# Fortcoders Code Library

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## Intro Main template #include <bits/stdc++.h> using namespace std; 1 #define FOR(x,n) for (int x=0; x< n; x++)#define form(i, n) for (int i = 0; i < int(n); i++) **Data Structures** #define all(v) v.begin(), v.end() using ll = long long; using ld = long double; using pii = pair<int, int>; const char nl = '\n'; <sup>1</sup>4 int main() { 14 cin.tie(nullptr)->sync\_with\_stdio(false); 14 cout << fixed << setprecision(20);</pre> rng(chrono::steady\_clock::now().time\_since\_epoch().count()); 6 Fast IO namespace io { Geometry 7 constexpr int SIZE = 1 << 16;</pre> char buf[SIZE], \*head, \*tail; 7 char get\_char() { if (head == tail) tail = (head = buf) + fread(buf, 1, SIZE, stdin): return \*head++; 11 read() { 10 11 x = 0, f = 1;Miscellaneous char c = get\_char(); for (; !isdigit(c); c = get\_char()) (c == '-') && (f = -1); 11 for (; isdigit(c); $c = get_char()) x = x * 10 + c - '0'$ ; **Graph Theory** 11 return x \* f; 11 PushRelabel Max-Flow (faster) . . . . . . . . . . . . . . . . string read\_s() { string str; char c = get\_char(); while (c == ' ' | | c == '\n' | | c == '\r') c = get\_char(); while (c != ' ' && c != '\n' && c != '\r') str += c, c = Maximum Bipartite Matching . . . . . . . . . . . . . . . get\_char(); 2-SAT and Strongly Connected Components . . . . . . return str; void print(int x) { if (x > 9) print(x / 10); 14 putchar(x % 10 | '0'); 25 void println(int x) { print(x), putchar('\n'); } Math **1**5 struct Read { **†**5 Read& operator>>(ll& x) { return x = read(), \*this; } Read& operator>>(long double& x) { return x = stold(read\_s()), \*this; } } in; } // namespace io Pragmas (lol) #pragma GCC optimize(2) #pragma GCC optimize(3) String #pragma GCC optimize("Ofast") #pragma GCC optimize("inline") #pragma GCC optimize("-fgcse") KMP....... 20 #pragma GCC optimize("-fgcse-lm") 20 #pragma GCC optimize("-fipa-sra") 20#pragma GCC optimize("-ftree-pre") #pragma GCC optimize("-ftree-vrp") #pragma GCC optimize("-fpeephole2") #pragma GCC optimize("-ffast-math") #pragma GCC optimize("-fsched-spec") 12 #pragma GCC optimize("unroll-loops") 13 #pragma GCC optimize("-falign-jumps") #pragma GCC optimize("-falign-loops")

Intro

Contents

1

```
#pragma GCC optimize("-falign-labels")
                                                                        33
                                                                               }
     #pragma GCC optimize("-fdevirtualize")
                                                                             };
17
                                                                        34
     #pragma GCC optimize("-fcaller-saves")
18
     \#pragma\ GCC\ optimize("-fcrossjumping")
                                                                                • Persistent implicit, range query + point update
19
     #pragma GCC optimize("-fthread-jumps")
#pragma GCC optimize("-funroll-loops")
20
                                                                             struct Node {
21
                                                                               int lc = 0, rc = 0, p = 0;
     #pragma GCC optimize("-fwhole-program")
                                                                         2
22
                                                                         3
     {\it \#pragma~GCC~optimize("-freorder-blocks")}
     #pragma GCC optimize("-fschedule-insns")
24
                                                                             struct SegTree {
     #pragma GCC optimize("inline-functions")
                                                                         5
25
                                                                               vector<Node> t = {{}}; // init all
     #pragma GCC optimize("-ftree-tail-merge")
     #pragma GCC optimize("-fschedule-insns2")
                                                                               SegTree() = default;
27
                                                                               SegTree(int n) { t.reserve(n * 20); }
     #pragma GCC optimize("-fstrict-aliasing")
                                                                               int modify(int p, int 1, int r, int x, int v) {
                                                                         9
     \textit{\#pragma GCC optimize("-fstrict-overflow")}
29
                                                                                 // p: original node, update a[x] \rightarrow v
                                                                        10
     #pragma GCC optimize("-falign-functions")
#pragma GCC optimize("-fcse-skip-blocks")
                                                                        11
                                                                                 t.push_back(t[p]);
31
     #pragma GCC optimize("-fcse-follow-jumps")
                                                                        12
                                                                                  int u = (int)t.size() - 1;
32
                                                                                  if (r - 1 == 1) {
     #pragma GCC optimize("-fsched-interblock")
                                                                        13
33
                                                                                   t[u].p = v;
                                                                        14
     #pragma GCC optimize("-fpartial-inlining")
34
                                                                                 } else {
                                                                        15
     #pragma GCC optimize("no-stack-protector")
                                                                                   int m = (1 + r) / 2;
     #pragma GCC optimize("-freorder-functions")
                                                                        16
36
                                                                        17
