Fortcoders Code Library

askd, yangster67, Nea1

April 29th 2022

Contents Intro

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Main template	1	1	<pre>#include <bits stdc++.h=""></bits></pre>
Fast IO	1	2	using namespace std;
Pragmas (lol)	1	3	and a manuspass sou,
		4	#define $FOR(x,n)$ for(int $x=0;x< n;x++)$
Data Structures	2	5	#define form(i, n) for (int $i = 0$; $i < int(n)$; $i++$)
Segment Tree	2	6	#define all(v) v.begin(), v.end()
Recursive	2	7	using ll = long long;
Iterating	2	9	<pre>using ld = long double; using pii = pair<int, int="">;</int,></pre>
Union Find	3	10	const char nl = '\n';
Fenwick Tree	4	11	,
		12	<pre>int main() {</pre>
PBDS	4	13	<pre>cin.tie(nullptr)->sync_with_stdio(false);</pre>
Treap	4	14	<pre>cout << fixed << setprecision(20);</pre>
Implicit treap	5	15	<pre>// mt19937 \(\to \text{ rng(chrono::steady_clock::now().time_since_epoch().count());} \) </pre>
Persistent implicit treap	5	16	}
2D Sparse Table	6	10	
K-D Tree	6		T TO
Link/Cut Tree	7		Fast IO
,		1	namespace io {
Geometry	7	2	constexpr int SIZE = 1 << 16;
Basic stuff	7	3	<pre>char buf[SIZE], *head, *tail;</pre>
Transformation	8	4	<pre>char get_char() {</pre>
Relation	8	5	<pre>if (head == tail) tail = (head = buf) + fread(buf, 1, SIZE,</pre>
			<pre> stdin); </pre>
Area	9	6 7	<pre>return *head++; }</pre>
Convex	10	8	ll read() {
Basic 3D	11	9	11 x = 0, f = 1;
Miscellaneous	11	10	<pre>char c = get_char();</pre>
		11	for (; !isdigit(c); c = get_char()) (c == '-') && (f = -1);
Graph Theory	11	12	for (; isdigit(c); c = get_char()) x = x * 10 + c - '0';
Max Flow	11	13	<pre>return x * f; }</pre>
PushRelabel Max-Flow (faster)	12	14 15	string read_s() {
Min-Cost Max-Flow	12	16	string str;
Heavy-Light Decomposition	13	17	<pre>char c = get_char();</pre>
General Unweight Graph Matching	13	18	while (c == ' ' c == '\n' c == '\r') c = get_char();
Maximum Bipartite Matching	13	19	while (c != ' ' && c != '\n' && c != '\r') str += c, c =
2-SAT and Strongly Connected Components	14		<pre> get_char(); return etm.</pre>
Enumerating Triangles	14	20 21	return str; }
		22	<pre>void print(int x) {</pre>
Tarjan	14	23	<pre>if (x > 9) print(x / 10);</pre>
Kruskal reconstruct tree	15	24	<pre>putchar(x % 10 '0');</pre>
		25	}
Math	15	26	<pre>void println(int x) { print(x), putchar('\n'); } </pre>
Inverse	15	27 28	<pre>struct Read { Read& operator>>(11& x) { return x = read(), *this; }</pre>
Mod Class	15	29	Read& operator>>(long double& x) { return x =
NTT, FFT, FWT \dots	16		<pre> stold(read_s()), *this; } </pre>
Polynomial Class	16	30	} in;
Sieve	18	31	} // namespace io
Gaussian Elimination	18		
is_prime	19		Pragmas (lol)
Radix Sort	19		raginas (101)
Radix Soft	19	1	<pre>#pragma GCC optimize(2)</pre>
String	20	2	#pragma GCC optimize(3)
String	20	3	#pragma GCC optimize("Ofast")
AC Automaton	20	4	<pre>#pragma GCC optimize("inline") #pragma GCC optimize("-fgcse")</pre>
KMP	20	5 6	<pre>#pragma GCC optimize("-fgcse") #pragma GCC optimize("-fgcse-lm")</pre>
Z function	20	7	#pragma GCC optimize("-fipa-sra")
General Suffix Automaton	20	8	<pre>#pragma GCC optimize("-ftree-pre")</pre>
Manacher	21	9	<pre>#pragma GCC optimize("-ftree-vrp")</pre>
Lyndon	21	10	<pre>#pragma GCC optimize("-fpeephole2")</pre>
		11	<pre>#pragma GCC optimize("-ffast-math") #pragma GCC optimize("-fsched-spec")</pre>
		12 13	<pre>#pragma GCC optimize("-fschea-spec") #pragma GCC optimize("unroll-loops")</pre>
		14	#pragma GCC optimize("-falign-jumps")
		15	#pragma GCC optimize("-falign-loops")

```
#pragma GCC optimize("-falign-labels")
                                                                          34 };
    #pragma GCC optimize("-fdevirtualize")
17
    #pragma GCC optimize("-fcaller-saves")
                                                                                 • Persistent implicit, range query + point update
18
    \#pragma\ GCC\ optimize("-fcrossjumping")
19
                                                                               struct Node {
    #pragma GCC optimize("-fthread-jumps")
#pragma GCC optimize("-funroll-loops")
20
                                                                          2
                                                                                 int lc = 0, rc = 0, p = 0;
21
    #pragma GCC optimize("-fwhole-program")
                                                                          3
                                                                              };
22
    #pragma GCC optimize("-freorder-blocks")
                                                                               struct SegTree {
                                                                          5
    #pragma GCC optimize("-fschedule-insns")
24
                                                                                 vector<Node> t = {{}}; // init all
     #pragma GCC optimize("inline-functions")
25
                                                                                 SegTree() = default;
    #pragma GCC optimize("-ftree-tail-merge")
    #pragma GCC optimize("-fschedule-insns2")
                                                                                 SegTree(int n) { t.reserve(n * 20); }
27
                                                                                 int modify(int p, int l, int r, int x, int v) {
    #pragma GCC optimize("-fstrict-aliasing")
                                                                                   // p: original node, update a[x] \rightarrow v
                                                                          10
    \textit{\#pragma GCC optimize("-fstrict-overflow")}
29
                                                                                   t.push_back(t[p]);
    #pragma GCC optimize("-falign-functions")
#pragma GCC optimize("-fcse-skip-blocks")
                                                                          11
                                                                                   int u = (int)t.size() - 1;
                                                                          12
31
                                                                                   if (r - 1 == 1) {
    #pragma GCC optimize("-fcse-follow-jumps")
                                                                          13
32
                                                                                    t[u].p = v;
    #pragma GCC optimize("-fsched-interblock")
33
    #pragma GCC optimize("-fpartial-inlining")
                                                                                   } else {
                                                                          15
34
                                                                                     int m = (1 + r) / 2;
                                                                          16
    #pragma GCC optimize("no-stack-protector")
    #pragma GCC optimize("-freorder-functions")
                                                                          17
                                                                                     if (x < m) {
36
                                                                                       t[u].lc = modify(t[p].lc, l, m, x, v);
    #pragma GCC optimize("-findirect-inlining")
                                                                          18
37
    #pragma GCC optimize("-fhoist-adjacent-loads")
                                                                          19
                                                                                       t[u].rc = t[p].rc;
38
                                                                                     } else {
                                                                          20
     #pragma GCC optimize("-frerun-cse-after-loop")
39
                                                                          ^{21}
                                                                                       t[u].lc = t[p].lc;
     #pragma GCC optimize("inline-small-functions")
    #pragma GCC optimize("-finline-small-functions")
                                                                                       t[u].rc = modify(t[p].rc, m, r, x, v);
                                                                          22
41
    #pragma GCC optimize("-ftree-switch-conversion")
                                                                          23
                                                                          24
                                                                                     t[u].p = t[t[u].lc].p + t[t[u].rc].p;
    #pragma GCC optimize("-foptimize-sibling-calls")
43
                                                                          25
     #pragma GCC optimize("-fexpensive-optimizations")
44
    #pragma GCC optimize("-funsafe-loop-optimizations")
                                                                                   return u;
    #pragma GCC optimize("inline-functions-called-once")
                                                                          27
46
                                                                                 int query(int p, int l, int r, int x, int y) {
    \textit{\#pragma GCC optimize("-fdelete-null-pointer-checks")}
                                                                                   // query sum a[x]...a[y-1] rooted at p
    #pragma GCC
     \leftrightarrow target("sse,sse2,sse3,sse4.1,sse4.2,avx,avx2,popcnt,tun2 native" t[p] holds the info of [l, r]
                                                                                   if (x <= 1 && r <= y) return t[p].p;
                                                                                   int m = (1 + r) / 2, res = 0;
                                                                                   if (x < m) res += query(t[p].lc, l, m, x, y);</pre>
    Data Structures
                                                                                   if (y > m) res += query(t[p].rc, m, r, x, y);
                                                                          34
                                                                          35
                                                                                   return res;
    Segment Tree
                                                                                 }
                                                                          36
                                                                              };
                                                                          37
    Recursive
```

• Implicit segment tree, range query + point update

```
struct Node {
      int lc, rc, p;
    struct SegTree {
5
      vector<Node> t = {{}};
      SegTree(int n) { t.reserve(n * 40); }
       int modify(int p, int 1, int r, int x, int v) {
        int u = p;
9
         if (p == 0) {
10
11
           t.push_back(t[p]);
           u = (int)t.size() - 1;
12
        if (r - l == 1) {
14
15
           t[u].p = t[p].p + v;
         } else {
16
          int m = (1 + r) / 2;
17
           if (x < m) {
             t[u].lc = modify(t[p].lc, l, m, x, v);
19
             t[u].rc = modify(t[p].rc, m, r, x, v);
21
22
          t[u].p = t[t[u].lc].p + t[t[u].rc].p;
23
24
        return u;
25
26
      int query(int p, int 1, int r, int x, int y) {
27
        if (x <= 1 && r <= y) return t[p].p;
28
29
         int m = (1 + r) / 2, res = 0;
         if (x < m) res += query(t[p].lc, l, m, x, y);</pre>
        if (y > m) res += query(t[p].rc, m, r, x, y);
31
        return res;
      }
```

Iterating

• Iterating, range query + point update

```
struct Node {
 1
      11 v = 0, init = 0;
    }:
3
    Node pull(const Node &a, const Node &b) {
       if (!a.init) return b;
       if (!b.init) return a;
      Node c;
       return c;
    }
10
11
12
     struct SegTree {
13
       vector<Node> t;
       SegTree(ll _n) : n(_n), t(2 * n){};
15
       void modify(ll p, const Node &v) {
17
        t[p += n] = v;
         for (p \neq 2; p; p \neq 2) t[p] = pull(t[p * 2], t[p * 2 +
18

→ 1]);

19
20
       Node query(ll 1, ll r) {
21
         Node left, right;
         for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
22
           if (1 & 1) left = pull(left, t[1++]);
23
           if (r & 1) right = pull(t[--r], right);
24
26
         return pull(left, right);
27
    };
28
```

• Iterating, range query + range update

```
struct SegTree {
                                                                        27
                                                                               T query_all() { return tree[1]; }
      11 n, h = 0;
                                                                               void consume(int i) { tree[i] = tree[i << 1] * tree[i << 1 |</pre>
       vector<Node> t;
      SegTree(ll _n) : n(_n), h((ll)log2(n)), t(n * 2) {}
                                                                             };
                                                                        29
       void apply(ll x, ll v) {
                                                                        30
        if (v == 0) {
                                                                        31
          t[x].one = 0;
                                                                             struct SegInfo {
                                                                        32
        } else {
                                                                        33
           t[x].one = t[x].total;
                                                                               SegInfo() : SegInfo(0) {}
9
                                                                        34
10
                                                                        35
                                                                                SegInfo(ll val) : v(val) {}
                                                                                SegInfo operator*(SegInfo b) {
        t[x].lazy = v;
11
                                                                                 return SegInfo(v + b.v);
12
                                                                        37
       void build(ll 1) {
                                                                               }
13
                                                                        38
        for (1 = (1 + n) / 2; 1 > 0; 1 /= 2) {
                                                                             }:
14
                                                                        39
15
           if (t[1].lazy == -1) {
16
             t[1] = pull(t[1 * 2], t[1 * 2 + 1]);
17
                                                                             Union Find
18
        }
19
                                                                             vector<int> p(n);
20
      void push(11 1) {
                                                                             iota(p.begin(), p.end(), 0);
        1 += n;
21
                                                                            function \langle int(int) \rangle find = [&](int x) { return p[x] == x ? x :
        for (ll s = h; s > 0; s--) {
                                                                              \Leftrightarrow (p[x] = find(p[x])); \};
           ll i = 1 >> s;
23
                                                                             auto merge = [&](int x, int y) { p[find(x)] = find(y); };
           if (t[i].lazy != -1) {
24
             apply(2 * i, t[i].lazy);
25
                                                                                • Persistent version
             apply(2 * i + 1, t[i].lazy);
26
                                                                             struct Node {
28
           t[i].lazy = -1;
                                                                               int lc, rc, p;
29
                                                                             };
                                                                         3
30
      void modify(ll 1, ll r, int v) {
31
                                                                             struct SegTree {
                                                                         5
        push(1), push(r - 1);
32
                                                                               vector<Node> t = \{\{0, 0, -1\}\}; // init all
         11\ 10 = 1, r0 = r;
33
                                                                               SegTree() = default;
         for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
34
                                                                               SegTree(int n) { t.reserve(n * 20); }
           if (1 & 1) apply(1++, v);
35
                                                                                int modify(int p, int l, int r, int x, int v) {
           if (r & 1) apply(--r, v);
36
                                                                         10
                                                                                 // p: original node, update a[x] \rightarrow v
37
                                                                                 t.push_back(t[p]);
                                                                        11
        build(10), build(r0 - 1);
38
                                                                                 int u = (int)t.size() - 1;
                                                                         12
39
                                                                                 if (r - 1 == 1) {
                                                                        13
      Node query(ll 1, ll r) {
40
                                                                         14
                                                                                   t[u].p = v;
        push(1), push(r - 1);
41
                                                                                 } else {
                                                                        15
         Node left, right;
42
                                                                                   int m = (1 + r) / 2;
                                                                        16
         for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
43
                                                                        17
                                                                                   if (x < m) {
44
           if (1 & 1) left = pull(left, t[1++]);
                                                                                      t[u].lc = modify(t[p].lc, l, m, x, v);
                                                                        18
           if (r & 1) right = pull(t[--r], right);
45
                                                                                      t[u].rc = t[p].rc;
46
                                                                                    } else {
                                                                        20
47
         return pull(left, right);
                                                                                      t[u].lc = t[p].lc;
48
                                                                                      t[u].rc = modify(t[p].rc, m, r, x, v);
                                                                        22
    };
                                                                         23
                                                                                    t[u].p = t[t[u].lc].p + t[t[u].rc].p;
       • AtCoder Segment Tree (recursive structure but iterative)
    template <class T> struct PointSegmentTree {
                                                                                 return u;
2
      int size = 1;
                                                                        27
       vector<T> tree;
                                                                                int query(int p, int l, int r, int x, int y) {
3
                                                                         28
      PointSegmentTree(int n) : PointSegmentTree(vector<T>(n)) {}
                                                                                 // query sum a[x]...a[y-1] rooted at p
                                                                                  // t[p] holds the info of [l, r)
      PointSegmentTree(vector<T>& arr) {
                                                                        30
        while(size < (int)arr.size())</pre>
                                                                                  if (x \le 1 \&\& r \le y) return t[p].p;
           size <<= 1:
                                                                                  int m = (1 + r) / 2, res = 0;
                                                                        32
         tree = vector<T>(size << 1);</pre>
                                                                         33
                                                                                  if (x < m) res += query(t[p].lc, l, m, x, y);
        for(int i = size + arr.size() - 1; i >= 1; i--)
                                                                                  if (y > m) res += query(t[p].rc, m, r, x, y);
9
                                                                        34
           if(i >= size) tree[i] = arr[i - size];
                                                                                  return res;
10
                                                                        35
           else consume(i);
                                                                               }
11
                                                                        36
                                                                             };
12
                                                                        37
       void set(int i, T val) {
13
        tree[i += size] = val;
                                                                             struct DSU {
14
                                                                        39
         for(i >>= 1; i >= 1; i >>= 1)
                                                                               int n;
15
                                                                        40
           consume(i);
                                                                        41
                                                                               SegTree seg;
16
                                                                               DSU(int _n) : n(_n), seg(n) {}
17
                                                                        42
      T get(int i) { return tree[i + size]; }
                                                                               int get(int p, int x) { return seg.query(p, 0, n, x, x + 1);
18
      T query(int 1, int r) {
19
                                                                              → }
                                                                               int set(int p, int x, int v) { return seg.modify(p, 0, n, x,
         T resl, resr;
20
         for(1 += size, r += size + 1; 1 < r; 1 >>= 1, r >>= 1) {
21
                                                                              22
           if(1 & 1) resl = resl * tree[1++];
                                                                        45
                                                                               int find(int p, int x) {
23
           if(r & 1) resr = tree[--r] * resr;
                                                                                 int parent = get(p, x);
                                                                                 if (parent < 0) return x;</pre>
24
                                                                        47
        return resl * resr;
                                                                                  return find(p, parent);
      }
                                                                        49
```

```
int is_same(int p, int x, int y) { return find(p, x) ==
     \rightarrow find(p, y); }
      int merge(int p, int x, int y) {
51
         int rx = find(p, x), ry = find(p, y);
52
         if (rx == ry) return -1;
53
         int rank_x = -get(p, rx), rank_y = -get(p, ry);
54
         if (rank_x < rank_y) {</pre>
55
           p = set(p, rx, ry);
         } else if (rank_x > rank_y) {
57
58
           p = set(p, ry, rx);
         } else {
59
           p = set(p, ry, rx);
60
           p = set(p, rx, -rx - 1);
61
62
63
         return p;
64
      }
    };
65
```

