout << get_rank(t, x) << "\n";</pre>
13
         } else if (op == 4) {
14
           cout << kth(t, x)->s << "\n";
         } else if (op == 5) {
16
17
           cout << get_prev(t, x)->s << "\n";
         } else {
           cout << get_next(t, x)->s << "\n";</pre>
19
20
      }
21
    }
    Implicit treap
```

• Split by size

struct Node {

```
Node *1, *r;
      int s, sz;
       // int lazy = 0;
      11 w:
      Node(int _s) : l(nullptr), r(nullptr), s(_s), sz(1),
     \rightarrow w(rnd()) {}
       void apply() {
         // for lazy propagation
9
         // lazy ^= 1;
10
       }
11
       void push() {
12
13
         // for lazy propagation
         // if (lazy) {
14
        // swap(l, r);
15
         // if (l != nullptr) l->apply();
             if (r != nullptr) r->apply();
         //
17
18
             lazy = 0;
        // }
19
20
       void pull() { sz = 1 + (1 ? 1->sz : 0) + (r ? r->sz : 0); }
21
22
    std::pair<Node *, Node *> split(Node *t, int v) {
24
      // first -> sz == v
25
       if (t == nullptr) return {nullptr, nullptr};
26
       t->push();
27
       int left_sz = t->1 ? t->1->sz : 0;
       if (left_sz < v) {</pre>
29
         auto [x, y] = split(t->r, v - left_sz - 1);
         t->r = x;
31
32
         t->pull();
         return {t, y};
33
34
       } else {
         auto [x, y] = split(t->1, v);
         t->1 = y;
36
         t->pull();
37
38
         return {x, t};
39
40
    }
41
    Node *merge(Node *p, Node *q) {
42
       if (p == nullptr) return q;
43
       if (q == nullptr) return p;
44
       if (p->w < q->w) {
         p->push();
46
47
         p->r = merge(p->r, q);
         p->pull();
48
        return p;
49
       } else {
50
         q->push();
51
         q->1 = merge(p, q->1);
52
         q->pull();
53
         return q;
54
55
      }
    }
56
```

Persistent implicit treap

```
pair<Node *, Node *> split(Node *t, int v) {
2
      // first->sz == v
      if (t == nullptr) return {nullptr, nullptr};
      t->push();
      int left_sz = t->1 ? t->1->sz : 0;
      t = new Node(*t);
      if (left_sz < v) {</pre>
         auto [x, y] = split(t->r, v - left_sz - 1);
         t->r = x:
         t->pull();
         return {t, y};
11
       } else {
12
         auto [x, y] = split(t->1, v);
13
         t->1 = v;
14
         t->pull();
16
         return {x, t};
17
    }
18
19
    Node *merge(Node *p, Node *q) {
      if (p == nullptr) return new Node(*q);
21
22
       if (q == nullptr) return new Node(*p);
      if (p->w < q->w) {
23
        p = new Node(*p);
24
        p->push();
         p->r = merge(p->r, q);
26
         p->pull();
28
        return p;
      } else {
29
30
         q = new Node(*q);
31
         q->push();
         q->1 = merge(p, q->1);
32
33
         q->pull();
34
         return q;
35
36
```

2D Sparse Table

Sorry that this sucks - askd

```
template <class T, class Compare = less<T>>
struct SparseTable2d {
 int n = 0, m = 0;
 T**** table;
 int* log;
  inline T choose(T x, T y) {
   return Compare()(x, y) ? x : y;
  SparseTable2d(vector<vector<T>>& grid) {
   if(grid.empty() || grid[0].empty()) return;
    n = grid.size(); m = grid[0].size();
   log = new int[max(n, m) + 1];
    log[1] = 0;
    for(int i = 2; i <= max(n, m); i++)
      log[i] = log[i - 1] + ((i ^ (i - 1)) > i);
    table = new T***[n];
    for(int i = n - 1; i >= 0; i--) {
     table[i] = new T**[m];
     for(int j = m - 1; j >= 0; j--) {
       table[i][j] = new T*[log[n - i] + 1];
       for(int k = 0; k <= log[n - i]; k++) {
          table[i][j][k] = new T[log[m - j] + 1];
          if(!k) table[i][j][k][0] = grid[i][j];
         else table[i][j][k][0] = choose(table[i][j][k-1][0],
   table[i+(1<<(k-1))][j][k-1][0]);
          for(int 1 = 1; 1 <= log[m - j]; 1++)
            table[i][j][k][l] = choose(table[i][j][k][l-1],
   table[i][j+(1<<(l-1))][k][l-1]);
   }
  T query(int r1, int r2, int c1, int c2) {
    assert(r1 >= 0 && r2 < n && r1 <= r2);
```

3

9

10

11

12

13

14

15

16

17

19

21

22

23

24

25

26

27

28

29

30

31

```
assert(c1 >= 0 \&\& c2 < m \&\& c1 <= c2);
                                                                                 if (rg.lx >= rec.lx && rg.rx <= rec.rx && rg.ly >= rec.ly
33
                                                                        51
         int rl = log[r2 - r1 + 1], cl = log[c2 - c1 + 1];
                                                                                 && rg.ry <= rec.ry) {
34
         T ca1 = choose(table[r1][c1][r1][c1],
                                                                         52
                                                                                   return nodes[id].num;
        table[r2-(1<<rl)+1][c1][r1][c1]);
                                                                                 }
                                                                        53
         T ca2 = choose(table[r1][c2-(1<<c1)+1][r1][c1],
                                                                                  int ans = 0;
     \leftrightarrow table[r2-(1<<rl)+1][c2-(1<<cl)+1][r1][c1]);
                                                                                 if (depth % 2) { // pruning
                                                                        55
         return choose(ca1, ca2);
                                                                        56
                                                                                   if (rec.lx <= nodes[id].point.x) ans +=</pre>
37
      }

    inner_query(nodes[id].lc, rec, depth + 1);

38
    };
                                                                                   if (rec.rx >= nodes[id].point.x) ans +=
                                                                        57
39

    inner_query(nodes[id].rc, rec, depth + 1);

    USAGE

                                                                                 } else {
                                                                         58
                                                                                    if (rec.ly <= nodes[id].point.y) ans +=</pre>
                                                                         59
    vector<vector<int>> test = {

    inner_query(nodes[id].lc, rec, depth + 1);

      \{1, 2, 3, 4\}, \{2, 3, 4, 5\}, \{9, 9, 9, 9\}, \{-1, -1, -1, -1\}
2
                                                                                    if (rec.ry >= nodes[id].point.y) ans +=
                                                                                 inner_query(nodes[id].rc, rec, depth + 1);
                                                                         61
    SparseTable2d<int> st(test);
                                                   // Range min query
                                                                                  if (is_in(nodes[id].point, rec)) ans += 1;
    SparseTable2d<int,greater<int>> st2(test); // Range max query
                                                                        63
                                                                                  return ans;
                                                                               int query(const Rectangle &rec) { return inner_query(root,
    K-D Tree
                                                                              \rightarrow rec, 0); }
    struct Point {
1
2
      int x, y;
3
                                                                             Link/Cut Tree
    struct Rectangle {
5
      int lx, rx, ly, ry;
6
                                                                             struct Node {
                                                                               Node *ch[2], *p;
    bool is_in(const Point &p, const Rectangle &rg) {
                                                                               int id:
      return (p.x >= rg.lx) && (p.x <= rg.rx) && (p.y >= rg.ly) &&
                                                                               bool rev;
                                                                               Node(int id) : ch{nullptr, nullptr}, p(nullptr), id(id),
         (p.y <= rg.ry);
10

→ rev(false) {}
                                                                               friend void reverse(Node *p) {
11
                                                                                 if (p != nullptr) {
    struct KDTree {
12
      vector<Point> points;
                                                                                    swap(p->ch[0], p->ch[1]);
13
      struct Node {
                                                                                    p->rev ^= 1;
14
                                                                         9
         int lc, rc;
                                                                         10
         Point point;
16
                                                                        11
         Rectangle range;
                                                                                void push() {
17
                                                                        12
18
         int num;
                                                                         13
                                                                                 if (rev) {
      };
                                                                                   reverse(ch[0]);
19
                                                                         14
      vector<Node> nodes;
                                                                                    reverse(ch[1]);
20
                                                                         15
       int root = -1:
                                                                                    rev = false:
21
                                                                        16
       KDTree(const vector<Point> &points_) {
22
                                                                         17
                                                                               }
23
         points = points_;
                                                                         18
24
         Rectangle range = {-1e9, 1e9, -1e9, 1e9};
                                                                         19
                                                                               void pull() {}
         root = tree_construct(0, (int)points.size(), range, 0);
                                                                               bool is_root() { return p == nullptr || p->ch[0] != this &&
25

    p->ch[1] != this; }

26
      int tree_construct(int 1, int r, Rectangle range, int depth)
                                                                               bool pos() { return p->ch[1] == this; }
                                                                               void rotate() {
     22
                                                                                 Node *q = p;
         if (1 == r) return -1;
                                                                        23
28
         if (1 > r) throw;
                                                                                 bool x = !pos();
29
                                                                        24
                                                                                  q->ch[!x] = ch[x];
         int mid = (1 + r) / 2;
30
                                                                        25
         auto comp = (depth % 2) ? [](Point &a, Point &b) { return
                                                                                  if (ch[x] != nullptr) ch[x] -> p = q;
     \rightarrow a.x < b.x; }
                                                                        27
                                                                                 p = q->p;
                                  : [](Point &a, Point &b) { return
                                                                                 if (!q->is\_root()) q->p->ch[q->pos()] = this;
32
     \rightarrow a.y < b.y; };
                                                                                  ch[x] = q;
         nth_element(points.begin() + 1, points.begin() + mid,
                                                                                  q->p = this;
33
     → points.begin() + r, comp);
                                                                                 pull();
                                                                         31
         Rectangle l_range(range), r_range(range);
34
                                                                        32
                                                                                  q->pull();
         if (depth % 2) {
                                                                         33
           l_range.rx = points[mid].x;
                                                                                void splay() {
36
                                                                        34
           r_range.lx = points[mid].x;
                                                                                  vector<Node *> s;
37
                                                                        35
38
         } else {
                                                                                 for (Node *i = this; !i->is_root(); i = i->p)
           1_range.ry = points[mid].y;

    s.push_back(i→p);
39
           r_range.ly = points[mid].y;
                                                                                  while (!s.empty()) s.back()->push(), s.pop_back();
40
41
                                                                                 push();
         Node node = {tree_construct(1, mid, 1_range, depth + 1),
                                                                                  while (!is_root()) {
42
                                                                        39
                      tree_construct(mid + 1, r, r_range, depth +
                                                                                    if (!p->is_root()) {
43
        1), points[mid], range, r - 1);
                                                                                      if (pos() == p->pos()) {
                                                                        41
44
         nodes.push_back(node);
                                                                         42
                                                                                        p->rotate();
         return (int)nodes.size() - 1;
                                                                                      } else {
45
                                                                         43
                                                                                        rotate();
46
                                                                                      }
47
                                                                         45
       int inner_query(int id, const Rectangle &rec, int depth) {
48
                                                                         46
         if (id == -1) return 0;
                                                                                    rotate();
49
                                                                        47
         Rectangle rg = nodes[id].range;
                                                                         48
```

```
pull();
49
50
51
       void access() {
         for (Node *i = this, *q = nullptr; i != nullptr; q = i, i
52
        = i->p) {
          i->splay();
53
           i->ch[1] = q;
54
           i->pull();
55
56
         splay();
57
       }
58
       void makeroot() {
59
60
         access():
         reverse(this);
61
      }
62
    }:
63
64
    void link(Node *x, Node *y) {
65
      x->makeroot();
      x->p = y;
66
    7
67
    void split(Node *x, Node *y) {
68
       x->makeroot();
69
      y->access();
70
    void cut(Node *x, Node *y) {
72
       split(x, y);
73
       x->p = y->ch[0] = nullptr;
74
      y->pull();
75
    }
76
    bool connected(Node *p, Node *q) {
77
78
         p->access();
79
         q->access();
         return p->p != nullptr;
80
    }
81
```

Geometry

Basic stuff

```
using ll = long long;
    using ld = long double;
    constexpr auto eps = 1e-8;
    const auto PI = acos(-1);
    int sgn(1d x) \{ return (abs(x) \le eps) ? 0 : (x < 0 ? -1 : 1); 
    struct Point {
      1d x = 0, y = 0;
      Point() = default;
      Point(ld _x, ld _y) : x(_x), y(_y) {}
11
      bool operator < (const Point &p) const { return !sgn(p.x - x)
     \rightarrow ? sgn(y - p.y) < 0 : x < p.x; }
      bool operator==(const Point &p) const { return !sgn(p.x - x)
     Point operator+(const Point &p) const { return {x + p.x, y +
     \rightarrow p.y}; }
      Point operator-(const Point &p) const { return {x - p.x, y -
15
      → p.y}; }
      Point operator*(ld a) const { return {x * a, y * a}; }
16
      Point operator/(ld a) const { return {x / a, y / a}; }
      auto operator*(const Point &p) const { return x * p.x + y *
     \hookrightarrow p.y; } // dot
      auto operator^(const Point &p) const { return x * p.y - y *

    p.x; } // cross

      friend auto &operator>>(istream &i, Point &p) { return i >>
20
     \rightarrow p.x >> p.y; }
      friend auto &operator<<(ostream &o, Point p) { return o <<</pre>
21

    p.x << ' ' << p.y; }
</pre>
    }:
22
23
    struct Line {
24
      Point s = \{0, 0\}, e = \{0, 0\};
25
      Line() = default;
26
      Line(Point _s, Point _e) : s(_s), e(_e) {}
```