                                                                                    if (x < m) {
     #pragma GCC optimize("-findirect-inlining")
37
     #pragma GCC optimize("-fhoist-adjacent-loads")
                                                                        18
                                                                                     t[u].lc = modify(t[p].lc, l, m, x, v);
38
                                                                                      t[u].rc = t[p].rc;
                                                                        19
     #pragma GCC optimize("-frerun-cse-after-loop")
39
                                                                                   } else {
     {\it \#pragma~GCC~optimize("inline-small-functions")}
                                                                                      t[u].lc = t[p].lc;
     #pragma GCC optimize("-finline-small-functions")
                                                                        21
41
     #pragma GCC optimize("-ftree-switch-conversion")
                                                                        22
                                                                                      t[u].rc = modify(t[p].rc, m, r, x, v);
                                                                        23
     \textit{\#pragma GCC optimize("-foptimize-sibling-calls")}
43
                                                                                   t[u].p = t[t[u].lc].p + t[t[u].rc].p;
     #pragma GCC optimize("-fexpensive-optimizations")
44
                                                                                 }
     #pragma GCC optimize("-funsafe-loop-optimizations")
    #pragma GCC optimize("inline-functions-called-once")
                                                                        26
                                                                                 return u;
46
     \textit{\#pragma GCC optimize("-fdelete-null-pointer-checks")}
                                                                               int query(int p, int l, int r, int x, int y) {
                                                                        28
    #pragma GCC
     \leftrightarrow target("sse, sse2, sse3, sse3, sse4.1, sse4.2, avx, avx2, popent, t_{a}^{2}he=native")query sum a[x] \dots a[y-1] rooted at p
                                                                                  // t[p] holds the info of [l, r)
                                                                                  if (x \le 1 \&\& r \le y) return t[p].p;
                                                                         31
                                                                                  int m = (1 + r) / 2, res = 0;
     Data Structures
                                                                                  if (x < m) res += query(t[p].lc, l, m, x, y);
                                                                        33
                                                                                  if (y > m) res += query(t[p].rc, m, r, x, y);
                                                                        34
     Segment Tree
                                                                        35
                                                                                  return res;
                                                                        36
     Recursive
                                                                             };
                                                                         37
```

• Implicit segment tree, range query + point update

```
struct Node {
      int lc, rc, p;
    struct SegTree {
5
      vector<Node> t = {{}};
      SegTree(int n) { t.reserve(n * 40); }
      int modify(int p, int 1, int r, int x, int v) {
        int u = p;
9
         if (p == 0) {
10
11
          t.push_back(t[p]);
          u = (int)t.size() - 1;
12
        if (r - l == 1) {
14
15
          t[u].p = t[p].p + v;
         } else {
16
          int m = (1 + r) / 2;
17
          if (x < m) {
            t[u].lc = modify(t[p].lc, l, m, x, v); // ub before
19
     } else {
20
            t[u].rc = modify(t[p].rc, m, r, x, v);
21
22
          t[u].p = t[t[u].lc].p + t[t[u].rc].p;
23
24
25
        return u;
26
      int query(int p, int 1, int r, int x, int y) {
27
28
         if (x <= 1 && r <= y) return t[p].p;
         int m = (1 + r) / 2, res = 0;
         if (x < m) res += query(t[p].lc, 1, m, x, y);</pre>
30
         if (y > m) res += query(t[p].rc, m, r, x, y);
31
        return res;
```

## Iterating

• Iterating, range query + point update

```
struct Node {
      11 v = 0, init = 0;
2
    Node pull(const Node &a, const Node &b) {
      if (!a.init) return b;
      if (!b.init) return a;
      Node c;
9
      return c;
10
11
    struct SegTree {
12
       vector<Node> t;
14
15
       SegTree(ll _n) : n(_n), t(2 * n){};
       void modify(ll p, const Node &v) {
16
        t[p += n] = v;
17
         for (p \neq 2; p; p \neq 2) t[p] = pull(t[p * 2], t[p * 2 + 1]);
19
20
      Node query(ll 1, ll r) {
21
        Node left, right;
         for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
22
           if (1 & 1) left = pull(left, t[1++]);
23
           if (r & 1) right = pull(t[--r], right);
24
26
        return pull(left, right);
27
    };
28
```

• Iterating, range query + range update

```
struct SegTree {
                                                                      27
                                                                             T query_all() { return tree[1]; }
      11 n, h = 0;
                                                                             void consume(int i) { tree[i] = tree[i << 1] * tree[i << 1 |</pre>
                                                                      28
       vector<Node> t;
      SegTree(ll _n) : n(_n), h((ll)log2(n)), t(n * 2) {}
                                                                           }:
                                                                      29
       void apply(ll x, ll v) {
                                                                      30
        if (v == 0) {
                                                                      31
          t[x].one = 0;
                                                                           struct SegInfo {
                                                                      32
        } else {
           t[x].one = t[x].total;
                                                                             SegInfo() : SegInfo(0) {}
9
                                                                      34
                                                                             SegInfo(ll val) : v(val) {}
10
                                                                      35
                                                                             SegInfo operator*(SegInfo b) {
11
        t[x].lazy = v;
                                                                      36
                                                                               return SegInfo(v + b.v);
12
                                                                      37
       void build(ll 1) {
                                                                             }
13
                                                                      38
        for (1 = (1 + n) / 2; 1 > 0; 1 /= 2) {
                                                                           }:
14
                                                                      39
15
           if (t[1].lazy == -1) {
16
             t[1] = pull(t[1 * 2], t[1 * 2 + 1]);
                                                                           Union Find
17
18
        }
19
                                                                           vector<int> p(n);
20
      void push(11 1) {
                                                                           iota(p.begin(), p.end(), 0);
        1 += n;
                                                                           function < int(int) > find = [&](int x) { return p[x] == x ? x :}
21
        for (ll s = h; s > 0; s--) {
                                                                            \hookrightarrow (p[x] = find(p[x])); };
           ll i = 1 >> s;
                                                                           auto merge = [&](int x, int y) { p[find(x)] = find(y); };
23
           if (t[i].lazy != -1) {
24
             apply(2 * i, t[i].lazy);
                                                                              • Persistent version
25
             apply(2 * i + 1, t[i].lazy);
26
                                                                           struct Node {
                                                                       1
27
                                                                             int lc, rc, p;
           t[i].lazy = -1;
28
                                                                           };
                                                                       3
29
      }
30
                                                                       4
                                                                           struct SegTree {
      void modify(ll 1, ll r, int v) {
31
                                                                             vector<Node> t = {{0, 0, -1}}; // init all
        push(1), push(r - 1);
                                                                       6
32
                                                                             SegTree() = default;
         11\ 10 = 1, r0 = r;
33
         for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
                                                                             SegTree(int n) { t.reserve(n * 20); }
34
                                                                             int modify(int p, int 1, int r, int x, int v) {
           if (1 & 1) apply(1++, v);
                                                                       9
35
           if (r & 1) apply(--r, v);
                                                                      10
                                                                               // p: original node, update a[x] \rightarrow v
36
                                                                               t.push_back(t[p]);
                                                                      11
37
                                                                      12
                                                                               int u = (int)t.size() - 1;
        build(10), build(r0 - 1);
38
                                                                               if (r - 1 == 1) {
                                                                      13
39
      Node query(11 1, 11 r) {
                                                                                 t[u].p = v;
                                                                      14
40
                                                                               } else {
        push(1), push(r - 1);
                                                                      15
41
                                                                                 int m = (1 + r) / 2;
         Node left, right;
                                                                      16
42
         for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
                                                                      17
                                                                                 if (x < m) {
43
                                                                                   t[u].lc = modify(t[p].lc, l, m, x, v);
44
           if (1 & 1) left = pull(left, t[1++]);
                                                                      18
                                                                      19
