# Fortcoders Code Library

askd, yangster67, Nea1

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## Contents

## Intro

Intro	1		Main template
Main template	1		
Fast IO	1	1 2	<pre>#include <bits stdc++.h=""> using namespace std;</bits></pre>
Pragmas (lol)	1	3	using numespace stu,
		4	#define $FOR(x,n)$ for(int $x=0;x< n;x++)$
Data Structures	<b>2</b>	5	#define form(i, n) for (int $i = 0$ ; $i < int(n)$ ; $i++$ )
Segment Tree	2	6 7	<pre>#define all(v) v.begin(),v.end() using 11 = long long;</pre>
Recursive	2	8	using ld = long double;
Iterating	2	9	using pii = pair <int, int="">;</int,>
Union Find	3	10	<pre>const char nl = '\n';</pre>
Fenwick Tree	4	11 12	<pre>int main() {</pre>
Fenwick2D Tree	4	13	<pre>cin.tie(nullptr)-&gt;sync_with_stdio(false);</pre>
PBDS	4	14	<pre>cout &lt;&lt; fixed &lt;&lt; setprecision(20);</pre>
Treap	4	15	// mt19937
Implicit treap	5	16	<pre>→ rng(chrono::steady_clock::now().time_since_epoch().count()); }</pre>
Persistent implicit treap	6	10	,
2D Sparse Table	6		F / IO
K-D Tree	6		Fast IO
Link/Cut Tree	7	1	namespace io {
·		2	<pre>constexpr int SIZE = 1 &lt;&lt; 16;</pre>
Geometry	7	3	<pre>char buf[SIZE], *head, *tail;</pre>
Basic stuff	7	4 5	<pre>char get_char() {   if (head == tail) tail = (head = buf) + fread(buf, 1, SIZE,</pre>
Transformation	8		<pre>stdin);</pre>
Relation	8	6	return *head++;
Area	9	7	}
Convex	10	8 9	<pre>11 read() {    11 x = 0, f = 1;</pre>
Basic 3D	11	10	<pre>char c = get_char();</pre>
Miscellaneous	11	11	for (; !isdigit(c); c = get_char()) (c == '-') && (f = -1);
		12	for (; isdigit(c); c = get_char()) x = x * 10 + c - '0';
Graph Theory	11	13 14	return x * f;
Max Flow	11	15	string read_s() {
PushRelabel Max-Flow (faster)	12	16	string str;
Min-Cost Max-Flow	12	17	<pre>char c = get_char();</pre>
Heavy-Light Decomposition	13	18 19	<pre>while (c == ' '    c == '\n'    c == '\r') c = get_char(); while (c != ' ' &amp;&amp; c != '\n' &amp;&amp; c != '\r') str += c, c =</pre>
General Unweight Graph Matching	13		<pre>     get_char();</pre>
Maximum Bipartite Matching	14	20	return str;
2-SAT and Strongly Connected Components	14	21 22	<pre>void print(int x) {</pre>
Enumerating Triangles	14	23	if (x > 9) print(x / 10);
Tarjan	14	24	putchar(x % 10   '0');
Kruskal reconstruct tree	15	25	}
		26	<pre>void println(int x) { print(x), putchar('\n'); } struct Read {</pre>
Math	15	27 28	Read& operator>>(ll& x) { return x = read(), *this; }
Inverse	15	29	Read& operator>>(long double& x) { return x =
Mod Class	15		<pre>     stold(read_s()), *this; } </pre>
Canaan mad alaga	16	30 31	<pre>} in; } // namespace io</pre>
Cancer mod class	16	31	j // Namespace 10
NTT, FFT, FWT	16		D (L1)
Polynomial Class	17		Pragmas (lol)
Sieve	18	1	#pragma GCC optimize(2)
Gaussian Elimination	19	2	#pragma GCC optimize(3)
is_prime	19	3	<pre>#pragma GCC optimize("Ofast")</pre>
Radix Sort	19	4 5	<pre>#pragma GCC optimize("inline") #pragma GCC optimize("-fgcse")</pre>
String	20	6	#pragma GCC optimize("-fgcse-lm")
AC Automaton	20	7	<pre>#pragma GCC optimize("-fipa-sra")</pre>
		8	<pre>#pragma GCC optimize("-ftree-pre")</pre>
KMP	$\frac{20}{21}$	9 10	<pre>#pragma GCC optimize("-ftree-vrp") #pragma GCC optimize("-fpeephole2")</pre>
General Suffix Automaton	21	10	<pre>#pragma GCC optimize("-ffeephote2") #pragma GCC optimize("-ffast-math")</pre>
		12	<pre>#pragma GCC optimize("-fsched-spec")</pre>
Manacher	21	13	<pre>#pragma GCC optimize("unroll-loops")</pre>
Lyndon	21	14	<pre>#pragma GCC optimize("-falign-jumps") #pragma GCC optimize("-falign-loops")</pre>
		15	mpragma accorptimize (-jatigh-toops)

```
#pragma GCC optimize("-falign-labels")
                                                                              34 };
16
     #pragma GCC optimize("-fdevirtualize")
#pragma GCC optimize("-fcaller-saves")
17
                                                                                      • Persistent implicit, range query + point update
     #pragma GCC optimize("-fcrossjumping")
19
     #pragma GCC optimize("-fthread-jumps")
                                                                                    int lc = 0, rc = 0, p = 0;
     #pragma GCC optimize("-funroll-loops")
                                                                              2
21
     #pragma GCC optimize("-fwhole-program")
#pragma GCC optimize("-freorder-blocks")
                                                                              3
22
     #pragma GCC optimize("-fschedule-insns")
                                                                                  struct SegTree {
                                                                              5
24
                                                                                     vector<Node> t = {{}}; // init all
     {\it \#pragma~GCC~optimize("inline-functions")}
                                                                                     SegTree() = default;
     #pragma GCC optimize("-ftree-tail-merge")
26
                                                                                     SegTree(int n) { t.reserve(n * 20); }
     #pragma GCC optimize("-fschedule-insns2")
#pragma GCC optimize("-fstrict-aliasing")
                                                                                     int modify(int p, int 1, int r, int x, int v) {
28
                                                                                       // p: original node, update a[x] \rightarrow v
     #pragma GCC optimize("-fstrict-overflow")
                                                                              10
29
     #pragma GCC optimize("-falign-functions")
                                                                                       t.push_back(t[p]);
                                                                              11
                                                                                       int u = (int)t.size() - 1;
     \textit{\#pragma GCC optimize("-fcse-skip-blocks")}
                                                                             12
31
                                                                                       if (r - 1 == 1) {
     #pragma GCC optimize("-fcse-follow-jumps")
#pragma GCC optimize("-fsched-interblock")
                                                                              13
                                                                             14
                                                                                         t[u].p = v;
33
     #pragma GCC optimize("-fpartial-inlining")
                                                                             15
                                                                                       } else {
34
                                                                                         int m = (1 + r) / 2;
                                                                             16
     #pragma GCC optimize("no-stack-protector")
35
                                                                                         if (x < m) {
     #pragma GCC optimize("-freorder-functions")
                                                                             17
36
     #pragma GCC optimize("-findirect-inlining")
                                                                              18
                                                                                            t[u].lc = modify(t[p].lc, 1, m, x, v);
                                                                                            t[u].rc = t[p].rc;
     #pragma GCC optimize("-fhoist-adjacent-loads")
                                                                             19
                                                                             20
                                                                                         } else {
     #pragma GCC optimize("-frerun-cse-after-loop")
                                                                              ^{21}
                                                                                            t[u].lc = t[p].lc;
     #pragma GCC optimize("inline-small-functions")
40
                                                                                            t[u].rc = modify(t[p].rc, m, r, x, v);
     #pragma GCC optimize("-finline-small-functions")
#pragma GCC optimize("-ftree-switch-conversion")
                                                                              22
41
     #pragma GCC optimize("-foptimize-sibling-calls")
                                                                                         t[u].p = t[t[u].lc].p + t[t[u].rc].p;
                                                                              24
43
     #pragma GCC optimize("-fexpensive-optimizations")
     #pragma GCC optimize("-funsafe-loop-optimizations")
                                                                             26
                                                                                       return u;
45
                                                                             27
     #pragma GCC optimize("inline-functions-called-once")
46
                                                                                     int query(int p, int 1, int r, int x, int y) {
    #pragma GCC optimize("-fdelete-null-pointer-checks")
47
                                                                              29
                                                                                       // query sum a[x]...a[y-1] rooted at p
    #pragma GCC
     \leftrightarrow target("sse,sse2,sse3,sse4.1,sse4.2,avx,avx2,popcnt,tun2\textcapenative" t[p] holds the info of [l, r)
                                                                                       if (x <= 1 && r <= y) return t[p].p;
                                                                                       int m = (1 + r) / 2, res = 0;
                                                                             33
                                                                                       if (x < m) res += query(t[p].lc, l, m, x, y);
     Data Structures
                                                                                       if (y > m) res += query(t[p].rc, m, r, x, y);
                                                                              34
                                                                              35
                                                                                       return res;
     Segment Tree
                                                                              36
                                                                                  };
```

#### Recursive

struct Node {

• Implicit segment tree, range query + point update

```
2
      int lc, rc, p;
    struct SegTree {
      vector<Node> t = {{}};
      SegTree(int n) { t.reserve(n * 40); }
       int modify(int p, int 1, int r, int x, int v) {
        int u = p;
         if (p == 0) {
           t.push_back(t[p]);
11
12
           u = (int)t.size() - 1;
13
        if (r - l == 1) {
14
           t[u].p = t[p].p + v;
         } else {
16
           int m = (1 + r) / 2;
17
           if (x < m) {
18
            t[u].lc = modify(t[p].lc, 1, m, x, v);
19
           } else {
20
             t[u].rc = modify(t[p].rc, m, r, x, v);
21
22
          t[u].p = t[t[u].lc].p + t[t[u].rc].p;
23
24
25
        return u;
26
27
       int query(int p, int l, int r, int x, int y) {
         if (x <= 1 && r <= y) return t[p].p;</pre>
28
         int m = (1 + r) / 2, res = 0;
29
         if (x < m) res += query(t[p].lc, l, m, x, y);
30
         if (y > m) res += query(t[p].rc, m, r, x, y);
31
32
        return res;
33
```

#### Iterating

• Iterating, range query + point update

```
struct Node {
      11 v = 0, init = 0;
2
3
    Node pull(const Node &a, const Node &b) {
      if (!a.init) return b;
      if (!b.init) return a;
      Node c:
9
      return c;
10
    struct SegTree {
12
13
       vector<Node> t;
14
      SegTree(ll _n) : n(_n), t(2 * n){};
15
      void modify(ll p, const Node &v) {
        t[p += n] = v;
17
         for (p /= 2; p; p /= 2) t[p] = pull(t[p * 2], t[p * 2 +
     19
      Node query(ll 1, ll r) {
20
21
        Node left, right;
         for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
22
          if (1 & 1) left = pull(left, t[1++]);
23
           if (r & 1) right = pull(t[--r], right);
25
26
        return pull(left, right);
      }
27
    };
28
```