```
friend auto &operator>>(istream &i, Line &1) { return i >>
     \leftrightarrow 1.s >> 1.e; } // ((x1, y1), (x2, y2)
    }:
29
30
    struct Segment : Line {
      using Line::Line;
32
33
34
    struct Circle {
35
      Point o = \{0, 0\};
      ld r = 0;
37
       Circle() = default;
      Circle(Point _o, ld _r) : o(_o), r(_r) {}
39
40
    auto dist2(const Point &a) { return a * a; }
    auto dist2(const Point &a, const Point &b) { return dist2(a -

    b); }

    auto dist(const Point &a) { return sqrt(dist2(a)); }
    auto dist(const Point &a, const Point &b) { return

    sqrt(dist2(a - b)); }

    auto dist(const Point &a, const Line &l) { return abs((a -
     \hookrightarrow l.s) ^ (l.e - l.s)) / dist(l.s, l.e); }
    auto dist(const Point &p, const Segment &1) {
      if (1.s == 1.e) return dist(p, 1.s);
      auto d = dist2(1.s, 1.e), t = min(d, max((1d)0, (p - 1.s) *)
     return dist((p - 1.s) * d, (1.e - 1.s) * t) / d;
9
10
     /* Needs is_intersect
11
    auto dist(const Segment &l1, const Segment &l2) {
12
      if (is_intersect(l1, l2)) return (ld)0;
      return min({dist(l1.s, l2), dist(l1.e, l2), dist(l2.s, l1),
14
     \leftrightarrow dist(l2.e, l1)});
    } */
15
    Point perp(const Point &p) { return Point(-p.y, p.x); }
17
18
    auto rad(const Point &p) { return atan2(p.y, p.x); }
```

Transformation

```
Point project(const Point &p, const Line &1) {
  return 1.s + ((1.e - 1.s) * ((1.e - 1.s) * (p - 1.s))) /
\hookrightarrow dist2(l.e - l.s);
Point reflect(const Point &p, const Line &1) {
  return project(p, 1) * 2 - p;
Point dilate(const Point &p, ld scale_x = 1, ld scale_y = 1) {

→ return Point(p.x * scale_x, p.y * scale_y); }

Line dilate(const Line &1, ld scale_x = 1, ld scale_y = 1) {

→ return Line(dilate(1.s, scale_x, scale_y), dilate(1.e,

    scale_x, scale_y)); }

Segment dilate(const Segment &1, ld scale_x = 1, ld scale_y =

    dilate(l.e, scale_x, scale_y)); }

vector<Point> dilate(const vector<Point> &p, ld scale_x = 1,
 \rightarrow ld scale_y = 1) {
 int n = p.size();
  vector<Point> res(n);
  for (int i = 0; i < n; i++)
   res[i] = dilate(p[i], scale_x, scale_y);
  return res;
}
Point rotate(const Point &p, ld a) { return Point(p.x * cos(a)
 \rightarrow - p.y * sin(a), p.x * sin(a) + p.y * cos(a)); }
Line rotate(const Line &1, ld a) { return Line(rotate(1.s, a),

→ rotate(l.e, a)); }
Segment rotate(const Segment &1, ld a) { return

→ Segment(rotate(l.s, a), rotate(l.e, a)); }

Circle rotate(const Circle &c, ld a) { return
vector<Point> rotate(const vector<Point> &p, ld a) {
```

13

16

17

```
auto d1 = sgn((a.e - a.s) \hat{ } (b.s - a.s)), d2 = sgn((a.e - a.s))
      int n = p.size();
25
                                                                       40
      vector<Point> res(n);
                                                                             \rightarrow a.s) ^ (b.e - a.s));
26
                                                                             if (d1 * d2 < 0) return 2; // intersect at non-end point
      for (int i = 0; i < n; i++)
27
                                                                        41
        res[i] = rotate(p[i], a);
                                                                              return d1 == 0 || d2 == 0;
                                                                       42
28
      return res:
29
    }
30
                                                                       44
31
                                                                        45
                                                                            Point intersect(const Line &a, const Line &b) {
    Point translate(const Point &p, ld dx = 0, ld dy = 0) { return
                                                                              auto u = a.e - a.s, v = b.e - b.s;
     \rightarrow Point(p.x + dx, p.y + dy); }
                                                                              auto t = ((b.s - a.s) ^ v) / (u ^ v);
                                                                        47
    Line translate(const Line &1, ld dx = 0, ld dy = 0) { return
                                                                              return a.s + u * t;
     49
    Segment translate(const Segment &1, ld dx = 0, ld dy = 0) {
                                                                       50
                                                                            int is_intersect(const Circle &c, const Line &l) {

→ return Segment(translate(1.s, dx, dy), translate(1.e, dx,
                                                                       51
     \rightarrow dy)); }
                                                                              auto d = dist(c.o, 1);
                                                                        52
    Circle translate(const Circle &c, ld dx = 0, ld dy = 0) {
                                                                              return sgn(d - c.r) < 0 ? 2 : !sgn(d - c.r);

→ return Circle(translate(c.o, dx, dy), c.r); }
                                                                       54
    vector<Point> translate(const vector<Point> &p, ld dx = 0, ld
     \rightarrow dy = 0) {
                                                                            vector<Point> intersect(const Circle &a, const Circle &b) {
                                                                       56
      int n = p.size();
                                                                              auto relation = get_relation(a, b);
37
                                                                        57
      vector<Point> res(n);
                                                                              if (relation == Relation::INSIDE || relation ==
38
      for (int i = 0; i < n; i++)
                                                                             ⇔ Relation::SEPARATE) return {};
39
        res[i] = translate(p[i], dx, dy);
                                                                              auto vec = b.o - a.o;
                                                                       59
                                                                              auto d2 = dist2(vec);
41
      return res;
                                                                       60
                                                                              auto p = (d2 + a.r * a.r - b.r * b.r) / ((long double)2 *
    }
                                                                             \hookrightarrow d2), h2 = a.r * a.r - p * p * d2;
                                                                              auto mid = a.o + vec * p, per = perp(vec) * sqrt(max((long
                                                                        62

    double)0, h2) / d2);

    Relation
                                                                              if (relation == Relation::OVERLAP)
                                                                        63
                                                                                return {mid + per, mid - per};
    enum class Relation { SEPARATE, EX_TOUCH, OVERLAP, IN_TOUCH,
                                                                       65
                                                                              else
     → INSIDE }:
                                                                                return {mid};
                                                                       66
    Relation get_relation(const Circle &a, const Circle &b) {
                                                                            }
                                                                       67
      auto c1c2 = dist(a.o, b.o);
                                                                       68
      auto r1r2 = a.r + b.r, diff = abs(a.r - b.r);
                                                                            vector<Point> intersect(const Circle &c, const Line &l) {
       if (sgn(c1c2 - r1r2) > 0) return Relation::SEPARATE;
                                                                              if (!is_intersect(c, 1)) return {};
                                                                        70
       if (sgn(c1c2 - r1r2) == 0) return Relation::EX_TOUCH;
                                                                              auto v = 1.e - 1.s, t = v / dist(v);
                                                                        71
      if (sgn(c1c2 - diff) > 0) return Relation::OVERLAP;
                                                                              Point a = 1.s + t * ((c.o - 1.s) * t);
                                                                        72
       if (sgn(c1c2 - diff) == 0) return Relation::IN_TOUCH;
                                                                        73
                                                                              auto d = sqrt(max((ld)0, c.r * c.r - dist2(c.o, a)));
      return Relation::INSIDE;
9
                                                                              if (!sgn(d)) return {a};
10
                                                                              return {a - t * d, a + t * d};
                                                                        75
11
    auto get_cos_from_triangle(ld a, ld b, ld c) { return (a * a +
12
     \rightarrow b * b - c * c) / (2.0 * a * b); }
                                                                            int in_poly(const vector<Point> &p, const Point &a) {
                                                                        78
13
                                                                              int cnt = 0, n = (int)p.size();
    bool on_line(const Line &1, const Point &p) { return !sgn((1.s
14
                                                                              for (int i = 0; i < n; i++) {
                                                                        80
     \rightarrow - p) ^ (1.e - p)); }
                                                                                auto q = p[(i + 1) \% n];
15
                                                                                if (on_segment(Segment(p[i], q), a)) return 1; // on the
                                                                        82
    bool on_segment(const Segment &1, const Point &p) {
                                                                             \rightarrow edge of the polygon
     return !sgn((1.s - p) ^ (1.e - p)) && sgn((1.s - p) * (1.e -
17
                                                                        83
                                                                                cnt \hat{} = ((a.y < p[i].y) - (a.y < q.y)) * ((p[i] - a) \hat{} (q -

    p)) <= 0;
</pre>
                                                                             \rightarrow a)) > 0;
18
                                                                              }
19
                                                                              return cnt ? 2 : 0;
                                                                        85
    bool on_segment2(const Segment &1, const Point &p) { // assume
                                                                            }
     \hookrightarrow p on Line l
      if (1.s == p || 1.e == p) return true;
21
                                                                        88
                                                                            int is_intersect(const vector<Point> &p, const Line &a) {
      if (\min(l.s, l.e)  return true;
22
                                                                              // 1: touching, >=2: intersect count
23
                                                                              int cnt = 0, edge_cnt = 0, n = (int)p.size();
                                                                       90
24
                                                                              for (int i = 0; i < n; i++) {
25
                                                                                auto q = p[(i + 1) \% n];
                                                                        92
    bool is_parallel(const Line &a, const Line &b) { return
                                                                                if (on_line(a, p[i]) && on_line(a, q)) return -1; //
                                                                       93
     \rightarrow !sgn((a.s - a.e) ^ (b.s - b.e)); }
                                                                             bool is_orthogonal(const Line &a, const Line &b) { return
                                                                                auto t = is_intersect(a, Segment(p[i], q));
                                                                       94
     \rightarrow !sgn((a.s - a.e) * (b.s - b.e)); }
                                                                                (t == 1) && edge_cnt++, (t == 2) && cnt++;
                                                                        95
                                                                       96
29
    int is_intersect(const Segment &a, const Segment &b) {
                                                                       97
                                                                              return cnt + edge_cnt / 2;
     auto d1 = sgn((a.e - a.s) ^ (b.s - a.s)), d2 = sgn((a.e - a.s))
30
                                                                       98
     \rightarrow a.s) ^ (b.e - a.s));
                                                                       99
     auto d3 = sgn((b.e - b.s) ^ (a.s - b.s)), d4 = sgn((b.e - b.s))
                                                                            vector<Point> tangent(const Circle &c, const Point &p) {
                                                                       100
     \rightarrow b.s) ^ (a.e - b.s));
                                                                             auto d = dist(c.o, p), l = c.r * c.r / d, h = sqrt(c.r * c.r)
                                                                       101
     if (d1 * d2 < 0 && d3 * d4 < 0) return 2; // intersect at
                                                                             \rightarrow -1 * 1);

→ non-end point

                                                                             auto v = (p - c.o) / d;
                                                                       102
33
      return (d1 == 0 && sgn((b.s - a.s) * (b.s - a.e)) <= 0) ||
                                                                              return {c.o + v * 1 + perp(v) * h, c.o + v * 1 - perp(v) *
                                                                       103
              (d2 == 0 \&\& sgn((b.e - a.s) * (b.e - a.e)) <= 0) ||
34
              (d3 == 0 \&\& sgn((a.s - b.s) * (a.s - b.e)) <= 0) ||
35
                                                                            }
                                                                       104
              (d4 == 0 \&\& sgn((a.e - b.s) * (a.e - b.e)) <= 0);
36
37
                                                                            Circle get circumscribed(const Point &a. const Point &b. const
                                                                       106
                                                                             → Point &c) {
```

int is_intersect(const Line &a, const Segment &b) {