                                                                                   t[u].rc = t[p].rc;
           if (r \& 1) right = pull(t[--r], right);
45
                                                                      20
                                                                                 } else {
46
                                                                                   t[u].lc = t[p].lc;
47
         return pull(left, right);
                                                                      21
                                                                                    t[u].rc = modify(t[p].rc, m, r, x, v);
                                                                      22
48
    };
                                                                      23
                                                                                 t[u].p = t[t[u].lc].p + t[t[u].rc].p;
                                                                               }

    AtCoder Segment Tree (recursive structure but iterative)

                                                                               return u;
    template <class T> struct PointSegmentTree {
                                                                      27
      int size = 1;
2
                                                                             int query(int p, int l, int r, int x, int y) {
                                                                      28
       vector<T> tree:
3
                                                                               // query sum a[x]...a[y-1] rooted at p
      PointSegmentTree(int n) : PointSegmentTree(vector<T>(n)) {}
                                                                               // t[p] holds the info of [l, r)
                                                                      30
      PointSegmentTree(vector<T>& arr) {
                                                                               if (x <= 1 && r <= y) return t[p].p;
        while(size < (int)arr.size())</pre>
                                                                               int m = (1 + r) / 2, res = 0;
                                                                      32
           size <<= 1:
                                                                               if (x < m) res += query(t[p].lc, l, m, x, y);</pre>
                                                                      33
         tree = vector<T>(size << 1);</pre>
                                                                               if (y > m) res += query(t[p].rc, m, r, x, y);
        for(int i = size + arr.size() - 1; i >= 1; i--)
9
                                                                               return res;
                                                                      35
           if(i >= size) tree[i] = arr[i - size];
10
                                                                      36
           else consume(i);
11
                                                                           };
                                                                      37
12
                                                                      38
       void set(int i, T val) {
13
                                                                           struct DSU {
                                                                      39
        tree[i += size] = val;
14
                                                                             int n;
                                                                      40
         for(i >>= 1; i >= 1; i >>= 1)
15
                                                                      41
                                                                             SegTree seg;
           consume(i);
16
                                                                             DSU(int _n) : n(_n), seg(n) {}
                                                                      42
17
                                                                             int get(int p, int x) { return seg.query(p, 0, n, x, x + 1); }
                                                                      43
      T get(int i) { return tree[i + size]; }
18
                                                                             int set(int p, int x, int v) { return seg.modify(p, 0, n, x,
      T query(int 1, int r) {
19
                                                                            → v); }
         T resl, resr;
20
                                                                             int find(int p, int x) {
         for(1 += size, r += size + 1; 1 < r; 1 >>= 1, r >>= 1) {
21
                                                                               int parent = get(p, x);
                                                                      46
22
           if(1 & 1) resl = resl * tree[1++];
                                                                               if (parent < 0) return x;</pre>
23
           if(r & 1) resr = tree[--r] * resr;
                                                                               return find(p, parent);
                                                                      48
24
                                                                      49
        return resl * resr;
                                                                             int is_same(int p, int x, int y) { return find(p, x) ==
      }

    find(p, y); }

26
```

```
int merge(int p, int x, int y) {
                                                                       using namespace __gnu_pbds;
         int rx = find(p, x), ry = find(p, y);
                                                                           template<typename T>
52
         if (rx == ry) return -1;
                                                                           using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
53