• Iterating, range query + range update

```
struct Node {
                                                                               T query(int 1, int r) {
                                                                        19
2
      11 v = 0;
                                                                                  T resl, resr;
                                                                        20
    };
                                                                                  for(1 += size, r += size + 1; 1 < r; 1 >>= 1, r >>= 1) {
3
                                                                        21
    struct Tag {
                                                                                    if(1 & 1) resl = resl * tree[l++];
4
                                                                        22
      11 v = 0;
                                                                                    if(r & 1) resr = tree[--r] * resr;
6
    }:
                                                                        24
    Node pull(const Node& a, const Node& b) { return {max(a.v,
                                                                        25
                                                                                 return resl * resr;
     \rightarrow b.v)}; }
                                                                        26
    Tag pull(const Tag& a, const Tag& b) { return {a.v + b.v}; }
                                                                               T query_all() { return tree[1]; }
                                                                        27
    Node apply_tag(const Node& a, const Tag& b) { return {a.v +
                                                                               void consume(int i) { tree[i] = tree[i << 1] * tree[i << 1 |</pre>
     \rightarrow b.v\}; }
                                                                              };
10
                                                                         29
11
    struct SegTree {
                                                                        30
      11 n, h;
12
                                                                        31
      vector<Node> t;
                                                                             struct SegInfo {
13
      vector<Tag> lazy;
                                                                               11 v:
14
                                                                         33
      SegTree(ll _n) : n(_n), h((ll)log2(n)), t(2 * _n), lazy(2 *
                                                                                SegInfo() : SegInfo(0) {}
                                                                                SegInfo(ll val) : v(val) {}
         _n) {}
                                                                         35
      void apply(ll x, const Tag& tag) {
                                                                                SegInfo operator*(SegInfo b) {
16
                                                                        36
         t[x] = apply_tag(t[x], tag);
                                                                                 return SegInfo(v + b.v);
17
                                                                        37
         lazy[x] = pull(lazy[x], tag);
                                                                        38
18
                                                                             };
19
                                                                        39
      void build(ll 1) {
20
         for (1 = (1 + n) / 2; 1 > 0; 1 /= 2) {
                                                                             Union Find
           if (!lazy[1].v) t[1] = pull(t[1 * 2], t[2 * 1 + 1]);
22
23
      }
                                                                             vector<int> p(n);
24
      void push(11 1) {
                                                                             iota(p.begin(), p.end(), 0);
25
                                                                             function<int(int)> find = [&](int x) { return p[x] == x ? x :
         1 += n;
         for (ll s = h; s > 0; s--) {
27
                                                                              \leftrightarrow (p[x] = find(p[x])); \};
           11 i = 1 >> s;
                                                                             auto merge = [&](int x, int y) { p[find(x)] = find(y); };
28
           if (lazy[i].v) {
29
             apply(2 * i, lazy[i]);
                                                                                • Persistent version
30
31
             apply(2 * i + 1, lazy[i]);
                                                                             struct Node {
32
           lazy[i] = Tag();
                                                                         2
                                                                               int lc, rc, p;
33
                                                                             };
        }
                                                                         3
34
35
                                                                             struct SegTree {
       void modify(ll l, ll r, const Tag& v) {
                                                                         5
                                                                               vector<Node> t = \{\{0, 0, -1\}\}; // init all
         push(1), push(r - 1);
37
                                                                               SegTree() = default;
38
         11\ 10 = 1, r0 = r;
         for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
                                                                                SegTree(int n) { t.reserve(n * 20); }
39
                                                                                int modify(int p, int 1, int r, int x, int v) {
           if (1 & 1) apply(1++, v);
40
                                                                                 // p: original node, update a[x] \rightarrow v
                                                                         10
           if (r & 1) apply(--r, v);
41
                                                                                  t.push_back(t[p]);
                                                                         11
42
                                                                                 int u = (int)t.size() - 1;
        build(10), build(r0 - 1);
                                                                        12
43
                                                                                  if (r - 1 == 1) {
                                                                         13
44
                                                                        14
                                                                                    t[u].p = v;
      Node query(ll l, ll r) {
45
                                                                                  } else {
46
         push(1), push(r - 1);
                                                                        15
                                                                                    int m = (1 + r) / 2;
         Node left, right;
47
                                                                                    if (x < m) {
48
         for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
                                                                        17
                                                                                      t[u].lc = modify(t[p].lc, l, m, x, v);
           if (1 & 1) left = pull(left, t[1++]);
49
                                                                                      t[u].rc = t[p].rc;
50
           if (r \& 1) right = pull(t[--r], right);
                                                                        19
                                                                                    } else {
                                                                        20
51
                                                                        21
                                                                                      t[u].lc = t[p].lc;
52
         return pull(left, right);
                                                                                      t[u].rc = modify(t[p].rc, m, r, x, v);
      }
                                                                        22
53
    };
54
                                                                                    t[u].p = t[t[u].lc].p + t[t[u].rc].p;
                                                                         24
       • AtCoder Segment Tree (recursive structure but iterative)
                                                                                 return u;
                                                                        26
    template <class T> struct PointSegmentTree {
1
                                                                        27
       int size = 1;
                                                                                int query(int p, int l, int r, int x, int y) {
       vector<T> tree;
                                                                         29
                                                                                 // query sum a[x]...a[y-1] rooted at p
       PointSegmentTree(int n) : PointSegmentTree(vector<T>(n)) {}
                                                                                  // t[p] holds the info of [l, r)
                                                                                 if (x \le 1 \&\& r \le y) return t[p].p;
      PointSegmentTree(vector<T>& arr) {
                                                                        31
         while(size < (int)arr.size())</pre>
                                                                                  int m = (1 + r) / 2, res = 0;
                                                                        32
           size <<= 1;
                                                                                  if (x < m) res += query(t[p].lc, l, m, x, y);
                                                                        33
         tree = vector<T>(size << 1);</pre>
                                                                                  if (y > m) res += query(t[p].rc, m, r, x, y);
                                                                        34
         for(int i = size + arr.size() - 1; i >= 1; i--)
                                                                        35
                                                                                  return res;
10
           if(i >= size) tree[i] = arr[i - size];
                                                                               }
                                                                        36
           else consume(i);
11
                                                                             };
                                                                        37
12
      }
                                                                        38
      void set(int i, T val) {
13
                                                                             struct DSU {
                                                                        39
         tree[i += size] = val;
14
                                                                               int n;
                                                                        40
         for(i >>= 1; i >= 1; i >>= 1)
15
                                                                               SegTree seg;
                                                                        41
           consume(i);
16
                                                                               DSU(int _n) : n(_n), seg(n) {}
17
                                                                        43
                                                                               int get(int p, int x) { return seg.query(p, 0, n, x, x + 1);
      T get(int i) { return tree[i + size]; }
```

```
int set(int p, int x, int v) { return seg.modify(p, 0, n, x,
                                                                                ll sum(ll x, ll y) { // [(0, 0), (x, y))
                                                                         18
                                                                                  11 \text{ ans} = 0;
45
      int find(int p, int x) {
                                                                         19
                                                                                  for (int i = x; i > 0; i -= i & -i) {
         int parent = get(p, x);
46
                                                                         20
         if (parent < 0) return x;</pre>
                                                                                    for (int j = y; j > 0; j -= j & -j) {
47
                                                                         21
         return find(p, parent);
                                                                                      (ans += a[i - 1][j - 1]) \% = MOD;
48
                                                                         22
49
                                                                         23
      int is_same(int p, int x, int y) { return find(p, x) ==
                                                                         24
50

    find(p, y); }

                                                                         25
                                                                                  return ans;
51
      int merge(int p, int x, int y) {
                                                                         26
         int rx = find(p, x), ry = find(p, y);
                                                                             }:
52
         if (rx == ry) return -1;
53
         int rank_x = -get(p, rx), rank_y = -get(p, ry);
54
                                                                              PBDS
         if (rank_x < rank_y) {</pre>
55
          p = set(p, rx, ry);
                                                                              #include <bits/stdc++.h>
         } else if (rank_x > rank_y) {
57
                                                                             #include <ext/pb_ds/assoc_container.hpp>
          p = set(p, ry, rx);
                                                                             using namespace std;
59
         } else {
                                                                             using namespace __gnu_pbds;
          p = set(p, ry, rx);
60
                                                                              template<typename T>
61
          p = set(p, rx, -rx - 1);
                                                                              using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
62

    tree_order_statistics_node_update>;
63
         return p;
      }
                                                                             template<typename T, typename X>
64
                                                                             using ordered_map = tree<T, X, less<T>, rb_tree_tag,
    };

→ tree_order_statistics_node_update>;

                                                                              template<typename \textbf{T}\text{,} typename \textbf{X}\text{>}
    Fenwick Tree
                                                                              using fast_map = cc_hash_table<T, X>;
                                                                              template<typename T, typename X>
    template <typename T> struct FenwickTree {
                                                                              using ht = gp_hash_table<T, X>;
                                                                         12
      int size = 1, high_bit = 1;
                                                                              mt19937_64
      vector<T> tree;
                                                                              rng(chrono::steady_clock::now().time_since_epoch().count());
      FenwickTree(int _size) : size(_size) {
         tree.resize(size + 1);
                                                                              struct splitmix64 {
                                                                         15
         while((high_bit << 1) <= size) high_bit <<= 1;</pre>
                                                                                  size_t operator()(size_t x) const {
6
                                                                         16
                                                                                     static const size_t fixed =
      FenwickTree(vector<T>& arr) : FenwickTree(arr.size()) {
                                                                                  chrono::steady_clock::now().time_since_epoch().count();
         for(int i = 0; i < size; i++) update(i, arr[i]);</pre>
                                                                                     x += 0x9e3779b97f4a7c15 + fixed;
                                                                                      x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;

x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
10
                                                                         19
       int lower_bound(T x) {
                                                                         20
11
                                                                                      return x \hat{ } (x >> 31);
         int res = 0; T cur = 0;
12
                                                                         21
         for(int bit = high_bit; bit > 0; bit >>= 1) {
13
                                                                         22
           if((res|bit) <= size && cur + tree[res|bit] < x) {</pre>
                                                                              };
             res |= bit; cur += tree[res];
15
16
        }
                                                                              Treap
17
        return res;
18
                                                                                 • (No rotation version)
19
      T prefix_sum(int i) {
20
                                                                              struct Node {
21
                                                                                Node *1, *r;
         for(i++; i > 0; i -= (i & -i)) ret += tree[i];
22
                                                                                int s, sz;
         return ret;
23
                                                                                // int t = 0, a = 0, g = 0; // for lazy propagation
24
      }
      T range_sum(int 1, int r) { return (1 > r) ? 0 :
25

→ prefix_sum(r) - prefix_sum(l - 1); }

                                                                                Node(int _s) : l(nullptr), r(nullptr), s(_s), sz(1),
      void update(int i, T delta) { for(i++; i <= size; i += (i &</pre>
26
                                                                               \rightarrow w(rng()) {}
        -i)) tree[i] += delta; }
                                                                                void apply(int vt, int vg) {
27
                                                                                  // for lazy propagation
                                                                          9
                                                                                  // s -= vt;
                                                                         10
                                                                                  // t += vt, a += vg, g += vg;
    Fenwick2D Tree
                                                                         11
                                                                                }
                                                                         12
                                                                                void push() {
    struct Fenwick2D {
                                                                                  // for lazy propagation
      ll n, m;
                                                                         14
      vector<vector<11>>> a;
                                                                                  // if (l != nullptr) l->apply(t, g);
      Fenwick2D(11 _n, 11 _m) : n(_n), m(_m), a(n, vector<11>(m))
                                                                                  // if (r != nullptr) r->apply(t, g);
                                                                                  // t = g = 0;
                                                                         17
      void add(ll x, ll y, ll v) {
         for (int i = x + 1; i \le n; i += i & -i) {
                                                                                void pull() { sz = 1 + (1 ? 1->sz : 0) + (r ? r->sz : 0); }
                                                                         19
           for (int j = y + 1; j \le m; j += j & -j) {
                                                                         20
             (a[i - 1][j - 1] += v) \%= MOD;
                                                                         21
                                                                              std::pair<Node *, Node *> split(Node *t, int v) {
9
                                                                         22
        }
10
                                                                         23
                                                                                if (t == nullptr) return {nullptr, nullptr};
      }
                                                                                t->push();
11
                                                                         24
12
       void add(ll x1, ll x2, ll y1, ll y2, ll v) {
                                                                                if (t->s < v) {
                                                                         25
                                                                                  auto [x, y] = split(t->r, v);
13
         // [(x1, y1), (x2, y2))
                                                                         26
         add(x1, y1, v);
                                                                                  t->r = x;
14
                                                                         27
         add(x1, y2, MOD - v), add(x2, y1, MOD - v);
15
                                                                         28
                                                                                  t->pull();
```

29

return {t, y};

add(x2, y2, v);

```
} else {
30
         auto [x, y] = split(t->1, v);
31
32
        t->1 = y;
         t->pull();
33
         return {x, t};
34
      }
35
    }
36
37
    Node *merge(Node *p, Node *q) {
38
      if (p == nullptr) return q;
      if (q == nullptr) return p;
40
       if (p->w < q->w) swap(p, q);
41
42
      auto [x, y] = split(q, p->s + rng() % 2);
      p->push();
43
      p->1 = merge(p->1, x);
      p->r = merge(p->r, y);
45
46
      p->pull();
47
      return p;
48
49
    Node *insert(Node *t, int v) {
50
      auto [x, y] = split(t, v);
51
      return merge(merge(x, new Node(v)), y);
52
53
54
    Node *erase(Node *t, int v) {
55
      auto [x, y] = split(t, v);
56
      auto [p, q] = split(y, v + 1);
57
      return merge(merge(x, merge(p->1, p->r)), q);
59
60
61
    int get_rank(Node *&t, int v) {
      auto [x, y] = split(t, v);
62
      int res = (x ? x->sz : 0) + 1;
      t = merge(x, y);
64
65
      return res;
    }
66
67
    Node *kth(Node *t, int k) {
      k--:
69
      while (true) {
70
        int left_sz = t->1 ? t->1->sz : 0;
71
        if (k < left_sz) {</pre>
72
          t = t->1;
        } else if (k == left_sz) {
74
          return t;
        } else {
76
          k = left_sz + 1, t = t->r;
77
78
      }
79
    }
80
81
    Node *get_prev(Node *&t, int v) {
83
      auto [x, y] = split(t, v);
      Node *res = kth(x, x->sz);
84
85
      t = merge(x, y);
86
      return res;
88
89
    Node *get_next(Node *&t, int v) {
90
      auto [x, y] = split(t, v + 1);
      Node *res = kth(y, 1);
91
      t = merge(x, y);
92
      return res;
93
    }
94

    USAGE

    int main() {
      cin.tie(nullptr)->sync_with_stdio(false);
       int n;
      cin >> n;
      Node *t = nullptr;
      for (int op, x; n--;) {
        cin >> op >> x;
        if (op == 1) {
8
           t = insert(t, x);
        } else if (op == 2) {
```

```
t = erase(t, x);
11
         } else if (op == 3) {
12
           cout << get_rank(t, x) << "\n";</pre>
13
         } else if (op == 4) {
14
           cout << kth(t, x)->s << "\n";
         } else if (op == 5) {
16
17
           cout << get_prev(t, x)->s << "\n";
18
         } else {
           cout << get_next(t, x)->s << "\n";</pre>
19
20
21
       }
    }
22
```

#### Implicit treap

• Split by size

```
struct Node {
       Node *1, *r;
       int s, sz;
       // int lazy = 0;
4
       11 w:
       Node(int _s) : l(nullptr), r(nullptr), s(_s), sz(1),
     \rightarrow w(rnd()) {}
       void apply() {
8
         // for lazy propagation
9
         // lazy ^= 1;
10
       }
11
       void push() {
12
         // for lazy propagation
// if (lazy) {
13
14
         // swap(l, r);
15
         // if (l != nullptr) l->apply();
         // if (r != nullptr) r->apply();
// lazy = 0;
17
18
         1/ }
19
20
       void pull() { sz = 1 + (1 ? 1->sz : 0) + (r ? r->sz : 0); }
^{21}
22
     std::pair<Node *, Node *> split(Node *t, int v) {
24
       // first->sz == v
25
       if (t == nullptr) return {nullptr, nullptr};
26
       t->push();
27
       int left_sz = t->1 ? t->1->sz : 0;
28
       if (left_sz < v) {</pre>
29
         auto [x, y] = split(t->r, v - left_sz - 1);
         t->r = x;
31
32
         t->pull();
         return {t, y};
33
       } else {
34
         auto [x, y] = split(t->1, v);
         t->1 = y;
36
37
         t->pull();
38
         return {x, t};
39
40
    }
41
    Node *merge(Node *p, Node *q) {
^{42}
       if (p == nullptr) return q;
43
       if (q == nullptr) return p;
44
       if (p->w < q->w) {
         p->push();
46
47
         p->r = merge(p->r, q);
48
         p->pull();
         return p;
49
       } else {
50
         q->push();
51
         q->1 = merge(p, q->1);
52
         q->pull();
53
         return q;
54
55
       }
56
```

#### Persistent implicit treap

```
pair<Node *, Node *> split(Node *t, int v) {
       // first->sz == v
       if (t == nullptr) return {nullptr, nullptr};
       t->push();
       int left_sz = t->1 ? t->1->sz : 0;
      t = new Node(*t);
       if (left_sz < v) {</pre>
         auto [x, y] = split(t->r, v - left_sz - 1);
         t->r = x:
         t->pull();
         return {t, y};
11
       } else {
12
         auto [x, y] = split(t->1, v);
13
         t->1 = v;
14
         t->pull();
16
         return {x, t};
17
    }
18
19
    Node *merge(Node *p, Node *q) {
       if (p == nullptr) return new Node(*q);
21
22
       if (q == nullptr) return new Node(*p);
       if (p->w < q->w) {
23
         p = new Node(*p);
24
        p->push();
25
         p->r = merge(p->r, q);
26
27
         p->pull();
28
        return p;
       } else {
29
         q = new Node(*q);
30
         q->push();
31
         q->1 = merge(p, q->1);
32
33
         q->pull();
34
         return q;
35
```