Fenwick Tree

• askd version

```
template <typename T> struct FenwickTree {
      int size = 1, high_bit = 1;
      vector<T> tree;
      FenwickTree(int _size) : size(_size) {
         tree.resize(size + 1);
6
         while((high_bit << 1) <= size) high_bit <<= 1;</pre>
      FenwickTree(vector<T>& arr) : FenwickTree(arr.size()) {
         for(int i = 0; i < size; i++) update(i, arr[i]);</pre>
10
      }
11
      int lower_bound(T x) {
         int res = 0; T cur = 0;
12
         for(int bit = high_bit; bit > 0; bit >>= 1) {
13
           if((res|bit) <= size && cur + tree[res|bit] < x) {</pre>
             res |= bit; cur += tree[res];
15
16
17
         }
18
        return res;
      T prefix_sum(int i) {
20
         T ret = 0;
21
         for(i++; i > 0; i -= (i \& -i)) ret += tree[i];
22
         return ret;
23
      T range_sum(int 1, int r) { return (1 > r) ? 0 :
25

→ prefix_sum(r) - prefix_sum(1 - 1); }

      void update(int i, T delta) { for(i++; i <= size; i += (i &</pre>
26
     → -i)) tree[i] += delta; }
    };
```

• Nea1 version

```
template <typename T>
    struct Fenwick {
      const int n;
      vector<T> a;
      Fenwick(int n) : n(n), a(n) {}
      void add(int x, T v) {
        for (int i = x + 1; i \le n; i += i \& -i) {
           a[i - 1] += v;
8
9
10
      T sum(int x) {
11
         T ans = 0;
12
13
         for (int i = x; i > 0; i -= i & -i) {
14
           ans += a[i - 1];
15
        return ans;
16
17
      T rangeSum(int 1, int r) { return sum(r) - sum(1); }
18
    };
```

PBDS

```
#include <bits/stdc++.h>
    #include <ext/pb_ds/assoc_container.hpp>
    using namespace std;
    using namespace __gnu_pbds;
    template<typename T>
    using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,

    tree_order_statistics_node_update>;
    template<typename T, typename X>
    using ordered_map = tree<T, X, less<T>, rb_tree_tag,

    tree_order_statistics_node_update>;

    template<typename T, typename X>
    using fast_map = cc_hash_table<T, X>;
    template<typename T, typename X>
11
    using ht = gp_hash_table<T, X>;
12
13
    mt19937_64

    rng(chrono::steady_clock::now().time_since_epoch().count());

14
    struct splitmix64 {
        size_t operator()(size_t x) const {
16
            static const size_t fixed =
17
        chrono::steady_clock::now().time_since_epoch().count();
            x += 0x9e3779b97f4a7c15 + fixed;
18
            x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
            x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
20
             return x \hat{} (x >> 31);
21
22
    };
23
```

Treap

• (No rotation version)

```
struct Node {
      Node *1, *r;
       int s, sz;
       // int t = 0, a = 0, g = 0; // for lazy propagation
      Node(int _s) : l(nullptr), r(nullptr), s(_s), sz(1),

    w(rng()) {}
      void apply(int vt, int vg) {
        // for lazy propagation
9
        // s -= vt;
        // t += vt, a += vg, g += vg;
11
13
      void push() {
        // for lazy propagation
14
         // if (l != nullptr) l->apply(t, g);
        // if (r != nullptr) r->apply(t, g);
         // t = g = 0;
18
       void pull() { sz = 1 + (1 ? 1->sz : 0) + (r ? r->sz : 0); }
19
20
    }:
21
    std::pair<Node *, Node *> split(Node *t, int v) {
      if (t == nullptr) return {nullptr, nullptr};
23
24
       t->push();
      if (t->s < v) {
25
        auto [x, y] = split(t->r, v);
26
        t->r = x:
27
        t->pull();
28
29
        return {t, y};
       } else {
30
31
         auto [x, y] = split(t->1, v);
         t->1 = y;
32
        t->pull();
33
34
         return {x, t};
35
    }
36
37
38
    Node *merge(Node *p, Node *q) {
      if (p == nullptr) return q;
       if (q == nullptr) return p;
40
       if (p->w < q->w) swap(p, q);
      auto [x, y] = split(q, p->s + rng() % 2);
```

```
43
      p->push();
      p->1 = merge(p->1, x);
44
      p->r = merge(p->r, y);
      p->pull();
46
47
      return p;
48
49
    Node *insert(Node *t, int v) {
      auto [x, y] = split(t, v);
51
      return merge(merge(x, new Node(v)), y);
52
53
54
    Node *erase(Node *t, int v) {
      auto [x, y] = split(t, v);
56
      auto [p, q] = split(y, v + 1);
58
      return merge(merge(x, merge(p->1, p->r)), q);
59
60
    int get_rank(Node *&t, int v) {
61
      auto [x, y] = split(t, v);
      int res = (x ? x->sz : 0) + 1;
63
      t = merge(x, y);
65
      return res;
66
67
    Node *kth(Node *t, int k) {
68
      while (true) {
70
         int left_sz = t->1 ? t->1->sz : 0;
71
72
         if (k < left_sz) {</pre>
          t = t->1;
73
        } else if (k == left_sz) {
          return t:
75
         } else {
76
          k \rightarrow left_sz + 1, t = t->r;
77
78
80
81
    Node *get_prev(Node *&t, int v) {
82
      auto [x, y] = split(t, v);
83
      Node *res = kth(x, x->sz);
      t = merge(x, y);
85
86
      return res;
87
88
89
    Node *get_next(Node *&t, int v) {
      auto [x, y] = split(t, v + 1);
90
      Node *res = kth(y, 1);
91
      t = merge(x, y);
92
      return res;
       • USAGE
    int main() {
      cin.tie(nullptr)->sync_with_stdio(false);
      cin >> n;
      Node *t = nullptr;
6
      for (int op, x; n--;) {
        cin >> op >> x;
        if (op == 1) {
          t = insert(t, x);
        } else if (op == 2) {
10
           t = erase(t, x);
11
        } else if (op == 3) {
12
13
          cout << get_rank(t, x) << "\n";
         } else if (op == 4) {
           cout << kth(t, x)->s << "\n";
15
         } else if (op == 5) {
           cout << get_prev(t, x)->s << "\n";</pre>
17
18
19
           \verb|cout| << | get_next(t, x) -> s | << "\n";
20
      }
21
   }
```

Implicit treap

• Split by size

```
struct Node {
2
       Node *1, *r;
       int s, sz;
       // int lazy = 0;
       Node(int _s) : l(nullptr), r(nullptr), s(_s), sz(1),
      \rightarrow w(rnd()) {}
       void apply() {
        // for lazy propagation
9
         // lazy ^= 1;
10
       }
11
       void push() {
12
         // for lazy propagation
13
         // if (lazy) {
14
         // swap(l, r);
// if (l != nullptr) l->apply();
// if (r != nullptr) r->apply();
16
17
            lazy = 0;
         //
18
         // }
19
       }
20
       void pull() { sz = 1 + (1 ? 1->sz : 0) + (r ? r->sz : 0); }
21
22
23
     std::pair<Node *, Node *> split(Node *t, int v) {
24
       // first->sz == v
       if (t == nullptr) return {nullptr, nullptr};
26
27
       t->push();
       int left_sz = t->1 ? t->1->sz : 0;
28
       if (left_sz < v) {</pre>
30
         auto [x, y] = split(t->r, v - left_sz - 1);
         t->r = x;
31
         t->pull();
         return {t, y};
33
       } else {
         auto [x, y] = split(t->1, v);
35
         t->1 = y;
36
37
         t->pull();
         return {x, t};
38
39
    }
40
41
     Node *merge(Node *p, Node *q) {
42
       if (p == nullptr) return q;
43
       if (q == nullptr) return p;
       if (p->_W < q->_W) {
45
46
         p->push();
47
         p->r = merge(p->r, q);
         p->pull();
48
         return p;
       } else {
50
         q->push();
         q->1 = merge(p, q->1);
52
         q->pull();
53
         return q;
54
55
```

Persistent implicit treap

```
pair<Node *, Node *> split(Node *t, int v) {
      // first -> sz == v
      if (t == nullptr) return {nullptr, nullptr};
      t->push();
      int left_sz = t->1 ? t->1->sz : 0;
      t = new Node(*t);
      if (left_sz < v) \{
        auto [x, y] = split(t->r, v - left_sz - 1);
9
        t->r = x;
10
        t->pull();
        return {t, y};
11
      } else {
        auto [x, y] = split(t->1, v);
```

```
t->1 = y;
        t->pull();
                                                                            SparseTable2d<int> st(test);
                                                                                                                         // Range min query
15
         return {x, t};
                                                                            SparseTable2d<int,greater<int>>> st2(test); // Range max query
16
      }
17
18
                                                                            K-D Tree
19
    Node *merge(Node *p, Node *q) {
20
                                                                            struct Point {
      if (p == nullptr) return new Node(*q);
                                                                        1
      if (q == nullptr) return new Node(*p);
                                                                        2
                                                                             int x, y;
22
                                                                           }:
      if (p->w < q->w) {
                                                                        3
23
                                                                            struct Rectangle {
        p = new Node(*p);
24
                                                                             int lx, rx, ly, ry;
        p->push();
25
                                                                        6
        p->r = merge(p->r, q);
        p->pull();
27
                                                                            bool is_in(const Point &p, const Rectangle &rg) {
         return p;
                                                                             return (p.x >= rg.lx) && (p.x <= rg.rx) && (p.y >= rg.ly) &&
29
      } else {
                                                                            q = new Node(*q);
30
                                                                       10
31
         q->push();
         q->1 = merge(p, q->1);
                                                                       11
32
                                                                            struct KDTree {
         q->pull();
                                                                       12
                                                                              vector<Point> points;
                                                                       13
34
        return q;
                                                                              struct Node {
35
                                                                       14
                                                                                int lc, rc;
    }
                                                                       15
                                                                                Point point;
                                                                       16
                                                                                Rectangle range:
                                                                       17
    2D Sparse Table
                                                                              };
                                                                       19
                                                                       20
                                                                              vector<Node> nodes;

    Sorry that this sucks - askd

                                                                       21
                                                                              int root = -1;
    template <class T, class Compare = less<T>>
                                                                              KDTree(const vector<Point> &points_) {
                                                                       22
    struct SparseTable2d {
                                                                                points = points_;
      int n = 0, m = 0;
                                                                                Rectangle range = {-1e9, 1e9, -1e9, 1e9};
                                                                       24
      T**** table;
                                                                                root = tree_construct(0, (int)points.size(), range, 0);
                                                                       25
      int* log;
                                                                       26
      inline T choose(T x, T y) {
                                                                              int tree_construct(int 1, int r, Rectangle range, int depth)
                                                                       27
        return Compare()(x, y) ? x : y;
                                                                                if (1 == r) return -1;
                                                                       28
      SparseTable2d(vector<vector<T>>& grid) {
                                                                       29
                                                                                if (1 > r) throw;
                                                                                int mid = (1 + r) / 2;
         if(grid.empty() || grid[0].empty()) return;
                                                                       30
10
         n = grid.size(); m = grid[0].size();
                                                                                auto comp = (depth % 2) ? [](Point &a, Point &b) { return
                                                                       31
11
         log = new int[max(n, m) + 1];
                                                                            \rightarrow a.x < b.x; }
         log[1] = 0;
                                                                                                         : [](Point &a, Point &b) { return
13
                                                                       32
         for(int i = 2; i <= max(n, m); i++)
                                                                            \rightarrow a.y < b.y; };
          log[i] = log[i - 1] + ((i ^ (i - 1)) > i);
                                                                                nth_element(points.begin() + 1, points.begin() + mid,
15
                                                                       33

→ points.begin() + r, comp);

         table = new T***[n];
16
         for(int i = n - 1; i >= 0; i--) {
                                                                                Rectangle l_range(range), r_range(range);
                                                                       34
17
                                                                                if (depth % 2) {
18
           table[i] = new T**[m];
                                                                       35
           for(int j = m - 1; j >= 0; j--) {
                                                                                  l_range.rx = points[mid].x;
                                                                                  r_range.lx = points[mid].x;
            table[i][j] = new T*[log[n - i] + 1];
20
                                                                       37
            for(int k = 0; k <= log[n - i]; k++) {</pre>
22
               table[i][j][k] = new T[log[m - j] + 1];
                                                                       39
                                                                                  l_range.ry = points[mid].y;
               if(!k) table[i][j][k][0] = grid[i][j];
                                                                                  r_range.ly = points[mid].y;
                                                                       40
23
               else table[i][j][k][0] = choose(table[i][j][k-1][0],
                                                                                Node node = {tree_construct(1, mid, 1_range, depth + 1),
        table[i+(1<<(k-1))][j][k-1][0]);
                                                                       42
               for(int 1 = 1; 1 <= log[m - j]; 1++)
                                                                                             tree_construct(mid + 1, r, r_range, depth +
25
                 table[i][j][k][l] = choose(table[i][j][k][l-1],
                                                                            → 1), points[mid], range, r - 1);
26
        table[i][j+(1<<(1-1))][k][1-1]);
                                                                       44
                                                                                nodes.push_back(node);
27
                                                                       45
                                                                                return (int)nodes.size() - 1;
          }
28
                                                                       46
        }
29
                                                                       47
      }
                                                                              int inner_query(int id, const Rectangle &rec, int depth) {
30
                                                                       48
                                                                                if (id == -1) return 0;
      T query(int r1, int r2, int c1, int c2) {
31
         assert(r1 >= 0 \&\& r2 < n \&\& r1 <= r2);
                                                                                Rectangle rg = nodes[id].range;
32
                                                                       50
         assert(c1 >= 0 && c2 < m && c1 <= c2);
                                                                                if (rg.lx >= rec.lx && rg.rx <= rec.rx && rg.ly >= rec.ly
33
                                                                       51
         int rl = log[r2 - r1 + 1], cl = log[c2 - c1 + 1];
                                                                            return nodes[id].num;
         T ca1 = choose(table[r1][c1][r1][c1],
35
                                                                       52
        table[r2-(1<<rl)+1][c1][r1][c1]);
                                                                       53
                                                                                int ans = 0;
         T ca2 = choose(table[r1][c2-(1<<c1)+1][r1][c1],
                                                                       54
                                                                                if (depth % 2) { // pruning
        table[r2-(1<<rl)+1][c2-(1<<cl)+1][r1][c1]);
                                                                       55
                                                                                  if (rec.lx <= nodes[id].point.x) ans +=</pre>
37
         return choose(ca1, ca2);
                                                                       56
      }

    inner_query(nodes[id].lc, rec, depth + 1);

38
                                                                       57
                                                                                  if (rec.rx >= nodes[id].point.x) ans +=
                                                                                inner_query(nodes[id].rc, rec, depth + 1);
       • USAGE
                                                                       58
                                                                                  if (rec.ly <= nodes[id].point.y) ans +=</pre>
                                                                       59
    vector<vector<int>> test = {

    inner_query(nodes[id].lc, rec, depth + 1);

      \{1, 2, 3, 4\}, \{2, 3, 4, 5\}, \{9, 9, 9, 9\}, \{-1, -1, -1, -1\}
```