         int rank_x = -get(p, rx), rank_y = -get(p, ry);
                                                                            \  \, \hookrightarrow \  \, \texttt{tree\_order\_statistics\_node\_update>};
54
         if (rank_x < rank_y) {</pre>
                                                                           template<typename T, typename X>
55
           p = set(p, rx, ry);
                                                                           using ordered_map = tree<T, X, less<T>, rb_tree_tag,
56
         } else if (rank_x > rank_y) {
                                                                            \  \, \hookrightarrow \  \, \text{tree\_order\_statistics\_node\_update>;}
57
          p = set(p, ry, rx);
                                                                           template<typename T, typename X>
         } else {
                                                                           using fast_map = cc_hash_table<T, X>;
59
60
          p = set(p, ry, rx);
                                                                           template<typename T, typename X>
                                                                       11
61
             = set(p, rx, -rx - 1);
                                                                           using ht = gp_hash_table<T, X>;
                                                                       12
                                                                           mt19937_64
62

→ rng(chrono::steady_clock::now().time_since_epoch().count());
63
         return p;
      }
64
                                                                       14
    };
                                                                       15
                                                                           struct splitmix64 {
                                                                       16
                                                                                size_t operator()(size_t x) const {
                                                                                   static const size_t fixed =
                                                                       17
    Fenwick Tree

    chrono::steady_clock::now().time_since_epoch().count();

                                                                                    x += 0x9e3779b97f4a7c15 + fixed;
                                                                       18

    askd version

                                                                                    x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
                                                                                    x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
                                                                       20
    template <typename T> struct FenwickTree {
                                                                                    return x \hat{} (x >> 31);
      int size = 1, high_bit = 1;
                                                                       22
      vector<T> tree:
                                                                           };
                                                                       23
      FenwickTree(int _size) : size(_size) {
         tree.resize(size + 1);
         while((high_bit << 1) <= size) high_bit <<= 1;</pre>
6
                                                                            Treap
      FenwickTree(vector<T>& arr) : FenwickTree(arr.size()) {
8
                                                                              • (No rotation version)
9
        for(int i = 0; i < size; i++) update(i, arr[i]);</pre>
10
                                                                           struct Node {
      int lower_bound(T x) {
                                                                             Node *1, *r;
11
                                                                       2
         int res = 0; T cur = 0;
12
                                                                              int s, sz;
         for(int bit = high_bit; bit > 0; bit >>= 1) {
13
                                                                              // int t = 0, a = 0, g = 0; // for lazy propagation
           if((res|bit) \le size \&\& cur + tree[res|bit] < x) {
             res |= bit; cur += tree[res];
15
16
                                                                             Node(int _s) : l(nullptr), r(nullptr), s(_s), sz(1), w(rng())
        }
17
18
        return res;
                                                                             void apply(int vt, int vg) {
19
                                                                               // for lazy propagation
                                                                       9
      T prefix_sum(int i) {
20
                                                                       10
                                                                               // s -= vt;
                                                                               // t += vt, a += vg, g += vg;
21
                                                                       11
         for(i++; i > 0; i -= (i & -i)) ret += tree[i];
22
                                                                       12
        return ret;
23
                                                                       13
                                                                              void push() {
24
                                                                                // for lazy propagation
      T range_sum(int 1, int r) { return (1 > r) ? 0 : prefix_sum(r_i)
25
                                                                                // if (l != nullptr) l->apply(t, g);
                                                                                // if (r != nullptr) r->apply(t, g);
     → - prefix_sum(1 - 1); }
      void update(int i, T delta) { for(i++; i <= size; i += (i & 17</pre>