```
Line u((a + b) / 2, ((a + b) / 2) + perp(b - a));
                                                                                                                return asr(_l, _r, simpson(_l, _r));
107
                                                                                                      41
          Line v((b + c) / 2, ((b + c) / 2) + perp(c - b));
                                                                                                      42
108
109
          auto o = intersect(u, v);
                                                                                                       43
          return Circle(o, dist(o, a));
                                                                                                              vector<Point> half_plane_intersect(vector<Line> &L) {
110
                                                                                                       44
                                                                                                                 int n = (int)L.size(), l = 0, r = 0; // [left, right]
111
                                                                                                                 sort(L.begin(), L.end(),
112
                                                                                                       46
                                                                                                                        [](const Line &a, const Line &b) { return rad(a.s -
113
       Circle get_inscribed(const Point &a, const Point &b, const
                                                                                                       47
                                                                                                                   a.e) < rad(b.s - b.e); });
        → Point &c) {
          auto 11 = dist(b - c), 12 = dist(c - a), 13 = dist(a - b);
                                                                                                                vector<Point> p(n), res;
114
                                                                                                       48
115
          Point o = (a * 11 + b * 12 + c * 13) / (11 + 12 + 13);
                                                                                                                vector<Line> q(n);
          return Circle(o, dist(o, Line(a, b)));
                                                                                                                q[0] = L[0];
116
                                                                                                       50
                                                                                                                 for (int i = 1; i < n; i++) {
117
                                                                                                       51
118
                                                                                                                   while (l < r \&\& sgn((L[i].e - L[i].s) ^ (p[r - 1] -
       pair<ld, ld> get_centroid(const vector<Point> &p) {
                                                                                                               \hookrightarrow L[i].s)) <= 0) r--;
119
           int n = (int)p.size();
                                                                                                                    while (1 < r \&\& sgn((L[i].e - L[i].s) ^ (p[1] - L[i].s))
120
          ld x = 0, y = 0, sum = 0;
                                                                                                               121
122
           auto a = p[0], b = p[1];
                                                                                                       54
                                                                                                                   q[++r] = L[i];
                                                                                                                    if (sgn((q[r].e - q[r].s) ^ (q[r - 1].e - q[r - 1].s)) ==
          for (int i = 2; i < n; i++) {
123
                                                                                                       55
             auto c = p[i];
124
             auto s = area({a, b, c});
125
                                                                                                       56
             sum += s;
                                                                                                                      if (sgn((q[r].e - q[r].s) ^ (L[i].s - q[r].s)) > 0) q[r]
126
                                                                                                       57
             x += s * (a.x + b.x + c.x);
                                                                                                                  = L[i];
127
             y += s * (a.y + b.y + c.y);
128
                                                                                                       58
129
             swap(b, c);
                                                                                                       59
                                                                                                                   if (1 < r) p[r - 1] = intersect(q[r - 1], q[r]);
130
                                                                                                       60
                                                                                                                while (1 < r && sgn((q[1].e - q[1].s) \hat{} (p[r - 1] - q[1].s))
          return \{x / (3 * sum), y / (3 * sum)\};
131
                                                                                                       61
                                                                                                               132
                                                                                                               if (r - 1 <= 1) return {};
                                                                                                       62
                                                                                                                p[r] = intersect(q[r], q[1]);
        \mathbf{Area}
                                                                                                       64
                                                                                                                return vector<Point>(p.begin() + 1, p.begin() + r + 1);
                                                                                                       65
       auto area(const vector<Point> &p) {
           int n = (int)p.size();
          long double area = 0;
          for (int i = 0; i < n; i++) area += p[i] ^ p[(i + 1) % n];
                                                                                                              Convex
          return area / 2.0;
                                                                                                             vector<Point> get_convex(vector<Point> &points, bool
  6
                                                                                                               → allow_collinear = false) {
                                                                                                                // strict, no repeat, two pass
       auto area(const Point &a, const Point &b, const Point &c) {
          return ((long double)((b - a) ^ (c - a))) / 2.0;
                                                                                                                sort(points.begin(), points.end());
 10
                                                                                                                points.erase(unique(points.begin(), points.end()),

→ points.end());
 11
       auto area2(const Point &a, const Point &b, const Point &c) {
                                                                                                                vector<Point> L, U;

    return (b - a) ^ (c - a); }

                                                                                                                for (auto &t : points) {
                                                                                                                   for (ll sz = L.size(); sz > 1 && (sgn((t - L[sz - 2]) ^
 13
       auto area_intersect(const Circle &c, const vector<Point> &ps)
                                                                                                               \leftrightarrow (L[sz - 1] - L[sz - 2])) >= 0);
                                                                                                                           L.pop_back(), sz = L.size()) {
         int n = (int)ps.size();
         auto arg = [&](const Point &p, const Point &q) { return
                                                                                                                   L.push_back(t);
                                                                                                       10
        \rightarrow atan2(p ^ q, p * q); };
                                                                                                                7
                                                                                                       11
         auto tri = [&](const Point &p, const Point &q) {
                                                                                                                for (auto &t : points) {
 17
                                                                                                       12
             auto r2 = c.r * c.r / (long double)2;
                                                                                                                   for (ll sz = U.size(); sz > 1 && (sgn((t - U[sz - 2]) ^{\circ}
 18
                                                                                                       13
                                                                                                                   (U[sz - 1] - U[sz - 2])) <= 0);
             auto d = q - p;
             auto a = d * p / dist2(d), b = (dist2(p) - c.r * c.r) /
                                                                                                                           U.pop_back(), sz = U.size()) {
 20
                                                                                                       14

→ dist2(d);
             long double det = a * a - b;
                                                                                                                   U.push_back(t);
 21
                                                                                                       16
 22
             if (sgn(det) <= 0) return arg(p, q) * r2;</pre>
                                                                                                       17
                                                                                                                // contain repeats if all collinear, use a set to remove
             auto s = max((long double)0, -a - sqrt(det)), t =

    min((long double)1, -a + sqrt(det));

→ repeats

             if (sgn(t) < 0 \mid \mid sgn(1 - s) \le 0) return arg(p, q) * r2;
                                                                                                                if (allow_collinear) {
 24
             auto u = p + d * s, v = p + d * t;
                                                                                                                   for (int i = (int)U.size() - 2; i >= 1; i--)
 25
             return arg(p, u) * r2 + (u ^ v) / 2 + arg(v, q) * r2;
                                                                                                               } else {
 27
          long double sum = 0;
                                                                                                                    set<Point> st(L.begin(), L.end());
 28
          for (int i = 0; i < n; i++) sum += tri(ps[i] - c.o, ps[(i + c.
                                                                                                                    for (int i = (int)U.size() - 2; i >= 1; i--) {
        \hookrightarrow 1) % n] - c.o);
                                                                                                                      if (st.count(U[i]) == 0) L.push_back(U[i]),
         return sum;
                                                                                                                   st.insert(U[i]);
 30
       }
 31
                                                                                                       25
                                                                                                                   }
                                                                                                                }
 32
                                                                                                       26
       auto adaptive_simpson(ld _1, ld _r, function<ld(ld)> f) {
                                                                                                                return L;
 33
                                                                                                       27
         auto simpson = [\&] (ld l, ld r) { return (r - 1) * (f(1) + 4
                                                                                                       28
 34
        + * f((1 + r) / 2) + f(r)) / 6; };
         function<ld(ld, ld, ld)> asr = [\&](ld l, ld r, ld s) {
                                                                                                             vector<Point> get_convex2(vector<Point> &points, bool
 35
             auto mid = (1 + r) / 2;
                                                                                                               \hookrightarrow allow_collinear = false) { // strict, no repeat, one pass
 36
             auto left = simpson(1, mid), right = simpson(mid, r);
                                                                                                                nth_element(points.begin(), points.begin(), points.end());
 37
                                                                                                       31
             if (!sgn(left + right - s)) return left + right;
                                                                                                                sort(points.begin() + 1, points.end(), [&](const Point &a,
 38
                                                                                                       32
             return asr(1, mid, left) + asr(mid, r, right);
                                                                                                               39
          }:
                                                                                                                    int rad_diff = sgn((a - points[0]) ^ (b - points[0]));
                                                                                                       33
```

```
return !rad_diff ? (dist2(a - points[0]) < dist2(b -</pre>
                                                                                                            void polar_sort(RandomIt first, RandomIt last, Point origin =
                                                                                                     100
           points[0])) : (rad_diff > 0);
                                                                                                              ⇔ Point(0, 0)) {
        });
                                                                                                                auto get_quad = [&](const Point& p) {
35
                                                                                                     101
         if (allow_collinear) {
                                                                                                                   Point diff = p - origin;
36
                                                                                                     102
            int i = (int)points.size() - 1;
                                                                                                                   if (diff.x > 0 \&\& diff.y >= 0) return 1;
37
            while (i >= 0 && !sgn((points[i] - points[0]) ^ (points[i] 104
                                                                                                                   if (diff.x <= 0 && diff.y > 0) return 2;
38
                                                                                                                   if (diff.x < 0 && diff.y <= 0) return 3;
            - points.back()))) i--;
                                                                                                     105
            reverse(points.begin() + i + 1, points.end());
39
                                                                                                                   return 4:
                                                                                                     106
                                                                                                                }:
40
                                                                                                     107
41
         vector<Point> hull;
                                                                                                                auto polar_cmp = [&](const Point& p1, const Point& p2) {
         for (auto &t : points) {
                                                                                                                   int q1 = get_quad(p1), q2 = get_quad(p2);
42
                                                                                                     109
                                                                                                                   if (q1 != q2) return q1 < q2;
43
            for (ll sz = hull.size();
                                                                                                     110
                  sz > 1 && (sgn((t - hull[sz - 2]) ^ (hull[sz - 1] -
                                                                                                                   return ((p1 - origin) ^ (p2 - origin)) > 0;
                                                                                                     111
44
           hull[sz - 2])) >= allow_collinear);
                                                                                                                }:
                                                                                                     112
                   hull.pop_back(), sz = hull.size()) {
                                                                                                                sort(first, last, polar_cmp);
                                                                                                     113
                                                                                                     114
46
47
            hull.push_back(t);
48
                                                                                                             Basic 3D
         return hull;
49
50
                                                                                                             using ll = long long;
51
                                                                                                             using ld = long double;
      vector<Point> get_convex_safe(vector<Point> points, bool
       → allow_collinear = false) {
                                                                                                       3
                                                                                                             constexpr auto eps = 1e-8;
         return get_convex(points, allow_collinear);
                                                                                                             const auto PI = acos(-1);
      }
54
                                                                                                             int sgn(1d x) \{ return (abs(x) \le eps) ? 0 : (x < 0 ? -1 : 1); 
55
      vector<Point> get_convex2_safe(vector<Point> points, bool

    allow collinear = false) {
                                                                                                             struct Point3D {
         return get_convex2(points, allow_collinear);
57
                                                                                                                ld x = 0, y = 0, z = 0;
58
                                                                                                                Point3D() = default;
59
                                                                                                                Point3D(ld _x, ld _y, ld _z) : x(_x), y(_y), z(_z) {}
                                                                                                       11
      bool is_convex(const vector<Point> &p, bool allow_collinear =
                                                                                                                bool operator<(const Point3D &p) const { return !sgn(p.x -</pre>

  false) {
                                                                                                              \leftrightarrow x) ? (!sgn(p.y - y) ? sgn(p.z - z) < 0 : y < p.y) : x <
61
        int n = p.size();
                                                                                                              \rightarrow p.x; }
         int lo = 1, hi = -1;
62
                                                                                                               bool operator == (const Point3D &p) const { return !sgn(p.x -
         for (int i = 0; i < n; i++) {
63
                                                                                                              \rightarrow x) && !sgn(p.y - y) && !sgn(p.z - z); }
            int cur = sgn((p[(i + 2) \% n] - p[(i + 1) \% n]) ^ (p[(i +
64
                                                                                                               Point3D operator+(const Point3D &p) const { return {x + p.x,
           1) % n] - p[i]));
                                                                                                              \rightarrow y + p.y, z + p.z}; }
            lo = min(lo, cur); hi = max(hi, cur);
65
                                                                                                               Point3D operator-(const Point3D &p) const { return {x - p.x,
         }
66
                                                                                                              \rightarrow y - p.y, z - p.z}; }
         return allow_collinear ? (hi - lo) < 2 : (lo == hi && lo);
67
                                                                                                               Point3D operator*(ld a) const { return {x * a, y * a, z *
                                                                                                      16
68

    a}; }

69
                                                                                                               Point3D operator/(ld a) const { return {x / a, y / a, z /
      auto rotating_calipers(const vector<Point> &hull) {
70
                                                                                                              \leftrightarrow a}; }
         // use get convex2
71
                                                                                                               auto operator*(const Point3D &p) const { return x * p.x + y
         int n = (int)hull.size(); // return the square of longest
                                                                                                              \Rightarrow * p.y + z * p.z; } // dot
       \hookrightarrow dist
                                                                                                               Point3D operator (const Point3D &p) const { return {y * p.z
73
         assert(n > 1):
                                                                                                              \rightarrow - z * p.y, z * p.x - x * p.z, x * p.y - y * p.x}; } //
74
         if (n <= 2) return dist2(hull[0], hull[1]);</pre>
         ld res = 0;
75
                                                                                                               friend auto &operator>>(istream &i, Point3D &p) { return i
76
         for (int i = 0, j = 2; i < n; i++) {
                                                                                                              auto d = hull[i], e = hull[(i + 1) % n];
77
                                                                                                             };
            while (area2(d, e, hull[j]) < area2(d, e, hull[(j + 1) %
       \rightarrow n])) j = (j + 1) % n;
                                                                                                             struct Line3D {
           res = max(res, max(dist2(d, hull[j]), dist2(e, hull[j])));
79
                                                                                                                Point3D s = \{0, 0, 0\}, e = \{0, 0, 0\};
                                                                                                      24
80
                                                                                                      25
                                                                                                                Line3D() = default;
81
         return res;
                                                                                                                Line3D(Point3D _s, Point3D _e) : s(_s), e(_e) {}
                                                                                                      26
                                                                                                             };
                                                                                                      27
83
                                                                                                      28
      // Find polygon cut to the left of l
84
                                                                                                             struct Segment3D : Line3D {
                                                                                                      29
      vector<Point> convex_cut(const vector<Point> &p, const Line
                                                                                                                using Line3D::Line3D;
                                                                                                      30
       31
        int n = p.size();
86
                                                                                                      32
         vector<Point> cut;
87
                                                                                                      33
                                                                                                             auto dist2(const Point3D &a) { return a * a; }
         for (int i = 0; i < n; i++) {
88
                                                                                                             auto dist2(const Point3D &a, const Point3D &b) { return
            auto a = p[i], b = p[(i + 1) \% n];
89
                                                                                                              \rightarrow dist2(a - b); }
            if (sgn((1.e - 1.s) ^ (a - 1.s)) >= 0)
90
                                                                                                             auto dist(const Point3D &a) { return sqrt(dist2(a)); }
91
               cut.push_back(a);
                                                                                                             auto dist(const Point3D &a, const Point3D &b) { return
            if (sgn((1.e - 1.s) ^ (a - 1.s)) * sgn((1.e - 1.s) ^ (b - 1.s)) ^ (b - 1.s) 
92

    sqrt(dist2(a - b)); }

       \rightarrow 1.s)) == -1)
                                                                                                             auto dist(const Point3D &a, const Line3D &1) { return dist((a
               cut.push_back(intersect(Line(a, b), 1));
93