if (rec.ry >= nodes[id].point.y) ans +=
inner_query(nodes[id].rc, rec, depth + 1);

```
61
         if (is_in(nodes[id].point, rec)) ans += 1;
62
                                                                              64
63
64
                                                                              66
      int query(const Rectangle &rec) { return inner_query(root,
65
                                                                              67

→ rec, 0); }
                                                                              68
    }:
66
                                                                              69
                                                                                  }
                                                                              71
                                                                              72
     Link/Cut Tree
                                                                              73
                                                                              74
     struct Node {
       Node *ch[2], *p;
                                                                                  }
                                                                              76
       int id:
                                                                              77
       bool rev:
                                                                              78
       Node(int id) : ch{nullptr, nullptr}, p(nullptr), id(id),
                                                                              79

    rev(false) {}
                                                                              80
       friend void reverse(Node *p) {
                                                                              81
         if (p != nullptr) {
           swap(p->ch[0], p->ch[1]);
           p->rev ^= 1;
10
11
       }
       void push() {
12
         if (rev) {
13
           reverse(ch[0]);
14
           reverse(ch[1]);
15
                                                                               2
           rev = false;
         }
17
18
19
       void pull() {}
       \label{eq:bool} \begin{tabular}{ll} bool is\_root() & return $p == nullptr \mid \mid p -> ch[0] != this \&\& \\ \end{tabular}
20
      \rightarrow p->ch[1] != this; }
       bool pos() { return p->ch[1] == this; }
21
       void rotate() {
         Node *q = p;
23
                                                                              10
         bool x = !pos();
24
                                                                              11
         q->ch[!x] = ch[x];
         if (ch[x] != nullptr) ch[x]->p = q;
26
         p = q->p;
         if (!q->is\_root()) q->p->ch[q->pos()] = this;
28
         ch[x] = q;
29
                                                                              14
         q->p = this;
30
         pull();
31
                                                                              15
32
         q->pull();
33
                                                                              16
34
       void splay() {
                                                                              17
         vector<Node *> s;
35
         for (Node *i = this; !i->is_root(); i = i->p)
36
         s.push_back(i->p);
         while (!s.empty()) s.back()->push(), s.pop_back();
37
         push();
                                                                              20
39
         while (!is_root()) {
            if (!p->is_root()) {
40
                                                                              21
41
              if (pos() == p->pos()) {
                p->rotate();
42
                                                                              22
              } else {
                                                                              23
44
                rotate();
                                                                              24
45
           }
46
                                                                              26
           rotate();
47
                                                                              27
48
         pull();
49
51
       void access() {
         for (Node *i = this, *q = nullptr; i != nullptr; q = i, i
52
                                                                              31
         = i->p) {
                                                                              32
           i->splay();
53
                                                                              33
           i->ch[1] = q;
54
           i->pull();
55
                                                                              35
56
                                                                              36
57
         splay();
                                                                              37
58
                                                                              38
59
       void makeroot() {
         access():
60
                                                                              40
         reverse(this);
62
```

Geometry

Basic stuff

```
using ll = long long;
using ld = long double;
constexpr auto eps = 1e-8;
const auto PI = acos(-1);
int sgn(ld x) \{ return (abs(x) \le eps) ? 0 : (x < 0 ? -1 : 1); 
struct Point {
  1d x = 0, y = 0;
  Point() = default;
  Point(ld _x, ld _y) : x(_x), y(_y) {}
  bool operator<(const Point &p) const { return !sgn(p.x - x)</pre>
 \hookrightarrow \quad ? \quad \operatorname{sgn}(y - p.y) < 0 : x < p.x; \}
 bool operator==(const Point &p) const { return !sgn(p.x - x)
 \leftrightarrow && !sgn(p.y - y); }
 Point operator+(const Point &p) const { return {x + p.x, y +
\rightarrow p.y}; }
 Point operator-(const Point &p) const { return {x - p.x, y -
\rightarrow p.y}; }
  Point operator*(ld a) const { return {x * a, y * a}; }
  Point operator/(ld a) const { return {x / a, y / a}; }
  auto operator*(const Point &p) const { return x * p.x + y *
 \Rightarrow p.y; } // dot
  auto operator^(const Point &p) const { return x * p.y - y *

    p.x; } // cross

  friend auto &operator>>(istream &i, Point &p) { return i >>
\rightarrow p.x >> p.y; }
  friend auto &operator << (ostream &o, Point p) { return o <<

    p.x << ' ' << p.y; }
</pre>
}:
struct Line {
  Point s = \{0, 0\}, e = \{0, 0\};
  Line() = default;
  Line(Point _s, Point _e) : s(_s), e(_e) {}
  friend auto &operator>>(istream &i, Line &1) { return i >>
\hookrightarrow 1.s >> 1.e; } // ((x1, y1), (x2, y2)
struct Segment : Line {
  using Line::Line;
};
struct Circle {
  Point o = {0, 0};
  ld r = 0;
  Circle() = default;
  Circle(Point _o, ld _r) : o(_o), r(_r) {}
auto dist2(const Point &a) { return a * a; }
```

```
auto dist2(const Point &a, const Point &b) { return dist2(a -
                                                                    36 vector<Point> translate(const vector<Point> &p, ld dx = 0, ld
                                                                           \rightarrow dy = 0) {

    b); }

                                                                           int n = p.size();
    auto dist(const Point &a) { return sqrt(dist2(a)); }
    auto dist(const Point &a, const Point &b) { return
                                                                            vector<Point> res(n);
                                                                      38

    sqrt(dist2(a - b)); }

                                                                            for (int i = 0; i < n; i++)
                                                                      39
                                                                              res[i] = translate(p[i], dx, dy);
    auto dist(const Point &a, const Line &1) { return abs((a -
                                                                      40
     return res:
                                                                      41
    auto dist(const Point &p, const Segment &1) {
                                                                          }
     if (l.s == l.e) return dist(p, l.s);
      auto d = dist2(1.s, 1.e), t = min(d, max((1d)0, (p - 1.s) *)
                                                                          Relation
     \hookrightarrow (l.e - l.s)));
      return dist((p - 1.s) * d, (1.e - 1.s) * t) / d;
                                                                          enum class Relation { SEPARATE, EX_TOUCH, OVERLAP, IN_TOUCH,
   }
10
                                                                           → INSIDE };
    /* Needs is_intersect
11
                                                                          Relation get_relation(const Circle &a, const Circle &b) {
                                                                       2
    auto dist(const Segment &11, const Segment &12) {
                                                                            auto c1c2 = dist(a.o, b.o);
      if (is_intersect(l1, l2)) return (ld)0;
                                                                            auto r1r2 = a.r + b.r, diff = abs(a.r - b.r);
      return min({dist(l1.s, l2), dist(l1.e, l2), dist(l2.s, l1),
                                                                            if (sgn(c1c2 - r1r2) > 0) return Relation::SEPARATE;
     \rightarrow dist(l2.e, l1)});
                                                                             if (sgn(c1c2 - r1r2) == 0) return Relation::EX_TOUCH;
15
                                                                            if (sgn(c1c2 - diff) > 0) return Relation::OVERLAP;
16
                                                                             if (sgn(c1c2 - diff) == 0) return Relation::IN_TOUCH;
    Point perp(const Point &p) { return Point(-p.y, p.x); }
17
                                                                            return Relation::INSIDE;
                                                                      10
    auto rad(const Point &p) { return atan2(p.y, p.x); }
                                                                          auto get_cos_from_triangle(ld a, ld b, ld c) { return (a * a +
                                                                           \rightarrow b * b - c * c) / (2.0 * a * b); }
    Transformation
                                                                          bool on_line(const Line &1, const Point &p) { return !sgn((1.s
    Point project(const Point &p, const Line &1) {
                                                                           \rightarrow - p) \hat{} (l.e - p)); }
     return l.s + ((l.e - l.s) * ((l.e - l.s) * (p - l.s))) /
                                                                      15

    dist2(1.e - 1.s);

                                                                          bool on_segment(const Segment &1, const Point &p) {
                                                                           return !sgn((1.s - p) ^ (1.e - p)) && sgn((1.s - p) * (1.e -
                                                                      17

    p)) <= 0;
</pre>
    Point reflect(const Point &p, const Line &1) {
                                                                      18
     return project(p, 1) * 2 - p;
                                                                      19
                                                                          bool on_segment2(const Segment &1, const Point &p) { // assume
                                                                           \hookrightarrow p on Line l
    Point dilate(const Point &p, ld scale_x = 1, ld scale_y = 1) {
                                                                           if (1.s == p || 1.e == p) return true;

→ return Point(p.x * scale_x, p.y * scale_y); }

                                                                            if (\min(l.s, l.e)  return true;
    Line dilate(const Line &1, ld scale_x = 1, ld scale_y = 1) {
                                                                            return false;
                                                                      23

    return Line(dilate(1.s, scale_x, scale_y), dilate(1.e,
                                                                      24

    scale_x, scale_y)); }

                                                                      25
    Segment dilate(const Segment &1, ld scale_x = 1, ld scale_y =
                                                                          bool is_parallel(const Line &a, const Line &b) { return

→ 1) { return Segment(dilate(l.s, scale_x, scale_y),
                                                                           dilate(l.e, scale_x, scale_y)); }
                                                                          bool is_orthogonal(const Line &a, const Line &b) { return
    vector<Point> dilate(const vector<Point> &p, ld scale_x = 1,
                                                                           \rightarrow !sgn((a.s - a.e) * (b.s - b.e)); }
     \rightarrow ld scale_y = 1) {
      int n = p.size();
                                                                      28
13
                                                                          int is_intersect(const Segment &a, const Segment &b) {
      vector<Point> res(n);
                                                                           auto d1 = sgn((a.e - a.s) ^ (b.s - a.s)), d2 = sgn((a.e - a.s))
                                                                      30
      for (int i = 0; i < n; i++)
15
                                                                           \rightarrow a.s) ^ (b.e - a.s));
        res[i] = dilate(p[i], scale_x, scale_y);
                                                                           auto d3 = sgn((b.e - b.s) \hat{ } (a.s - b.s)), d4 = sgn((b.e - b.s))
17
      return res;
                                                                           \rightarrow b.s) ^ (a.e - b.s));
18
                                                                           if (d1 * d2 < 0 && d3 * d4 < 0) return 2; // intersect at
19
                                                                           \hookrightarrow non-end point
    Point rotate(const Point &p, ld a) { return Point(p.x * cos(a)
20
                                                                            return (d1 == 0 && sgn((b.s - a.s) * (b.s - a.e)) <= 0) ||
                                                                      33
     \rightarrow - p.y * sin(a), p.x * sin(a) + p.y * cos(a)); }
                                                                                    (d2 == 0 \&\& sgn((b.e - a.s) * (b.e - a.e)) <= 0) ||
                                                                      34
    Line rotate(const Line &1, ld a) { return Line(rotate(1.s, a),
                                                                                    (d3 == 0 \&\& sgn((a.s - b.s) * (a.s - b.e)) <= 0) ||
                                                                      35

→ rotate(l.e, a)); }
                                                                                    (d4 == 0 \&\& sgn((a.e - b.s) * (a.e - b.e)) <= 0);
    Segment rotate(const Segment &1, ld a) { return
                                                                          }
                                                                      37
     ⇔ Segment(rotate(l.s, a), rotate(l.e, a)); }
                                                                      38
    Circle rotate(const Circle &c, ld a) { return
                                                                          int is_intersect(const Line &a, const Segment &b) {
                                                                      39

    Gircle(rotate(c.o, a), c.r); }

                                                                           auto d1 = sgn((a.e - a.s) \hat{ } (b.s - a.s)), d2 = sgn((a.e - a.s))
    vector<Point> rotate(const vector<Point> &p, ld a) {
                                                                      40
                                                                           \hookrightarrow a.s) ^ (b.e - a.s));
     int n = p.size();
25
                                                                            if (d1 * d2 < 0) return 2; // intersect at non-end point
      vector<Point> res(n);
                                                                      41
26
                                                                            return d1 == 0 || d2 == 0;
                                                                      42
      for (int i = 0; i < n; i++)
27
                                                                      43
        res[i] = rotate(p[i], a);
28
                                                                      44
      return res;
29
                                                                          Point intersect(const Line &a, const Line &b) {
30
                                                                             auto u = a.e - a.s, v = b.e - b.s;
                                                                      46
31
                                                                             auto t = ((b.s - a.s) ^ v) / (u ^ v);
    Point translate(const Point &p, ld dx = 0, ld dy = 0) { return
                                                                            return a.s + u * t;
     \rightarrow Point(p.x + dx, p.y + dy); }
                                                                      48
                                                                      49
    Line translate(const Line &1, ld dx = 0, ld dy = 0) { return
     50
                                                                      51
                                                                          int is_intersect(const Circle &c, const Line &l) {
    Segment translate(const Segment &1, ld dx = 0, ld dy = 0) {
                                                                            auto d = dist(c.o, 1);

→ return Segment(translate(1.s, dx, dy), translate(1.e, dx,
                                                                            return sgn(d - c.r) < 0 ? 2 : !sgn(d - c.r);
                                                                      53
     \rightarrow dy)); }
                                                                          }
    Circle translate(const Circle &c, ld dx = 0, ld dy = 0) {
```