26
         -i)) tree[i] += delta; }
                                                                       18
    }:
27
                                                                              void pull() { sz = 1 + (1 ? 1->sz : 0) + (r ? r->sz : 0); }
                                                                       19
                                                                       20
       • Nea1 version
                                                                       21
                                                                            std::pair<Node *, Node *> split(Node *t, int v) {
    template <typename T>
                                                                       23
                                                                             if (t == nullptr) return {nullptr, nullptr};
    struct Fenwick {
                                                                       24
                                                                              t->push();
      const int n:
                                                                       25
                                                                              if (t->s < v) {
      vector<T> a;
                                                                               auto [x, y] = split(t->r, v);
                                                                       26
      Fenwick(int n) : n(n), a(n) {}
                                                                                t->r = x;
      void add(int x, T v) {
                                                                                t->pull();
                                                                       28
         for (int i = x + 1; i \le n; i += i \& -i) {
                                                                                return {t, y};
          a[i - 1] += v;
                                                                       30
                                                                              } else {
        }
                                                                                auto [x, y] = split(t->1, v);
                                                                       31
10
      }
                                                                                t->1 = y;
      T sum(int x) {
11
                                                                                t->pull();
                                                                       33
         T ans = 0;
12
                                                                       34
                                                                                return {x, t};
         for (int i = x; i > 0; i -= i & -i) {
13
                                                                       35
           ans += a[i - 1];
                                                                       36
15
                                                                       37
        return ans;
16
                                                                           Node *merge(Node *p, Node *q) {
                                                                       38
17
                                                                              if (p == nullptr) return q;
                                                                       39
      T rangeSum(int 1, int r) { return sum(r) - sum(1); }
18
                                                                              if (q == nullptr) return p;
                                                                       40
                                                                              if (p->w < q->w) swap(p, q);
                                                                       41
                                                                       42
                                                                              auto [x, y] = split(q, p\rightarrow s + rng() \% 2);
    PBDS
                                                                       43
                                                                              p->push();
                                                                              p->1 = merge(p->1, x);
                                                                              p->r = merge(p->r, y);
   #include <bits/stdc++.h>
                                                                       45
    #include <ext/pb_ds/assoc_container.hpp>
                                                                              p->pull();
   using namespace std;
                                                                       47
                                                                              return p;
```

```
Node *1, *r;
49
    Node *insert(Node *t, int v) {
                                                                            int s, sz;
50
      auto [x, y] = split(t, v);
                                                                            // int lazy = 0;
51
      return merge(merge(x, new Node(v)), y);
52
                                                                       5
53
                                                                            Node(int _s) : l(nullptr), r(nullptr), s(_s), sz(1), w(rnd())
54
55
    Node *erase(Node *t, int v) {
      auto [x, y] = split(t, v);
                                                                            void apply() {
56
                                                                       8
57
       auto [p, q] = split(y, v + 1);
                                                                       9
                                                                               // for lazy propagation
                                                                               // lazy ^= 1;
      return merge(merge(x, merge(p->1, p->r)), q);
58
                                                                      10