#### 2D Sparse Table

• Sorry that this sucks - askd

```
template <class T, class Compare = less<T>>
    struct SparseTable2d {
       int n = 0, m = 0;
      T**** table;
       int* log;
       inline T choose(T x, T y) {
        return Compare()(x, y) ? x : y;
8
       SparseTable2d(vector<vector<T>>& grid) {
9
         if(grid.empty() || grid[0].empty()) return;
10
         n = grid.size(); m = grid[0].size();
11
         log = new int[max(n, m) + 1];
12
13
         log[1] = 0;
         for(int i = 2; i <= max(n, m); i++)</pre>
14
           log[i] = log[i - 1] + ((i ^ (i - 1)) > i);
15
         table = new T***[n];
16
         for(int i = n - 1; i >= 0; i--) {
17
           table[i] = new T**[m];
           for(int j = m - 1; j >= 0; j--) {
19
             table[i][j] = new T*[log[n - i] + 1];
20
             for(int k = 0; k <= log[n - i]; k++) {</pre>
21
               table[i][j][k] = new T[log[m - j] + 1];
22
               if(!k) table[i][j][k][0] = grid[i][j];
23
               \verb|else table[i][j][k][0] = \verb|choose(table[i][j][k-1][0]|, \\
24
     \rightarrow table[i+(1<<(k-1))][j][k-1][0]);
25
               for(int l = 1; l \le log[m - j]; l++)
                 table[i][j][k][l] = choose(table[i][j][k][l-1],
26
        table[i][j+(1<<(l-1))][k][l-1]);
27
28
           }
        }
29
30
      T query(int r1, int r2, int c1, int c2) {
31
         assert(r1 >= 0 && r2 < n && r1 <= r2);
```

```
assert(c1 >= 0 && c2 < m && c1 <= c2);
33
        int rl = log[r2 - r1 + 1], cl = log[c2 - c1 + 1];
34
        T ca1 = choose(table[r1][c1][r1][c1],

    table[r2-(1<<rl)+1][c1][r1][c1]);
</pre>
        T ca2 = choose(table[r1][c2-(1<<c1)+1][r1][c1],
     \leftrightarrow table[r2-(1<<rl)+1][c2-(1<<cl)+1][r1][c1]);
37
        return choose(ca1, ca2);
38
    };
39
       • USAGE
    vector<vector<int>>> test = {
      \{1, 2, 3, 4\}, \{2, 3, 4, 5\}, \{9, 9, 9, 9\}, \{-1, -1, -1, -1\}
2
3
    SparseTable2d<int> st(test);
                                                 // Range min query
    SparseTable2d<int,greater<int>>> st2(test); // Range max query
    K-D Tree
    struct Point {
1
2
     int x, y;
3
    struct Rectangle {
5
      int lx, rx, ly, ry;
6
    bool is_in(const Point &p, const Rectangle &rg) {
      return (p.x >= rg.lx) && (p.x <= rg.rx) && (p.y >= rg.ly) &&
     10
11
    struct KDTree {
12
      vector<Point> points;
13
      struct Node {
14
        int lc, rc;
15
        Point point;
16
17
        Rectangle range;
18
        int num:
      };
19
      vector<Node> nodes;
20
      int root = -1:
21
      KDTree(const vector<Point> &points_) {
22
        points = points_;
23
        Rectangle range = \{-1e9, 1e9, -1e9, 1e9\};
24
25
        root = tree_construct(0, (int)points.size(), range, 0);
26
      int tree_construct(int 1, int r, Rectangle range, int depth)
     if (1 == r) return -1;
28
        if (1 > r) throw;
29
        int mid = (1 + r) / 2;
30
        auto comp = (depth \% 2) ? [](Point &a, Point &b) { return
31
     \rightarrow a.x < b.x: }
                                 : [](Point &a, Point &b) { return
32
     \rightarrow a.y < b.y; };
        nth_element(points.begin() + 1, points.begin() + mid,
33
     → points.begin() + r, comp);
        Rectangle l_range(range), r_range(range);
34
        if (depth % 2) {
          l_range.rx = points[mid].x;
36
          r_range.lx = points[mid].x;
        } else {
          l_range.ry = points[mid].y;
39
          r_range.ly = points[mid].y;
        Node node = {tree_construct(1, mid, 1_range, depth + 1),
42
                     tree_construct(mid + 1, r, r_range, depth +
     44
        nodes.push_back(node);
        return (int)nodes.size() - 1;
45
46
47
48
      int inner_query(int id, const Rectangle &rec, int depth) {
        if (id == -1) return 0;
49
        Rectangle rg = nodes[id].range;
50
```

```
pull();
         if (rg.lx >= rec.lx && rg.rx <= rec.rx && rg.ly >= rec.ly
                                                                          49
        && rg.ry <= rec.ry) {
                                                                          50
52
          return nodes[id].num;
                                                                          51
                                                                                 void access() {
         }
                                                                                   for (Node *i = this, *q = nullptr; i != nullptr; q = i, i
53
                                                                          52
         int ans = 0;
                                                                                \hookrightarrow = i->p) {
                                                                                    i->splay();
         if (depth % 2) { // pruning
55
                                                                          53
56
           if (rec.lx <= nodes[id].point.x) ans +=</pre>
                                                                          54
                                                                                     i\rightarrow ch[1] = q;

    inner_query(nodes[id].lc, rec, depth + 1);

                                                                          55
                                                                                     i->pull();
          if (rec.rx >= nodes[id].point.x) ans +=
57
                                                                          56
        inner_query(nodes[id].rc, rec, depth + 1);
                                                                                   splay();
         } else {
58
                                                                          58
           if (rec.ly <= nodes[id].point.y) ans +=</pre>
                                                                                 void makeroot() {
                                                                          59
59

    inner_query(nodes[id].lc, rec, depth + 1);

                                                                          60
                                                                                   access():
           if (rec.ry >= nodes[id].point.y) ans +=
                                                                                   reverse(this);
60
                                                                          61
        inner_query(nodes[id].rc, rec, depth + 1);
                                                                          62
                                                                              }:
61
                                                                          63
         if (is_in(nodes[id].point, rec)) ans += 1;
                                                                          64
                                                                               void link(Node *x, Node *y) {
63
         return ans;
                                                                          65
                                                                                 x->makeroot();
                                                                                 x->p = y;
64
                                                                          66
      int query(const Rectangle &rec) { return inner_query(root,
                                                                              }
                                                                          67
                                                                               void split(Node *x, Node *y) {
     \rightarrow rec, 0); }
                                                                          68
                                                                                 x->makeroot();
                                                                          69
                                                                                 y->access();
                                                                          70
                                                                               void cut(Node *x, Node *y) {
                                                                          72
    Link/Cut Tree
                                                                                 split(x, y);
                                                                          73
                                                                                 x->p = y->ch[0] = nullptr;
                                                                          74
    struct Node {
                                                                                 y->pull();
                                                                          75
      Node *ch[2], *p;
                                                                              }
       int id:
                                                                          77
                                                                               bool connected(Node *p, Node *q) {
       bool rev;
                                                                          78
                                                                                   p->access();
      Node(int id) : ch{nullptr, nullptr}, p(nullptr), id(id),
                                                                          79
                                                                                   q->access();
      → rev(false) {}
                                                                                   return p->p != nullptr;
                                                                          80
      friend void reverse(Node *p) {
                                                                              }
         if (p != nullptr) {
           swap(p->ch[0], p->ch[1]);
           p->rev ^= 1;
9
                                                                               Geometry
11
       void push() {
12
                                                                               Basic stuff
        if (rev) {
           reverse(ch[0]);
14
           reverse(ch[1]);
                                                                               using ll = long long;
15
                                                                               using ld = long double;
           rev = false:
16
17
      }
                                                                               constexpr auto eps = 1e-8;
18
19
       void pull() {}
                                                                               const auto PI = acos(-1);
      bool is_root() { return p == nullptr || p->ch[0] != this &&
                                                                               int sgn(1d x) \{ return (abs(x) \le eps) ? 0 : (x < 0 ? -1 : 1); 

    p->ch[1] != this; }

       bool pos() { return p->ch[1] == this; }
      void rotate() {
                                                                               struct Point {
22
         Node *q = p;
                                                                                 1d x = 0, y = 0;
23
         bool x = !pos();
                                                                                 Point() = default;
                                                                          10
         q->ch[!x] = ch[x];
                                                                                 Point(ld _x, ld _y) : x(_x), y(_y) {}
25
                                                                          11
         if (ch[x] != nullptr) ch[x]->p = q;
                                                                                 bool operator<(const Point &p) const { return !sgn(p.x - x)</pre>
                                                                                \hookrightarrow ? sgn(y - p.y) < 0 : x < p.x; }
         p = q->p;
27
28
         if (!q->is\_root()) q->p->ch[q->pos()] = this;
                                                                                bool operator==(const Point &p) const { return !sgn(p.x - x)
29
         ch[x] = q;
                                                                                \leftrightarrow \&\& !sgn(p.y - y); \}
         q->p = this;
                                                                                 Point operator+(const Point &p) const { return {x + p.x, y +
30
        pull();
                                                                                \rightarrow p.y}; }
31
         q->pull();
                                                                                Point operator-(const Point &p) const { return {x - p.x, y -
32
                                                                          15
33

    p.y}; }

       void splay() {
                                                                                 Point operator*(ld a) const { return {x * a, y * a}; }
34
                                                                          16
                                                                                 Point operator/(ld a) const { return {x / a, y / a}; }
         vector<Node *> s;
35
         for (Node *i = this; !i->is_root(); i = i->p)
                                                                                 auto operator*(const Point &p) const { return x * p.x + y *
        s.push_back(i->p);
                                                                                \leftrightarrow p.y; } // dot
         while (!s.empty()) s.back()->push(), s.pop_back();
                                                                                 auto operator^(const Point &p) const { return x * p.y - y *
37

    p.x; } // cross

38
         push();
         while (!is_root()) {
                                                                                 friend auto &operator>>(istream &i, Point &p) { return i >>
39
                                                                          20
           if (!p->is_root()) {
                                                                                \rightarrow p.x >> p.y; }
40
                                                                                friend auto &operator<<(ostream &o, Point p) { return o <<</pre>
             if (pos() == p->pos()) {
41
                                                                          21
                                                                                   p.x << ' ' << p.y; }
42
               p->rotate();
             } else {
                                                                               };
43
                                                                          22
               rotate();
                                                                          23
                                                                               struct Line {
45
                                                                          24
                                                                                 Point s = \{0, 0\}, e = \{0, 0\};
46
                                                                          25
```

26

47

rotate();

Line() = default;

Line(Point \_s, Point \_e) : s(\_s), e(\_e) {}

```
friend auto &operator>>(istream &i, Line &l) { return i >>
                                                                            int n = p.size();
     \leftrightarrow 1.s >> 1.e; } // ((x1, y1), (x2, y2)
                                                                            vector<Point> res(n);
                                                                      26
    }:
                                                                            for (int i = 0; i < n; i++)
29
                                                                      27
                                                                             res[i] = rotate(p[i], a);
30
                                                                      28
    struct Segment : Line {
                                                                            return res:
31
                                                                      29
     using Line::Line;
32
                                                                      30
33
                                                                      31
                                                                          Point translate(const Point &p, ld dx = 0, ld dy = 0) { return
34
                                                                      32
    struct Circle {
                                                                           ⇔ Point(p.x + dx, p.y + dy); }
35
      Point o = \{0, 0\};
                                                                          Line translate(const Line &1, ld dx = 0, ld dy = 0) { return
                                                                          ld r = 0;
37
      Circle() = default;
                                                                          Segment translate(const Segment &1, ld dx = 0, ld dy = 0) {
39
      Circle(Point _o, ld _r) : o(_o), r(_r) {}

→ return Segment(translate(l.s, dx, dy), translate(l.e, dx,
                                                                           \rightarrow dy)); }
40
                                                                          Circle translate(const Circle &c, ld dx = 0, ld dy = 0) {
    auto dist2(const Point &a) { return a * a; }

→ return Circle(translate(c.o, dx, dy), c.r); }
    auto dist2(const Point &a, const Point &b) { return dist2(a -
                                                                          vector<Point> translate(const vector<Point> &p, ld dx = 0, ld
                                                                           \rightarrow dy = 0) {
    auto dist(const Point &a) { return sqrt(dist2(a)); }
                                                                           int n = p.size();
    auto dist(const Point &a, const Point &b) { return
                                                                            vector<Point> res(n);

    sqrt(dist2(a - b)); }

                                                                            for (int i = 0; i < n; i++)
                                                                      39
    auto dist(const Point &a, const Line &l) { return abs((a -
                                                                             res[i] = translate(p[i], dx, dy);
                                                                     40
     return res:
                                                                     41
    auto dist(const Point &p, const Segment &1) {
      if (1.s == 1.e) return dist(p, 1.s);
      auto d = dist2(1.s, 1.e), t = min(d, max((1d)0, (p - 1.s) *)
     \leftrightarrow (l.e - l.s)));
                                                                          Relation
      return dist((p - 1.s) * d, (1.e - 1.s) * t) / d;
9
10
                                                                      enum class Relation { SEPARATE, EX_TOUCH, OVERLAP, IN_TOUCH,
    /* Needs is_intersect
11
    auto dist(const Segment &11, const Segment &12) {
                                                                           → INSIDE }:
12
      if (is_intersect(l1, l2)) return (ld)0;
                                                                          Relation get_relation(const Circle &a, const Circle &b) {
                                                                            auto c1c2 = dist(a.o, b.o);
      return min({dist(l1.s, l2), dist(l1.e, l2), dist(l2.s, l1),
14
                                                                            auto r1r2 = a.r + b.r, diff = abs(a.r - b.r);
     \leftrightarrow dist(l2.e, l1)});
                                                                            if (sgn(c1c2 - r1r2) > 0) return Relation::SEPARATE;
    } */
15
                                                                            if (sgn(c1c2 - r1r2) == 0) return Relation::EX_TOUCH;
16
                                                                            if (sgn(c1c2 - diff) > 0) return Relation::OVERLAP;
if (sgn(c1c2 - diff) == 0) return Relation::IN_TOUCH;
    Point perp(const Point &p) { return Point(-p.y, p.x); }
17
18
                                                                            return Relation::INSIDE;
    auto rad(const Point &p) { return atan2(p.y, p.x); }
                                                                      9
                                                                      10
                                                                      11
    Transformation
                                                                          auto get_cos_from_triangle(ld a, ld b, ld c) { return (a * a +
                                                                      12
                                                                           \rightarrow b * b - c * c) / (2.0 * a * b); }
    Point project(const Point &p, const Line &l) {
      return 1.s + ((1.e - 1.s) * ((1.e - 1.s) * (p - 1.s))) /
                                                                          bool on_line(const Line &1, const Point &p) { return !sgn((1.s

→ dist2(1.e - 1.s);

                                                                           \rightarrow - p) \hat{} (l.e - p)); }
                                                                      15
                                                                          bool on_segment(const Segment &1, const Point &p) {
    Point reflect(const Point &p, const Line &1) {
                                                                           return !sgn((l.s - p) ^ (l.e - p)) && sgn((l.s - p) * (l.e -
                                                                      17
                                                                           \rightarrow p)) <= 0;
      return project(p, 1) * 2 - p;
                                                                      18
                                                                      19
    Point dilate(const Point &p, ld scale_x = 1, ld scale_y = 1) {
                                                                          bool on_segment2(const Segment &1, const Point &p) { // assume

→ return Point(p.x * scale_x, p.y * scale_y); }

                                                                           \hookrightarrow p on Line l
    Line dilate(const Line &1, ld scale_x = 1, ld scale_y = 1) {
                                                                           if (1.s == p || 1.e == p) return true;

→ return Line(dilate(l.s, scale_x, scale_y), dilate(l.e,
                                                                            if (\min(l.s, l.e)  return true;
                                                                      22

    scale_x, scale_y)); }

                                                                      23
                                                                            return false:
                                                                          }
    Segment dilate(const Segment &1, ld scale_x = 1, ld scale_y =
                                                                      24

    dilate(l.e, scale_x, scale_y)); }

                                                                          bool is_parallel(const Line &a, const Line &b) { return
    vector<Point> dilate(const vector<Point> &p, ld scale_x = 1,
                                                                           \rightarrow !sgn((a.s - a.e) ^ (b.s - b.e)); }
     \rightarrow ld scale_y = 1) {
                                                                          bool is_orthogonal(const Line &a, const Line &b) { return
     int n = p.size();
                                                                           \rightarrow !sgn((a.s - a.e) * (b.s - b.e)); }
13
      vector<Point> res(n);
14
      for (int i = 0; i < n; i++)
                                                                          int is_intersect(const Segment &a, const Segment &b) {
15
        res[i] = dilate(p[i], scale_x, scale_y);
                                                                          auto d1 = sgn((a.e - a.s) ^ (b.s - a.s)), d2 = sgn((a.e - a.s))
16
                                                                           \rightarrow a.s) ^ (b.e - a.s));
      return res;
17
                                                                           auto d3 = sgn((b.e - b.s) ^ (a.s - b.s)), d4 = sgn((b.e - b.s))
18
                                                                           \rightarrow b.s) ^ (a.e - b.s));
19
                                                                           if (d1 * d2 < 0 && d3 * d4 < 0) return 2; // intersect at
    Point rotate(const Point &p, ld a) { return Point(p.x * cos(a)
     \rightarrow - p.y * sin(a), p.x * sin(a) + p.y * cos(a)); }
                                                                           \hookrightarrow non-end point
    Line rotate(const Line &1, ld a) { return Line(rotate(1.s, a),
                                                                            return (d1 == 0 && sgn((b.s - a.s) * (b.s - a.e)) <= 0) ||
                                                                                   (d2 == 0 && sgn((b.e - a.s) * (b.e - a.e)) <= 0) ||

    rotate(1.e, a)); }

                                                                      34
    Segment rotate(const Segment &1, ld a) { return
                                                                                    (d3 == 0 \&\& sgn((a.s - b.s) * (a.s - b.e)) <= 0) ||
                                                                                   (d4 == 0 \&\& sgn((a.e - b.s) * (a.e - b.e)) <= 0);

→ Segment(rotate(l.s, a), rotate(l.e, a)); }

                                                                     36
    Circle rotate(const Circle &c, ld a) { return
                                                                      37
```