    - l.s) ^ (l.e - l.s)) / dist(l.s, l.e); }

         }
94
                                                                                                             auto dist(const Point3D &p, const Segment3D &1) {
                                                                                                      38
95
         return cut;
                                                                                                                if (l.s == l.e) return dist(p, l.s);
96
                                                                                                                auto d = dist2(1.s, 1.e), t = min(d, max((ld)0, (p - 1.s) *)
                                                                                                      40
                                                                                                              // Sort by angle in range [0, 2pi)
98
                                                                                                              return dist((p - 1.s) * d, (1.e - 1.s) * t) / d;
                                                                                                      41
      template <class RandomIt>
                                                                                                      42
```

Miscellaneous vector<int> d, cur; 9 Dinic(int _n) : n(_n), g(n), d(n), cur(n) {} 10 tuple<int,int,ld> closest_pair(vector<Point> &p) { 11 void add_edge(int u, int v, int c) { using Pt = pair<Point,int>; g[u].push_back((int)e.size()); 12 int n = p.size(); e.push_back({u, v, c, c}); assert(n > 1); g[v].push_back((int)e.size()); 14 vector<Pt> pts(n), buf; 15 e.push_back({v, u, 0, 0}); for (int i = 0; i < n; i++) pts[i] = {p[i], i}; 16 sort(pts.begin(), pts.end()); 11 max_flow(int s, int t) { 17 buf.reserve(n); int inf = 1e9; auto cmp_y = [](const Pt% p1, const Pt% p2) { return auto bfs = [&]() { 19 p1.first.y < p2.first.y; };</pre> fill(d.begin(), d.end(), inf), fill(cur.begin(), function<tuple<int,int,ld>(int, int)> recurse = [&](int 1, cur.end(), 0): int r) → tuple<int,int,ld> { d[s] = 0;21 int i = pts[1].second, j = pts[1 + 1].second; vector<int> q{s}, nq; 22 ld d = dist(pts[1].first, pts[1 + 1].first); 12 for (int step = 1; q.size(); swap(q, nq), nq.clear(), 23 if (r - 1 < 5) { step++) { for (int a = 1; a < r; a++) for (int b = a + 1; b < r; 14 for (auto& node : q) { 24 → b++) { for (auto& edge : g[node]) { 25 ld cur = dist(pts[a].first, pts[b].first); 15 int ne = e[edge].to; if (cur < d) { i = pts[a].second; j = pts[b].second; d</pre> 16 if (!e[edge].remain || d[ne] <= step) continue;</pre> = cur: } d[ne] = step, nq.push_back(ne); 17 if (ne == t) return true; sort(pts.begin() + 1, pts.begin() + r, cmp_y); 18 } 19 } 31 else { 20 } 32 int mid = (1 + r)/2; 21 return false; 33 ld x = pts[mid].first.x; 22 }; 34 auto [li, lj, ldist] = recurse(l, mid); function<int(int, int)> find = [&](int node, int limit) { auto [ri, rj, rdist] = recurse(mid, r); if (node == t || !limit) return limit; 24 36 if (ldist < rdist) { i = li; j = lj; d = ldist; }</pre> int flow = 0; 37 else { i = ri; j = rj; d = rdist; } 26 for (int i = cur[node]; i < g[node].size(); i++) {</pre> inplace_merge(pts.begin() + 1, pts.begin() + mid, 27 cur[node] = i; 39 pts.begin() + r, cmp_y); int edge = g[node][i], oe = edge ^ 1, ne = e[edge].to; 40 buf.clear(): 28 if (!e[edge].remain || d[ne] != d[node] + 1) continue; 41 for (int a = 1; a < r; a++) { 29 42 if (int temp = find(ne, min(limit - flow, if (abs(x - pts[a].first.x) >= d) continue; 30 e[edge].remain))) { for (int b = buf.size() - 1; b >= 0; b--) { 31 e[edge].remain -= temp, e[oe].remain += temp, flow 43 32 if (pts[a].first.y - buf[b].first.y >= d) break; += temp; ld cur = dist(pts[a].first, buf[b].first); 33 } else { 44 if (cur < d) { i = pts[a].second; j = buf[b].second;</pre> d[ne] = -1;d = cur; } 46 35 if (flow == limit) break; 47 36 buf.push_back(pts[a]); 7 48 37 return flow: 49 38 50 return {i, j, d}; 39 11 res = 0;51 40 while (bfs()) 52 41 return recurse(0, n); while (int flow = find(s, inf)) res += flow; 53 42 54 return res: 43 55 Line abc_to_line(ld a, ld b, ld c) { 44 }; 56 assert(!sgn(a) || !sgn(b)); 45 if(a == 0) return Line(Point(0, -c/b), Point(1, -c/b)); 46 • USAGE if(b == 0) return Line(Point(-c/a, 0), Point(-c/a, 1)); 47 48 Point s(0, -c/b), e(1, (-c - a)/b), diff = e - s; int main() { return Line(s, s + diff/dist(diff)); int n, m, s, t; 49 2 50 cin >> n >> m >> s >> t;Dinic dinic(n); 51 tuple<ld,ld,ld> line_to_abc(const Line& 1) { 52 for (int i = 0, u, v, c; i < m; i++) { cin >> u >> v >> c; Point diff = l.e - l.s; 53 return {-diff.y, diff.x, -(diff ^ 1.s)}; dinic.add_edge(u - 1, v - 1, c); 54 cout << dinic.max_flow(s - 1, t - 1) << '\n';</pre>

Graph Theory

Max Flow

```
struct Edge {
   int from, to, cap, remain;
};