59
                                                                      11
                                                                             void push() {
60
    int get_rank(Node *&t, int v) {
61
                                                                      13
                                                                              // for lazy propagation
62
       auto [x, y] = split(t, v);
                                                                               // if (lazy) {
      int res = (x ? x->sz : 0) + 1;
63
                                                                      15
                                                                                   swap(l, r);
      t = merge(x, y);
                                                                              // if (l != nullptr) l->apply();
64
                                                                      16
                                                                               // if (r != nullptr) r->apply();
65
      return res;
                                                                               //
                                                                                   lazy = 0;
66
                                                                      18
    Node *kth(Node *t, int k) {
68
                                                                      20
                                                                             void pull() { sz = 1 + (1 ? 1->sz : 0) + (r ? r->sz : 0); }
69
70
      while (true) {
                                                                      22
         int left_sz = t->1 ? t->1->sz : 0;
71
                                                                      23
         if (k < left_sz) {</pre>
                                                                          std::pair<Node *, Node *> split(Node *t, int v) {
72
          t = t -> 1:
                                                                            // first -> sz == v
73
                                                                      25
         } else if (k == left_sz) {
                                                                             if (t == nullptr) return {nullptr, nullptr};
75
          return t;
                                                                      27
                                                                            t->push();
         } else {
                                                                             int left_sz = t->l ? t->l->sz : 0;
76
                                                                      28
          k -= left_sz + 1, t = t->r;
77
                                                                      29
                                                                             if (left_sz < v) {</pre>
                                                                              auto [x, y] = split(t->r, v - left_sz - 1);
78
                                                                      30
      }
79
                                                                              t->r = x;
    }
                                                                              t->pull();
80
                                                                      32
                                                                               return {t, y};
81
                                                                      33
    Node *get_prev(Node *&t, int v) {
82
                                                                      34
                                                                            } else {
      auto [x, y] = split(t, v);
                                                                              auto [x, y] = split(t->1, v);
83
                                                                      35
      Node *res = kth(x, x->sz);
                                                                               t->1 = v;
      t = merge(x, y);
                                                                              t->pull();
85
                                                                      37
86
      return res;
                                                                      38
                                                                               return {x, t};
                                                                            }
87
                                                                      39
88
                                                                      40
    Node *get_next(Node *&t, int v) {
                                                                      41
                                                                          Node *merge(Node *p, Node *q) {
      auto [x, y] = split(t, v + 1);
90
                                                                      42
91
      Node *res = kth(y, 1);
                                                                             if (p == nullptr) return q;
                                                                            if (q == nullptr) return p;
92
      t = merge(x, y);
                                                                      44
       return res;
                                                                            if (p->w < q->w) {
                                                                      45
93
                                                                              p->push();
                                                                      46
                                                                              p->r = merge(p->r, q);
                                                                      47
       • USAGE
                                                                               p->pull();
                                                                               return p;
                                                                      49