25

int is\_intersect(const Line &a, const Segment &b) {

vector<Point> rotate(const vector<Point> &p, ld a) {

```
auto d1 = sgn((a.e - a.s) \hat{ } (b.s - a.s)), d2 = sgn((a.e - a.s))
                                                                                Line u((a + b) / 2, ((a + b) / 2) + perp(b - a));
                                                                        107
      \rightarrow a.s) ^ (b.e - a.s));
                                                                                Line v((b + c) / 2, ((b + c) / 2) + perp(c - b));
                                                                        108
      if (d1 * d2 < 0) return 2; // intersect at non-end point
41
                                                                        109
                                                                                auto o = intersect(u, v);
       return d1 == 0 || d2 == 0;
                                                                                return Circle(o, dist(o, a));
42
                                                                        110
43
                                                                        111
44
                                                                        112
45
     Point intersect(const Line &a, const Line &b) {
                                                                        113
                                                                              Circle get_inscribed(const Point &a, const Point &b, const
       auto u = a.e - a.s, v = b.e - b.s;
                                                                               → Point &c) {
46
       auto t = ((b.s - a.s) ^ v) / (u ^ v);
                                                                                auto 11 = dist(b - c), 12 = dist(c - a), 13 = dist(a - b);
47
                                                                        114
       return a.s + u * t;
                                                                        115
                                                                                Point o = (a * 11 + b * 12 + c * 13) / (11 + 12 + 13);
                                                                                return Circle(o, dist(o, Line(a, b)));
49
                                                                        116
50
                                                                        117
     int is_intersect(const Circle &c, const Line &l) {
51
                                                                        118
      auto d = dist(c.o, 1);
                                                                              pair<ld, ld> get_centroid(const vector<Point> &p) {
                                                                        119
52
       return sgn(d - c.r) < 0 ? 2 : !sgn(d - c.r);
                                                                                int n = (int)p.size();
                                                                        120
                                                                                ld x = 0, y = 0, sum = 0;
54
                                                                        121
55
                                                                        122
                                                                                auto a = p[0], b = p[1];
                                                                                for (int i = 2; i < n; i++) {
     vector<Point> intersect(const Circle &a, const Circle &b) {
56
                                                                        123
       auto relation = get_relation(a, b);
                                                                                  auto c = p[i];
57
                                                                        124
       if (relation == Relation::INSIDE || relation ==
                                                                                  auto s = area({a, b, c});
                                                                        125
      ⇔ Relation::SEPARATE) return {};
                                                                                  sum += s;
                                                                        126
       auto vec = b.o - a.o;
                                                                                  x += s * (a.x + b.x + c.x);
                                                                        127
       auto d2 = dist2(vec);
                                                                                  y += s * (a.y + b.y + c.y);
60
                                                                        128
      auto p = (d2 + a.r * a.r - b.r * b.r) / ((long double)2 *
                                                                                  swap(b, c);
      \leftrightarrow d2), h2 = a.r * a.r - p * p * d2;
                                                                        130
      auto mid = a.o + vec * p, per = perp(vec) * sqrt(max((long
                                                                                return \{x / (3 * sum), y / (3 * sum)\};
62
                                                                        131

    double)0, h2) / d2);

                                                                        132
      if (relation == Relation::OVERLAP)
63
         return {mid + per, mid - per};
                                                                              Area
65
       else
         return {mid};
66
                                                                              auto area(const vector<Point> &p) {
     }
67
                                                                                int n = (int)p.size();
68
                                                                                long double area = 0;
     vector<Point> intersect(const Circle &c, const Line &l) {
                                                                                for (int i = 0; i < n; i++) area += p[i] ^ p[(i + 1) % n];
       if (!is_intersect(c, 1)) return {};
70
                                                                                return area / 2.0;
       auto v = 1.e - 1.s, t = v / dist(v);
71
                                                                          6
       Point a = 1.s + t * ((c.o - 1.s) * t);
72
       auto d = sqrt(max((1d)0, c.r * c.r - dist2(c.o, a)));
73
                                                                              auto area(const Point &a, const Point &b, const Point &c) {
       if (!sgn(d)) return {a};
                                                                                return ((long double)((b - a) ^ (c - a))) / 2.0;
       return {a - t * d, a + t * d};
75
                                                                         10
76
                                                                         11
77
                                                                              auto area2(const Point &a, const Point &b, const Point &c) {
     int in_poly(const vector<Point> &p, const Point &a) {
78
                                                                              \hookrightarrow return (b - a) \hat{} (c - a); }
       int cnt = 0, n = (int)p.size();
79
       for (int i = 0; i < n; i++) {
80
                                                                              auto area_intersect(const Circle &c, const vector<Point> &ps)
         auto q = p[(i + 1) \% n];
         if (on\_segment(Segment(p[i], q), a)) return 1; // on the
82
                                                                                int n = (int)ps.size();
      \rightarrow edge of the polygon
                                                                               auto arg = [&](const Point &p, const Point &q) { return
         cnt \hat{} = ((a.y < p[i].y) - (a.y < q.y)) * ((p[i] - a) \hat{} (q -
83
                                                                               \rightarrow atan2(p ^ q, p * q); };
      \rightarrow a)) > 0;
                                                                                auto tri = [&](const Point &p, const Point &q) {
                                                                         17
      }
                                                                                  auto r2 = c.r * c.r / (long double)2;
                                                                         18
       return cnt ? 2 : 0;
85
                                                                                  auto d = q - p;
                                                                         19
86
     }
                                                                                  auto a = d * p / dist2(d), b = (dist2(p) - c.r * c.r) /
                                                                         20
87

    dist2(d);
     int is_intersect(const vector<Point> &p, const Line &a) {
88
                                                                                  long double det = a * a - b:
                                                                         21
       // 1: touching, >=2: intersect count
89
                                                                                  if (sgn(det) <= 0) return arg(p, q) * r2;</pre>
       int cnt = 0, edge_cnt = 0, n = (int)p.size();
90
                                                                                  auto s = max((long double)0, -a - sqrt(det)), t =
       for (int i = 0; i < n; i++) {

    min((long double)1, -a + sqrt(det));

         auto q = p[(i + 1) \% n];
92
                                                                                  if (sgn(t) < 0 \mid \mid sgn(1 - s) \le 0) return arg(p, q) * r2;
         if (on_line(a, p[i]) && on_line(a, q)) return -1; //
93
                                                                                  auto u = p + d * s, v = p + d * t;
                                                                         25
      return arg(p, u) * r2 + (u ^ v) / 2 + arg(v, q) * r2;
         auto t = is_intersect(a, Segment(p[i], q));
94
                                                                         27
         (t == 1) && edge_cnt++, (t == 2) && cnt++;
95
                                                                                long double sum = 0;
       }
96
                                                                                for (int i = 0; i < n; i++) sum += tri(ps[i] - c.o, ps[(i +
97
       return cnt + edge_cnt / 2;
                                                                               \hookrightarrow 1) % n] - c.o);
98
                                                                               return sum;
99
                                                                         31
100
     vector<Point> tangent(const Circle &c, const Point &p) {
      auto d = dist(c.o, p), l = c.r * c.r / d, h = sqrt(c.r * c.r
101
                                                                              auto adaptive_simpson(ld _1, ld _r, function<ld(ld)> f) {
      \hookrightarrow -1 * 1);
                                                                               auto simpson = [\&](1d 1, 1d r) \{ return (r - 1) * (f(1) + 4) \}
      auto v = (p - c.o) / d;
102
                                                                               \leftrightarrow * f((1 + r) / 2) + f(r)) / 6; };
      return {c.o + v * 1 + perp(v) * h, c.o + v * 1 - perp(v) *
103
                                                                               function<ld(ld, ld, ld)> asr = [&](ld l, ld r, ld s) {
                                                                         35
                                                                                  auto mid = (1 + r) / 2;
     7
104
                                                                                  auto left = simpson(1, mid), right = simpson(mid, r);
                                                                         37
                                                                                  if (!sgn(left + right - s)) return left + right;
                                                                         38
     Circle get_circumscribed(const Point &a, const Point &b, const
106
                                                                                  return asr(1, mid, left) + asr(mid, r, right);
                                                                         39
     → Point &c) {
                                                                                }:
                                                                         40
```

```
return !rad_diff ? (dist2(a - points[0]) < dist2(b -</pre>
      return asr(_1, _r, simpson(_1, _r));
41
                                                                       34
                                                                               points[0])) : (rad_diff > 0);
42
                                                                             });
43
                                                                       35
                                                                              if (allow_collinear) {
    vector<Point> half_plane_intersect(vector<Line> &L) {
44
                                                                       36
      int n = (int)L.size(), l = 0, r = 0; // [left, right]
                                                                                int i = (int)points.size() - 1;
      sort(L.begin(), L.end(),
                                                                                while (i >= 0 && !sgn((points[i] - points[0]) ^ (points[i]
46
                                                                                - points.back()))) i--;
47
            [](const Line &a, const Line &b) { return rad(a.s -

    a.e) < rad(b.s - b.e); });</pre>
                                                                                reverse(points.begin() + i + 1, points.end());
                                                                       39
      vector<Point> p(n), res;
48
                                                                       40
49
      vector<Line> q(n);
                                                                       41
                                                                              vector<Point> hull;
      q[0] = L[0];
                                                                              for (auto &t : points) {
50
                                                                       42
      for (int i = 1; i < n; i++) {
                                                                       43
                                                                                for (ll sz = hull.size();
51
        while (1 < r && sgn((L[i].e - L[i].s) \hat{} (p[r - 1] -
                                                                                     sz > 1 \&\& (sgn((t - hull[sz - 2]) ^ (hull[sz - 1] -
     \hookrightarrow L[i].s)) <= 0) r--;

    hull[sz - 2])) >= allow_collinear);
        while (1 < r \text{ && sgn}((L[i].e - L[i].s) ^ (p[1] - L[i].s))
                                                                                     hull.pop_back(), sz = hull.size()) {
     46
        q[++r] = L[i];
                                                                       47
                                                                                hull.push_back(t);
         if (sgn((q[r].e - q[r].s) ^ (q[r - 1].e - q[r - 1].s)) ==
                                                                              }
55
                                                                       48

→ 0) {

                                                                              return hull;
                                                                       49
56
          if (sgn((q[r].e - q[r].s) ^ (L[i].s - q[r].s)) > 0) q[r]
57
                                                                       51
                                                                            vector<Point> get_convex_safe(vector<Point> points, bool
        = L[i];

    allow_collinear = false) {
58
        if (1 < r) p[r - 1] = intersect(q[r - 1], q[r]);</pre>
                                                                              return get_convex(points, allow_collinear);
59
60
                                                                       54
      while (1 < r \text{ && sgn}((q[1].e - q[1].s) \hat{ } (p[r - 1] - q[1].s))
61
                                                                       55
     vector<Point> get_convex2_safe(vector<Point> points, bool
      if (r - 1 <= 1) return {};

    allow collinear = false) {
62
      p[r] = intersect(q[r], q[1]);
                                                                              return get_convex2(points, allow_collinear);
      return vector<Point>(p.begin() + 1, p.begin() + r + 1);
64
                                                                       58
65
                                                                       59
                                                                            bool is_convex(const vector<Point> &p, bool allow_collinear =

  false) {
                                                                       61
                                                                              int n = p.size();
    Convex
                                                                              int lo = 1, hi = -1;
                                                                       62
                                                                              for (int i = 0; i < n; i++) {
                                                                       63
    vector<Point> get_convex(vector<Point> &points, bool
                                                                                int cur = sgn((p[(i + 2) \% n] - p[(i + 1) \% n]) ^ (p[(i +
                                                                       64
     → allow_collinear = false) {
                                                                             // strict, no repeat, two pass
                                                                                lo = min(lo, cur); hi = max(hi, cur);
      sort(points.begin(), points.end());
                                                                       66
      points.erase(unique(points.begin(), points.end()),
                                                                              return allow_collinear ? (hi - lo) < 2 : (lo == hi && lo);
                                                                       67

→ points.end());
                                                                       68
      vector<Point> L, U;
      for (auto &t : points) {
                                                                            auto rotating_calipers(const vector<Point> &hull) {
         for (ll sz = L.size(); sz > 1 && (sgn((t - L[sz - 2]) ^
                                                                              // use get convex2
                                                                       71
     \leftrightarrow (L[sz - 1] - L[sz - 2])) >= 0);
                                                                              int n = (int)hull.size(); // return the square of longest
             L.pop_back(), sz = L.size()) {

    dist

                                                                              assert(n > 1):
                                                                       73
        L.push_back(t);
10
                                                                       74
                                                                              if (n <= 2) return dist2(hull[0], hull[1]);</pre>
      }
11
                                                                              ld res = 0;
                                                                       75
      for (auto &t : points) {
12
                                                                              for (int i = 0, j = 2; i < n; i++) {
        for (ll sz = U.size(); sz > 1 && (sgn((t - U[sz - 2]) ^{\circ}
13
                                                                                auto d = hull[i], e = hull[(i + 1) % n];
        (U[sz - 1] - U[sz - 2])) <= 0);
                                                                                while (area2(d, e, hull[j]) < area2(d, e, hull[(j + 1) %
             U.pop_back(), sz = U.size()) {
14
                                                                            \rightarrow n])) j = (j + 1) % n;
        7
15
                                                                       79
                                                                               res = max(res, max(dist2(d, hull[j]), dist2(e, hull[j])));
        U.push_back(t);
16
                                                                              }
                                                                       80
17
                                                                       81
                                                                              return res;
      /\!/\ contain\ repeats\ if\ all\ collinear,\ use\ a\ set\ to\ remove

→ repeats

                                                                       83
      if (allow_collinear) {
19
                                                                       84
                                                                            // Find polygon cut to the left of l
        for (int i = (int)U.size() - 2; i >= 1; i--)
20
                                                                            vector<Point> convex_cut(const vector<Point> &p, const Line
                                                                       85
     21
      } else {
                                                                             int n = p.size();
         set<Point> st(L.begin(), L.end());
22
                                                                              vector<Point> cut;
                                                                       87
23
         for (int i = (int)U.size() - 2; i >= 1; i--) {
                                                                              for (int i = 0; i < n; i++) {
                                                                       88
          if (st.count(U[i]) == 0) L.push_back(U[i]),
24
                                                                                auto a = p[i], b = p[(i + 1) \% n];
                                                                       89
        st.insert(U[i]);
                                                                                if (sgn((l.e - l.s)
                                                                                                     (a - l.s)) >= 0)
                                                                       90
25
        }
                                                                       91
                                                                                  cut.push_back(a);
      }
26
                                                                                if (sgn((1.e - 1.s) ^ (a - 1.s)) * sgn((1.e - 1.s) ^ (b -
                                                                       92
      return L;
27
                                                                            \rightarrow 1.s)) == -1)
28
                                                                       93
                                                                                  cut.push_back(intersect(Line(a, b), 1));
29
                                                                              }
                                                                       94
    vector<Point> get_convex2(vector<Point> &points, bool
30
                                                                              return cut;
     \leftrightarrow allow_collinear = false) { // strict, no repeat, one pass
                                                                       96
31
      nth_element(points.begin(), points.begin(), points.end());
      sort(points.begin() + 1, points.end(), [&](const Point &a,
32
                                                                            // Sort by angle in range [0, 2pi)
     template <class RandomIt>
         int rad_diff = sgn((a - points[0]) ^ (b - points[0]));
```