→ return Circle(translate(c.o, dx, dy), c.r); }

```
vector<Point> intersect(const Circle &a, const Circle &b) {
                                                                       123
                                                                               for (int i = 2; i < n; i++) {
                                                                                 auto c = p[i];
      auto relation = get_relation(a, b);
57
                                                                       124
      if (relation == Relation::INSIDE || relation ==
                                                                                  auto s = area({a, b, c});

→ Relation::SEPARATE) return {};
                                                                                 sum += s:
                                                                        126
       auto vec = b.o - a.o;
                                                                        127
                                                                                 x += s * (a.x + b.x + c.x);
59
       auto d2 = dist2(vec);
                                                                                 y += s * (a.y + b.y + c.y);
                                                                        128
      auto p = (d2 + a.r * a.r - b.r * b.r) / ((long double)2 *
                                                                                 swap(b, c);
                                                                        129
61
      \rightarrow d2), h2 = a.r * a.r - p * p * d2;
                                                                               }
      auto mid = a.o + vec * p, per = perp(vec) * sqrt(max((long
                                                                               return \{x / (3 * sum), y / (3 * sum)\};
62
                                                                        131
      \leftrightarrow double)0, h2) / d2);
       if (relation == Relation::OVERLAP)
63
        return {mid + per, mid - per};
64
                                                                             Area
         return {mid}:
66
                                                                             auto area(const vector<Point> &p) {
67
     }
                                                                               int n = (int)p.size();
68
                                                                               long double area = 0;
     vector<Point> intersect(const Circle &c, const Line &l) {
69
                                                                               for (int i = 0; i < n; i++) area += p[i] \hat{p}[(i + 1) \% n];
       if (!is_intersect(c, 1)) return {};
70
                                                                               return area / 2.0;
       auto v = 1.e - 1.s, t = v / dist(v);
71
       Point a = 1.s + t * ((c.o - 1.s) * t);
       auto d = sqrt(max((ld)0, c.r * c.r - dist2(c.o, a)));
73
                                                                             auto area(const Point &a, const Point &b, const Point &c) {
       if (!sgn(d)) return {a};
                                                                               return ((long double)((b - a) ^ (c - a))) / 2.0;
       return \{a - t * d, a + t * d\};
75
76
                                                                         11
77
                                                                             auto area2(const Point &a, const Point &b, const Point &c) {
     int in_poly(const vector<Point> &p, const Point &a) {
78

    return (b - a) ^ (c - a); }

       int cnt = 0, n = (int)p.size();
       for (int i = 0; i < n; i++) {
80
                                                                             auto area_intersect(const Circle &c, const vector<Point> &ps)
         auto q = p[(i + 1) \% n];
81
                                                                              if (on_segment(Segment(p[i], q), a)) return 1; // on the
                                                                               int n = (int)ps.size();

    ⇔ edge of the polygon

                                                                               auto arg = [&](const Point &p, const Point &q) { return
         cnt \hat{} = ((a.y < p[i].y) - (a.y < q.y)) * ((p[i] - a) \hat{} (q -
                                                                              \rightarrow atan2(p ^ q, p * q); };
      \rightarrow a)) > 0;
                                                                               auto tri = [&](const Point &p, const Point &q) {
84
                                                                        18
                                                                                 auto r2 = c.r * c.r / (long double)2;
       return cnt ? 2 : 0;
 85
                                                                                  auto d = q - p;
86
                                                                                 auto a = d * p / dist2(d), b = (dist2(p) - c.r * c.r) /
                                                                              \rightarrow dist2(d):
     int is_intersect(const vector<Point> &p, const Line &a) {
88
                                                                        21
                                                                                 long double det = a * a - b;
       // 1: touching, >=2: intersect count
89
                                                                                 if (sgn(det) <= 0) return arg(p, q) * r2;</pre>
       int cnt = 0, edge_cnt = 0, n = (int)p.size();
                                                                        22
90
                                                                        23
                                                                                  auto s = max((long double)0, -a - sqrt(det)), t =
       for (int i = 0; i < n; i++) {
91

→ min((long double)1, -a + sqrt(det));
         auto q = p[(i + 1) \% n];
                                                                                  if (sgn(t) < 0 \mid \mid sgn(1 - s) \le 0) return arg(p, q) * r2;
         if (on_line(a, p[i]) && on_line(a, q)) return -1; //
93
                                                                                  auto u = p + d * s, v = p + d * t;
                                                                        25
                                                                                 return arg(p, u) * r2 + (u ^ v) / 2 + arg(v, q) * r2;
                                                                        26
         auto t = is_intersect(a, Segment(p[i], q));
94
                                                                        27
         (t == 1) && edge_cnt++, (t == 2) && cnt++;
95
                                                                                long double sum = 0:
                                                                        28
96
       }
                                                                               for (int i = 0; i < n; i++) sum += tri(ps[i] - c.o, ps[(i +
97
       return cnt + edge_cnt / 2;
                                                                              \rightarrow 1) % n] - c.o);
98
                                                                               return sum;
                                                                        30
99
                                                                             }
     vector<Point> tangent(const Circle &c, const Point &p) {
100
                                                                        32
101
      auto d = dist(c.o, p), l = c.r * c.r / d, h = sqrt(c.r * c.r)
                                                                             auto adaptive_simpson(ld _1, ld _r, function<ld(ld)> f) {
      \rightarrow -1 * 1);
                                                                              auto simpson = [\&] (ld 1, ld r) { return (r - 1) * (f(1) + 4
      auto v = (p - c.o) / d;
                                                                              \Rightarrow * f((1 + r) / 2) + f(r)) / 6; };
       return {c.o + v * 1 + perp(v) * h, c.o + v * 1 - perp(v) *
103
                                                                               function<ld(ld, ld, ld)> asr = [k](ld l, ld r, ld s) {
                                                                        35
                                                                                 auto mid = (l + r) / 2;
                                                                        36
104
                                                                                  auto left = simpson(1, mid), right = simpson(mid, r);
105
                                                                                  if (!sgn(left + right - s)) return left + right;
                                                                        38
     Circle get_circumscribed(const Point &a, const Point &b, const
106
                                                                                 return asr(l, mid, left) + asr(mid, r, right);
      → Point &c) {
                                                                               };
                                                                        40
       Line u((a + b) / 2, ((a + b) / 2) + perp(b - a));
                                                                               return asr(_1, _r, simpson(_1, _r));
       Line v((b + c) / 2, ((b + c) / 2) + perp(c - b));
                                                                        41
108
                                                                        42
       auto o = intersect(u, v);
109
                                                                        43
110
       return Circle(o, dist(o, a));
                                                                             vector<Point> half_plane_intersect(vector<Line> &L) {
111
                                                                               int n = (int)L.size(), 1 = 0, r = 0; // [left, right]
                                                                        45
                                                                                sort(L.begin(), L.end(),
                                                                        46
     Circle get_inscribed(const Point &a, const Point &b, const
113
                                                                                    [](const Line &a, const Line &b) { return rad(a.s -
                                                                              \rightarrow a.e) < rad(b.s - b.e); });
      auto 11 = dist(b - c), 12 = dist(c - a), 13 = dist(a - b);
114
                                                                               vector<Point> p(n), res;
       Point o = (a * 11 + b * 12 + c * 13) / (11 + 12 + 13);
115
                                                                               vector<Line> q(n);
                                                                        49
       return Circle(o, dist(o, Line(a, b)));
                                                                               q[0] = L[0];
                                                                        50
117
                                                                               for (int i = 1; i < n; i++) {
                                                                        51
118
                                                                                 while (1 < r \&\& sgn((L[i].e - L[i].s) ^ (p[r - 1] -
                                                                        52
119
     pair<ld, ld> get_centroid(const vector<Point> &p) {
                                                                              \hookrightarrow L[i].s)) <= 0) r--;
      int n = (int)p.size();
120
                                                                                while (1 < r && sgn((L[i].e - L[i].s) ^ (p[1] - L[i].s))
                                                                        53
       ld x = 0, y = 0, sum = 0;
121
                                                                              auto a = p[0], b = p[1];
122
                                                                                 q[++r] = L[i];
                                                                        54
```

```
if (sgn((q[r].e - q[r].s) ^ (q[r - 1].e - q[r - 1].s)) ==
                                                                                                      49
                                                                                                                 return hull:
        → 0) {
                                                                                                              }
                                                                                                        50
56
               if (sgn((q[r].e - q[r].s) ^ (L[i].s - q[r].s)) > 0) q[r]
                                                                                                               vector<Point> get_convex_safe(vector<Point> points, bool
57
             = L[i];

    allow_collinear = false) {
                                                                                                                 return get_convex(points, allow_collinear);
58
            if (1 < r) p[r - 1] = intersect(q[r - 1], q[r]);</pre>
59
                                                                                                        54
         }
         while (1 < r \&\& sgn((q[1].e - q[1].s) ^ (p[r - 1] - q[1].s))
                                                                                                               vector<Point> get_convex2_safe(vector<Point> points, bool
61

    allow_collinear = false) {
        if (r - 1 <= 1) return {};
                                                                                                                  return get_convex2(points, allow_collinear);
62
         p[r] = intersect(q[r], q[1]);
63
                                                                                                        58
         return vector<Point>(p.begin() + 1, p.begin() + r + 1);
                                                                                                               bool is_convex(const vector<Point> &p, bool allow_collinear =
65
                                                                                                        60

  false) {
                                                                                                                 int n = p.size();
                                                                                                        61
       Convex
                                                                                                                  int lo = 1, hi = -1;
                                                                                                        62
                                                                                                         63
                                                                                                                  for (int i = 0; i < n; i++) {
      vector<Point> get_convex(vector<Point> &points, bool
                                                                                                                     int cur = sgn((p[(i + 2) \% n] - p[(i + 1) \% n]) ^ (p[(i +
                                                                                                        64

    allow collinear = false) {
                                                                                                                    1) % n] - p[i]));
         // strict, no repeat, two pass
                                                                                                                     lo = min(lo, cur); hi = max(hi, cur);
                                                                                                        65
         sort(points.begin(), points.end());
         points.erase(unique(points.begin(), points.end()),
                                                                                                                  return allow_collinear ? (hi - lo) < 2 : (lo == hi && lo);
                                                                                                        67

→ points.end());
                                                                                                        68
         vector<Point> L, U;
         for (auto &t : points) {
                                                                                                               auto rotating calipers(const vector<Point> &hull) {
                                                                                                        70
            for (ll sz = L.size(); sz > 1 && (sgn((t - L[sz - 2]) ^
                                                                                                                  // use get_convex2
        \leftrightarrow (L[sz - 1] - L[sz - 2])) >= 0);
                                                                                                                  int n = (int)hull.size(); // return the square of longest
                                                                                                        72
                    L.pop_back(), sz = L.size()) {

    dist

                                                                                                        73
                                                                                                                  assert(n > 1);
10
            L.push_back(t);
                                                                                                                  if (n <= 2) return dist2(hull[0], hull[1]);</pre>
                                                                                                        74
         }
11
                                                                                                                  ld res = 0;
         for (auto &t : points) {
12
                                                                                                                  for (int i = 0, j = 2; i < n; i++) {
                                                                                                        76
            for (ll sz = U.size(); sz > 1 && (sgn((t - U[sz - 2]) ^{\circ}
                                                                                                                     auto d = hull[i], e = hull[(i + 1) % n];
                                                                                                        77
            (U[sz - 1] - U[sz - 2])) \le 0);
                                                                                                                     while (area2(d, e, hull[j]) < area2(d, e, hull[(j + 1) \%
                                                                                                        78
                    U.pop_back(), sz = U.size()) {
                                                                                                                \rightarrow n])) j = (j + 1) % n;
15
                                                                                                                     res = max(res, max(dist2(d, hull[j]), dist2(e, hull[j])));
            U.push_back(t);
16
                                                                                                        80
         }
17
                                                                                                        81
                                                                                                                  return res;
         // contain repeats if all collinear, use a set to remove
18
                                                                                                               }
                                                                                                        82
            repeats
                                                                                                        83
         if (allow_collinear) {
19
                                                                                                               // Find polygon cut to the left of l
            for (int i = (int)U.size() - 2; i >= 1; i--)
20
                                                                                                               vector<Point> convex_cut(const vector<Point> &p, const Line
                                                                                                        85

    L.push_back(U[i]);
                                                                                                                } else {
21
                                                                                                                 int n = p.size();
                                                                                                        86
             set<Point> st(L.begin(), L.end());
22
                                                                                                                  vector<Point> cut;
                                                                                                        87
             for (int i = (int)U.size() - 2; i >= 1; i--) {
23
                                                                                                                  for (int i = 0; i < n; i++) {
                                                                                                        88
               if (st.count(U[i]) == 0) L.push_back(U[i]),
                                                                                                                     auto a = p[i], b = p[(i + 1) \% n];
                                                                                                        89
           st.insert(U[i]):
                                                                                                                     if (sgn((1.e - 1.s) ^ (a - 1.s)) >= 0)
25
            }
                                                                                                                        cut.push_back(a);
                                                                                                        91
         }
26
                                                                                                                     if (sgn((1.e - 1.s) ^ (a - 1.s)) * sgn((1.e - 1.s) ^ (b - 1.s)) ^ (b - 1.s) 
27
         return L:
                                                                                                                \rightarrow 1.s)) == -1)
                                                                                                                        cut.push back(intersect(Line(a, b), 1));
                                                                                                        93
29
                                                                                                                  }
                                                                                                        94
      vector<Point> get_convex2(vector<Point> &points, bool
30
                                                                                                        95
                                                                                                                  return cut;
       \leftrightarrow allow_collinear = false) { // strict, no repeat, one pass
                                                                                                               }
         nth_element(points.begin(), points.begin(), points.end());
31
                                                                                                        97
         sort(points.begin() + 1, points.end(), [&](const Point &a,
                                                                                                               // Sort by angle in range [0, 2pi)
                                                                                                        98

    const Point &b) {
                                                                                                               template <class RandomIt>
                                                                                                        99
33
             int rad_diff = sgn((a - points[0]) ^ (b - points[0]));
                                                                                                               void polar_sort(RandomIt first, RandomIt last, Point origin =
                                                                                                       100
            return !rad_diff ? (dist2(a - points[0]) < dist2(b -
34
                                                                                                                ⇔ Point(0, 0)) {
           points[0])) : (rad_diff > 0);
                                                                                                       101
                                                                                                                  auto get_quad = [&](const Point& p) {
         });
35
                                                                                                                     Point diff = p - origin;
                                                                                                       102
         if (allow_collinear) {
36
                                                                                                                     if (diff.x > 0 && diff.y >= 0) return 1;
                                                                                                       103
             int i = (int)points.size() - 1;
                                                                                                                     if (diff.x <= 0 && diff.y > 0) return 2;
                                                                                                       104
            while (i >= 0 && !sgn((points[i] - points[0]) \hat{} (points[i]
                                                                                                                     if (diff.x < 0 && diff.y <= 0) return 3;
        → - points.back()))) i--;
                                                                                                                     return 4:
                                                                                                       106
            reverse(points.begin() + i + 1, points.end());
39
                                                                                                       107
40
                                                                                                                  auto polar_cmp = [&](const Point& p1, const Point& p2) {
                                                                                                       108
          vector<Point> hull;
41
                                                                                                                     int q1 = get_quad(p1), q2 = get_quad(p2);
                                                                                                       109
42
         for (auto &t : points) {
                                                                                                                     if (q1 != q2) return q1 < q2;
                                                                                                       110
            for (ll sz = hull.size();
43
                                                                                                                     return ((p1 - origin) ^ (p2 - origin)) > 0;
                                                                                                       111
                    sz > 1 \&\& (sgn((t - hull[sz - 2]) ^ (hull[sz - 1] -
44
        → hull[sz - 2])) >= allow_collinear);
                                                                                                       113
                                                                                                                  sort(first, last, polar_cmp);
45
                    hull.pop_back(), sz = hull.size()) {
                                                                                                       114
46
            hull.push_back(t);
         }
```