struct Dinic {
   int n;
   vector<Edge> e;
   vector<vector<int>> g;
```

```
PushRelabel Max-Flow (faster)
```

```
struct PushRelabel {
                                                                                 while (!que.empty()) {
      struct Edge {
                                                                                   auto [d, u] = que.top();
10
                                                                        15
11
         int dest, back;
                                                                        16
                                                                                   que.pop();
                                                                                   if (dis[u] != d) continue;
        ll f, c;
12
                                                                        17
                                                                                   for (int i : g[u]) {
      vector<vector<Edge>> g;
                                                                                     auto [v, f, c] = e[i];
14
                                                                        19
                                                                                     if (c > 0 \&\& dis[v] > d + h[u] - h[v] + f) {
15
       vector<11> ec;
                                                                        20
                                                                                       dis[v] = d + h[u] - h[v] + f;
      vector<Edge*> cur;
                                                                        21
16
      vector<vi> hs;
                                                                                       pre[v] = i;
17
                                                                        22
18
      vi H;
                                                                                       que.emplace(dis[v], v);
      PushRelabel(int n) : g(n), ec(n), cur(n), hs(2 * n), H(n) \{ \}
19
20
21
       void addEdge(int s, int t, ll cap, ll rcap = 0) {
         if (s == t) return;
                                                                                 return dis[t] != INF;
22
                                                                        27
         g[s].push_back({t, sz(g[t]), 0, cap});
23
                                                                        28
         g[t].push_back({s, sz(g[s]) - 1, 0, rcap});
                                                                               MCMF(int n) : n(n), g(n) {}
24
                                                                        29
25
                                                                               void add_edge(int u, int v, int fee, int c) {
                                                                                 g[u].push_back(e.size());
26
                                                                        31
       void addFlow(Edge& e, ll f) {
                                                                                 e.emplace_back(v, fee, c);
27
                                                                        32
        Edge& back = g[e.dest][e.back];
                                                                                 g[v].push_back(e.size());
28
                                                                        33
         if (!ec[e.dest] && f) hs[H[e.dest]].push_back(e.dest);
                                                                                 e.emplace_back(u, -fee, 0);
29
                                                                        34
30
                                                                        35
         e.c -= f;
                                                                               pair<11, 11> max_flow(const int s, const int t) {
31
                                                                        36
         ec[e.dest] += f;
                                                                        37
                                                                                 int flow = 0, cost = 0;
33
         back.f -= f;
                                                                        38
                                                                                 h.assign(n, 0);
         back.c += f;
                                                                        39
                                                                                 while (dijkstra(s, t)) {
34
         ec[back.dest] -= f;
                                                                                   for (int i = 0; i < n; ++i) h[i] += dis[i];
35
                                                                        40
                                                                                   for (int i = t; i != s; i = get<0>(e[pre[i] ^ 1])) {
36
                                                                        41
      ll calc(int s, int t) {
                                                                                      --get<2>(e[pre[i]]);
37
                                                                        42
                                                                                     ++get<2>(e[pre[i] ^ 1]);
38
         int v = sz(g);
                                                                        43
        H[s] = v;
                                                                        44
39
        ec[t] = 1;
                                                                        45
                                                                                   ++flow;
40
         vi co(2 * v);
                                                                                   cost += h[t];
41
                                                                        46
42
         co[0] = v - 1;
                                                                        47
         rep(i, 0, v) cur[i] = g[i].data();
43
                                                                        48
                                                                                 return {flow, cost};
         for (Edge& e : g[s]) addFlow(e, e.c);
                                                                        49
44
45
                                                                             };
                                                                        50
         for (int hi = 0;;) {
46
           while (hs[hi].empty())
47
                                                                             Max Cost Feasible Flow
             if (!hi--) return -ec[s];
48
           int u = hs[hi].back();
49
                                                                             struct Edge {
50
           hs[hi].pop_back();
                                                                               int from, to, cap, remain, cost;
           while (ec[u] > 0) // discharge u
51
                                                                             }:
             if (cur[u] == g[u].data() + sz(g[u])) {
               H[u] = 1e9;
53
                                                                             struct MCMF {
               for (Edge& e : g[u])
                                                                               int n;
                 if (e.c && H[u] > H[e.dest] + 1) H[u] = H[e.dest]
55
                                                                               vector<Edge> e;
     vector<vector<int>> g;
               if (++co[H[u]], !--co[hi] \&\& hi < v)
56
                                                                               vector<11> d, pre;
                 rep(i, 0, v) if (hi < H[i] && H[i] < v)--
57
                                                                               MCMF(int _n) : n(_n), g(n), d(n), pre(n) {}
                                                                        10
     \hookrightarrow co[H[i]], H[i] = v + 1;
                                                                               void add_edge(int u, int v, int c, int w) {
                                                                        11
               hi = H[u];
58
                                                                                 g[u].push_back((int)e.size());
59
             } else if (cur[u] \rightarrow c \&\& H[u] == H[cur[u] \rightarrow dest] + 1)
                                                                                 e.push back({u, v, c, c, w}):
                                                                        13
               addFlow(*cur[u], min(ec[u], cur[u]->c));
60
                                                                                 g[v].push_back((int)e.size());
61
                                                                                 e.push_back({v, u, 0, 0, -w});
                                                                        15
               ++cur[u];
62
                                                                        16
        }
63
                                                                        17
                                                                               pair<11, 11> max_flow(int s, int t) {
                                                                                 11 inf = 1e18;
                                                                        18
      bool leftOfMinCut(int a) { return H[a] >= sz(g); }
65
                                                                                 auto spfa = [&]() {
                                                                        19
                                                                                   fill(d.begin(), d.end(), -inf); // important!
                                                                        20
                                                                                   vector<int> f(n), seen(n);
                                                                        21
                                                                                   d[s] = 0, f[s] = 1e9;
    Min-Cost Max-Flow
                                                                        22
                                                                        23
                                                                                   vector<int> q{s}, nq;
    class MCMF {
                                                                        24
                                                                                   for (; q.size(); swap(q, nq), nq.clear()) {
    public:
                                                                                     for (auto& node : q) {
2
                                                                        25
       static constexpr int INF = 1e9;
                                                                                        seen[node] = false;
                                                                        26
                                                                                       for (auto& edge : g[node]) {
      const int n:
                                                                        27
                                                                                          int ne = e[edge].to, cost = e[edge].cost;
      vector<tuple<int, int, int>> e;
                                                                        28
      vector<vector<int>> g;
                                                                                         if (!e[edge].remain || d[ne] >= d[node] + cost)
                                                                        29
       vector<int> h, dis, pre;
                                                                                 continue;
      bool dijkstra(int s, int t) {
                                                                        30
                                                                                          d[ne] = d[node] + cost, pre[ne] = edge;
                                                                                         f[ne] = min(e[edge].remain, f[node]);
        dis.assign(n, INF);
                                                                        31
        pre.assign(n, -1);
                                                                                          if (!seen[ne]) seen[ne] = true, nq.push_back(ne);
10
                                                                        32
         priority_queue<pair<int, int>, vector<pair<int, int>>,
11
                                                                        33
        greater<>> que;
                                                                        34
                                                                                   }
         dis[s] = 0;
12
                                                                        35
         que.emplace(0, s);
                                                                                   return f[t];
13
                                                                        36
```

14

General Unweight Graph Matching }; 37 11 flow = 0, cost = 0;38 • Complexity: $O(n^3)$ (?) 39 while (int temp = spfa()) { if (d[t] < 0) break; // important!</pre> 40 struct BlossomMatch { flow += temp, cost += temp * d[t]; 41 int n; 2 for (ll i = t; i != s; i = e[pre[i]].from) { 42 vector<vector<int>> e; e[pre[i]].remain -= temp, e[pre[i] ^ 1].remain += 43 BlossomMatch(int _n) : n(_n), e(_n) {} temp; void add_edge(int u, int v) { e[u].push_back(v), 44 e[v].push_back(u); } 45 } vector<int> find_matching() { return {flow, cost}; 46 vector < int > match(n, -1), vis(n), link(n), f(n), dep(n);47 function<int(int)> find = [&](int x) { return f[x] == x ? 48 }: x : (f[x] = find(f[x])); }; auto lca = [&](int u, int v) { u = find(u), v = find(v);10 Heavy-Light Decomposition while (u != v) { 11 if (dep[u] < dep[v]) swap(u, v);</pre> 12 int root = 0, cur = 0; u = find(link[match[u]]); vector<int> parent(n), deep(n), hson(n, -1), top(n), sz(n), } 14 \rightarrow dfn(n, -1); return u; function<int(int, int, int)> dfs = [&](int node, int fa, int }; 16 → dep) { queue<int> que; 17 deep[node] = dep, sz[node] = 1, parent[node] = fa; auto blossom = [&](int u, int v, int p) { for (auto &ne : g[node]) { while (find(u) != p) { 19 if (ne == fa) continue; link[u] = v, v = match[u];sz[node] += dfs(ne, node, dep + 1); if (vis[v] == 0) vis[v] = 1, que.push(v); if (hson[node] == -1|| sz[ne] > sz[hson[node]]) hson[node] f[u] = f[v] = p, u = link[v]; } 23 } 9 24 }; 10 return sz[node]; // find an augmenting path starting from u and augment (if }; 11 exist) function<void(int, int)> dfs2 = [&](int node, int t) { 12 auto augment = [&](int node) { 26 top[node] = t, dfn[node] = cur++; while (!que.empty()) que.pop(); 27 if (hson[node] == -1) return; 14 iota(f.begin(), f.end(), 0); 28 dfs2(hson[node], t); 15 // vis = 0 corresponds to inner vertices, vis = 1 16 for (auto &ne : g[node]) { corresponds to outer vertices if (ne == parent[node] || ne == hson[node]) continue; 17 fill(vis.begin(), vis.end(), -1); 30 18 dfs2(ne, ne); que.push(node); 31 } 19 vis[node] = 1, dep[node] = 0; 32 20 33 while (!que.empty()) { // read in graph as vector<vector<int>> g(n) 21 int u = que.front(); 34 dfs(root, -1, 0), dfs2(root, root); que.pop(); 35 for (auto v : e[u]) { • USAGE: get LCA 36 if (vis[v] == -1) { 37 function<int(int, int)> lca = [&](int x, int y) { vis[v] = 0, link[v] = u, dep[v] = dep[u] + 1; 1 38 while (top[x] != top[y]) { // found an augmenting path 39 if (deep[top[x]] < deep[top[y]]) swap(x, y);</pre> if (match[v] == -1) { 40 for (int x = v, y = u, temp; y != -1; x = temp, x = parent[top[x]]; 41 $y = x == -1 ? -1 : link[x]) {$ temp = match[y], match[x] = y, match[y] = x; return deep[x] < deep[y] ? x : y; 6 42 } 43 44 return; vector<ll> light(n); 45 SegTree heavy(n), form_parent(n); vis[match[v]] = 1, dep[match[v]] = dep[u] + 2; 46 // cin >> x >> y, x--, y--; que.push(match[v]); 47 int z = lca(x, y);48 } else if $(vis[v] == 1 && find(v) != find(u)) {$ while (x != z) { 49 // found a blossom if (dfn[top[x]] <= dfn[top[z]]) {</pre> int p = lca(u, v); 50 // [dfn[z], dfn[x]), from heavyblossom(u, v, p), blossom(v, u, p); 51 heavy.modify(dfn[z], dfn[x], 1); 52 9 break; } 53 10 } 54 $// x \rightarrow top[x];$ 11 }: 55 heavy.modify(dfn[top[x]], dfn[x], 1); 12 56 // find a maximal matching greedily (decrease constant) light[parent[top[x]]] += a[top[x]]; 13 auto greedy = [&]() { 57 x = parent[top[x]]; for (int u = 0; u < n; ++u) { 58 } 15 if (match[u] != -1) continue; 59 while $(y != z) {$ 16 for (auto v : e[u]) { 60 if (dfn[top[y]] <= dfn[top[z]]) {</pre> 17 if (match[v] == -1) { 61 // (dfn[z], dfn[y]], from heavy 18 match[u] = v, match[v] = u; 62 form_parent.modify(dfn[z] + 1, dfn[y] + 1, 1); 19 63 break: break: 20 64 21 } $// y \rightarrow top[y];$ 22 } 66 form_parent.modify(dfn[top[y]], dfn[y] + 1, 1); 23 67 24 = parent[top[y]]; greedy(); 68 25 for (int u = 0; u < n; ++u)

```
if (match[u] == -1) augment(u);
                                                                                  int ny = y \le n ? y + n : y - n;
70
                                                                        51
         return match;
                                                                                  g[nx].push_back(y);
71
                                                                        52
      }
72
                                                                        53
                                                                                 g[ny].push_back(x);
    };
73
                                                                        54
                                                                                int idx[2*n + 1];
                                                                        56
                                                                                scc(g, idx);
    Maximum Bipartite Matching
                                                                                for(int i = 1; i <= n; i++) {
                                                                        57
                                                                                 if(idx[i] == idx[i + n]) return {0, {}};
                                                                        58
       • Needs dinic, complexity \approx O(n + m\sqrt{n})
                                                                                  ans[i - 1] = idx[i + n] < idx[i];
                                                                        59
                                                                         60
    struct BipartiteMatch {
                                                                               return {1, ans};
                                                                        61
      int 1, r;
                                                                             }
      Dinic dinic = Dinic(0);
      dinic = Dinic(1 + r + 2);
                                                                             Enumerating Triangles
         for (int i = 1; i <= 1; i++) dinic.add_edge(0, i, 1);</pre>
         for (int i = 1; i <= r; i++) dinic.add_edge(1 + i, 1 + r +
                                                                                • Complexity: O(n + m\sqrt{m})
      }
                                                                             void enumerate_triangles(vector<pair<int,int>>& edges,
      void add_edge(int u, int v) { dinic.add_edge(u + 1, l + v +

    function < void(int,int,int) > f) {
     \hookrightarrow 1, 1); }
                                                                               int n = 0:
      ll max_matching() { return dinic.max_flow(0, 1 + r + 1); }
                                                                               for(auto [u, v] : edges) n = max({n, u + 1, v + 1});
10
                                                                                vector<int> deg(n);
                                                                                vector<int> g[n];
                                                                                for(auto [u, v] : edges) {
    2-SAT and Strongly Connected Components
                                                                                 deg[u]++;
                                                                                 deg[v]++;
    void scc(vector<vector<int>>& g, int* idx) {
                                                                               7
      int n = g.size(), ct = 0;
                                                                               for(auto [u, v] : edges) {
                                                                         10
       int out[n];
                                                                         11
                                                                                  if(u == v) continue;
      vector<int> ginv[n];
                                                                                  \label{eq:conditional_condition} \mbox{if}(\mbox{deg}[\mbox{u}] \ > \mbox{deg}[\mbox{v}] \ || \ (\mbox{deg}[\mbox{u}] \ == \mbox{deg}[\mbox{v}] \ \&\& \ u \ > \ v))
                                                                         12
      memset(out, -1, size of out);
                                                                                    swap(u, v);
                                                                         13
       memset(idx, -1, n * sizeof(int));
                                                                                 g[u].push_back(v);
                                                                         14
      function<void(int)> dfs = [&](int cur) {
                                                                        15
         out[cur] = INT_MAX;
                                                                                vector<int> flag(n);
                                                                         16
9
         for(int v : g[cur]) {
                                                                               for(int i = 0; i < n; i++) {</pre>
                                                                        17
           ginv[v].push_back(cur);
10
                                                                                  for(int v : g[i]) flag[v] = 1;
                                                                         18
           if(out[v] == -1) dfs(v);
                                                                                  for(int v : g[i]) for(int u : g[v]) {
                                                                        19
12
                                                                        20
                                                                                    if(flag[u]) f(i, v, u);
         ct++; out[cur] = ct;
13
                                                                        21
      };
14
                                                                                 for(int v : g[i]) flag[v] = 0;
                                                                        22
      vector<int> order;
15
                                                                               }
      for(int i = 0; i < n; i++) {
16
                                                                             }
                                                                        24
         order.push_back(i);
17
18
         if(out[i] == -1) dfs(i);
19
      }
                                                                             Tarjan
      sort(order.begin(), order.end(), [&](int& u, int& v) {
20
         return out[u] > out[v];
21
                                                                                • shrink all
                                                                                                 circles into points (2-edge-connected-
      }):
22
                                                                                  component)
      ct = 0;
      stack<int> s:
24
                                                                             int cnt = 0, now = 0;
      auto dfs2 = [&](int start) {
25
                                                                             vector<ll> dfn(n, -1), low(n), belong(n, -1), stk;
         s.push(start);
26
                                                                             function \langle void(11, 11) \rangle tarjan = [&](11 node, 11 fa) {
         while(!s.empty()) {
27
                                                                               dfn[node] = low[node] = now++, stk.push_back(node);
           int cur = s.top();
                                                                                for (auto& ne : g[node]) {
           s.pop();
29
                                                                                 if (ne == fa) continue;
30
           idx[cur] = ct;
                                                                                  if (dfn[ne] == -1) {
           for(int v : ginv[cur])
31
                                                                                    tarjan(ne, node);
             if(idx[v] == -1) s.push(v);
32
                                                                                    low[node] = min(low[node], low[ne]);
                                                                         9
        }
33
                                                                                  } else if (belong[ne] == -1) {
                                                                         10
      };
34
                                                                                    low[node] = min(low[node], dfn[ne]);
                                                                         11
      for(int v : order) {
35
                                                                                 }
                                                                         12
         if(idx[v] == -1) {
36
                                                                         13
                                                                               }
37
           dfs2(v):
                                                                               if (dfn[node] == low[node]) {
                                                                         14
38
                                                                                 while (true) {
                                                                         15
39
                                                                                   auto v = stk.back();
                                                                        16
      }
40
                                                                                    belong[v] = cnt;
    }
41
                                                                         18
                                                                                    stk.pop_back();
42
                                                                                    if (v == node) break;
                                                                         19
    // 0 => impossible, 1 => possible
43
                                                                        20
    pair<int, vector<int>> sat2(int n, vector<pair<int,int>>&
44
                                                                                  ++cnt;
                                                                        21
     }
      vector<int> ans(n):
45
                                                                             };
                                                                        23
      vector<vector<int>> g(2*n + 1);
46
```

int cnt = 0, now = 0;

vector<vector<ll>>> e1(n);

• 2-vertex-connected-component / Block forest

for(auto [x, y] : clauses) {

x = x < 0 ? -x + n : x;

y = y < 0 ? -y + n : y;

 $int nx = x \le n ? x + n : x - n;$

47

48