#### → Point(0, 0)) { auto get\_quad = [&](const Point& p) { 101 Point diff = p - origin; 102 if (diff.x > 0 && diff.y >= 0) return 1; 103 if (diff.x <= 0 && diff.y > 0) return 2; 104 if (diff.x < 0 && diff.y <= 0) return 3; 105 106 return 4: 107 108 auto polar\_cmp = [%](const Point% p1, const Point% p2) { int q1 = get\_quad(p1), q2 = get\_quad(p2); 109 if (q1 != q2) return q1 < q2; 110 return ((p1 - origin) ^ (p2 - origin)) > 0; 111 112 sort(first, last, polar\_cmp); 113 114 Basic 3D using ll = long long; using ld = long double; 3 constexpr auto eps = 1e-8; const auto PI = acos(-1); int $sgn(1d x) \{ return (abs(x) \le eps) ? 0 : (x < 0 ? -1 : 1);$ struct Point3D { ld x = 0, y = 0, z = 0; Point3D() = default; Point3D(ld $_x$ , ld $_y$ , ld $_z$ ) : $_x(_x)$ , $_y(_y)$ , $_z(_z)$ {} 11 bool operator<(const Point3D &p) const { return !sgn(p.x -</pre> $\rightarrow$ x) ? (!sgn(p.y - y) ? sgn(p.z - z) < 0 : y < p.y) : x < $\rightarrow$ p.x; } bool operator==(const Point3D &p) const { return !sgn(p.x - $\rightarrow$ x) && !sgn(p.y - y) && !sgn(p.z - z); } Point3D operator+(const Point3D &p) const { return {x + p.x, $\rightarrow$ y + p.y, z + p.z}; } Point3D operator-(const Point3D &p) const { return {x - p.x, 15 $\rightarrow$ y - p.y, z - p.z}; } Point3D operator\*(ld a) const { return {x \* a, y \* a, z \* a}; } Point3D operator/(ld a) const { return {x / a, y / a, z / auto operator\*(const Point3D &p) const { return x \* p.x + y $\Rightarrow$ \* p.y + z \* p.z; } // dot Point3D operator^(const Point3D &p) const { return {y \* p.z $\rightarrow$ -z \* p.y, z \* p.x - x \* p.z, x \* p.y - y \* p.x}; } // friend auto &operator>>(istream &i, Point3D &p) { return i ⇔ >> p.x >> p.y >> p.z; } }; 21 22 struct Line3D { Point3D s = $\{0, 0, 0\}, e = \{0, 0, 0\};$ 24 25 Line3D() = default; Line3D(Point3D $_s$ , Point3D $_e$ ) : $s(_s)$ , $e(_e)$ {} 26 27 28 struct Segment3D : Line3D { 29 using Line3D::Line3D; 30 31 32 33 auto dist2(const Point3D &a) { return a \* a; } auto dist2(const Point3D &a, const Point3D &b) { return dist2(a - b); } auto dist(const Point3D &a) { return sqrt(dist2(a)); } 35 auto dist(const Point3D &a, const Point3D &b) { return sqrt(dist2(a - b)); } auto dist(const Point3D &a, const Line3D &1) { return dist((a - l.s) ^ (l.e - l.s)) / dist(l.s, l.e); } auto dist(const Point3D &p, const Segment3D &1) { 38 if (1.s == 1.e) return dist(p, 1.s); auto d = dist2(1.s, 1.e), t = min(d, max((ld)0, (p - 1.s) \*40 $\leftrightarrow$ (l.e - l.s))); return dist((p - 1.s) \* d, (1.e - 1.s) \* t) / d; } 42

void polar\_sort(RandomIt first, RandomIt last, Point origin =

#### Miscellaneous

11

12

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54

55

```
tuple<int,int,ld> closest_pair(vector<Point> &p) {
  using Pt = pair<Point, int>;
  int n = p.size();
  assert(n > 1);
  vector<Pt> pts(n), buf;
  for (int i = 0; i < n; i++) pts[i] = {p[i], i};
  sort(pts.begin(), pts.end());
  buf.reserve(n);
  auto cmp_y = [](const Pt& p1, const Pt& p2) { return

   p1.first.y < p2.first.y; };</pre>
  function<tuple<int,int,ld>(int, int)> recurse = [&](int 1,

    int r) → tuple<int,int,ld> {
    int i = pts[l].second, j = pts[l + 1].second;
    ld d = dist(pts[1].first, pts[1 + 1].first);
    if (r - 1 < 5) {
      for (int a = 1; a < r; a++) for (int b = a + 1; b < r;

→ b++) {

        ld cur = dist(pts[a].first, pts[b].first);
        if (cur < d) { i = pts[a].second; j = pts[b].second; d</pre>
   = cur: }
      sort(pts.begin() + 1, pts.begin() + r, cmp_y);
    else {
      int mid = (1 + r)/2;
      ld x = pts[mid].first.x;
      auto [li, lj, ldist] = recurse(l, mid);
      auto [ri, rj, rdist] = recurse(mid, r);
      if (ldist < rdist) { i = li; j = lj; d = ldist; }</pre>
      else { i = ri; j = rj; d = rdist; }
      inplace_merge(pts.begin() + 1, pts.begin() + mid,
   pts.begin() + r, cmp_y);
      buf.clear():
      for (int a = 1; a < r; a++) {
        if (abs(x - pts[a].first.x) >= d) continue;
        for (int b = buf.size() - 1; b >= 0; b--) {
          if (pts[a].first.y - buf[b].first.y >= d) break;
          ld cur = dist(pts[a].first, buf[b].first);
          if (cur < d) { i = pts[a].second; j = buf[b].second;</pre>
\rightarrow d = cur; }
        buf.push_back(pts[a]);
    return {i, j, d};
  return recurse(0, n);
Line abc_to_line(ld a, ld b, ld c) {
  assert(!sgn(a) || !sgn(b));
  if(a == 0) return Line(Point(0, -c/b), Point(1, -c/b));
  if(b == 0) return Line(Point(-c/a, 0), Point(-c/a, 1));
  Point s(0, -c/b), e(1, (-c - a)/b), diff = e - s;
  return Line(s, s + diff/dist(diff));
tuple<ld,ld,ld> line_to_abc(const Line& 1) {
 Point diff = 1.e - 1.s;
  return {-diff.y, diff.x, -(diff ^ 1.s)};
```

### **Graph Theory**

#### Max Flow

```
struct Edge {
   int from, to, cap, remain;
};

struct Dinic {
   int n;
   vector<Edge> e;
   vector<vector<int>> g;
```

```
struct PushRelabel {
9
       vector<int> d, cur;
                                                                          9
       Dinic(int _n) : n(_n), g(n), d(n), cur(n) {}
                                                                                 struct Edge {
10
                                                                          10
11
       void add_edge(int u, int v, int c) {
                                                                          11
                                                                                   int dest, back;
         g[u].push_back((int)e.size());
                                                                                   ll f, c;
12
                                                                          12
                                                                                 };
         e.push_back({u, v, c, c});
         g[v].push_back((int)e.size());
14
                                                                          14
                                                                                 vector<vector<Edge>> g;
15
         e.push_back({v, u, 0, 0});
                                                                          15
                                                                                 vector<ll> ec;
      }
16
                                                                                 vector<Edge*> cur;
                                                                          16
      11 max_flow(int s, int t) {
                                                                                 vector<vi> hs;
17
                                                                          17
18
         int inf = 1e9;
                                                                                 vi H;
         auto bfs = \lceil \& \rceil() {
                                                                                 PushRelabel(int n) : g(n), ec(n), cur(n), hs(2 * n), H(n) {}
19
                                                                          19
           fill(d.begin(), d.end(), inf), fill(cur.begin(),
20
        cur.end(), 0);
                                                                          21
                                                                                 void addEdge(int s, int t, ll cap, ll rcap = 0) {
           d[s] = 0;
                                                                                   if (s == t) return;
21
                                                                          22
           vector<int> q{s}, nq;
                                                                                   g[s].push_back({t, sz(g[t]), 0, cap});
22
           for (int step = 1; q.size(); swap(q, nq), nq.clear(),
                                                                                   g[t].push_back({s, sz(g[s]) - 1, 0, rcap});
23
                                                                          24
         step++) {
             for (auto& node : q) {
24
                                                                          26
               for (auto& edge : g[node]) {
                                                                                 void addFlow(Edge& e, ll f) {
                                                                          27
25
                 int ne = e[edge].to;
                                                                                   Edge& back = g[e.dest][e.back];
26
                                                                          28
                 if (!e[edge].remain || d[ne] <= step) continue;</pre>
                                                                                   if (!ec[e.dest] && f) hs[H[e.dest]].push_back(e.dest);
27
                                                                          29
                 d[ne] = step, nq.push_back(ne);
                                                                                   e.f += f;
                 if (ne == t) return true;
                                                                                   e.c -= f;
29
                                                                          31
                                                                                   ec[e.dest] += f:
             }
                                                                          33
                                                                                   back.f -= f;
31
                                                                                   back.c += f;
32
                                                                          34
           return false;
                                                                                   ec[back.dest] -= f;
33
                                                                          35
34
         };
                                                                          36
         function<int(int, int)> find = [&](int node, int limit) {
                                                                                 ll calc(int s, int t) {
           if (node == t || !limit) return limit;
36
                                                                                   int v = sz(g);
           int flow = 0;
                                                                                   H[s] = v;
37
                                                                          39
                                                                                   ec[t] = 1;
           for (int i = cur[node]; i < g[node].size(); i++) {</pre>
38
                                                                          40
             cur[node] = i;
                                                                                   vi co(2 * v);
39
             int edge = g[node][i], oe = edge ^ 1, ne = e[edge].to;
40
                                                                                   co[0] = v - 1;
             if (!e[edge].remain || d[ne] != d[node] + 1) continue;
                                                                                   rep(i, 0, v) cur[i] = g[i].data();
41
                                                                          43
             if (int temp = find(ne, min(limit - flow,
                                                                                   for (Edge& e : g[s]) addFlow(e, e.c);
42
                                                                          44
        e[edge].remain))) {
                                                                          45
               e[edge].remain -= temp, e[oe].remain += temp, flow
                                                                                   for (int hi = 0;;) {
43
                                                                          46
                                                                                     while (hs[hi].empty())
        += temp;
                                                                                       if (!hi--) return -ec[s];
             } else {
44
                                                                          48
                                                                                     int u = hs[hi].back();
45
               d[ne] = -1;
                                                                          49
46
                                                                          50
                                                                                     hs[hi].pop_back();
             if (flow == limit) break;
                                                                                     while (ec[u] > 0) // discharge u
47
                                                                          51
           7
                                                                                       if (cur[u] == g[u].data() + sz(g[u])) {
                                                                          52
                                                                                         H[u] = 1e9;
           return flow:
49
                                                                          53
                                                                                         for (Edge& e : g[u])
                                                                                           if (e.c && H[u] > H[e.dest] + 1) H[u] = H[e.dest]
         11 \text{ res} = 0:
51
                                                                          55
         while (bfs())
                                                                               \rightarrow + 1, cur[u] = &e;
52
53
           while (int flow = find(s, inf)) res += flow;
                                                                          56
                                                                                         if (++co[H[u]], !--co[hi] && hi < v)
                                                                                           rep(i, 0, v) if (hi < H[i] && H[i] < v)--
54
         return res;
                                                                          57
55
      }
                                                                               \hookrightarrow co[H[i]], H[i] = v + 1;
    };
                                                                                         hi = H[u];
56
                                                                          58
                                                                                       } else if (\operatorname{cur}[u] -> c \&\& H[u] == H[\operatorname{cur}[u] -> \operatorname{dest}] + 1)

    USAGE

                                                                                         addFlow(*cur[u], min(ec[u], cur[u]->c));
                                                                          60
                                                                          61
    int main() {
                                                                                          ++cur[u];
                                                                          62
       int n, m, s, t;
2
                                                                                   }
                                                                          63
       cin >> n >> m >> s >> t;
      Dinic dinic(n);
                                                                                 bool leftOfMinCut(int a) { return H[a] >= sz(g); }
                                                                          65
       for (int i = 0, u, v, c; i < m; i++) {
         cin >> u >> v >> c;
         dinic.add\_edge(u - 1, v - 1, c);
                                                                               Min-Cost Max-Flow
       cout << dinic.max_flow(s - 1, t - 1) << '\n';</pre>
                                                                               struct MinCostFlow {
                                                                                 static constexpr int INF = 1e9;
                                                                           2
                                                                                 const int n;
    PushRelabel Max-Flow (faster)
                                                                                 vector<tuple<int, int, int>> e;
                                                                                 vector<vector<int>> g;
                                                                                 vector<int> h, dis, pre;
     4 https://github.com/kth-competitive-programming/kactl/blob/main/contebado/gradaphk/Pussuftienttos:/.int t) {
    #define rep(i, a, b) for (int i = a; i < (b); ++i)
                                                                                   dis.assign(n, INF);
    \#define \ all(x) \ begin(x), \ end(x)
                                                                                   pre.assign(n, -1);
    \#define\ sz(x)\ (int)(x).size()
                                                                                   priority_queue<pair<int, int>, vector<pair<int, int>>,
                                                                          10
    typedef long long 11;
                                                                                   greater<>> que;
    typedef pair<int, int> pii;
                                                                                   dis[s] = 0;
                                                                          11
    typedef vector<int> vi;
                                                                                   que.emplace(0, s);
                                                                          12
                                                                                   while (!que.empty()) {
                                                                          13
```

#### auto [d, u] = que.top(); 14 que.pop(); 15 • Complexity: $O(n^3)$ (?) if (dis[u] != d) continue; 16 for (int i : g[u]) { 17 struct BlossomMatch { auto [v, f, c] = e[i]; int n; if (c > 0 && dis[v] > d + h[u] - h[v] + f) { 2 19 vector<vector<int>> e; dis[v] = d + h[u] - h[v] + f;20 pre[v] = i; 21 que.emplace(dis[v], v); 22 e[v].push\_back(u); } } } 24 25 26 return dis[t] != INF; 27 $MinCostFlow(int _n) : n(_n), g(n) {}$ 28 10 void addEdge(int u, int v, int f, int c) { 29 while (u != v) { 11 30 g[u].push\_back((int)e.size()); 12 31 e.emplace\_back(v, f, c); 13 g[v].push\_back((int)e.size()); 32 } 14 e.emplace\_back(u, -f, 0); 33 return u; 34 }; 16 pair<int, int> minCostMaxFlow(const int s, const int t) { 35 queue<int> que; 17 int flow = 0, cost = 0; 36 37 h.assign(n. 0): 19 while (dijkstra(s, t)) { 38 for (int i = 0; i < n; ++i) h[i] += dis[i]; 39 21 for (int i = t; i != s; i = get<0>(e[pre[i] ^ 1])) { 40 22 41 --get<2>(e[pre[i]]); } 23 ++get<2>(e[pre[i] ^ 1]); 24 }; } 43 ++flow; 44 $\hookrightarrow$ exist) 45 cost += h[t]; 26 46 27 47 return {flow, cost}; 28 } 48 29 }; 49 30 que.push(node); 31 32 Heavy-Light Decomposition 33 while (!que.empty()) { int u = que.front(); 34 int root = 0, cur = 0; que.pop(); vector<int> parent(n), deep(n), hson(n, -1), top(n), sz(n), 36 $\rightarrow$ dfn(n, -1); function<int(int, int, int)> dfs = [&](int node, int fa, int 38 → dep) { 39 deep[node] = dep, sz[node] = 1, parent[node] = fa; 40 for (auto &ne : g[node]) { 41 if (ne == fa) continue; sz[node] += dfs(ne, node, dep + 1); 42 if (hson[node] == -1|| sz[ne] > sz[hson[node]]) hson[node] } 43 44 return; } 9 45 return sz[node]; 10 }; 11 47 function<void(int, int)> dfs2 = [&](int node, int t) { 12 48 top[node] = t, dfn[node] = cur++; 49 if (hson[node] == -1) return; 14 50 dfs2(hson[node], t); 15 for (auto &ne : g[node]) { 16 52 if (ne == parent[node] || ne == hson[node]) continue; 17 } dfs2(ne, ne); 18 } 54 19 }: 55 56 // read in graph as vector<vector<int>> g(n)21 auto greedy = [&]() { 57 dfs(root, -1, 0), dfs2(root, root); 58