Basic 3D using ll = long long; using ld = long double; constexpr auto eps = 1e-8; const auto PI = acos(-1); int sgn(ld x) { return (abs(x) <= eps) ? 0 : (x < 0 ? -1 : 1);</pre> struct Point3D { 1d x = 0, y = 0, z = 0;Point3D() = default; Point3D(ld $_x$, ld $_y$, ld $_z$) : $x(_x)$, $y(_y)$, $z(_z)$ {} 11 bool operator<(const Point3D &p) const { return !sgn(p.x -</pre> \leftrightarrow x) ? (!sgn(p.y - y) ? sgn(p.z - z) < 0 : y < p.y) : x < p.x; } bool operator==(const Point3D &p) const { return !sgn(p.x - \rightarrow x) && !sgn(p.y - y) && !sgn(p.z - z); } Point3D operator+(const Point3D &p) const { return {x + p.x, \rightarrow y + p.y, z + p.z}; } Point3D operator-(const Point3D &p) const { return {x - p.x, \rightarrow y - p.y, z - p.z}; } Point3D operator*(ld a) const { return {x * a, y * a, z * Point3D operator/(ld a) const { return $\{x / a, y / a, z / a\}$ 17 auto operator*(const Point3D &p) const { return x * p.x + y \Rightarrow * p.y + z * p.z; } // dot Point3D operator^(const Point3D &p) const { return {y * p.z \rightarrow - z * p.y, z * p.x - x * p.z, x * p.y - y * p.x}; } // friend auto &operator>>(istream &i, Point3D &p) { return i 21 22 struct Line3D { Point3D s = $\{0, 0, 0\}, e = \{0, 0, 0\};$ 24 Line3D() = default; Line3D(Point3D _s, Point3D _e) : s(_s), e(_e) {} 26 27 28 struct Segment3D : Line3D { 29 using Line3D::Line3D; 30 31 32 auto dist2(const Point3D &a) { return a * a; } auto dist2(const Point3D &a, const Point3D &b) { return dist2(a - b); } auto dist(const Point3D &a) { return sqrt(dist2(a)); } 35 auto dist(const Point3D &a, const Point3D &b) { return sqrt(dist2(a - b)); } auto dist(const Point3D &a, const Line3D &1) { return dist((a - l.s) ^ (l.e - l.s)) / dist(l.s, l.e); } auto dist(const Point3D &p, const Segment3D &1) { 38 if (1.s == 1.e) return dist(p, 1.s); auto d = dist2(1.s, 1.e), t = min(d, max((1d)0, (p - 1.s) *) \hookrightarrow (l.e - l.s))); return dist((p - 1.s) * d, (1.e - 1.s) * t) / d;41 Miscellaneous tuple<int,int,ld> closest_pair(vector<Point> &p) { using Pt = pair<Point,int>; int n = p.size(); assert(n > 1);vector<Pt> pts(n), buf; for (int i = 0; i < n; i++) pts[i] = {p[i], i}; sort(pts.begin(), pts.end()); buf.reserve(n); auto cmp_y = [](const Pt& p1, const Pt& p2) { return p1.first.y < p2.first.y; };</pre>

function<tuple<int,int,ld>(int, int)> recurse = [&](int 1,

int i = pts[l].second, j = pts[l + 1].second;

ld d = dist(pts[1].first, pts[1 + 1].first);

int r) → tuple<int,int,ld> {

```
if (r - 1 < 5) {
      for (int a = 1; a < r; a++) for (int b = a + 1; b < r;
        ld cur = dist(pts[a].first, pts[b].first);
        if (cur < d) { i = pts[a].second; j = pts[b].second; d</pre>
   = cur: }
      sort(pts.begin() + 1, pts.begin() + r, cmp_y);
      int mid = (1 + r)/2;
      ld x = pts[mid].first.x;
      auto [li, lj, ldist] = recurse(l, mid);
      auto [ri, rj, rdist] = recurse(mid, r);
      if (ldist < rdist) { i = li; j = lj; d = ldist; }</pre>
      else { i = ri; j = rj; d = rdist; }
      inplace_merge(pts.begin() + 1, pts.begin() + mid,

  pts.begin() + r, cmp_y);
      buf.clear();
      for (int a = 1; a < r; a++) {
        if (abs(x - pts[a].first.x) >= d) continue;
        for (int b = buf.size() - 1; b >= 0; b--) {
          if (pts[a].first.y - buf[b].first.y >= d) break;
          ld cur = dist(pts[a].first, buf[b].first);
          if (cur < d) { i = pts[a].second; j = buf[b].second;</pre>
   d = cur; }
        }
        buf.push_back(pts[a]);
    return {i, j, d};
  return recurse(0, n):
Line abc_to_line(ld a, ld b, ld c) {
  assert(!sgn(a) || !sgn(b));
  if(a == 0) return Line(Point(0, -c/b), Point(1, -c/b));
  if(b == 0) return Line(Point(-c/a, 0), Point(-c/a, 1));
  Point s(0, -c/b), e(1, (-c - a)/b), diff = e - s;
  return Line(s, s + diff/dist(diff));
}
tuple<ld,ld,ld> line_to_abc(const Line& 1) {
  Point diff = 1.e - 1.s;
  return {-diff.y, diff.x, -(diff ^ 1.s)};
```

Graph Theory

Max Flow

13

14

15

16

24

33

37

39

41

42

43

44

46

49

50

51

```
struct Edge {
      int from, to, cap, remain;
    struct Dinic {
      int n:
      vector<Edge> e;
      vector<vector<int>> g;
      vector<int> d, cur;
      Dinic(int _n) : n(_n), g(n), d(n), cur(n) {}
       void add_edge(int u, int v, int c) {
         g[u].push_back((int)e.size());
         e.push_back({u, v, c, c});
         g[v].push_back((int)e.size());
14
         e.push_back({v, u, 0, 0});
16
      11 max_flow(int s, int t) {
        int inf = 1e9;
19
         auto bfs = [&]() {
         fill(d.begin(), d.end(), inf), fill(cur.begin(),
     \rightarrow cur.end(), 0):
          d[s] = 0;
          vector<int> q{s}, nq;
```

```
for (int step = 1; q.size(); swap(q, nq), nq.clear(),
                                                                                g[t].push_back({s, sz(g[s]) - 1, 0, rcap});
     \hookrightarrow step++) {
                                                                       25
            for (auto& node : q) {
                                                                       26
              for (auto\& edge : g[node]) {
                                                                               void addFlow(Edge& e, ll f) {
25
                                                                       27
                 int ne = e[edge].to;
                                                                                Edge& back = g[e.dest][e.back];
26
                                                                       28
                 if (!e[edge].remain || d[ne] <= step) continue;</pre>
                                                                                if (!ec[e.dest] && f) hs[H[e.dest]].push_back(e.dest);
                                                                       29
27
                 d[ne] = step, nq.push_back(ne);
                                                                                e.f += f;
28
                                                                       30
                 if (ne == t) return true;
                                                                                 e.c -= f;
                                                                                 ec[e.dest] += f;
30
                                                                       32
31
                                                                        33
                                                                                 back.f -= f;
          7
                                                                                back.c += f;
                                                                       34
32
                                                                                 ec[back.dest] -= f;
33
          return false:
                                                                       35
         function<int(int, int)> find = [&](int node, int limit) {
                                                                              ll calc(int s. int t) {
35
                                                                       37
           if (node == t || !limit) return limit;
                                                                                int v = sz(g);
          int flow = 0;
                                                                                H[s] = v;
37
                                                                        39
           for (int i = cur[node]; i < g[node].size(); i++) {</pre>
                                                                                ec[t] = 1;
38
                                                                        40
39
            cur[node] = i;
                                                                        41
                                                                                vi co(2 * v);
             int edge = g[node][i], oe = edge ^ 1, ne = e[edge].to;
                                                                                co[0] = v - 1;
40
                                                                       42
41
            if (!e[edge].remain || d[ne] != d[node] + 1) continue;
                                                                                rep(i, 0, v) cur[i] = g[i].data();
            if (int temp = find(ne, min(limit - flow,
                                                                                for (Edge& e : g[s]) addFlow(e, e.c);
42
                                                                       44
        e[edge].remain))) {
                                                                                for (int hi = 0;;) {
43
              e[edge].remain -= temp, e[oe].remain += temp, flow
                                                                        46
        += temp;
                                                                                  while (hs[hi].empty())
                                                                        47
            } else {
                                                                                    if (!hi--) return -ec[s];
                                                                                  int u = hs[hi].back();
              d[ne] = -1;
45
                                                                       49
                                                                                  hs[hi].pop_back();
            if (flow == limit) break;
                                                                                  while (ec[u] > 0) // discharge u
47
                                                                       51
                                                                                     if (cur[u] == g[u].data() + sz(g[u])) {
                                                                       52
48
49
          return flow;
                                                                       53
                                                                                      H[u] = 1e9;
        };
                                                                                       for (Edge& e : g[u])
50
                                                                       54
         11 \text{ res} = 0;
                                                                                         if (e.c && H[u] > H[e.dest] + 1) H[u] = H[e.dest]
51
         while (bfs())
                                                                             52
           while (int flow = find(s, inf)) res += flow;
                                                                                       if (++co[H[u]], !--co[hi] && hi < v)
53
                                                                       56
                                                                                        rep(i, 0, v) if (hi < H[i] && H[i] < v)--
54
         return res;
                                                                       57
      }
                                                                             \hookrightarrow co[H[i]], H[i] = v + 1;
55
    };
                                                                                      hi = H[u];
                                                                                    } else if (cur[u]->c \&\& H[u] == H[cur[u]->dest] + 1)
                                                                       59
       • USAGE
                                                                                       addFlow(*cur[u], min(ec[u], cur[u]->c));
                                                                        60
                                                                                     else
                                                                       61
    int main() {
                                                                                       ++cur[u];
                                                                       62
      int n, m, s, t;
                                                                                }
                                                                       63
      cin >> n >> m >> s >> t;
                                                                              }
                                                                       64
      Dinic dinic(n);
                                                                       65
                                                                              bool leftOfMinCut(int a) { return H[a] >= sz(g); }
      for (int i = 0, u, v, c; i < m; i++) {
                                                                       66
         cin >> u >> v >> c;
         dinic.add_edge(u - 1, v - 1, c);
                                                                            Min-Cost Max-Flow
      cout << dinic.max_flow(s - 1, t - 1) << '\n';
9
                                                                            struct MinCostFlow {
                                                                              static constexpr int INF = 1e9;
                                                                              const int n;
    PushRelabel Max-Flow (faster)
                                                                              vector<tuple<int, int, int>> e;
                                                                              vector<vector<int>>> g;
                                                                        5
                                                                               vector<int> h, dis, pre;

→ https://github.com/kth-competitive-programming/kactl/blob/main/contendo/grabpjk$Pusakialtistle.j.int t) {

    #define rep(i, a, b) for (int i = a; i < (b); ++i)
                                                                                dis.assign(n, INF);
                                                                        8
    #define all(x) begin(x), end(x)
                                                                                 pre.assign(n, -1);
    #define sz(x) (int)(x).size()
                                                                                priority_queue<pair<int, int>, vector<pair<int, int>>,
                                                                        10
    typedef long long 11;
                                                                                greater<>> que;
                                                                                dis[s] = 0;
    typedef pair<int, int> pii;
                                                                        11
    typedef vector<int> vi;
                                                                                 que.emplace(0, s);
                                                                       12
                                                                                 while (!que.empty()) {
                                                                        13
                                                                                  auto [d, u] = que.top();
    struct PushRelabel {
9
                                                                       14
      struct Edge {
                                                                                   que.pop();
                                                                        15
        int dest, back;
                                                                                  if (dis[u] != d) continue;
11
                                                                       16
        11 f, c;
                                                                                   for (int i : g[u]) {
12
                                                                       17
      };
                                                                                    auto [v, f, c] = e[i];
13
                                                                        18
      vector<vector<Edge>> g;
                                                                                    if (c > 0 \&\& dis[v] > d + h[u] - h[v] + f) {
14
                                                                       19
       vector<11> ec;
                                                                                      dis[v] = d + h[u] - h[v] + f;
15
                                                                                      pre[v] = i;
      vector<Edge*> cur;
16
                                                                       21
       vector<vi> hs;
                                                                                       que.emplace(dis[v], v);
17
18
      PushRelabel(int n) : g(n), ec(n), cur(n), hs(2 * n), H(n) {}
19
20
      void addEdge(int s, int t, ll cap, ll rcap = 0) {
                                                                                return dis[t] != INF;
21
                                                                       26
         if (s == t) return;
         g[s].push_back({t, sz(g[t]), 0, cap});
                                                                              MinCostFlow(int _n) : n(_n), g(n) {}
23
```

```
g[u].push_back((int)e.size());
                                                                                    u = find(link[match[u]]);
30
                                                                       13
                                                                                  }
31
         e.emplace_back(v, f, c);
         g[v].push_back((int)e.size());
32
                                                                       15
                                                                                  return u:
33
         e.emplace_back(u, -f, 0);
                                                                                };
                                                                       16
34
                                                                       17
                                                                                queue<int> que;
                                                                                auto blossom = [&](int u, int v, int p) {
      pair<int, int> minCostMaxFlow(const int s, const int t) {
35
                                                                       18
                                                                                  while (find(u) != p) {
         int flow = 0, cost = 0;
        h.assign(n, 0);
                                                                                    link[u] = v, v = match[u];
37
                                                                       20
                                                                                    if (vis[v] == 0) vis[v] = 1, que.push(v);
38
         while (dijkstra(s, t)) {
                                                                       21
          for (int i = 0; i < n; ++i) h[i] += dis[i];</pre>
                                                                                    f[u] = f[v] = p, u = link[v];
39
           for (int i = t; i != s; i = get<0>(e[pre[i] ^ 1])) {
                                                                                  }
40
                                                                       23
             --get<2>(e[pre[i]]);
                                                                                };
41
                                                                       24
             ++get<2>(e[pre[i] ^ 1]);
                                                                                // find an augmenting path starting from u and augment (if
42
                                                                       25
43
          ++flow;
                                                                                auto augment = [&](int node) {
44
                                                                       26
           cost += h[t];
                                                                                  while (!que.empty()) que.pop();
45
                                                                       27
46
                                                                       28
                                                                                  iota(f.begin(), f.end(), 0);
        return {flow, cost};
                                                                                  // vis = 0 corresponds to inner vertices, vis = 1
47
                                                                       29
48
      }
                                                                             \hookrightarrow corresponds to outer vertices
    };
                                                                                  fill(vis.begin(), vis.end(), -1);
49
                                                                       30
                                                                       31
                                                                                  que.push(node);
                                                                                  vis[node] = 1, dep[node] = 0;
                                                                       32
    Heavy-Light Decomposition
                                                                                  while (!que.empty()) {
                                                                       33
                                                                                    int u = que.front();
    int root = 0, cur = 0;
                                                                                    que.pop();
                                                                       35
    vector<int> parent(n), deep(n), hson(n, -1), top(n), sz(n),
                                                                                    for (auto v : e[u]) {
     \rightarrow dfn(n, -1);
                                                                                      if (vis[v] == -1) {
    function<int(int, int, int)> dfs = [&](int node, int fa, int
                                                                                        vis[v] = 0, link[v] = u, dep[v] = dep[u] + 1;
                                                                       38

    dep) {

                                                                       39
                                                                                        // found an augmenting path
      deep[node] = dep, sz[node] = 1, parent[node] = fa;
                                                                                        if (match[v] == -1) {
                                                                       40
      for (auto &ne : g[node]) {
                                                                                          for (int x = v, y = u, temp; y != -1; x = temp,
         if (ne == fa) continue;
                                                                               y = x == -1 ? -1 : link[x]) {
         sz[node] += dfs(ne, node, dep + 1);
                                                                                            temp = match[y], match[x] = y, match[y] = x;
                                                                       42
         if (hson[node] == -1|| sz[ne] > sz[hson[node]]) hson[node]
                                                                                          }
                                                                       43
                                                                                          return:
                                                                       44
      }
9
                                                                                        }
      return sz[node];
10
                                                                                        vis[match[v]] = 1, dep[match[v]] = dep[u] + 2;
                                                                       46
11
    };
                                                                                        que.push(match[v]);
    function<void(int, int)> dfs2 = [&](int node, int t) {
12
                                                                                      } else if (vis[v] == 1 && find(v) != find(u)) {
                                                                       48
13
      top[node] = t, dfn[node] = cur++;
                                                                                        // found a blossom
                                                                       49
      if (hson[node] == -1) return;
14
                                                                                        int p = lca(u, v);
      dfs2(hson[node], t);
                                                                                        blossom(u, v, p), blossom(v, u, p);
                                                                       51
      for (auto &ne : g[node]) {
16
17
         if (ne == parent[node] || ne == hson[node]) continue;
                                                                                    }
                                                                       53
        dfs2(ne, ne);
18
                                                                                  }
                                                                       54
19
                                                                       55
                                                                                };
    };
20
                                                                                // find a maximal matching greedily (decrease constant)
                                                                       56
    // read in graph as vector<vector<int>> q(n)
21
                                                                                auto greedy = [&]() {
                                                                       57
    dfs(root, -1, 0), dfs2(root, root);
                                                                                  for (int u = 0; u < n; ++u) {
                                                                       58
                                                                                    if (match[u] != -1) continue;
       • USAGE: get LCA
                                                                                    for (auto v : e[u]) {
                                                                       60
                                                                                      if (match[v] == -1) {
    function<int(int, int)> lca = [&](int x, int y) {
                                                                       61
                                                                                        match[u] = v, match[v] = u;
      while (top[x] != top[y]) {
                                                                       62
         if (deep[top[x]] < deep[top[y]]) swap(x, y);</pre>
                                                                       63
                                                                                        break;
                                                                                      }
        x = parent[top[x]];
                                                                                    }
                                                                       65
                                                                                  }
      return deep[x] < deep[y] ? x : y;</pre>
                                                                       66
                                                                       67
                                                                                greedy();
                                                                       68
                                                                                for (int u = 0; u < n; ++u)
    General Unweight Graph Matching
                                                                                  if (match[u] == -1) augment(u);
                                                                       70
                                                                       71
                                                                                return match;
       • Complexity: O(n^3) (?)
                                                                       72
                                                                              }
                                                                           };
                                                                       73
    struct BlossomMatch {
      int n;
      vector<vector<int>> e;
                                                                            Maximum Bipartite Matching
      BlossomMatch(int _n) : n(_n), e(_n) {}
      void add_edge(int u, int v) { e[u].push_back(v),
                                                                              • Needs dinic, complexity \approx O(n + m\sqrt{n})

    e[v].push_back(u); }

      vector<int> find_matching() {
        vector \le int > match(n, -1), vis(n), link(n), f(n), dep(n);
                                                                            struct BipartiteMatch {
         function<int(int)> find = [&](int x) { return f[x] == x ?
                                                                        2
                                                                              int 1, r;
        x : (f[x] = find(f[x])); \};
                                                                              Dinic dinic = Dinic(0);
         auto lca = [&](int u, int v) {
                                                                              \label{eq:bipartiteMatch(int l, int r) : l(l), r(r) {} \\
          u = find(u), v = find(v);
                                                                                dinic = Dinic(1 + r + 2);
                                                                                for (int i = 1; i <= 1; i++) dinic.add_edge(0, i, 1);</pre>
          while (u != v) {
```