```
vector<ll> dfn(n, -1), low(n), stk;
    function<void(l1)> tarjan = [&](l1 node) {
      dfn[node] = low[node] = now++, stk.push_back(node);
      for (auto& ne : g[node]) {
         if (dfn[ne] == -1) {
          tarjan(ne);
           low[node] = min(low[node], low[ne]);
9
           if (low[ne] == dfn[node]) {
10
            e1.push_back({});
11
            while (true) {
              auto x = stk.back();
13
               stk.pop_back();
14
              e1[n + cnt].push_back(x);
15
               // e1[x].push back(n + cnt); // undirected
16
              if (x == ne) break;
18
19
            e1[node].push_back(n + cnt);
             // e1[n + cnt].push_back(node); // undirected
20
21
          7
22
        } else {
23
           low[node] = min(low[node], dfn[ne]);
24
25
26
      }
    };
27
```

Kruskal reconstruct tree

```
int n. m:
    cin >> _n >> m; // _n: # of node, m: # of edge
    int n = 2 * _n - 1; // root: n-1
    vector<array<int, 3>> edges(m);
    for (auto& [w, u, v] : edges) {
      cin >> u >> v >> w, u--, v--;
6
    sort(edges.begin(), edges.end());
    vector<int> p(n);
10
    iota(p.begin(), p.end(), 0);
    function<int(int)> find = [&](int x) { return p[x] == x ? x :
     \rightarrow (p[x] = find(p[x])); };
    auto merge = [&](int x, int y) { p[find(x)] = find(y); };
12
    vector<vector<int>> g(n);
    vector<int> val(m);
14
15
    val.reserve(n);
    for (auto [w, u, v] : edges) {
16
      u = find(u), v = find(v);
17
      if (u == v) continue;
      val.push_back(w);
19
      int node = (int)val.size() - 1;
20
      g[node].push_back(u), g[node].push_back(v);
21
22
      merge(u, node), merge(v, node);
```

Math

Inverse

```
vector<Z> f(MAX_N, 1), rf(MAX_N, 1);
for (int i = 2; i < MAX_N; i++) f[i] = f[i - 1] * i % MOD;

rf[MAX_N - 1] = power(f[MAX_N - 1], MOD - 2);
for (int i = MAX_N - 2; i > 1; i--) rf[i] = rf[i + 1] * (i + ... 1) % MOD;

auto binom = [&](ll n, ll r) -> Z {
   if (n < 0 || r < 0 || n < r) return 0;
   return f[n] * rf[n - r] * rf[r];
};</pre>
```

Mod Class

```
constexpr 11 norm(11 x) { return (x % MOD + MOD) % MOD; }
    template <typename T>
    constexpr T power(T a, ll b, T res = 1) {
      for (; b; b /= 2, (a *= a) \%= MOD)
4
        if (b & 1) (res *= a) %= MOD;
      return res;
6
    }
    struct Z {
8
9
      11 x:
      constexpr Z(11 _x = 0) : x(norm(_x)) {}
10
      // auto operator<=>(const Z &) const = default; // cpp20
11
      Z operator-() const { return Z(norm(MOD - x)); }
12
13
      Z inv() const { return power(*this, MOD - 2); }
      Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
14
     → *this; }
      Z &operator+=(const Z &rhs) { return x = norm(x + rhs.x),

→ *this: }

      Z &operator-=(const Z &rhs) { return x = norm(x - rhs.x),

    *this: }

17
      Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
      Z &operator%=(const ll &rhs) { return x %= rhs, *this; }
18
      friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs;
19
     friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs;
20
      friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs;
21
     → }
     friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs;
     → }
      friend Z operator%(Z lhs, const ll &rhs) { return lhs %=

    rhs; }

     friend auto &operator>>(istream &i, Z &z) { return i >> z.x;
24
     friend auto &operator << (ostream &o, const Z &z) { return o
25
     };
26
```

• large mod (for NTT to do FFT in ll range without modulo)

```
using ll = long long;
    using i128 = __int128;
    constexpr i128 MOD = 9223372036737335297;
    constexpr i128 norm(i128 x) { return x < 0 ? (x + MOD) \% MOD :
     \rightarrow x % MOD; }
    template <typename T>
    constexpr T power(T a, i128 b, T res = 1) {
      for (; b; b /= 2, (a *= a) \%= MOD)
9
        if (b & 1) (res *= a) \%= MOD;
10
      return res;
    }
11
    struct Z {
^{12}
      i128 x:
13
       constexpr Z(i128 _x = 0) : x(norm(_x)) {}
       Z operator-() const { return Z(norm(MOD - x)); }
15
       Z inv() const { return power(*this, MOD - 2); }
       // auto operator<=>(const Z&) const = default;
      Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,

    *this; }

     Z \& operator += (const Z \& rhs) \{ return x = norm(x + rhs.x), \}
19
     → *this; }
      Z &operator-=(const Z &rhs) { return x = norm(x - rhs.x),
20

    *this; }

21
      Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
      Z &operator%=(const i128 &rhs) { return x %= rhs, *this; }
22
      friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs;
     → }
24
      friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs;
     → }
     friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs;
25
      friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs;
26
```

```
};
       • fastest mod class! be careful with overflow, only use
         when the time limit is tight
    constexpr int MOD = 998244353;
    constexpr int norm(int x) {
      if (x < 0) x += MOD;
4
      if (x >= MOD) x -= MOD;
6
      return x:
    template <typename T>
    constexpr T power(T a, int b, T res = 1) {
9
10
      for (; b; b /= 2, (a *= a) %= MOD)
        if (b & 1) (res *= a) \%= MOD;
11
      return res:
12
13
    }
    struct Z {
14
      constexpr Z(int _x = 0) : x(norm(_x)) {}
16
      // constexpr auto operator <=> (const Z &) const = default; //
17

→ cpp20 only

      constexpr Z operator-() const { return Z(norm(MOD - x)); }
18
      constexpr Z inv() const { return power(*this, MOD - 2); }
      constexpr Z &operator*=(const Z &rhs) { return x = 11(x) *
20

    rhs.x % MOD, *this; }

     constexpr Z &operator+=(const Z &rhs) { return x = norm(x +
21

    rhs.x), *this; }

     constexpr Z &operator-=(const Z &rhs) { return x = norm(x -

    rhs.x), *this; }

      constexpr Z &operator/=(const Z &rhs) { return *this *=
     → rhs.inv(): }
      constexpr Z &operator%=(const ll &rhs) { return x %= rhs,
24
     → *this; }
     constexpr friend Z operator*(Z lhs, const Z &rhs) { return
25
     → lhs *= rhs; }
      constexpr friend Z operator+(Z lhs, const Z &rhs) { return
26
     constexpr friend Z operator-(Z lhs, const Z &rhs) { return
     → lhs -= rhs; }
      constexpr friend Z operator/(Z lhs, const Z &rhs) { return
     → lhs /= rhs: }
      constexpr friend Z operator%(Z lhs, const ll &rhs) { return
     friend auto &operator>>(istream &i, Z &z) { return i >> z.x;
     friend auto &operator << (ostream &o, const Z &z) { return o
31
     \hookrightarrow << z.x; }
    };
32
```

friend Z operator%(Z lhs, const i128 &rhs) { return lhs %=

Cancer mod class

- Explanation: for some prime modulo p, maintains numbers of form p^x * y, where y is a nonzero remainder
- Be careful with calling Cancer(x, y), it doesn't fix the input if y > p

```
struct Cancer {
      11 x; 11 y;
      Cancer() : Cancer(0, 1) {}
      Cancer(11 _y) {
         x = 0, y = _y;
         while(y \% MOD == 0) {
          y /= MOD;
           x++;
9
        }
      }
10
      Cancer(11 _x, 11 _y) : x(_x), y(_y) {}
11
      Cancer inv() { return Cancer(-x, power(y, MOD - 2)); }
12
      Cancer operator*(const Cancer &c) { return Cancer(x + c.x,
     \rightarrow (y * c.y) % MOD); }
```

```
Cancer operator*(11 m) {
   11 p = 0;
   while(m % MOD == 0) {
     m /= MOD;
   return Cancer(x + p, (m * y) % MOD);
 friend auto &operator << (ostream &o, Cancer c) { return o <<

    c.x << ' ' << c.y; }
</pre>
```

NTT, FFT, FWT

• ntt

14

15

16

17

20

21

22

23

10

12

13

14

15

16

17

18

19

21

22

23

 24

9

```
void ntt(vector<Z>& a, int f) {
  int n = int(a.size());
  vector<Z> w(n);
  vector<int> rev(n);
  for (int i = 0; i < n; i++) rev[i] = (rev[i / 2] / 2) | ((i
 \hookrightarrow & 1) * (n / 2));
  for (int i = 0; i < n; i++) {
    if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
  Z wn = power(f ? (MOD + 1) / 3 : 3, (MOD - 1) / n);
  w[0] = 1;
  for (int i = 1; i < n; i++) w[i] = w[i - 1] * wn;
  for (int mid = 1; mid < n; mid *= 2) {</pre>
    for (int i = 0; i < n; i += 2 * mid) {
      for (int j = 0; j < mid; j++) {
        Z x = a[i + j], y = a[i + j + mid] * w[n / (2 * mid) *
        a[i + j] = x + y, a[i + j + mid] = x - y;
    }
  }
  if (f) {
    Z iv = power(Z(n), MOD - 2);
    for (auto& x : a) x *= iv;
}
```

• USAGE: Polynomial multiplication

```
vector<Z> mul(vector<Z> a, vector<Z> b) {
 int n = 1, m = (int)a.size() + (int)b.size() - 1;
  while (n < m) n *= 2;
  a.resize(n), b.resize(n);
 ntt(a, 0), ntt(b, 0);
 for (int i = 0; i < n; i++) a[i] *= b[i];
 ntt(a, 1);
 a.resize(m);
 return a:
```

• FFT (should prefer NTT, only use this when input is not integer)

```
const double PI = acos(-1);
    auto mul = [&](const vector<double>& aa, const vector<double>&
     → bb) {
      int n = (int)aa.size(), m = (int)bb.size(), bit = 1;
      while ((1 << bit) < n + m - 1) bit++;
      int len = 1 << bit;</pre>
      vector<complex<double>>> a(len), b(len);
      vector<int> rev(len);
      for (int i = 0; i < n; i++) a[i].real(aa[i]);</pre>
      for (int i = 0; i < m; i++) b[i].real(bb[i]);</pre>
9
      for (int i = 0; i < len; i++) rev[i] = (rev[i >> 1] >> 1) |
10
     auto fft = [&](vector<complex<double>>& p, int inv) {
11
        for (int i = 0; i < len; i++)
12
          if (i < rev[i]) swap(p[i], p[rev[i]]);</pre>
13
        for (int mid = 1; mid < len; mid *= 2) {</pre>
          auto w1 = complex<double>(cos(PI / mid), (inv ? -1 : 1)

    * sin(PI / mid));
```

```
for (int i = 0; i < len; i += mid * 2) {
                                                                                for (int i = 0; i < n; i += 2 * mid) {
16
                                                                       43
             auto wk = complex<double>(1, 0);
                                                                                  for (int j = 0; j < mid; j++) {
17
                                                                       44
            for (int j = 0; j < mid; j++, wk = wk * w1) {
                                                                                    Z x = a[i + j], y = a[i + j + mid] * w[n / (2 * mid) *
                                                                       45
              auto x = p[i + j], y = wk * p[i + j + mid];
19
              p[i + j] = x + y, p[i + j + mid] = x - y;
                                                                                    a[i + j] = x + y, a[i + j + mid] = x - y;
                                                                                  7
21
                                                                       47
                                                                                }
22
                                                                        48
        }
                                                                              }
23
                                                                        49
         if (inv == 1) {
                                                                              if (f) {
24
                                                                       50
           for (int i = 0; i < len; i++) p[i].real(p[i].real() /
                                                                                Z iv = power(Z(n), MOD - 2);
        len):
                                                                                for (int i = 0; i < n; i++) a[i] *= iv;
                                                                       52
26
                                                                        53
                                                                            }
27
      }:
                                                                       54
      fft(a, 0), fft(b, 0);
28
                                                                       55
      for (int i = 0; i < len; i++) a[i] = a[i] * b[i];
                                                                            struct Poly {
      fft(a, 1):
                                                                              vector<Z> a:
30
                                                                       57
31
      a.resize(n + m - 1);
                                                                              Poly() {}
      vector<double> res(n + m - 1);
                                                                              Poly(const vector<Z> &_a) : a(_a) {}
32
                                                                        59
      for (int i = 0; i < n + m - 1; i++) res[i] = a[i].real();
                                                                              int size() const { return (int)a.size(); }
33
                                                                              void resize(int n) { a.resize(n); }
34
                                                                        61
    }:
                                                                              Z operator[](int idx) const {
35
                                                                        62
                                                                                if (idx < 0 || idx >= size()) return 0;
                                                                        63
                                                                                return a[idx];
                                                                       64
    Polynomial Class
                                                                              Z &operator[](int idx) { return a[idx]; }
                                                                       66
    using ll = long long;
                                                                       67
                                                                              Poly mulxk(int k) const {
    constexpr 11 MOD = 998244353;
                                                                                auto b = a;
                                                                       69
                                                                                b.insert(b.begin(), k, 0);
    11 norm(11 x) { return (x % MOD + MOD) % MOD; }
                                                                                return Poly(b);
    template <class T>
                                                                       71
    T power(T a, ll b, T res = 1) {
                                                                              Poly modxk(int k) const { return Poly(vector<Z>(a.begin(),
                                                                       72
       for (; b; b /= 2, (a *= a) %= MOD)
                                                                             \rightarrow a.begin() + min(k, size()))); }
         if (b & 1) (res *= a) \%= MOD;
                                                                              Poly divxk(int k) const {
                                                                       73
      return res;
                                                                       74
                                                                                if (size() <= k) return Poly();</pre>
    }
10
                                                                                return Poly(vector<Z>(a.begin() + k, a.end()));
                                                                       75
11
                                                                        76
    struct Z {
12
                                                                              friend Poly operator+(const Poly &a, const Poly &b) {
                                                                       77
                                                                       78
                                                                                vector<Z> res(max(a.size(), b.size()));
      Z(11 _x = 0) : x(norm(_x)) {}
14
                                                                                for (int i = 0; i < (int)res.size(); i++) res[i] = a[i] +
       // auto operator<=>(const Z &) const = default;
15
                                                                             ⇔ b[i]:
      Z operator-() const { return Z(norm(MOD - x)); }
                                                                                return Poly(res);
                                                                        80
      Z inv() const { return power(*this, MOD - 2); }
17
                                                                        81
      Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
                                                                              friend Poly operator-(const Poly &a, const Poly &b) {
                                                                        82