#### • USAGE: get LCA

```
function<int(int, int)> lca = [&](int x, int y) {
      while (top[x] != top[y]) {
2
        if (deep[top[x]] < deep[top[y]]) swap(x, y);</pre>
        x = parent[top[x]];
     return deep[x] < deep[y] ? x : y;</pre>
```

#### General Unweight Graph Matching

```
{\tt BlossomMatch(int \_n) : n(\_n), e(\_n) \{} \\
 void add_edge(int u, int v) { e[u].push_back(v),
 vector<int> find_matching() {
   vector < int > match(n, -1), vis(n), link(n), f(n), dep(n);
   function<int(int)> find = [&](int x) { return f[x] == x ?
\rightarrow x : (f[x] = find(f[x])); };
   auto lca = [&](int u, int v) {
     u = find(u), v = find(v);
       if (dep[u] < dep[v]) swap(u, v);</pre>
       u = find(link[match[u]]);
   auto blossom = [&](int u, int v, int p) {
     while (find(u) != p) {
       link[u] = v, v = match[u];
       if (vis[v] == 0) vis[v] = 1, que.push(v);
       f[u] = f[v] = p, u = link[v];
   // find an augmenting path starting from u and augment (if
   auto augment = [&](int node) {
     while (!que.empty()) que.pop();
     iota(f.begin(), f.end(), 0);
     // vis = 0 corresponds to inner vertices, vis = 1
fill(vis.begin(), vis.end(), -1);
     vis[node] = 1, dep[node] = 0;
       for (auto v : e[u]) {
         if (vis[v] == -1) {
           vis[v] = 0, link[v] = u, dep[v] = dep[u] + 1;
           // found an augmenting path
           if (match[v] == -1) {
            for (int x = v, y = u, temp; y != -1; x = temp,
  y = x == -1 ? -1 : link[x]) {
              temp = match[y], match[x] = y, match[y] = x;
           vis[match[v]] = 1, dep[match[v]] = dep[u] + 2;
           que.push(match[v]);
         } else if (vis[v] == 1 && find(v) != find(u)) {
           // found a blossom
           int p = lca(u, v);
           blossom(u, v, p), blossom(v, u, p);
   // find a maximal matching greedily (decrease constant)
     for (int u = 0; u < n; ++u) {
       if (match[u] != -1) continue;
       for (auto v : e[u]) {
         if (match[v] == -1) {
           match[u] = v, match[v] = u;
           break:
       }
     }
   greedy();
   for (int u = 0; u < n; ++u)
```

59

60

61

62

63

64

65

66 67

68

69

```
if (match[u] == -1) augment(u);
                                                                                  int ny = y \le n ? y + n : y - n;
70
                                                                         51
         return match;
                                                                                  g[nx].push_back(y);
71
                                                                         52
      }
72
                                                                         53
                                                                                  g[ny].push_back(x);
    };
73
                                                                         54
                                                                                int idx[2*n + 1];
                                                                         56
                                                                                scc(g, idx);
    Maximum Bipartite Matching
                                                                                for(int i = 1; i <= n; i++) {
                                                                         57
                                                                                  if(idx[i] == idx[i + n]) return {0, {}};
                                                                         58
       • Needs dinic, complexity \approx O(n + m\sqrt{n})
                                                                                  ans[i - 1] = idx[i + n] < idx[i];
                                                                         59
                                                                         60
    struct BipartiteMatch {
                                                                               return {1, ans};
                                                                         61
      int 1, r;
                                                                              }
      Dinic dinic = Dinic(0);
      dinic = Dinic(1 + r + 2);
                                                                              Enumerating Triangles
         for (int i = 1; i <= 1; i++) dinic.add_edge(0, i, 1);</pre>
         for (int i = 1; i <= r; i++) dinic.add_edge(1 + i, 1 + r +
                                                                                • Complexity: O(n + m\sqrt{m})
      }
                                                                              void enumerate_triangles(vector<pair<int,int>>& edges,
      void add_edge(int u, int v) { dinic.add_edge(u + 1, l + v +

    function < void(int,int,int) > f) {
     \hookrightarrow 1, 1); }
                                                                               int n = 0:
      ll max_matching() { return dinic.max_flow(0, 1 + r + 1); }
                                                                                for(auto [u, v] : edges) n = max({n, u + 1, v + 1});
10
                                                                                vector<int> deg(n);
                                                                                vector<int> g[n];
                                                                                for(auto [u, v] : edges) {
    2-SAT and Strongly Connected Components
                                                                                  deg[u]++;
                                                                                  deg[v]++;
    void scc(vector<vector<int>>& g, int* idx) {
                                                                                7
      int n = g.size(), ct = 0;
                                                                                for(auto [u, v] : edges) {
                                                                         10
       int out[n];
                                                                         11
                                                                                  if(u == v) continue;
      vector<int> ginv[n];
                                                                                  \label{eq:conditional_condition} \mbox{if}(\mbox{deg}[\mbox{$u$}] \ > \mbox{deg}[\mbox{$v$}] \ || \ (\mbox{deg}[\mbox{$u$}] \ == \mbox{deg}[\mbox{$v$}] \ \&\& \ u \ > \ v))
                                                                         12
      memset(out, -1, size of out);
                                                                                    swap(u, v);
                                                                         13
       memset(idx, -1, n * sizeof(int));
                                                                                  g[u].push_back(v);
                                                                         14
      function<void(int)> dfs = [&](int cur) {
                                                                         15
         out[cur] = INT_MAX;
                                                                                vector<int> flag(n);
                                                                         16
9
         for(int v : g[cur]) {
                                                                                for(int i = 0; i < n; i++) {</pre>
                                                                         17
           ginv[v].push_back(cur);
10
                                                                                  for(int v : g[i]) flag[v] = 1;
                                                                         18
           if(out[v] == -1) dfs(v);
                                                                                  for(int v : g[i]) for(int u : g[v]) {
                                                                         19
12
                                                                         20
                                                                                    if(flag[u]) f(i, v, u);
         ct++; out[cur] = ct;
13
                                                                         21
      };
14
                                                                                  for(int v : g[i]) flag[v] = 0;
                                                                         22
      vector<int> order;
15
                                                                                }
      for(int i = 0; i < n; i++) {
16
                                                                             }
                                                                         24
         order.push_back(i);
17
18
         if(out[i] == -1) dfs(i);
19
      }
                                                                              Tarjan
      sort(order.begin(), order.end(), [&](int& u, int& v) {
20
         return out[u] > out[v];
21
                                                                                • shrink all
                                                                                                 circles into points (2-edge-connected-
      }):
22
                                                                                   component)
      ct = 0;
      stack<int> s:
24
                                                                              int cnt = 0, now = 0;
      auto dfs2 = [&](int start) {
25
                                                                              vector<ll> dfn(n, -1), low(n), belong(n, -1), stk;
         s.push(start);
26
                                                                              function \langle void(11, 11) \rangle tarjan = [&](11 node, 11 fa) {
         while(!s.empty()) {
27
                                                                                dfn[node] = low[node] = now++, stk.push_back(node);
           int cur = s.top();
                                                                                for (auto& ne : g[node]) {
           s.pop();
29
                                                                                  if (ne == fa) continue;
30
           idx[cur] = ct;
                                                                                  if (dfn[ne] == -1) {
           for(int v : ginv[cur])
31
                                                                                    tarjan(ne, node);
             if(idx[v] == -1) s.push(v);
32
                                                                                    low[node] = min(low[node], low[ne]);
                                                                         9
        }
33
                                                                                  } else if (belong[ne] == -1) {
                                                                         10
      };
34
                                                                                    low[node] = min(low[node], dfn[ne]);
                                                                         11
      for(int v : order) {
35
                                                                                  }
                                                                         12
         if(idx[v] == -1) {
36
                                                                         13
                                                                                }
37
           dfs2(v):
                                                                                if (dfn[node] == low[node]) {
                                                                         14
38
                                                                                  while (true) {
                                                                         15
39
                                                                                    auto v = stk.back();
                                                                         16
      }
40
                                                                                    belong[v] = cnt;
    }
41
                                                                         18
                                                                                    stk.pop_back();
42
                                                                                    if (v == node) break;
                                                                         19
    // 0 => impossible, 1 => possible
43
                                                                         20
    pair<int, vector<int>> sat2(int n, vector<pair<int,int>>&
44
                                                                                  ++cnt;
                                                                         21
     }
      vector<int> ans(n):
45
                                                                             };
                                                                         23
```

int cnt = 0, now = 0;

vector<vector<ll>>> e1(n);

• 2-vertex-connected-component / Block forest

vector<vector<int>> g(2\*n + 1);

 $int nx = x \le n ? x + n : x - n;$ 

for(auto [x, y] : clauses) {

x = x < 0 ? -x + n : x;

y = y < 0 ? -y + n : y;

46

47

48

49

```
vector<ll> dfn(n, -1), low(n), stk;
    function<void(l1)> tarjan = [&](l1 node) {
      dfn[node] = low[node] = now++, stk.push_back(node);
      for (auto& ne : g[node]) {
         if (dfn[ne] == -1) {
          tarjan(ne);
           low[node] = min(low[node], low[ne]);
           if (low[ne] == dfn[node]) {
10
            e1.push_back({});
11
            while (true) {
              auto x = stk.back();
13
               stk.pop_back();
              e1[n + cnt].push_back(x);
15
               // e1[x].push back(n + cnt); // undirected
16
              if (x == ne) break;
18
19
            e1[node].push_back(n + cnt);
             // e1[n + cnt].push_back(node); // undirected
20
21
          7
22
        } else {
23
           low[node] = min(low[node], dfn[ne]);
24
25
26
      }
    };
27
```

#### Kruskal reconstruct tree

```
cin >> _n >> m; // _n: # of node, m: # of edge
    int n = 2 * _n - 1; // root: n-1
    vector<array<int, 3>> edges(m);
    for (auto& [w, u, v] : edges) {
       cin >> u >> v >> w, u--, v--;
8
    sort(edges.begin(), edges.end());
    vector<int> p(n);
    iota(p.begin(), p.end(), 0);
10
    function \langle int(int) \rangle find = [&] (int x) { return p[x] == x ? x :
     \leftrightarrow (p[x] = find(p[x])); \};
    auto merge = [&](int x, int y) { p[find(x)] = find(y); };
12
    vector<vector<int>> g(n);
13
    vector<int> val(m);
14
    val.reserve(n);
    for (auto [w, u, v] : edges) {
16
       u = find(u), v = find(v);
      if (u == v) continue;
18
       val.push_back(w);
19
       int node = (int)val.size() - 1;
20
       g[node].push_back(u), g[node].push_back(v);
21
      merge(u, node), merge(v, node);
22
```

#### Math

#### Inverse

• USAGE: get factorial

#### **Mod Class**

```
constexpr ll norm(ll x) { return (x % MOD + MOD) % MOD; }
    template <typename T>
    constexpr T power(T a, ll b, T res = 1) {
      for (; b; b /= 2, (a *= a) \%= MOD)
4
        if (b & 1) (res *= a) %= MOD;
      return res;
6
    }
    struct Z {
8
9
      11 x:
      constexpr Z(11 _x = 0) : x(norm(_x)) {}
10
      // auto operator<=>(const Z &) const = default; // cpp20
11
      Z operator-() const { return Z(norm(MOD - x)); }
12
13
      Z inv() const { return power(*this, MOD - 2); }
      Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
14

    *this; }

      Z \& perator += (const Z \& rhs) \{ return x = norm(x + rhs.x), \}

→ *this: }

      Z &operator-=(const Z &rhs) { return x = norm(x - rhs.x),

    *this: }

17
      Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
      Z &operator%=(const ll &rhs) { return x %= rhs, *this; }
18
      friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs;
19
     friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs;
20
      friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs;
21
     → }
     friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs;
     → }
      friend Z operator%(Z lhs, const ll &rhs) { return lhs %=

   rhs; }

     friend auto &operator>>(istream &i, Z &z) { return i >> z.x;
24
     friend auto &operator << (ostream &o, const Z &z) { return o
25
     };
26
```

• large mod (for NTT to do FFT in ll range without modulo)

```
using ll = long long;
    using i128 = __int128;
     constexpr i128 MOD = 9223372036737335297;
     constexpr i128 norm(i128 x) { return x < 0 ? (x + MOD) \% MOD :
     \rightarrow x % MOD; }
    template <typename T>
     constexpr T power(T a, i128 b, T res = 1) {
       for (; b; b /= 2, (a *= a) \%= MOD)
9
         if (b & 1) (res *= a) \%= MOD;
10
       return res;
    }
11
    struct Z {
^{12}
       i128 x:
13
       constexpr Z(i128 _x = 0) : x(norm(_x)) {}
       Z operator-() const { return Z(norm(MOD - x)); }
15
       Z inv() const { return power(*this, MOD - 2); }
       // auto operator<=>(const Z&) const = default;
      Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
18

    *this; }

     Z \text{ & operator} += (\text{const } Z \text{ & rhs}) \{ \text{ return } x = \text{norm}(x + \text{rhs.}x), \}
19

    *this; }

      Z &operator = (const Z &rhs) { return x = norm(x - rhs.x),
20

    *this; }

      Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
       Z &operator%=(const i128 &rhs) { return x %= rhs, *this; }
       friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs;
     → }
      friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs;
24
     → }
      friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs;
25
      friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs;
```

```
};
       • fastest mod class! be careful with overflow, only use
         when the time limit is tight
    constexpr int MOD = 998244353;
    constexpr int norm(int x) {
      if (x < 0) x += MOD;
4
      if (x >= MOD) x -= MOD;
6
      return x:
    template <typename T>
    constexpr T power(T a, int b, T res = 1) {
9
10
      for (; b; b /= 2, (a *= a) %= MOD)
        if (b & 1) (res *= a) \%= MOD;
11
      return res:
12
13
    }
    struct Z {
14
      constexpr Z(int _x = 0) : x(norm(_x)) {}
16
      // constexpr auto operator <=> (const Z &) const = default; //
17

→ cpp20 only

      constexpr Z operator-() const { return Z(norm(MOD - x)); }
18
      constexpr Z inv() const { return power(*this, MOD - 2); }
      constexpr Z &operator*=(const Z &rhs) { return x = 11(x) *
20

    rhs.x % MOD, *this; }

     constexpr Z &operator+=(const Z &rhs) { return x = norm(x +
21

    rhs.x), *this; }

     constexpr Z &operator-=(const Z &rhs) { return x = norm(x -

    rhs.x), *this; }

      constexpr Z &operator/=(const Z &rhs) { return *this *=
     → rhs.inv(): }
      constexpr Z &operator%=(const ll &rhs) { return x %= rhs,
24
     → *this; }
     constexpr friend Z operator*(Z lhs, const Z &rhs) { return
25
     → lhs *= rhs; }
      constexpr friend Z operator+(Z lhs, const Z &rhs) { return
26
     constexpr friend Z operator-(Z lhs, const Z &rhs) { return
     → lhs -= rhs; }
      constexpr friend Z operator/(Z lhs, const Z &rhs) { return
     → lhs /= rhs: }
      constexpr friend Z operator%(Z lhs, const ll &rhs) { return
     friend auto &operator>>(istream &i, Z &z) { return i >> z.x;
     friend auto &operator << (ostream &o, const Z &z) { return o
31
     \hookrightarrow << z.x; }
    };
32
```

friend Z operator%(Z lhs, const i128 &rhs) { return lhs %=

#### Cancer mod class

- Explanation: for some prime modulo p, maintains numbers of form p^x \* y, where y is a nonzero remainder
- Be careful with calling Cancer(x, y), it doesn't fix the input if y > p

```
struct Cancer {
      11 x; 11 y;
      Cancer() : Cancer(0, 1) {}
      Cancer(11 _y) {
         x = 0, y = _y;
         while(y \% MOD == 0) {
          y /= MOD;
           x++;
9
        }
      }
10
      Cancer(11 _x, 11 _y) : x(_x), y(_y) {}
11
      Cancer inv() { return Cancer(-x, power(y, MOD - 2)); }
12
      Cancer operator*(const Cancer &c) { return Cancer(x + c.x,
     \rightarrow (y * c.y) % MOD); }
```

```
Cancer operator*(11 m) {
   11 p = 0;
   while(m % MOD == 0) {
     m /= MOD;
   return Cancer(x + p, (m * y) % MOD);
 friend auto &operator << (ostream &o, Cancer c) { return o <<

    c.x << ' ' << c.y; }
</pre>
```