12

if (dep[u] < dep[v]) swap(u, v);</pre>

void addEdge(int u, int v, int f, int c) {

```
for (int i = 1; i <= r; i++) dinic.add_edge(l + i, l + r +
     \leftrightarrow 1, 1);
      }
      void add_edge(int u, int v) { dinic.add_edge(u + 1, 1 + v +

    1, 1); }

     ll max_matching() { return dinic.max_flow(0, l + r + 1); }
10
    }:
11
    2-SAT and Strongly Connected Components
    void scc(vector<vector<int>>& g, int* idx) {
      int n = g.size(), ct = 0;
      int out[n];
```

9

10

12

13

14

15

16

17

18 19

20

22

23

24

25

27

29

30

31

32

33

34

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54

55

56

57

58

59

60

61

62

```
vector<int> ginv[n];
  memset(out, -1, sizeof out);
  memset(idx, -1, n * sizeof(int));
  function<void(int)> dfs = [&](int cur) {
    out[cur] = INT_MAX;
    for(int v : g[cur]) {
      ginv[v].push_back(cur);
      if(out[v] == -1) dfs(v);
    }
    ct++; out[cur] = ct;
  };
  vector<int> order;
  for(int i = 0; i < n; i++) {
    order.push_back(i);
    if(out[i] == -1) dfs(i);
  sort(order.begin(), order.end(), [&](int& u, int& v) {
    return out[u] > out[v];
  });
  ct = 0;
  stack<int> s;
  auto dfs2 = [&](int start) {
    s.push(start);
    while(!s.empty()) {
      int cur = s.top();
      s.pop();
      idx[cur] = ct;
      for(int v : ginv[cur])
        if(idx[v] == -1) s.push(v);
    }
  for(int v : order) {
    if(idx[v] == -1) {
      dfs2(v);
      ct++;
  }
}
// 0 => impossible, 1 => possible
pair<int, vector<int>>> sat2(int n, vector<pair<int,int>>&
 vector<int> ans(n);
  vector<vector<int>> g(2*n + 1);
  for(auto [x, y] : clauses) {
    x = x < 0 ? -x + n : x;
    y = y < 0 ? -y + n : y;
    int nx = x <= n ? x + n : x - n;</pre>
    int ny = y <= n ? y + n : y - n;</pre>
    g[nx].push_back(y);
    g[ny].push_back(x);
  }
  int idx[2*n + 1];
  scc(g, idx);
  for(int i = 1; i <= n; i++) {
    if(idx[i] == idx[i + n]) return {0, {}};
    ans[i - 1] = idx[i + n] < idx[i];
  return {1, ans};
```

Enumerating Triangles

• Complexity: $O(n + m\sqrt{m})$

```
void enumerate_triangles(vector<pair<int,int>>& edges,

    function < void(int,int,int) > f) {
      int n = 0;
      for(auto [u, v] : edges) n = max({n, u + 1, v + 1});
      vector<int> deg(n);
       vector<int> g[n];
      for(auto [u, v] : edges) {
         deg[u]++;
         deg[v]++;
       for(auto [u, v] : edges) {
10
         if(u == v) continue;
11
         if(deg[u] > deg[v] \mid \mid (deg[u] == deg[v] \&\& u > v))
12
13
           swap(u, v);
         g[u].push_back(v);
14
15
16
       vector<int> flag(n);
       for(int i = 0; i < n; i++) {
17
         for(int v : g[i]) flag[v] = 1;
18
         for(int v : g[i]) for(int u : g[v]) {
19
           if(flag[u]) f(i, v, u);
21
         for(int v : g[i]) flag[v] = 0;
23
    }
24
```

Tarjan

• shrink all circles into points (2-edge-connectedcomponent)

```
int cnt = 0, now = 0;
    vector<ll> dfn(n, -1), low(n), belong(n, -1), stk;
    function < void(11, 11) > tarjan = [\&](11 node, 11 fa) {
      dfn[node] = low[node] = now++, stk.push_back(node);
      for (auto& ne : g[node]) {
        if (ne == fa) continue;
         if (dfn[ne] == -1) {
          tarjan(ne, node);
          low[node] = min(low[node], low[ne]);
        } else if (belong[ne] == -1) {
10
           low[node] = min(low[node], dfn[ne]);
11
12
13
       if (dfn[node] == low[node]) {
14
15
        while (true) {
          auto v = stk.back();
16
          belong[v] = cnt;
17
          stk.pop_back();
18
           if (v == node) break;
        }
20
21
         ++cnt;
      }
22
    };
23
```

• 2-vertex-connected-component / Block forest

```
int cnt = 0, now = 0;
vector<vector<ll>> e1(n);
vector<ll> dfn(n, -1), low(n), stk;
function < void(11) > tarjan = [\&](11 node) {
  dfn[node] = low[node] = now++, stk.push_back(node);
  for (auto& ne : g[node]) {
   if (dfn[ne] == -1) {
      tarjan(ne);
      low[node] = min(low[node], low[ne]);
      if (low[ne] == dfn[node]) {
        e1.push_back({});
        while (true) {
          auto x = stk.back();
          stk.pop_back();
          e1[n + cnt].push_back(x);
          // e1[x].push_back(n + cnt); // undirected
```

9

10

11

12

```
if (x == ne) break:
                                                                      12
                                                                             Z operator-() const { return Z(norm(MOD - x)); }
                                                                             Z inv() const { return power(*this, MOD - 2); }
18
                                                                      13
            e1[node].push_back(n + cnt);
                                                                             Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
19
                                                                       14
            // e1[n + cnt].push_back(node); // undirected
                                                                            20
                                                                            Z \& perator += (const Z \& rhs) \{ return x = norm(x + rhs.x), \}
21
                                                                      15
          }

    *this; }

22
        } else {
                                                                            Z & operator = (const Z & rhs) { return x = norm(x - rhs.x),
23
                                                                      16
24
          low[node] = min(low[node], dfn[ne]);
                                                                             Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
25
                                                                      17
                                                                             Z &operator%=(const ll &rhs) { return x %= rhs, *this; }
26
                                                                       18
    };
                                                                             friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs;
27
                                                                      19
                                                                             friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs;
    Kruskal reconstruct tree
                                                                            → }
                                                                      21
                                                                            friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs;
    int _n, m;
    cin >> _n >> m; // _n: # of node, m: # of edge
                                                                             friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs;
                                                                      22
    int n = 2 * _n - 1; // root: n-1
                                                                            _ }
    vector<array<int, 3>> edges(m);
                                                                            friend Z operator%(Z lhs, const ll &rhs) { return lhs %=
                                                                      23
    for (auto& [w, u, v] : edges) {

    rhs; }

      cin >> u >> v >> w, u--, v--;
                                                                            friend auto &operator>>(istream &i, Z &z) { return i >> z.x;
                                                                      24
    sort(edges.begin(), edges.end());
                                                                            friend auto &operator << (ostream &o, const Z &z) { return o
                                                                      25
    vector<int> p(n);
                                                                            iota(p.begin(), p.end(), 0);
                                                                           };
    function < int(int) > find = [&](int x) { return p[x] == x ? x :}
     \hookrightarrow (p[x] = find(p[x])); };
                                                                              • large mod (for NTT to do FFT in ll range without mod-
    auto merge = [\&](int x, int y) \{ p[find(x)] = find(y); \};
12
    vector<vector<int>> g(n);
13
    vector<int> val(m);
                                                                           using ll = long long;
    val.reserve(n):
15
                                                                           using i128 = __int128;
                                                                           constexpr i128 MOD = 9223372036737335297;
16
    for (auto [w, u, v] : edges) {
      u = find(u), v = find(v);
17
      if (u == v) continue;
                                                                           constexpr i128 norm(i128 x) { return x < 0 ? (x + MOD) \% MOD :
18
      val.push_back(w);
                                                                            \hookrightarrow x % MOD; }
      int node = (int)val.size() - 1;
20
                                                                       6
                                                                           template <typename T>
      g[node].push_back(u), g[node].push_back(v);
                                                                           constexpr T power(T a, i128 b, T res = 1) {
21
      merge(u, node), merge(v, node);
                                                                             for (; b; b /= 2, (a *= a) \%= MOD)
22
23
                                                                               if (b & 1) (res *= a) %= MOD;
                                                                       9
                                                                       10
                                                                             return res;
                                                                      11
                                                                      12
                                                                           struct Z {
    Math
                                                                      13
                                                                             i128 x:
                                                                             constexpr Z(i128 _x = 0) : x(norm(_x)) {}
                                                                      14
    Inverse
                                                                             Z operator-() const { return Z(norm(MOD - x)); }
                                                                             Z inv() const { return power(*this, MOD - 2); }
                                                                      16
    11 inv(11 a, 11 m) { return a == 1 ? 1 : ((m - m / a) * inv(m
                                                                             // auto operator<=>(const Z&) const = default;
                                                                      17
     \rightarrow % a, m) % m); }
                                                                             Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
    // or

→ *this: }

    power(a, MOD - 2)
                                                                            Z &operator+=(const Z &rhs) { return x = norm(x + rhs.x),

    *this: }

    USAGE: get factorial

                                                                             Z &operator-=(const Z &rhs) { return x = norm(x - rhs.x),
                                                                      20

    *this: }

    vector<ll> f(MAX_N, 1), rf(MAX_N, 1);
                                                                            Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
                                                                      ^{21}
    for (int i = 1; i < MAX_N; i++) f[i] = (f[i - 1] * i) % MOD;
                                                                             Z &operator%=(const i128 &rhs) { return x %= rhs, *this; }
    for (int i = 1; i < MAX_N; i++) rf[i] = (rf[i - 1] * inv(i,
                                                                             friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs;

   MOD)) % MOD;

                                                                            → }
    // or (the later one should be preferred
                                                                            friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs;
                                                                      24
    vector<ll> f(MAX_N, 1), rf(MAX_N, 1);
                                                                            → }
   for (int i = 2; i < MAX_N; i++) f[i] = f[i - 1] * i % MOD;
                                                                             friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs;
    rf[MAX_N - 1] = power(f[MAX_N - 1], MOD - 2);
                                                                            → }
    for (int i = MAX_N - 2; i > 1; i--) rf[i] = rf[i + 1] * (i +
                                                                            friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs;

→ 1) % MOD;

                                                                             friend Z operator%(Z lhs, const i128 &rhs) { return lhs %=
    Mod Class

    rhs; }

                                                                      28
    constexpr ll norm(ll x) { return (x % MOD + MOD) % MOD; }
                                                                              • fastest mod class! be careful with overflow, only use
    template <typename T>
    constexpr T power(T a, ll b, T res = 1) {
                                                                                when the time limit is tight
      for (; b; b /= 2, (a *= a) \%= MOD)
                                                                           constexpr int MOD = 998244353;
        if (b & 1) (res *= a) \%= MOD;
                                                                       1
      return res;
                                                                           constexpr int norm(int x) {
    7
                                                                       4
                                                                             if (x < 0) x += MOD;
    struct Z {
                                                                             if (x >= MOD) x -= MOD;
```

}

constexpr $Z(11 _x = 0) : x(norm(_x)) \{ \}$

// auto operator<=>(const Z &) const = default; // cpp20

10

onlu

return x:

template <typename T>

```
constexpr T power(T a, int b, T res = 1) {
                                                                            ntt(a, 1);
      for (; b; b /= 2, (a *= a) \%= MOD)
                                                                            a.resize(m);
10
        if (b & 1) (res *= a) \%= MOD;
                                                                            return a;
11
                                                                     10 }
      return res:
12
13
                                                                             • FFT (should prefer NTT, only use this when input is not
    struct Z {
14
     int x:
15
      constexpr Z(int _x = 0) : x(norm(_x)) {}
      // constexpr auto operator <=> (const Z &) const = default; //
                                                                         const double PI = acos(-1);
17
                                                                          auto mul = [&](const vector<double>& aa, const vector<double>&
      constexpr Z operator-() const { return Z(norm(MOD - x)); }
                                                                           18
      constexpr Z inv() const { return power(*this, MOD - 2); }
                                                                           int n = (int)aa.size(), m = (int)bb.size(), bit = 1;
19
      constexpr Z &operator*=(const Z &rhs) { return x = ll(x) *
                                                                            while ((1 << bit) < n + m - 1) bit++;
     \hookrightarrow rhs.x % MOD, *this; }
                                                                            int len = 1 << bit;</pre>
     constexpr Z &operator+=(const Z &rhs) { return x = norm(x +
                                                                            vector<complex<double>> a(len), b(len);
                                                                            vector<int> rev(len);

    rhs.x), *this; }

     constexpr Z &operator-=(const Z &rhs) { return x = norm(x -
                                                                            for (int i = 0; i < n; i++) a[i].real(aa[i]);</pre>
                                                                            for (int i = 0; i < m; i++) b[i].real(bb[i]);</pre>

    rhs.x), *this; }

     constexpr Z &operator/=(const Z &rhs) { return *this *=
                                                                            for (int i = 0; i < len; i++) rev[i] = (rev[i >> 1] >> 1) |
23

    rhs.inv(); }

                                                                           \leftrightarrow ((i & 1) << (bit - 1));
                                                                            auto fft = [&](vector<complex<double>>& p, int inv) {
     constexpr Z &operator%=(const ll &rhs) { return x %= rhs,
                                                                     11
                                                                              for (int i = 0; i < len; i++)</pre>

    *this: }

     constexpr friend Z operator*(Z lhs, const Z &rhs) { return
                                                                                if (i < rev[i]) swap(p[i], p[rev[i]]);</pre>
                                                                     13
     14
                                                                              for (int mid = 1; mid < len; mid *= 2) {
                                                                                auto w1 = complex<double>(cos(PI / mid), (inv ? -1 : 1)
     constexpr friend Z operator+(Z lhs, const Z &rhs) { return
                                                                     15

    * sin(PI / mid));
     constexpr friend Z operator-(Z lhs, const Z &rhs) { return
                                                                                for (int i = 0; i < len; i += mid * 2) {
                                                                                  auto wk = complex<double>(1, 0);
     17
                                                                                  for (int j = 0; j < mid; j++, wk = wk * w1) {
     constexpr friend Z operator/(Z lhs, const Z &rhs) { return
                                                                      18
28
                                                                                   auto x = p[i + j], y = wk * p[i + j + mid];
     19
     constexpr friend Z operator%(Z lhs, const 11 &rhs) { return
                                                                                    p[i + j] = x + y, p[i + j + mid] = x - y;
                                                                     20
                                                                                  }
     → lhs %= rhs; }
     friend auto &operator>>(istream &i, Z &z) { return i >> z.x;
                                                                                }
                                                                     22
                                                                              }
                                                                     23
     friend auto &operator << (ostream &o, const Z &z) { return o
                                                                              if (inv == 1) {
                                                                     24
                                                                                for (int i = 0; i < len; i++) p[i].real(p[i].real() /</pre>
     \leftrightarrow << z.x: }
                                                                     25
                                                                           → len);
                                                                              }
                                                                     26
                                                                      27
    NTT, FFT, FWT
                                                                            fft(a, 0), fft(b, 0);
                                                                     28
                                                                            for (int i = 0; i < len; i++) a[i] = a[i] * b[i];
                                                                     29
                                                                            fft(a, 1);

    ntt

                                                                     30
                                                                            a.resize(n + m - 1);
                                                                     31
    void ntt(vector<Z>& a, int f) {
                                                                            vector<double> res(n + m - 1);
      int n = int(a.size());
                                                                            for (int i = 0; i < n + m - 1; i++) res[i] = a[i].real();
                                                                     33
      vector<Z> w(n);
      vector<int> rev(n):
                                                                          };
      for (int i = 0; i < n; i++) rev[i] = (rev[i / 2] / 2) | ((i
     for (int i = 0; i < n; i++) {
                                                                          Polynomial Class
        if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
                                                                          using ll = long long;
      Z wn = power(f ? (MOD + 1) / 3 : 3, (MOD - 1) / n);
                                                                          constexpr 11 MOD = 998244353;
      w[0] = 1:
10
      for (int i = 1; i < n; i++) w[i] = w[i - 1] * wn;
                                                                          11 norm(11 x) { return (x % MOD + MOD) % MOD; }
11
                                                                          template <class T>
      for (int mid = 1; mid < n; mid *= 2) {</pre>
12
        for (int i = 0; i < n; i += 2 * mid) {
                                                                          T power(T a, 11 b, T res = 1) {
13
          for (int j = 0; j < mid; j++) {
                                                                            for (; b; b /= 2, (a *= a) %= MOD)
14
            Z x = a[i + j], y = a[i + j + mid] * w[n / (2 * mid) *
                                                                              if (b & 1) (res *= a) %= MOD;
15
                                                                            return res:
            a[i + j] = x + y, a[i + j + mid] = x - y;
16
                                                                     10
17
        }
18
                                                                     12
                                                                          struct Z {
      7
19
                                                                     13
                                                                            Z(11 _x = 0) : x(norm(_x)) {}
20
      if (f) {
                                                                     14
        Z iv = power(Z(n), MOD - 2);
                                                                            // auto operator<=>(const Z &) const = default;
21
                                                                     15
                                                                            Z operator-() const { return Z(norm(MOD - x)); }
22
        for (auto\& x : a) x *= iv;
                                                                     16
                                                                            Z inv() const { return power(*this, MOD - 2); }
23
                                                                     17
   }
                                                                            Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
24
                                                                     18

    *this: }

       • USAGE: Polynomial multiplication
                                                                            Z \& perator += (const Z \& rhs) \{ return x = norm(x + rhs.x), \}
                                                                     19
                                                                             *this; }
    vector<Z> mul(vector<Z> a, vector<Z> b) {
                                                                           Z &operator == (const Z &rhs) { return x = norm(x - rhs.x),
                                                                     20
2
      int n = 1, m = (int)a.size() + (int)b.size() - 1;
      while (n < m) n *= 2;
                                                                            Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
                                                                     21
      a.resize(n), b.resize(n);
                                                                     22
                                                                            Z &operator%=(const ll &rhs) { return x %= rhs, *this; }
```

friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs;

ntt(a, 0), ntt(b, 0);

for (int i = 0; i < n; i++) a[i] *= b[i];

```
friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs;
                                                                                  while (n < m) n *= 2;
                                                                                  a.resize(n), b.resize(n);
     → }
                                                                         91
      friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs;
                                                                                   ntt(a.a, 0), ntt(b.a, 0);
                                                                                  for (int i = 0; i < n; i++) a[i] *= b[i];
     → }
                                                                         93
      friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs;
                                                                                  ntt(a.a, 1);
26
                                                                         94
                                                                                  a.resize(m);
                                                                         95
      friend Z operator%(Z lhs, const ll &rhs) { return lhs %=
                                                                                  return a:
27
                                                                         96
      friend auto &operator>>(istream &i, Z &z) { return i >> z.x;
                                                                                friend Poly operator*(Z a, Poly b) {
28
                                                                         98
                                                                                   for (int i = 0; i < (int)b.size(); i++) b[i] *= a;
                                                                         99
      friend auto &operator << (ostream &o, const Z &z) { return o
                                                                                   return b;
                                                                         100
     \leftrightarrow << z.x: }
                                                                         101
    };
                                                                                friend Poly operator*(Poly a, Z b) {
30
                                                                         102
                                                                                  for (int i = 0; i < (int)a.size(); i++) a[i] *= b;
31
                                                                         103
32
    void ntt(vector<Z> &a, int f) {
                                                                         104
                                                                                   return a;
      int n = (int)a.size();
33
                                                                         105
      vector<Z> w(n);
                                                                                Poly & operator += (Poly b) { return (*this) = (*this) + b; }
                                                                         106
34
35
      vector<int> rev(n);
                                                                         107
                                                                                Poly &operator = (Poly b) { return (*this) = (*this) - b; }
      for (int i = 0; i < n; i++) rev[i] = (rev[i / 2] / 2) | ((i
                                                                                Poly &operator *= (Poly b) { return (*this) = (*this) * b; }
                                                                        108
36
     \leftrightarrow & 1) * (n / 2));
                                                                                Poly deriv() const {
      for (int i = 0; i < n; i++)
                                                                                   if (a.empty()) return Poly();
37
                                                                         110
         if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
                                                                                   vector<Z> res(size() - 1);
      Z wn = power(f ? (MOD + 1) / 3 : 3, (MOD - 1) / n);
                                                                                   for (int i = 0; i < size() - 1; ++i) res[i] = (i + 1) *
39
                                                                        112
      w[0] = 1;
                                                                               \rightarrow a[i + 1];
40
       for (int i = 1; i < n; i++) w[i] = w[i - 1] * wn;
                                                                                  return Poly(res);
41
                                                                         113
      for (int mid = 1; mid < n; mid *= 2) {</pre>
42
                                                                         114
         for (int i = 0; i < n; i += 2 * mid) {
                                                                                Poly integr() const {
43
44
           for (int j = 0; j < mid; j++) {
                                                                         116
                                                                                   vector<Z> res(size() + 1);
             Z x = a[i + j], y = a[i + j + mid] * w[n / (2 * mid) * 117
                                                                                   for (int i = 0; i < size(); ++i) res[i + 1] = a[i] / (i +
45
                                                                                  1);
             a[i + j] = x + y, a[i + j + mid] = x - y;
                                                                                  return Poly(res);
46
                                                                         118
47
                                                                         119
        }
                                                                                Poly inv(int m) const {
48
                                                                         120
       }
                                                                                  Poly x({a[0].inv()});
49
                                                                         121
50
       if (f) {
                                                                         122
                                                                                   int k = 1;
         Z iv = power(Z(n), MOD - 2);
                                                                                   while (k < m) {
51
                                                                         123
52
         for (int i = 0; i < n; i++) a[i] *= iv;
                                                                                    k *= 2;
                                                                                     x = (x * (Poly({2}) - modxk(k) * x)).modxk(k);
53
                                                                         125
    }
54
                                                                         126
55
                                                                         127
                                                                                  return x.modxk(m);
    struct Poly {
56
                                                                         128
       vector<Z> a;
                                                                                Poly log(int m) const { return (deriv() *
      Polv() {}

    inv(m)).integr().modxk(m); }

58
59
       Poly(const vector\langle Z \rangle \&_a) : a(_a) {}
                                                                         130
                                                                                Poly exp(int m) const {
       int size() const { return (int)a.size(); }
60
                                                                         131
                                                                                  Poly \mathbf{x}(\{1\});
       void resize(int n) { a.resize(n); }
                                                                                   int k = 1:
61
                                                                         132
       Z operator[](int idx) const {
                                                                                   while (k < m) {
62
                                                                         133
                                                                                    k *= 2;
         if (idx < 0 || idx >= size()) return 0;
63
                                                                         134
         return a[idx];
                                                                                     x = (x * (Poly({1}) - x.log(k) + modxk(k))).modxk(k);
64
                                                                         135
65
                                                                         136
       Z &operator[](int idx) { return a[idx]; }
                                                                         137
                                                                                  return x.modxk(m);
66
                                                                                }
67
      Poly mulxk(int k) const {
                                                                         138
         auto b = a;
                                                                                Poly pow(int k, int m) const {
                                                                         139
68
         b.insert(b.begin(), k, 0);
                                                                                   int i = 0;
69
                                                                         140
                                                                                   while (i < size() && a[i].x == 0) i++;
70
         return Poly(b);
                                                                         141
                                                                                   if (i == size() || 1LL * i * k >= m) {
71
      Poly modxk(int k) const { return Poly(vector<Z>(a.begin(),
                                                                                    return Poly(vector<Z>(m));
                                                                         143
72

    a.begin() + min(k, size()))); }

                                                                         144
      Poly divxk(int k) const {
                                                                                   Z v = a[i];
73
                                                                         145
         if (size() <= k) return Poly();</pre>
                                                                                   auto f = divxk(i) * v.inv();
74
                                                                         146
         return Poly(vector<Z>(a.begin() + k, a.end()));
                                                                                   return (f.log(m - i * k) * k).exp(m - i * k).mulxk(i * k)
75
                                                                         147
76
      }
                                                                                  * power(v, k);
      friend Poly operator+(const Poly &a, const Poly &b) {
77
                                                                         148
78
         vector<Z> res(max(a.size(), b.size()));
                                                                                Poly sqrt(int m) const {
                                                                         149
         for (int i = 0; i < (int)res.size(); i++) res[i] = a[i] +
                                                                                  Poly x(\{1\});
                                                                         150
79
     \rightarrow b[i];
                                                                                   int k = 1;
        return Poly(res);
                                                                                   while (k < m) {
80
                                                                         152
81
                                                                         153
                                                                                    k *= 2;
      friend Poly operator-(const Poly &a, const Poly &b) {
                                                                                    x = (x + (modxk(k) * x.inv(k)).modxk(k)) * ((MOD + 1) /
82
                                                                         154
         vector<Z> res(max(a.size(), b.size()));

→ 2);

83
         for (int i = 0; i < (int)res.size(); i++) res[i] = a[i] -
                                                                                  }
     ⇔ b[i]:
                                                                                  return x.modxk(m);
                                                                         156
        return Poly(res);
85
                                                                         157
      }
86
                                                                         158
                                                                                Poly mulT(Poly b) const {
                                                                                   if (b.size() == 0) return Poly();
      friend Poly operator*(Poly a, Poly b) {
87
                                                                         159
         if (a.size() == 0 || b.size() == 0) return Poly();
                                                                         160
                                                                                   int n = b.size();
88
         int n = 1, m = (int)a.size() + (int)b.size() - 1;
                                                                                  reverse(b.a.begin(), b.a.end());
89
                                                                         161
```

```
162
         return ((*this) * b).divxk(n - 1);
                                                                        16
                                                                                 mu[i * p] = -mu[i];
                                                                               }
                                                                        17
163
164
       Poly divmod(Poly b) const {
                                                                         18
                                                                             }
         auto n = size(), m = b.size();
165
         auto t = *this;
                                                                                • Euler's totient function
166
167
         reverse(t.a.begin(), t.a.end());
                                                                             vector<int> min_p(MAX_N), phi(MAX_N), primes;
         reverse(b.a.begin(), b.a.end());
168
                                                                             phi[1] = 1, primes.reserve(1e5);
         Poly res = (t * b.inv(n)).modxk(n - m + 1);
                                                                             for (int i = 2; i < MAX_N; i++) {
                                                                         3
         reverse(res.a.begin(), res.a.end());
170
                                                                                if (min_p[i] == 0) {
171
                                                                                  min_p[i] = i;
172
                                                                                  primes.push_back(i);
       vector<Z> eval(vector<Z> x) const {
173
                                                                                  phi[i] = i - 1;
         if (size() == 0) return vector<Z>(x.size(), 0);
         const int n = max(int(x.size()), size());
175
                                                                                for (auto p : primes) {
176
         vector<Poly> q(4 * n);
                                                                                 if (i * p >= MAX_N) break;
                                                                         10
         vector<Z> ans(x.size());
177
                                                                         11
                                                                                  min_p[i * p] = p;
         x.resize(n);
178
                                                                                  if (i \% p == 0) {
         function<void(int, int, int)> build = [&](int p, int 1,
179
                                                                                    phi[i * p] = phi[i] * p;
                                                                         13
        int r) {
180
           if (r - 1 == 1) {
                                                                                  }
                                                                         15
             q[p] = Poly(\{1, -x[1]\});
181
                                                                                  phi[i * p] = phi[i] * phi[p];
                                                                         16
182
                                                                         17
             int m = (1 + r) / 2;
183
                                                                             }
             build(2 * p, 1, m), build(2 * p + 1, m, r);
                                                                         18
184
             q[p] = q[2 * p] * q[2 * p + 1];
185
           }
186
                                                                              Gaussian Elimination
         };
187
188
         build(1, 0, n);
                                                                             bool is_0(Z v) { return v.x == 0; }
         auto work = [&] (auto self, int p, int l, int r, const Poly
189
                                                                             Z abs(Z v) { return v; }
      bool is_0(double v) { return abs(v) < 1e-9; }</pre>
           if (r - 1 == 1) {
190
             if (1 < int(ans.size())) ans[1] = num[0];</pre>
191
                                                                             // 1 => unique solution, 0 => no solution, -1 => multiple
           } else {
192
                                                                              \hookrightarrow solutions
             int m = (1 + r) / 2;
193
                                                                             template <typename T>
             self(self,\ 2\ *\ p,\ l,\ m,\ num.mulT(q[2\ *\ p\ +\ l]).modxk(m
194
                                                                              int gaussian_elimination(vector<vector<T>>> &a, int limit) {
        - 1));
                                                                                  if (a.empty() || a[0].empty()) return -1;
             self(self, 2 * p + 1, m, r, num.mulT(q[2 * p]).modxk(r)
                                                                                int h = (int)a.size(), w = (int)a[0].size(), r = 0;
         - m));
                                                                                for (int c = 0; c < limit; c++) {
196
           }
                                                                                  int id = -1;
                                                                         11
197
                                                                         12
                                                                                  for (int i = r; i < h; i++) {
         work(work, 1, 0, n, mulT(q[1].inv(n)));
198
                                                                                   if (!is_0(a[i][c]) && (id == -1 || abs(a[id][c]) <
                                                                         13
199
         return ans;
                                                                                  abs(a[i][c]))) {
       }
200
                                                                         14
                                                                                      id = i:
     };
                                                                                    }
                                                                         15
                                                                                  7
                                                                                  if (id == -1) continue;
                                                                         17
     Sieve
                                                                                  if (id > r) {
                                                                         18
                                                                         19
                                                                                    swap(a[r], a[id]);

    linear sieve

                                                                                    for (int j = c; j < w; j++) a[id][j] = -a[id][j];
                                                                         20
                                                                                  7
                                                                         ^{21}
     vector<int> min_primes(MAX_N), primes;
                                                                                  vector<int> nonzero;
                                                                         22
     primes.reserve(1e5);
                                                                                  for (int j = c; j < w; j++) {
     for (int i = 2; i < MAX_N; i++) {
                                                                                    if (!is_0(a[r][j])) nonzero.push_back(j);
       if (!min_primes[i]) min_primes[i] = i, primes.push_back(i);
                                                                         24
                                                                         25
       for (auto& p : primes) {
                                                                         26
                                                                                  T inv_a = 1 / a[r][c];
         if (p * i >= MAX_N) break;
                                                                                  for (int i = r + 1; i < h; i++) {
                                                                         27
         min_primes[p * i] = p;
                                                                         28
                                                                                    if (is_0(a[i][c])) continue;
         if (i % p == 0) break;
                                                                                    T coeff = -a[i][c] * inv a;
                                                                         29
       }
 9
                                                                         30
                                                                                    for (int j : nonzero) a[i][j] += coeff * a[r][j];
     }
10
                                                                                  }
                                                                         31

    mobius function

                                                                         32
                                                                                7
                                                                         33
     vector<int> min_p(MAX_N), mu(MAX_N), primes;
                                                                                for (int row = h - 1; row >= 0; row--) {
                                                                         34
     mu[1] = 1, primes.reserve(1e5);
                                                                                  for (int c = 0; c < limit; c++) {
     for (int i = 2; I < MAX_N; i++) {</pre>
                                                                                    if (!is_0(a[row][c])) {
                                                                         36
       if (min_p[i] == 0) {
                                                                         37
                                                                                      T inv_a = 1 / a[row][c];
                                                                                      for (int i = row - 1; i >= 0; i--) {
         min_p[i] = i;
                                                                         38
         primes.push_back(i);
                                                                                        if (is_0(a[i][c])) continue;
 6
                                                                         39
         mu[i] = -1;
                                                                                        T coeff = -a[i][c] * inv_a;
                                                                         40
                                                                                        for (int j = c; j < w; j++) a[i][j] += coeff *
 8
                                                                         41
       for (auto p : primes) {
                                                                                  a[row][j];
 10
         if (i * p >= MAX_N) break;
                                                                         42
                                                                                      }
11
         min_p[i * p] = p;
                                                                         43
                                                                                      break;
12
         if (i % p == 0) {
                                                                         44
                                                                                    }
           mu[i * p] = 0;
13
                                                                         45
                                                                                } // not-free variables: only it on its line
                                                                                for(int i = r; i < h; i++) if(!is_0(a[i][limit])) return 0;</pre>
         }
15
```

```
return (r == limit) ? 1 : -1;
                                                                         24
                                                                                    return:
49
                                                                         25
                                                                         26
                                                                                  11 p = x;
50
                                                                                  while (p >= x) p = pollard_rho(x);
    template <tvpename T>
51
                                                                         27
    pair<int, vector<T>> solve_linear(vector<vector<T>> a, const
                                                                                  while ((x \% p) == 0) x /= p;
                                                                         28

  vector<T> &b, int w) {

                                                                         29
                                                                                  fac(x), fac(p);
      int h = (int)a.size();
                                                                                };
53
                                                                         30
      for (int i = 0; i < h; i++) a[i].push_back(b[i]);</pre>
                                                                         31
                                                                                fac(_x);
      int sol = gaussian_elimination(a, w);
                                                                               return max_factor;
55
                                                                         32
       if(!sol) return {0, vector<T>()};
56
57
      vector<T> x(w, 0);
      for (int i = 0; i < h; i++) {
58
                                                                              Radix Sort
         for (int j = 0; j < w; j++) {
           if (!is_0(a[i][j])) {
60
                                                                              struct identity {
61
             x[j] = a[i][w] / a[i][j];
                                                                                  template<typename T>
                                                                          2
62
             break;
                                                                                  T operator()(const T &x) const {
63
                                                                                      return x:
                                                                          4
64
65
                                                                             };
                                                                          6
66
      return {sol, x};
                                                                              // A stable sort that sorts in passes of `bits_per_pass` bits
                                                                              template<typename T, typename T_extract_key = identity>
    is prime
                                                                              void radix_sort(vector<T> &data, int bits_per_pass = 10, const

    T_extract_key &extract_key = identity()) {
       • (Miller–Rabin primality test)
                                                                                  if (int64_t(data.size()) * (64 -
                                                                                  __builtin_clzll(data.size())) < 2 * (1 << bits_per_pass))
    i128 power(i128 a, i128 b, i128 MOD = 1, i128 res = 1) {
      for (; b; b /= 2, (a *= a) \%= MOD)
                                                                                      \verb|stable_sort(data.begin(), data.end(), [\&](const T \& a,
                                                                         12
         if (b & 1) (res *= a) \%= MOD;
                                                                                  const T &b) {
      return res;
                                                                                          return extract_key(a) < extract_key(b);</pre>
                                                                         13
5
                                                                                      });
                                                                         14
6
                                                                         15
                                                                                      return;
    bool is_prime(ll n) {
                                                                         16
      if (n < 2) return false;
       static constexpr int A[] = {2, 3, 5, 7, 11, 13, 17, 19, 23};
                                                                                  using T_key = decltype(extract_key(data.front()));
      int s = __builtin_ctzll(n - 1);
10
                                                                                  T_key minimum = numeric_limits<T_key>::max();
                                                                         19
      11 d = (n - 1) >> s;
11
                                                                         20
      for (auto a : A) {
12
                                                                                  for (T &x : data)
                                                                         21
         if (a == n) return true;
13
                                                                                      minimum = min(minimum, extract_key(x));
         11 x = (11)power(a, d, n);
         if (x == 1 \mid | x == n - 1) continue;
                                                                         23
15
                                                                                  int max_bits = 0;
                                                                         24
         bool ok = false;
16
                                                                         25
         for (int i = 0; i < s - 1; ++i) {
17
                                                                         26
                                                                                  for (T &x : data) {
           x = 11((i128)x * x % n); // potential overflow!
18
                                                                                      T_key key = extract_key(x);
                                                                         27
           if (x == n - 1) {
19
                                                                                      max_bits = max(max_bits, key == minimum ? 0 : 64 -
                                                                         28
             ok = true;
20
                                                                                  __builtin_clzll(key - minimum));
21
             break;
                                                                         29
22
                                                                         30
                                                                                  int passes = max((max_bits + bits_per_pass / 2) /
                                                                         31
24
         if (!ok) return false;

→ bits_per_pass, 1);

25
                                                                         32
26
      return true;
                                                                                  if (64 - __builtin_clzll(data.size()) <= 1.5 * passes) {</pre>
                                                                         33
27
                                                                                      stable_sort(data.begin(), data.end(), [&](const T &a,
                                                                         34
    11 pollard_rho(11 x) {
                                                                                  const T &b) {
      ll s = 0, t = 0, c = rng() % (x - 1) + 1;
                                                                                          return extract_key(a) < extract_key(b);</pre>
                                                                         35
      ll stp = 0, goal = 1, val = 1;
                                                                                      });
      for (goal = 1;; goal *= 2, s = t, val = 1) {
                                                                         37
                                                                                      return;
         for (stp = 1; stp <= goal; ++stp) {</pre>
                                                                         38
           t = 11(((i128)t * t + c) \% x);
                                                                         39
           val = 11((i128)val * abs(t - s) % x);
                                                                                  vector<T> buffer(data.size());
                                                                         40
           if ((stp \% 127) == 0) {
                                                                         41
                                                                                  vector<int> counts;
             11 d = gcd(val, x);
                                                                                  int bits_so_far = 0;
9
                                                                         42
             if (d > 1) return d;
                                                                         43
                                                                                  for (int p = 0; p < passes; p++) {
11
                                                                         44
                                                                                      int bits = (max_bits + p) / passes;
12
                                                                         45
         11 d = gcd(val, x);
                                                                                      counts.assign(1 << bits, 0);</pre>
13
                                                                         46
         if (d > 1) return d;
                                                                         47
14
                                                                                      for (T &x : data) \{
15
                                                                         48
    }
                                                                                          T_key key = T_key(extract_key(x) - minimum);
16
                                                                         49
                                                                                          counts[(key >> bits_so_far) & ((1 << bits) -</pre>
17
                                                                         50
    11 get_max_factor(ll _x) {

    1)]++;

18
19
      11 max_factor = 0;
                                                                         51
20
      function \langle void(11) \rangle fac = [&](11 x) {
         if (x <= max_factor || x < 2) return;</pre>
                                                                                      int count sum = 0:
21
                                                                         53
         if (is_prime(x)) {
           max_factor = max_factor > x ? max_factor : x;
                                                                                      for (int &count : counts) {
23
```

```
int current = count;
                 count = count_sum;
57
                 count_sum += current;
59
60
             for (T &x : data) {
61
                 T_key key = T_key(extract_key(x) - minimum);
62
                 int key_section = int((key >> bits_so_far) & ((1
        << bits) - 1));
                 buffer[counts[key_section]++] = x;
64
65
             }
66
             swap(data, buffer);
67
             bits_so_far += bits;
68
69
    }
70

    USAGE

    radix_sort(edges, 10, [&](const edge &e) -> int { return
     \rightarrow abs(e.weight - x); });
```