    *this: }

                                                                                vector<Z> res(max(a.size(), b.size()));
      Z &operator+=(const Z &rhs) { return x = norm(x + rhs.x),
19
                                                                                for (int i = 0; i < (int)res.size(); i++) res[i] = a[i] -
                                                                        84
     → *this; }
                                                                                b[i];
      Z & operator = (const Z & rhs) { return x = norm(x - rhs.x),
20
                                                                                return Poly(res);
                                                                        85
                                                                              }
                                                                        86
      Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
21
                                                                        87
                                                                              friend Poly operator*(Poly a, Poly b) {
      Z &operator%=(const ll &rhs) { return x %= rhs, *this; }
                                                                                if (a.size() == 0 || b.size() == 0) return Poly();
                                                                        88
      friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs;
                                                                                int n = 1, m = (int)a.size() + (int)b.size() - 1;
                                                                                while (n < m) n *= 2;
      friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs;
                                                                                a.resize(n), b.resize(n);
     → }
                                                                                ntt(a.a, 0), ntt(b.a, 0);
                                                                        92
      friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs;
                                                                                for (int i = 0; i < n; i++) a[i] *= b[i];
                                                                        93
     → }
                                                                                ntt(a.a, 1);
                                                                        94
      friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs;
                                                                                a.resize(m);
                                                                       95
      friend Z operator%(Z lhs, const ll &rhs) { return lhs %=
                                                                       97
                                                                        98
                                                                              friend Poly operator*(Z a, Poly b) {
      friend auto &operator>>(istream &i, Z &z) { return i >> z.x;
28
                                                                                for (int i = 0; i < (int)b.size(); i++) b[i] *= a;
                                                                       99
                                                                       100
                                                                                return b;
      friend auto &operator << (ostream &o, const Z &z) { return o
29
                                                                       101
                                                                              friend Poly operator*(Poly a, Z b) {
                                                                       102
30
    }:
                                                                                for (int i = 0; i < (int)a.size(); i++) a[i] *= b;
                                                                       103
31
                                                                       104
                                                                                return a:
    void ntt(vector<Z> &a, int f) {
32
                                                                       105
      int n = (int)a.size();
33
                                                                              Poly & operator += (Poly b) { return (*this) = (*this) + b; }
                                                                       106
      vector<Z> w(n);
34
                                                                              Poly &operator = (Poly b) { return (*this) = (*this) - b; }
                                                                       107
      vector<int> rev(n);
35
                                                                              Poly &operator *= (Poly b) { return (*this) = (*this) * b; }
      for (int i = 0; i < n; i++) rev[i] = (rev[i / 2] / 2) | ((i
36
                                                                       109
                                                                              Polv deriv() const {
     \leftrightarrow & 1) * (n / 2));
                                                                                if (a.empty()) return Poly();
                                                                       110
      for (int i = 0; i < n; i++)
37
                                                                                vector<Z> res(size() - 1);
                                                                       111
        if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
38
                                                                       112
                                                                                for (int i = 0; i < size() - 1; ++i) res[i] = (i + 1) *
      Z wn = power(f ? (MOD + 1) / 3 : 3, (MOD - 1) / n);
39
                                                                                a[i + 1];
      w[0] = 1;
40
                                                                                return Poly(res);
                                                                       113
      for (int i = 1; i < n; i++) w[i] = w[i - 1] * wn;
41
                                                                       114
      for (int mid = 1; mid < n; mid *= 2) {
```

```
Poly integr() const {
                                                                                  };
         vector<Z> res(size() + 1);
                                                                                   build(1, 0, n);
116
                                                                         188
         for (int i = 0; i < size(); ++i) res[i + 1] = a[i] / (i +
                                                                                   auto work = [&] (auto self, int p, int l, int r, const Poly
117
                                                                                  &num) -> void {
         return Poly(res);
                                                                                    if (r - 1 == 1) {
118
                                                                                      if (1 < int(ans.size())) ans[1] = num[0];</pre>
       }
119
                                                                         191
120
       Poly inv(int m) const {
                                                                         192
                                                                                     } else {
                                                                                       int m = (1 + r) / 2;
121
         Poly x({a[0].inv()});
                                                                         193
         int k = 1;
                                                                                       self(self, 2 * p, 1, m, num.mulT(q[2 * p + 1]).modxk(m)
122
                                                                         194
123
         while (k < m) {
           k *= 2:
                                                                                       self(self, 2 * p + 1, m, r, num.mulT(q[2 * p]).modxk(r)
124
                                                                         195
            x = (x * (Poly({2}) - modxk(k) * x)).modxk(k);
125
                                                                                    m));
126
                                                                         196
                                                                                    }
                                                                                  };
         return x.modxk(m);
127
                                                                         197
                                                                                   work(work, 1, 0, n, mulT(q[1].inv(n)));
128
                                                                         198
       Poly log(int m) const { return (deriv() *
                                                                                   return ans:
129
                                                                         199
         inv(m)).integr().modxk(m); }
                                                                         200
130
       Poly exp(int m) const {
                                                                         201
                                                                              };
         Poly x(\{1\});
131
         int k = 1;
132
         while (k < m) {
133
                                                                               Sieve
           k *= 2;
134
             = (x * (Poly({1}) - x.log(k) + modxk(k))).modxk(k);
135

    linear sieve

136
137
         return x.modxk(m);
                                                                              vector<int> min_primes(MAX_N), primes;
138
                                                                              primes.reserve(1e5);
       Poly pow(int k, int m) const {
139
                                                                              for (int i = 2; i < MAX_N; i++) {
140
         int i = 0;
                                                                                if (!min_primes[i]) min_primes[i] = i, primes.push_back(i);
         while (i < size() && a[i].x == 0) i++;
                                                                                 for (auto& p : primes) {
         if (i == size() || 1LL * i * k >= m) {
142
                                                                                  if (p * i >= MAX_N) break;
           return Poly(vector<Z>(m));
143
                                                                                  min_primes[p * i] = p;
144
                                                                                   if (i % p == 0) break;
         Z v = a[i];
145
                                                                          9
146
         auto f = divxk(i) * v.inv();
                                                                              }
                                                                          10
         return (f.log(m - i * k) * k).exp(m - i * k).mulxk(i * k)
147
         * power(v, k);
                                                                                 • mobius function
148
       }
       Poly sqrt(int m) const {
149
         Poly x(\{1\});
                                                                              vector<int> min_p(MAX_N), mu(MAX_N), primes;
         int k = 1:
151
                                                                              mu[1] = 1, primes.reserve(1e5);
         while (k < m) {
152
                                                                              for (int i = 2; I < MAX_N; i++) {</pre>
           k *= 2:
153
                                                                                 if (\min_p[i] == 0) {
           x = (x + (modxk(k) * x.inv(k)).modxk(k)) * ((MOD + 1) /
                                                                                  min_p[i] = i;
154
         2);
                                                                                  primes.push_back(i);
         }
155
                                                                                  mu[i] = -1;
156
         return x.modxk(m);
157
                                                                                for (auto p : primes) {
       Poly mulT(Poly b) const {
                                                                                  if (i * p >= MAX_N) break;
158
                                                                          10
159
         if (b.size() == 0) return Poly();
                                                                          11
                                                                                  min_p[i * p] = p;
         int n = b.size();
160
                                                                         12
                                                                                  if (i % p == 0) {
161
         reverse(b.a.begin(), b.a.end());
                                                                                     mu[i * p] = 0;
                                                                         13
         return ((*this) * b).divxk(n - 1);
162
                                                                                     break;
                                                                         14
163
                                                                         15
       Poly divmod(Poly b) const {
164
                                                                                   mu[i * p] = -mu[i];
                                                                         16
165
         auto n = size(), m = b.size();
                                                                                }
                                                                         17
         auto t = *this;
                                                                              }
166
                                                                         18
         reverse(t.a.begin(), t.a.end());
167
         reverse(b.a.begin(), b.a.end());
168
                                                                                 • Euler's totient function
         Poly res = (t * b.inv(n)).modxk(n - m + 1);
169
170
         reverse(res.a.begin(), res.a.end());
                                                                              vector<int> min_p(MAX_N), phi(MAX_N), primes;
171
         return res;
                                                                              phi[1] = 1, primes.reserve(1e5);
172
                                                                              for (int i = 2; i < MAX_N; i++) {
       vector<Z> eval(vector<Z> x) const {
173
                                                                                if (min_p[i] == 0) {
         if (size() == 0) return vector<Z>(x.size(), 0);
174
                                                                                  min_p[i] = i;
         const int n = max(int(x.size()), size());
175
                                                                                  primes.push_back(i);
         vector<Poly> q(4 * n);
176
                                                                                  phi[i] = i - 1;
177
         vector<Z> ans(x.size());
178
         x.resize(n);
                                                                                for (auto p : primes) {
         function<void(int, int, int)> build = [&](int p, int 1,
179
                                                                                  if (i * p >= MAX_N) break;
                                                                          10
         int r) {
                                                                                  min_p[i * p] = p;
                                                                          11
           if (r - 1 == 1) {
180
                                                                                   if (i % p == 0) {
             q[p] = Poly(\{1, -x[1]\});
181
                                                                                     phi[i * p] = phi[i] * p;
                                                                          13
            } else {
182
                                                                          14
             int m = (1 + r) / 2;
183
                                                                         15
             build(2 * p, 1, m), build(2 * p + 1, m, r);
184
                                                                                  phi[i * p] = phi[i] * phi[p];
                                                                         16
             q[p] = q[2 * p] * q[2 * p + 1];
185
                                                                         17
186
                                                                         18
```

187

Gaussian Elimination

```
bool is_0(Z v) { return v.x == 0; }
    Z abs(Z v) { return v; }
    bool is_0(double v) { return abs(v) < 1e-9; }</pre>
    // 1 => unique solution, 0 => no solution, -1 => multiple

→ solutions

    template <typename T>
6
     int gaussian_elimination(vector<vector<T>> &a, int limit) {
         if (a.empty() || a[0].empty()) return -1;
       int h = (int)a.size(), w = (int)a[0].size(), r = 0;
      for (int c = 0; c < limit; c++) {
10
         int id = -1;
11
         for (int i = r; i < h; i++) {
12
          if (!is_0(a[i][c]) \&\& (id == -1 || abs(a[id][c]) <
13
         abs(a[i][c]))) {
14
            id = i:
15
        }
16
         if (id == -1) continue;
17
         if (id > r) {
           swap(a[r], a[id]);
19
20
           for (int j = c; j < w; j++) a[id][j] = -a[id][j];
21
         vector<int> nonzero;
22
         for (int j = c; j < w; j++) {
23
           if (!is_0(a[r][j])) nonzero.push_back(j);
24
25
        T inv_a = 1 / a[r][c];
26
         for (int i = r + 1; i < h; i++) {
27
           if (is_0(a[i][c])) continue;
28
29
           T coeff = -a[i][c] * inv_a;
           for (int j : nonzero) a[i][j] += coeff * a[r][j];
30
        }
31
32
      }
33
34
      for (int row = h - 1; row >= 0; row--) {
35
         for (int c = 0; c < limit; c++) {
           if (!is_0(a[row][c])) {
36
37
             T inv_a = 1 / a[row][c];
             for (int i = row - 1; i >= 0; i--) {
38
               if (is_0(a[i][c])) continue;
39
40
               T coeff = -a[i][c] * inv_a;
               for (int j = c; j < w; j++) a[i][j] += coeff *
41
        a[row][j];
42
             }
43
             break;
          }
44
45
      } // not-free variables: only it on its line
46
      for(int i = r; i < h; i++) if(!is_0(a[i][limit])) return 0;</pre>
47
      return (r == limit) ? 1 : -1;
48
49
50
51
    template <typename T>
    pair<int, vector<T>> solve_linear(vector<vector<T>> a, const
52
     \rightarrow vector<T> &b, int w) {
      int h = (int)a.size();
53
      for (int i = 0; i < h; i++) a[i].push_back(b[i]);</pre>
54
      int sol = gaussian_elimination(a, w);
55
56
      if(!sol) return {0, vector<T>()};
57
      vector<T> x(w, 0);
      for (int i = 0; i < h; i++) {
58
         for (int j = 0; j < w; j++) {
           if (!is_0(a[i][j])) {
60
61
             x[j] = a[i][w] / a[i][j];
62
             break;
63
        }
64
      }
65
66
      return {sol, x};
67
```

is prime

• (Miller–Rabin primality test)