#### NTT, FFT, FWT

• ntt

14

15

16

17

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21

22

23

10

12

13

14

15

16

17

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21

22

23

24

9

```
void ntt(vector<Z>& a, int f) {
  int n = int(a.size());
  vector<Z> w(n);
  vector<int> rev(n);
  for (int i = 0; i < n; i++) rev[i] = (rev[i / 2] / 2) | ((i
 \hookrightarrow & 1) * (n / 2));
  for (int i = 0; i < n; i++) {
    if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
  Z wn = power(f ? (MOD + 1) / 3 : 3, (MOD - 1) / n);
  w[0] = 1;
  for (int i = 1; i < n; i++) w[i] = w[i - 1] * wn;
  for (int mid = 1; mid < n; mid *= 2) {</pre>
    for (int i = 0; i < n; i += 2 * mid) {
      for (int j = 0; j < mid; j++) {
        Z x = a[i + j], y = a[i + j + mid] * w[n / (2 * mid) *
        a[i + j] = x + y, a[i + j + mid] = x - y;
    }
  }
  if (f) {
    Z iv = power(Z(n), MOD - 2);
    for (auto& x : a) x *= iv;
}
```

• USAGE: Polynomial multiplication

```
vector<Z> mul(vector<Z> a, vector<Z> b) {
 int n = 1, m = (int)a.size() + (int)b.size() - 1;
  while (n < m) n *= 2;
  a.resize(n), b.resize(n);
 ntt(a, 0), ntt(b, 0);
 for (int i = 0; i < n; i++) a[i] *= b[i];
 ntt(a, 1);
 a.resize(m);
 return a:
```

• FFT (should prefer NTT, only use this when input is not integer)

```
const double PI = acos(-1);
    auto mul = [&](const vector<double>& aa, const vector<double>&
     → bb) {
      int n = (int)aa.size(), m = (int)bb.size(), bit = 1;
      while ((1 << bit) < n + m - 1) bit++;
      int len = 1 << bit;</pre>
      vector<complex<double>>> a(len), b(len);
      vector<int> rev(len);
      for (int i = 0; i < n; i++) a[i].real(aa[i]);</pre>
      for (int i = 0; i < m; i++) b[i].real(bb[i]);</pre>
9
      for (int i = 0; i < len; i++) rev[i] = (rev[i >> 1] >> 1) |
10
     \rightarrow ((i & 1) << (bit - 1));
      auto fft = [&](vector<complex<double>>& p, int inv) {
11
         for (int i = 0; i < len; i++)
12
           if (i < rev[i]) swap(p[i], p[rev[i]]);</pre>
13
         for (int mid = 1; mid < len; mid *= 2) {</pre>
           auto w1 = complex<double>(cos(PI / mid), (inv ? -1 : 1)

    * sin(PI / mid));
```

```
for (int i = 0; i < len; i += mid * 2) {
                                                                                for (int i = 0; i < n; i += 2 * mid) {
16
                                                                        43
             auto wk = complex<double>(1, 0);
                                                                                  for (int j = 0; j < mid; j++) {
17
                                                                        44
            for (int j = 0; j < mid; j++, wk = wk * w1) {
                                                                                    Z x = a[i + j], y = a[i + j + mid] * w[n / (2 * mid) *
                                                                        45
              auto x = p[i + j], y = wk * p[i + j + mid];
19
              p[i + j] = x + y, p[i + j + mid] = x - y;
                                                                                    a[i + j] = x + y, a[i + j + mid] = x - y;
                                                                                  7
21
                                                                        47
                                                                                }
22
                                                                        48
        }
                                                                              }
23
                                                                        49
         if (inv == 1) {
                                                                              if (f) {
24
                                                                        50
           for (int i = 0; i < len; i++) p[i].real(p[i].real() /
                                                                                Z iv = power(Z(n), MOD - 2);
        len):
                                                                                for (int i = 0; i < n; i++) a[i] *= iv;
                                                                        52
26
                                                                        53
                                                                            }
27
      }:
                                                                        54
      fft(a, 0), fft(b, 0);
28
                                                                        55
      for (int i = 0; i < len; i++) a[i] = a[i] * b[i];
                                                                            struct Poly {
      fft(a, 1):
                                                                              vector<Z> a:
30
                                                                        57
31
      a.resize(n + m - 1);
                                                                              Poly() {}
      vector<double> res(n + m - 1);
                                                                              Poly(const vector<Z> &_a) : a(_a) {}
32
                                                                        59
      for (int i = 0; i < n + m - 1; i++) res[i] = a[i].real();
                                                                               int size() const { return (int)a.size(); }
33
                                                                               void resize(int n) { a.resize(n); }
34
                                                                        61
    }:
                                                                               Z operator[](int idx) const {
35
                                                                        62
                                                                                 if (idx < 0 || idx >= size()) return 0;
                                                                        63
                                                                                return a[idx];
                                                                        64
    Polynomial Class
                                                                              Z &operator[](int idx) { return a[idx]; }
                                                                        66
    using ll = long long;
                                                                        67
                                                                               Poly mulxk(int k) const {
    constexpr 11 MOD = 998244353;
                                                                                 auto b = a;
                                                                        69
                                                                                b.insert(b.begin(), k, 0);
    11 norm(11 x) { return (x % MOD + MOD) % MOD; }
                                                                                 return Poly(b);
    template <class T>
                                                                        71
    T power(T a, ll b, T res = 1) {
                                                                              Poly modxk(int k) const { return Poly(vector<Z>(a.begin(),
                                                                        72
       for (; b; b /= 2, (a *= a) %= MOD)
                                                                             \rightarrow a.begin() + min(k, size()))); }
         if (b & 1) (res *= a) \%= MOD;
                                                                              Poly divxk(int k) const {
                                                                        73
      return res;
                                                                        74
                                                                                 if (size() <= k) return Poly();</pre>
10
                                                                                return Poly(vector<Z>(a.begin() + k, a.end()));
                                                                        75
11
                                                                        76
    struct Z {
12
                                                                              friend Poly operator+(const Poly &a, const Poly &b) {
                                                                        77
                                                                        78
                                                                                 vector<Z> res(max(a.size(), b.size()));
      Z(11 _x = 0) : x(norm(_x)) {}
14
                                                                                 for (int i = 0; i < (int)res.size(); i++) res[i] = a[i] +
       // auto operator<=>(const Z &) const = default;
15
                                                                             ⇔ b[i]:
      Z operator-() const { return Z(norm(MOD - x)); }
                                                                                return Poly(res);
                                                                        80
      Z inv() const { return power(*this, MOD - 2); }
17
                                                                        81
      Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
                                                                              friend Poly operator-(const Poly &a, const Poly &b) {
                                                                        82

    *this: }

                                                                                 vector<Z> res(max(a.size(), b.size()));
      Z &operator+=(const Z &rhs) { return x = norm(x + rhs.x),
19
                                                                                 for (int i = 0; i < (int)res.size(); i++) res[i] = a[i] -
                                                                        84
     → *this; }
                                                                                b[i];
      Z \& operator = (const Z \& rhs) \{ return x = norm(x - rhs.x), \}
20
                                                                                return Poly(res);
                                                                        85
                                                                              }
                                                                        86
      Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
21
                                                                        87
                                                                              friend Poly operator*(Poly a, Poly b) {
      Z &operator%=(const ll &rhs) { return x %= rhs, *this; }
                                                                                 if (a.size() == 0 || b.size() == 0) return Poly();
                                                                        88
      friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs;
                                                                                 int n = 1, m = (int)a.size() + (int)b.size() - 1;
                                                                                 while (n < m) n *= 2;
      friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs;
                                                                                 a.resize(n), b.resize(n);
     → }
                                                                                ntt(a.a, 0), ntt(b.a, 0);
                                                                        92
      friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs;
                                                                                 for (int i = 0; i < n; i++) a[i] *= b[i];
                                                                        93
     → }
                                                                                ntt(a.a, 1);
                                                                        94
      friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs;
                                                                                a.resize(m);
                                                                        95
      friend Z operator%(Z lhs, const ll &rhs) { return lhs %=
                                                                        97
                                                                        98
                                                                               friend Poly operator*(Z a, Poly b) {
      friend auto &operator>>(istream &i, Z &z) { return i >> z.x;
28
                                                                                for (int i = 0; i < (int)b.size(); i++) b[i] *= a;
                                                                        99
                                                                       100
                                                                                return b;
      friend auto &operator << (ostream &o, const Z &z) { return o
29
                                                                       101
                                                                              friend Poly operator*(Poly a, Z b) {
                                                                       102
30
    }:
                                                                                 for (int i = 0; i < (int)a.size(); i++) a[i] *= b;
                                                                       103
31
                                                                       104
                                                                                return a:
    void ntt(vector<Z> &a, int f) {
32
                                                                       105
      int n = (int)a.size();
33
                                                                              Poly & operator += (Poly b) { return (*this) = (*this) + b; }
                                                                       106
      vector<Z> w(n);
34
                                                                              Poly &operator = (Poly b) { return (*this) = (*this) - b; }
                                                                       107
      vector<int> rev(n);
35
                                                                               Poly &operator *= (Poly b) { return (*this) = (*this) * b; }
      for (int i = 0; i < n; i++) rev[i] = (rev[i / 2] / 2) | ((i
36
                                                                       109
                                                                               Polv deriv() const {
     \leftrightarrow & 1) * (n / 2));
                                                                                 if (a.empty()) return Poly();
                                                                       110
      for (int i = 0; i < n; i++)
37
                                                                                 vector<Z> res(size() - 1);
                                                                       111
        if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
38
                                                                       112
                                                                                for (int i = 0; i < size() - 1; ++i) res[i] = (i + 1) *
      Z wn = power(f ? (MOD + 1) / 3 : 3, (MOD - 1) / n);
39
                                                                                a[i + 1];
      w[0] = 1;
40
                                                                                return Poly(res);
                                                                       113
      for (int i = 1; i < n; i++) w[i] = w[i - 1] * wn;
41
                                                                       114
      for (int mid = 1; mid < n; mid *= 2) {
```

```
Poly integr() const {
                                                                                   };
115
                                                                         187
         vector<Z> res(size() + 1);
                                                                                   build(1, 0, n);
116
                                                                         188
         for (int i = 0; i < size(); ++i) res[i + 1] = a[i] / (i +
                                                                                   auto work = [&] (auto self, int p, int l, int r, const Poly
117
                                                                                   &num) -> void {
         return Poly(res);
                                                                                    if (r - 1 == 1) {
118
                                                                                      if (1 < int(ans.size())) ans[1] = num[0];</pre>
       }
119
                                                                         191
120
       Poly inv(int m) const {
                                                                         192
                                                                                     } else {
                                                                                       int m = (1 + r) / 2;
121
         Poly x({a[0].inv()});
                                                                         193
         int k = 1;
                                                                                       self(self, 2 * p, 1, m, num.mulT(q[2 * p + 1]).modxk(m)
122
                                                                         194
123
         while (k < m) {
           k *= 2:
                                                                                       self(self, 2 * p + 1, m, r, num.mulT(q[2 * p]).modxk(r)
124
                                                                         195
            x = (x * (Poly({2}) - modxk(k) * x)).modxk(k);
125
                                                                                    m));
126
                                                                         196
                                                                                    }
                                                                                   };
         return x.modxk(m);
127
                                                                         197
                                                                                   work(work, 1, 0, n, mulT(q[1].inv(n)));
128
                                                                         198
       Poly log(int m) const { return (deriv() *
                                                                                   return ans:
129
                                                                         199
         inv(m)).integr().modxk(m); }
                                                                         200
130
       Poly exp(int m) const {
                                                                         201
                                                                              };
         Poly x(\{1\});
131
         int k = 1;
132
         while (k < m) {
133
                                                                               Sieve
           k *= 2;
134
             = (x * (Poly({1}) - x.log(k) + modxk(k))).modxk(k);
135

    linear sieve

136
137
         return x.modxk(m);
                                                                              vector<int> min_primes(MAX_N), primes;
138
                                                                              primes.reserve(1e5);
       Poly pow(int k, int m) const {
139
                                                                              for (int i = 2; i < MAX_N; i++) {
140
         int i = 0;
                                                                                if (!min_primes[i]) min_primes[i] = i, primes.push_back(i);
         while (i < size() && a[i].x == 0) i++;
                                                                                 for (auto& p : primes) {
         if (i == size() || 1LL * i * k >= m) {
142
                                                                                   if (p * i >= MAX_N) break;
           return Poly(vector<Z>(m));
143
                                                                                   min_primes[p * i] = p;
144
                                                                                   if (i % p == 0) break;
         Z v = a[i];
145
                                                                          9
146
         auto f = divxk(i) * v.inv();
                                                                              }
         return (f.log(m - i * k) * k).exp(m - i * k).mulxk(i * k)
147
         * power(v, k);
                                                                                 • mobius function
148
       }
       Poly sqrt(int m) const {
149
         Poly x(\{1\});
                                                                              vector<int> min_p(MAX_N), mu(MAX_N), primes;
         int k = 1:
151
                                                                              mu[1] = 1, primes.reserve(1e5);
         while (k < m) {
152
                                                                              for (int i = 2; I < MAX_N; i++) {</pre>
           k *= 2:
153
                                                                                 if (\min_p[i] == 0) {
           x = (x + (modxk(k) * x.inv(k)).modxk(k)) * ((MOD + 1) /
                                                                                  min_p[i] = i;
154
         2);
                                                                                  primes.push_back(i);
         }
155
                                                                                   mu[i] = -1;
156
         return x.modxk(m);
157
                                                                                for (auto p : primes) {
       Poly mulT(Poly b) const {
                                                                                   if (i * p >= MAX_N) break;
158
                                                                          10
159
         if (b.size() == 0) return Poly();
                                                                          11
                                                                                   min_p[i * p] = p;
         int n = b.size();
160
                                                                         12
                                                                                   if (i % p == 0) {
161
         reverse(b.a.begin(), b.a.end());
                                                                                     mu[i * p] = 0;
                                                                         13
         return ((*this) * b).divxk(n - 1);
162
                                                                                     break;
                                                                         14
163
                                                                         15
       Poly divmod(Poly b) const {
164
                                                                                   mu[i * p] = -mu[i];
                                                                         16
165
         auto n = size(), m = b.size();
                                                                                }
                                                                         17
         auto t = *this;
                                                                              }
166
                                                                         18
         reverse(t.a.begin(), t.a.end());
167
         reverse(b.a.begin(), b.a.end());
168
                                                                                 • Euler's totient function
         Poly res = (t * b.inv(n)).modxk(n - m + 1);
169
170
         reverse(res.a.begin(), res.a.end());
                                                                              vector<int> min_p(MAX_N), phi(MAX_N), primes;
171
         return res;
                                                                              phi[1] = 1, primes.reserve(1e5);
172
                                                                              for (int i = 2; i < MAX_N; i++) {
       vector<Z> eval(vector<Z> x) const {
173
                                                                                if (min_p[i] == 0) {
         if (size() == 0) return vector<Z>(x.size(), 0);
174
                                                                                   min_p[i] = i;
         const int n = max(int(x.size()), size());
175
                                                                                   primes.push_back(i);
         vector<Poly> q(4 * n);
176
                                                                                  phi[i] = i - 1;
177
         vector<Z> ans(x.size());
178
         x.resize(n);
                                                                                for (auto p : primes) {
         function<void(int, int, int)> build = [&](int p, int 1,
179
                                                                                  if (i * p >= MAX_N) break;
                                                                          10
         int r) {
                                                                                   min_p[i * p] = p;
                                                                          11
           if (r - 1 == 1) {
180
                                                                                   if (i % p == 0) {
             q[p] = Poly(\{1, -x[1]\});
181
                                                                                     phi[i * p] = phi[i] * p;
                                                                          13
            } else {
182
                                                                          14
             int m = (1 + r) / 2;
183
                                                                         15
             build(2 * p, 1, m), build(2 * p + 1, m, r);
184
                                                                                   phi[i * p] = phi[i] * phi[p];
                                                                         16
             q[p] = q[2 * p] * q[2 * p + 1];
185
                                                                         17
186
                                                                         18
```