String

AC Automaton struct AC_automaton {

```
int sz = 26:
       vector<vector<int>>> e = {vector<int>(sz)}; // vector is
     \,\, \hookrightarrow \,\, faster \,\, than \,\, unordered\_map
       vector<int> fail = {0};
       vector<int> end = {0};
       void insert(string& s) {
         int p = 0;
9
         for (auto c : s) {
           c -= 'a';
10
           if (!e[p][c]) {
11
             e.emplace_back(sz);
             fail.emplace_back();
13
14
             end.emplace_back();
             e[p][c] = e.size() - 1;
15
16
             = e[p][c];
17
18
         end[p] += 1;
19
20
21
22
       void build() {
         queue<int> q;
23
         for (int i = 0; i < sz; i++)
24
           if (e[0][i]) q.push(e[0][i]);
25
         while (!q.empty()) {
26
27
           int p = q.front();
           q.pop();
28
           for (int i = 0; i < sz; i++) {
             if (e[p][i]) {
30
                fail[e[p][i]] = e[fail[p]][i];
31
                q.push(e[p][i]);
32
33
             } else {
                e[p][i] = e[fail[p]][i];
34
35
36
           }
         }
37
38
    };
```

KMP

• nex[i]: length of longest common prefix & suffix for pat[0..i]

```
vector<int> get_next(vector<int> &pat) {
  int m = (int)pat.size();
  vector<int> nex(m);
 for (int i = 1, j = 0; i < m; i++) {
```

```
while (j && pat[j] != pat[i]) j = nex[j - 1];
        if (pat[j] == pat[i]) j++;
6
        nex[i] = j;
9
      return nex;
10
      • kmp match for txt and pat
    auto nex = get_next(pat);
    for (int i = 0, j = 0; i < n; i++) {
      while (j && pat[j] != txt[i]) j = nex[j - 1];
      if (pat[j] == txt[i]) j++;
      if (j == m) {
        // do what you want with the match
        // start index is `i - m + 1`
        j = nex[j - 1];
      }
   }
10
```

Z function

9

2

10

11

12

13

14

15

17

18

19

20

21

22

23

24

25

26

• z[i]: length of longest common prefix of s and s[i:]

```
vector<int> z_function(string s) {
      int n = (int)s.size();
      vector<int> z(n);
      for (int i = 1, l = 0, r = 0; i < n; ++i) {
        if (i <= r) z[i] = min(r - i + 1, z[i - 1]);
        while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]]) ++z[i];
        if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
      }
      return z;
10
```

General Suffix Automaton

```
constexpr int SZ = 26;
struct GSAM {
 vector<vector<int>> e = {vector<int>(SZ)}; // the labeled
\hookrightarrow edges from node i
 vector<int> parent = {-1};
                                               // the parent of
vector<int> length = {0};
                                               // the length of
\hookrightarrow the longest string
 GSAM(int n) { e.reserve(2 * n), parent.reserve(2 * n),

    length.reserve(2 * n); };

 int extend(int c, int p) { // character, last
   bool f = true;
                              // if already exist
    int r = 0;
                              // potential new node
    if (!e[p][c]) {
                              // only extend when not exist
      f = false:
      e.push_back(vector<int>(SZ));
      parent.push_back(0);
      length.push_back(length[p] + 1);
      r = (int)e.size() - 1;
      for (; ~p && !e[p][c]; p = parent[p]) e[p][c] = r; //
    update parents
    if (f || ~p) {
      int q = e[p][c];
      if (length[q] == length[p] + 1) {
        if (f) return q;
        parent[r] = q;
      } else {
        e.push_back(e[q]);
        parent.push_back(parent[q]);
        length.push_back(length[p] + 1);
        int qq = parent[q] = (int)e.size() - 1;
        for (; p \& \& e[p][c] == q; p = parent[p]) e[p][c] =

→ qq;

        if (f) return qq;
        parent[r] = qq;
    }
```

32

```
35
        return r;
                                                                            int main() {
      }
                                                                              string s;
36
                                                                        16
37
   };
                                                                               cin >> s;
                                                                               duval(s);
                                                                        18
       • Topo sort on GSAM
                                                                        19
    11 sz = gsam.e.size();
    vector<int> c(sz + 1);
    vector<int> order(sz);
   for (int i = 1; i < sz; i++) c[gsam.length[i]]++;
    for (int i = 1; i < sz; i++) c[i] += c[i - 1];
    for (int i = 1; i < sz; i++) order[c[gsam.length[i]]--] = i;</pre>
   reverse(order.begin(), order.end()); // reverse so that large
     \,\,\hookrightarrow\,\,\,\, \textit{len to small}
       • can be used as an ordinary SAM
       • USAGE (the number of distinct substring)
    int main() {
      int n, last = 0;
      string s;
      cin >> n;
      auto a = GSAM();
      for (int i = 0; i < n; i++) {
        cin >> s;
        last = 0; // reset last
9
        for (auto&& c : s) last = a.extend(c, last);
10
11
      11 \text{ ans} = 0;
      for (int i = 1; i < a.e.size(); i++) {</pre>
12
        ans += a.length[i] - a.length[a.parent[i]];
14
15
      cout << ans << endl;</pre>
16
      return 0;
    }
17
    Manacher
    string longest_palindrome(string& s) {
      // init "abc" -> "^$a#b#c$'
      vector<char> t{'^', '#'};
      for (char c : s) t.push_back(c), t.push_back('#');
      t.push_back('$');
      // manacher
      int n = t.size(), r = 0, c = 0;
      vector<int> p(n, 0);
      for (int i = 1; i < n - 1; i++) {
        if (i < r + c) p[i] = min(p[2 * c - i], r + c - i);
10
        while (t[i + p[i] + 1] == t[i - p[i] - 1]) p[i]++;
        if (i + p[i] > r + c) r = p[i], c = i;
12
13
         // s[i] \rightarrow p[2 * i + 2] (even), p[2 * i + 2] (odd)
14
       // output answer
15
16
      int index = 0;
      for (int i = 0; i < n; i++)
17
        if (p[index] < p[i]) index = i;</pre>
18
      return s.substr((index - p[index]) / 2, p[index]);
19
20
    Lyndon
       • def: suf(s) > s
    void duval(const string &s) {
      int n = (int)s.size();
      for (int i = 0; i < n;) {
        int j = i, k = i + 1;
        for (; j < n && s[j] <= s[k]; j++, k++)
           if (s[j] < s[k]) j = i - 1;
         while (i <= j) {
           // cout << s.substr(i, k - j) << '\n';
9
10
           i += k - j;
11
      }
12
   }
13
```