```
i128 power(i128 a, i128 b, i128 MOD = 1, i128 res = 1) {
      for (; b; b /= 2, (a *= a) %= MOD)
2
        if (b & 1) (res *= a) %= MOD;
      return res;
    bool is_prime(ll n) {
      if (n < 2) return false;
      static constexpr int A[] = \{2, 3, 5, 7, 11, 13, 17, 19, 23\};
      int s = __builtin_ctzll(n - 1);
      11 d = (n - 1) >> s;
11
12
      for (auto a : A) {
        if (a == n) return true;
13
         11 x = (11)power(a, d, n);
14
         if (x == 1 | | x == n - 1) continue;
         bool ok = false;
16
         for (int i = 0; i < s - 1; ++i) {
          x = 11((i128)x * x % n); // potential overflow!
18
           if (x == n - 1) {
19
             ok = true;
20
21
             break;
22
23
         if (!ok) return false;
      }
25
      return true;
26
27
    ll pollard_rho(ll x) {
      11 s = 0, t = 0, c = rng() \% (x - 1) + 1;
2
      ll stp = 0, goal = 1, val = 1;
3
      for (goal = 1;; goal *= 2, s = t, val = 1) {
        for (stp = 1; stp <= goal; ++stp) {</pre>
          t = 11(((i128)t * t + c) \% x);
           val = 11((i128)val * abs(t - s) % x);
           if ((stp \% 127) == 0) {
             11 d = gcd(val, x);
             if (d > 1) return d;
10
11
           }
        }
12
         11 d = gcd(val, x);
13
         if (d > 1) return d;
14
      }
15
    }
16
17
    11 get_max_factor(ll _x) {
18
      11 max_factor = 0;
19
      function \langle void(11) \rangle fac = [\&](11 x) \{
20
         if (x <= max_factor || x < 2) return;</pre>
22
         if (is_prime(x)) {
           max_factor = max_factor > x ? max_factor : x;
23
           return;
25
         11 p = x;
         while (p >= x) p = pollard_rho(x);
27
         while ((x \% p) == 0) x /= p;
28
29
         fac(x), fac(p);
      }:
30
      fac(_x);
31
32
      return max_factor;
    Radix Sort
    struct identity {
         template<typename T>
2
3
         T operator()(const T &x) const {
4
             return x:
```

```
struct identity {
    template<typename T>
    T operator()(const T &x) const {
        return x;
    }
};

// A stable sort that sorts in passes of `bits_per_pass` bits
        at a time.
template<typename T, typename T_extract_key = identity>
void radix_sort(vector<T> &data, int bits_per_pass = 10, const
        T_extract_key &extract_key = identity()) {
```

```
if (int64_t(data.size()) * (64 -
        __builtin_clzll(data.size())) < 2 * (1 << bits_per_pass)) {
             stable_sort(data.begin(), data.end(), [&](const T &a,
12
         const T &b) {
                 return extract_key(a) < extract_key(b);</pre>
13
             });
14
             return:
15
16
         using T_key = decltype(extract_key(data.front()));
18
         T_key minimum = numeric_limits<T_key>::max();
19
20
         for (T &x : data)
21
             minimum = min(minimum, extract_key(x));
23
         int max_bits = 0;
25
         for (T &x : data) {
26
27
             T_key key = extract_key(x);
             max_bits = max(max_bits, key == minimum ? 0 : 64 -
28
         __builtin_clzll(key - minimum));
29
30
         int passes = max((max_bits + bits_per_pass / 2) /
31
        bits_per_pass, 1);
32
         if (64 - __builtin_clzll(data.size()) <= 1.5 * passes) {</pre>
33
             stable_sort(data.begin(), data.end(), [&](const T &a,
         const T &b) {
                 return extract_key(a) < extract_key(b);</pre>
35
36
             });
             return;
37
38
         }
39
         vector<T> buffer(data.size());
40
         vector<int> counts:
41
         int bits_so_far = 0;
42
43
         for (int p = 0; p < passes; p++) {
44
             int bits = (max_bits + p) / passes;
             counts.assign(1 << bits, 0);</pre>
46
47
             for (T &x : data) {
48
                 T_key key = T_key(extract_key(x) - minimum);
49
                 counts[(key >> bits_so_far) & ((1 << bits) -</pre>
        1)]++;
51
52
             int count_sum = 0;
53
             for (int &count : counts) {
55
                 int current = count;
57
                 count = count_sum;
58
                 count_sum += current;
             }
60
             for (T &x : data) {
                 T_key key = T_key(extract_key(x) - minimum);
62
                 int key_section = int((key >> bits_so_far) & ((1
63
         << bits) - 1));
                 buffer[counts[key_section]++] = x;
64
             }
65
66
             swap(data, buffer);
67
             bits_so_far += bits;
68
         }
69
    }
70
```

• USAGE

```
radix_sort(edges, 10, [&](const edge &e) -> int { return 

abs(e.weight - x); });
```

lucas

parity of n choose m

```
auto get_parity = [&](11 _n, 11 _m) -> int {
  if (_n == 0 || _m == 0) return 1;
  if ((_n - 1) < _m || _m < 0) return 0;
  return (((_n - 1) - _m) & _m) == 0;
};</pre>
```

String

AC Automaton

```
struct AC_automaton {
      int sz = 26;
      vector<vector<int>> e = {vector<int>(sz)}; // vector is
     vector < int > fail = {0}, end = {0};
      vector<int> fast = {0}; // closest end
      int insert(string& s) {
        int p = 0:
        for (auto c : s) {
          c -= 'a';
10
          if (!e[p][c]) {
11
12
            e.emplace_back(sz);
            fail.emplace_back();
13
14
            end.emplace_back();
            fast.emplace_back();
15
            e[p][c] = (int)e.size() - 1;
16
17
18
          p = e[p][c];
19
        end[p] += 1;
20
21
        return p;
22
      void build() {
24
        queue<int> q;
        for (int i = 0; i < sz; i++)
26
          if (e[0][i]) q.push(e[0][i]);
27
        while (!q.empty()) {
28
          int p = q.front();
29
          q.pop();
          fast[p] = end[p] ? p : fast[fail[p]];
31
          for (int i = 0; i < sz; i++) {
32
            if (e[p][i]) {
33
              fail[e[p][i]] = e[fail[p]][i];
34
              q.push(e[p][i]);
            } else {
36
              e[p][i] = e[fail[p]][i];
38
          }
39
40
        }
41
    };
```

KMP

• nex[i]: length of longest common prefix & suffix for pat[0..i]

```
vector<int> get_next(vector<int> &pat) {
   int m = (int)pat.size();
   vector<int> nex(m);
   for (int i = 1, j = 0; i < m; i++) {
      while (j && pat[j] != pat[i]) j = nex[j - 1];
}</pre>
```

```
if (pat[j] == pat[i]) j++;
                                                                             }
                                                                      36
        nex[i] = j;
                                                                          };
                                                                              • Topo sort on GSAM
      return nex;
9
                                                                          11 sz = gsam.e.size();
                                                                           vector<int> c(sz + 1);
                                                                       2
       • kmp match for txt and pat
                                                                           vector<int> order(sz);
                                                                       3
    auto nex = get_next(pat);
                                                                           for (int i = 1; i < sz; i++) c[gsam.length[i]]++;</pre>
    for (int i = 0, j = 0; i < n; i++) {
                                                                       5 for (int i = 1; i < sz; i++) c[i] += c[i - 1];</pre>
      while (j && pat[j] != txt[i]) j = nex[j - 1];
                                                                       6 for (int i = 1; i < sz; i++) order[c[gsam.length[i]]--] = i;</pre>
      if (pat[j] == txt[i]) j++;
                                                                       7 reverse(order.begin(), order.end()); // reverse so that large
      if (j == m) {
                                                                               len to small
        // do what you want with the match
                                                                              • can be used as an ordinary SAM
        // start index is `i - m + 1`
        j = nex[j - 1];
                                                                              • USAGE (the number of distinct substring)
9
    }
                                                                             int n, last = 0;
                                                                             string s;
                                                                       3
    Z function
                                                                             cin >> n;
                                                                             auto a = GSAM();
       • z[i]: length of longest common prefix of s and s[i:]
                                                                             for (int i = 0; i < n; i++) {
                                                                               cin >> s;
    vector<int> z_function(string s) {
                                                                               last = 0; // reset last
      int n = (int)s.size();
                                                                               for (auto&& c : s) last = a.extend(c, last);
                                                                       9
      vector<int> z(n);
                                                                       10
      for (int i = 1, l = 0, r = 0; i < n; ++i) {
                                                                             11 \text{ ans} = 0;
        if (i <= r) z[i] = min(r - i + 1, z[i - 1]);
                                                                             for (int i = 1; i < a.e.size(); i++) {</pre>
                                                                       12
        while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]]) ++z[i];
                                                                       13
                                                                               ans += a.length[i] - a.length[a.parent[i]];
        if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
                                                                      14
8
                                                                             cout << ans << endl;</pre>
                                                                      15
9
      return z;
                                                                             return 0;
                                                                      17
    General Suffix Automaton
                                                                           Manacher
    constexpr int SZ = 26;
                                                                           string longest_palindrome(string& s) {
                                                                             // init "abc" -> "^$a#b#c$"
    struct GSAM {
                                                                             vector<char> t{'^', '#'};
      vector<vector<int>>> e = {vector<int>(SZ)}; // the labeled
                                                                             for (char c : s) t.push_back(c), t.push_back('#');
     \hookrightarrow edges from node i
                                                                             t.push_back('$');
                                                   // the parent of
      vector<int> parent = {-1};
                                                                             // manacher
                                                                             int n = t.size(), r = 0, c = 0;
      vector<int> length = {0};
                                                   // the length of
                                                                             vector<int> p(n, 0);
     for (int i = 1; i < n - 1; i++) {
                                                                               if (i < r + c) p[i] = min(p[2 * c - i], r + c - i);
                                                                       10
      GSAM(int n) { e.reserve(2 * n), parent.reserve(2 * n),
                                                                               while (t[i + p[i] + 1] == t[i - p[i] - 1]) p[i]++;

    length.reserve(2 * n); };

                                                                      12
                                                                               if (i + p[i] > r + c) r = p[i], c = i;
      int extend(int c, int p) { // character, last
                                                                      13
        bool f = true;
                                  // if already exist
10
                                                                               // s[i] \rightarrow p[2 * i + 2] (even), p[2 * i + 2] (odd)
        int r = 0;
                                   // potential new node
11
                                                                             // output answer
                                                                      15
        if (!e[p][c]) {
                                   // only extend when not exist
12
                                                                             int index = 0:
          f = false;
13
                                                                       17
                                                                             for (int i = 0; i < n; i++)
          e.push_back(vector<int>(SZ));
                                                                               if (p[index] < p[i]) index = i;</pre>
                                                                       18
          parent.push_back(0);
15
                                                                             return s.substr((index - p[index]) / 2, p[index]);
                                                                       19
16
          length.push_back(length[p] + 1);
                                                                      20
          r = (int)e.size() - 1;
17
          for (; ~p && !e[p][c]; p = parent[p]) e[p][c] = r; //
18
        update parents
                                                                           Lyndon
        }
19
        if (f || ~p) {
20
                                                                              • def: suf(s) > s
          int q = e[p][c];
21
          if (length[q] == length[p] + 1) {
                                                                           void duval(const string &s) {
23
            if (f) return q;
                                                                       2
                                                                             int n = (int)s.size();
                                                                             for (int i = 0; i < n;) {
            parent[r] = q;
24
          } else {
                                                                               int j = i, k = i + 1;
25
            e.push_back(e[q]);
                                                                               for (; j < n \&\& s[j] \le s[k]; j++, k++)
26
            parent.push_back(parent[q]);
                                                                                 if (s[j] < s[k]) j = i - 1;
27
            length.push_back(length[p] + 1);
28
            int qq = parent[q] = (int)e.size() - 1;
                                                                               while (i <= j) {
29
            for (; \neg p && e[p][c] == q; p = parent[p]) e[p][c] =
30
                                                                                 // cout << s.substr(i, k - j) << '\n';
                                                                                 i += k - j;
                                                                       10
31
             if (f) return qq;
                                                                               }
                                                                       11
            parent[r] = qq;
                                                                             }
32
                                                                      12
33
                                                                      13
```

14

int main() {

}

return r:

34

```
16 string s;
17 cin >> s;
18 duval(s);
19 }
```