#### Gaussian Elimination

```
bool is_0(Z v) { return v.x == 0; }
    Z abs(Z v) { return v; }
    bool is_0(double v) { return abs(v) < 1e-9; }</pre>
    // 1 => unique solution, 0 => no solution, -1 => multiple

→ solutions

    template <typename T>
6
     int gaussian_elimination(vector<vector<T>> &a, int limit) {
         if (a.empty() || a[0].empty()) return -1;
       int h = (int)a.size(), w = (int)a[0].size(), r = 0;
      for (int c = 0; c < limit; c++) {
10
         int id = -1;
11
         for (int i = r; i < h; i++) {
12
          if (!is_0(a[i][c]) \&\& (id == -1 || abs(a[id][c]) <
13
         abs(a[i][c]))) {
14
            id = i:
15
        }
16
         if (id == -1) continue;
17
         if (id > r) {
           swap(a[r], a[id]);
19
20
           for (int j = c; j < w; j++) a[id][j] = -a[id][j];
21
         vector<int> nonzero;
22
         for (int j = c; j < w; j++) {
23
           if (!is_0(a[r][j])) nonzero.push_back(j);
24
25
        T inv_a = 1 / a[r][c];
26
         for (int i = r + 1; i < h; i++) {
27
           if (is_0(a[i][c])) continue;
28
29
           T coeff = -a[i][c] * inv_a;
           for (int j : nonzero) a[i][j] += coeff * a[r][j];
30
        }
31
32
      }
33
34
      for (int row = h - 1; row >= 0; row--) {
35
         for (int c = 0; c < limit; c++) {
           if (!is_0(a[row][c])) {
36
37
             T inv_a = 1 / a[row][c];
             for (int i = row - 1; i >= 0; i--) {
38
               if (is_0(a[i][c])) continue;
39
40
               T coeff = -a[i][c] * inv_a;
               for (int j = c; j < w; j++) a[i][j] += coeff *
41
        a[row][j];
42
             }
43
             break;
          }
44
45
46
      } // not-free variables: only it on its line
      for(int i = r; i < h; i++) if(!is_0(a[i][limit])) return 0;</pre>
47
      return (r == limit) ? 1 : -1;
48
49
50
51
    template <typename T>
    pair<int, vector<T>> solve_linear(vector<vector<T>> a, const
52
     \rightarrow vector<T> &b, int w) {
      int h = (int)a.size();
53
      for (int i = 0; i < h; i++) a[i].push_back(b[i]);</pre>
54
      int sol = gaussian_elimination(a, w);
55
56
      if(!sol) return {0, vector<T>()};
57
      vector<T> x(w, 0);
      for (int i = 0; i < h; i++) {
58
         for (int j = 0; j < w; j++) {
           if (!is_0(a[i][j])) {
60
61
             x[j] = a[i][w] / a[i][j];
62
             break;
63
        }
64
      }
65
66
      return {sol, x};
67
```

#### is prime

• (Miller–Rabin primality test)

```
i128 power(i128 a, i128 b, i128 MOD = 1, i128 res = 1) {
      for (; b; b /= 2, (a *= a) %= MOD)
2
        if (b & 1) (res *= a) %= MOD;
      return res;
    bool is_prime(ll n) {
      if (n < 2) return false;
      static constexpr int A[] = \{2, 3, 5, 7, 11, 13, 17, 19, 23\};
      int s = __builtin_ctzll(n - 1);
      11 d = (n - 1) >> s;
11
12
      for (auto a : A) {
        if (a == n) return true;
13
         11 x = (11)power(a, d, n);
14
         if (x == 1 | | x == n - 1) continue;
         bool ok = false;
16
         for (int i = 0; i < s - 1; ++i) {
          x = 11((i128)x * x % n); // potential overflow!
18
           if (x == n - 1) {
19
             ok = true;
20
21
             break;
22
23
         if (!ok) return false;
      }
25
      return true;
26
27
    ll pollard_rho(ll x) {
      11 s = 0, t = 0, c = rng() \% (x - 1) + 1;
2
      ll stp = 0, goal = 1, val = 1;
3
      for (goal = 1;; goal *= 2, s = t, val = 1) {
        for (stp = 1; stp <= goal; ++stp) {</pre>
          t = 11(((i128)t * t + c) \% x);
           val = 11((i128)val * abs(t - s) % x);
           if ((stp \% 127) == 0) {
             11 d = gcd(val, x);
             if (d > 1) return d;
10
11
           }
        }
12
         11 d = gcd(val, x);
13
         if (d > 1) return d;
14
      }
15
    }
16
17
    11 get_max_factor(ll _x) {
18
      11 max_factor = 0;
19
      function \langle void(11) \rangle fac = [\&](11 x) \{
20
         if (x <= max_factor || x < 2) return;</pre>
22
         if (is_prime(x)) {
           max_factor = max_factor > x ? max_factor : x;
23
           return;
25
         11 p = x;
         while (p >= x) p = pollard_rho(x);
27
         while ((x \% p) == 0) x /= p;
28
29
         fac(x), fac(p);
      }:
30
      fac(_x);
31
32
      return max_factor;
    Radix Sort
    struct identity {
         template<typename T>
2
3
         T operator()(const T &x) const {
4
             return x:
```

```
if (int64_t(data.size()) * (64 -
         __builtin_clzll(data.size())) < 2 * (1 << bits_per_pass)) {
             stable_sort(data.begin(), data.end(), [&](const T &a,
12
         const T &b) {
                 return extract_key(a) < extract_key(b);</pre>
13
             });
14
             return:
15
16
         using T_key = decltype(extract_key(data.front()));
18
         T_key minimum = numeric_limits<T_key>::max();
19
20
         for (T &x : data)
21
             minimum = min(minimum, extract_key(x));
23
         int max_bits = 0;
25
         for (T &x : data) {
26
27
             T_key key = extract_key(x);
             max_bits = max(max_bits, key == minimum ? 0 : 64 -
28
         __builtin_clzll(key - minimum));
29
30
         int passes = max((max_bits + bits_per_pass / 2) /
31
        bits_per_pass, 1);
32
         if (64 - __builtin_clzll(data.size()) <= 1.5 * passes) {</pre>
33
             stable_sort(data.begin(), data.end(), [&](const T &a,
         const T &b) {
                  return extract_key(a) < extract_key(b);</pre>
35
36
             });
             return;
37
         }
39
         vector<T> buffer(data.size());
40
         vector<int> counts:
41
         int bits_so_far = 0;
42
43
         for (int p = 0; p < passes; p++) {
44
             int bits = (max_bits + p) / passes;
             counts.assign(1 << bits, 0);</pre>
46
47
             for (T &x : data) {
48
                  T_key key = T_key(extract_key(x) - minimum);
49
                  counts[(key >> bits_so_far) & ((1 << bits) -</pre>
        1)]++;
51
52
             int count_sum = 0;
53
             for (int &count : counts) {
55
                  int current = count;
57
                  count = count_sum;
58
                  count_sum += current;
             }
60
             for (T &x : data) {
                 T_key key = T_key(extract_key(x) - minimum);
62
                  int key_section = int((key >> bits_so_far) & ((1
63
         << bits) - 1));
                 buffer[counts[key_section]++] = x;
64
             }
65
66
             swap(data, buffer);
67
             bits_so_far += bits;
68
         }
69
70
    }

    USAGE

    radix_sort(edges, 10, [&](const edge &e) -> int { return
     \rightarrow abs(e.weight - x); });
```

#### String

#### AC Automaton

```
struct AC_automaton {
      int sz = 26:
      vector<vector<int>> e = {vector<int>(sz)}; // vector is
     vector<int> fail = {0};
      vector<int> end = {0};
      void insert(string& s) {
        int p = 0;
        for (auto c : s) {
          c -= 'a';
10
          if (!e[p][c]) {
12
            e.emplace_back(sz);
13
            fail.emplace_back();
            end.emplace_back();
14
            e[p][c] = e.size() - 1;
          p = e[p][c];
17
18
        end[p] += 1;
19
20
21
      void build() {
22
        for (int i = 0; i < sz; i++)
24
          if (e[0][i]) q.push(e[0][i]);
        while (!q.empty()) {
          int p = q.front();
27
          q.pop();
          for (int i = 0; i < sz; i++) {
29
            if (e[p][i]) {
30
31
              fail[e[p][i]] = e[fail[p]][i];
              q.push(e[p][i]);
32
33
            } else {
              e[p][i] = e[fail[p]][i];
34
36
37
38
      }
    };
39
```

#### KMP

• nex[i]: length of longest common prefix & suffix for pat[0..i]

```
vector<int> get_next(vector<int> &pat) {
   int m = (int)pat.size();
   vector<int> nex(m);
   for (int i = 1, j = 0; i < m; i++) {
      while (j && pat[j] != pat[i]) j = nex[j - 1];
      if (pat[j] == pat[i]) j++;
      nex[i] = j;
   }
   return nex;
}</pre>
```

• kmp match for txt and pat

9

10

#### Z function

9

```
• z[i]: length of longest common prefix of s and s[i:]
vector<int> z_function(string s) {
  int n = (int)s.size();
  vector<int> z(n);
  for (int i = 1, 1 = 0, r = 0; i < n; ++i) {
    if (i <= r) z[i] = min(r - i + 1, z[i - 1]);
    while (i + z[i] < n && s[z[i]] == s[i + z[i]]) ++z[i];
    if (i + z[i] - 1 > r) 1 = i, r = i + z[i] - 1;
  }
  return z;
```

#### General Suffix Automaton

```
constexpr int SZ = 26;
2
    struct GSAM {
     vector<vector<int>>> e = {vector<int>(SZ)}; // the labeled
     \hookrightarrow edges from node i
      vector<int> parent = {-1};
                                                   // the parent of
      vector<int> length = {0};
                                                   // the length of
     GSAM(int n) { e.reserve(2 * n), parent.reserve(2 * n),

    length.reserve(2 * n); };

      int extend(int c, int p) { // character, last
        bool f = true;
                                  // if already exist
10
        int r = 0;
                                  // potential new node
                                  // only extend when not exist
        if (!e[p][c]) {
12
          f = false;
          e.push_back(vector<int>(SZ));
14
          parent.push_back(0);
15
          length.push_back(length[p] + 1);
          r = (int)e.size() - 1;
17
          for (; ~p && !e[p][c]; p = parent[p]) e[p][c] = r; //
18
        update\ parents
        }
19
        if (f || ~p) {
20
          int q = e[p][c];
21
          if (length[q] == length[p] + 1) {
            if (f) return q;
23
            parent[r] = q;
          } else {
25
            e.push_back(e[q]);
26
            parent.push_back(parent[q]);
27
            length.push_back(length[p] + 1);
28
            int qq = parent[q] = (int)e.size() - 1;
            for (; ~p && e[p][c] == q; p = parent[p]) e[p][c] =
30
            if (f) return qq;
31
            parent[r] = qq;
32
        }
34
35
        return r:
      }
36
    };
37
       • Topo sort on GSAM
    11 sz = gsam.e.size();
    vector<int> c(sz + 1);
    vector<int> order(sz);
   for (int i = 1; i < sz; i++) c[gsam.length[i]]++;
    for (int i = 1; i < sz; i++) c[i] += c[i - 1];
    for (int i = 1; i < sz; i++) order[c[gsam.length[i]]--] = i;</pre>
    reverse(order.begin(), order.end()); // reverse so that large
```

• can be used as an ordinary SAM

• USAGE (the number of distinct substring)

```
int main() {
   int n, last = 0;
   string s;
```

```
cin >> n;
4
       auto a = GSAM();
       for (int i = 0; i < n; i++) {
         cin >> s;
         last = 0; // reset last
         for (auto&& c : s) last = a.extend(c, last);
10
       11 \text{ ans} = 0:
11
       for (int i = 1; i < a.e.size(); i++) {</pre>
12
         ans += a.length[i] - a.length[a.parent[i]];
14
       cout << ans << endl;</pre>
15
16
       return 0:
17
```

#### Manacher

```
string longest_palindrome(string& s) {
  // init "abc" -> "^$a#b#c$'
  vector<char> t{'^', '#'};
 for (char c : s) t.push_back(c), t.push_back('#');
  t.push_back('$');
  // manacher
  int n = t.size(), r = 0, c = 0;
  vector<int> p(n, 0);
  for (int i = 1; i < n - 1; i++) {
    if (i < r + c) p[i] = min(p[2 * c - i], r + c - i);
    while (t[i + p[i] + 1] == t[i - p[i] - 1]) p[i]++;
    if (i + p[i] > r + c) r = p[i], c = i;
  }
    // s[i] \rightarrow p[2 * i + 2] (even), p[2 * i + 2] (odd)
  // output answer
  int index = 0;
  for (int i = 0; i < n; i++)
    if (p[index] < p[i]) index = i;</pre>
  return s.substr((index - p[index]) / 2, p[index]);
```

#### Lyndon

10

11

12

14

16

17

18

19

10

11

12

13 14

15

16

17

18

19

• def: suf(s) > svoid duval(const string &s) { int n = (int)s.size(); for (int i = 0; i < n;) { int j = i, k = i + 1; for (;  $j < n \&\& s[j] \le s[k]$ ; j++, k++) if (s[j] < s[k]) j = i - 1;while (i <= j) { // cout << s.substr(i, k - j) << '\n'; i += k - j; } } int main() { string s; cin >> s: duval(s);