    int main() {
                                                                            } else {
      cin.tie(nullptr)->sync_with_stdio(false);
                                                                      51
                                                                               q->push();
       int n;
                                                                               q->1 = merge(p, q->1);
                                                                      52
       cin >> n;
                                                                               q->pull();
                                                                      53
      Node *t = nullptr;
                                                                      54
                                                                               return q;
      for (int op, x; n--;) {
         cin >> op >> x;
                                                                          }
                                                                      56
         if (op == 1) {
          t = insert(t, x);
                                                                          Persistent implicit treap
        } else if (op == 2) {
10
          t = erase(t, x);
                                                                          pair<Node *, Node *> split(Node *t, int v) {
12
        } else if (op == 3) {
                                                                            // first \rightarrow sz == v
           cout << get_rank(t, x) << "\n";</pre>
13
                                                                            if (t == nullptr) return {nullptr, nullptr};
         } else if (op == 4) {
                                                                       3
14
                                                                             t->push();
          cout << kth(t, x)->s << "\n";
15
                                                                            int left_sz = t->1 ? t->1->sz : 0;
         } else if (op == 5) {
16
                                                                             t = new Node(*t);
           cout << get_prev(t, x)->s << "\n";</pre>
17
                                                                            if (left_sz < v) {</pre>
         } else {
                                                                              auto [x, y] = split(t->r, v - left_sz - 1);
           cout << get_next(t, x)->s << "\n";</pre>
19
20
                                                                      10
                                                                              t->pull();
      }
21
                                                                              return {t, y};
                                                                      11
                                                                      12
                                                                            } else {
                                                                      13
                                                                              auto [x, y] = split(t->1, v);
                                                                               t->1 = y;
    Implicit treap
                                                                              t->pull();
                                                                      15
                                                                               return {x, t};
```

struct Node {

• Split by size

48

#### K-D Tree } 19 struct Point { Node \*merge(Node \*p, Node \*q) { 20 int x, y; if (p == nullptr) return new Node(\*q); 21 }; if (q == nullptr) return new Node(\*p); 3 22 struct Rectangle { if (p->w < q->w) { 4 23 int lx, rx, ly, ry; p = new Node(\*p); 24 p->push(); 6 p->r = merge(p->r, q);26 bool is\_in(const Point &p, const Rectangle &rg) { 27 p->pull(); return (p.x >= rg.lx) && (p.x <= rg.rx) && (p.y >= rg.ly) && return p; 28 $\hookrightarrow$ (p.y <= rg.ry); } else { 29 q = new Node(\*q); 10 30 11 31 q->push(); struct KDTree { 32 q->1 = merge(p, q->1);12 vector<Point> points; 13 33 q->pull(); struct Node { return q; 34 int lc, rc; 15 35 Point point; 36 Rectangle range; 17 18 19 }; 2D Sparse Table vector<Node> nodes; 20 $^{21}$ int root = -1; Sorry that this sucks - askd KDTree(const vector<Point> &points\_) { 22 points = points\_; template <class T, class Compare = less<T>> Rectangle range = {-1e9, 1e9, -1e9, 1e9}; 24 struct SparseTable2d { 25 root = tree\_construct(0, (int)points.size(), range, 0); int n = 0, m = 0;26 T\*\*\*\* table; 27 int tree\_construct(int 1, int r, Rectangle range, int depth) { int\* log; if (1 == r) return -1; inline T choose(T x, T y) { if (1 > r) throw; 29 return Compare()(x, y) ? x : y; int mid = (1 + r) / 2;auto comp = (depth % 2) ? [](Point &a, Point &b) { return 31 SparseTable2d(vector<vector<T>>& grid) { $\rightarrow$ a.x < b.x; } if(grid.empty() || grid[0].empty()) return; : [](Point &a, Point &b) { return n = grid.size(); m = grid[0].size(); 11 $\rightarrow$ a.y < b.y; }; log = new int[max(n, m) + 1];12 nth\_element(points.begin() + 1, points.begin() + mid, 33 log[1] = 0;13 points.begin() + r, comp); for(int i = 2; i <= max(n, m); i++)</pre> 14 Rectangle l\_range(range), r\_range(range); 34 $log[i] = log[i - 1] + ((i ^ (i - 1)) > i);$ 35 if (depth % 2) { 16 table = new T\*\*\*[n]; l\_range.rx = points[mid].x; 36 for(int i = n - 1; i >= 0; i--) { 17 37 r\_range.lx = points[mid].x; table[i] = new T\*\*[m]; 18 } else { 38 for(int $j = m - 1; j >= 0; j--) {$ 19 l\_range.ry = points[mid].y; 39 table[i][j] = new T\*[log[n - i] + 1];r\_range.ly = points[mid].y; 40 for(int k = 0; $k \le log[n - i]$ ; k++) { 21 41 table[i][j][k] = new T[log[m - j] + 1];Node node = {tree\_construct(1, mid, 1\_range, depth + 1), if(!k) table[i][j][k][0] = grid[i][j]; 23 tree\_construct(mid + 1, r, r\_range, depth + 1), else table[i][j][k][0] = choose(table[i][j][k-1][0], points[mid], range, r - 1}; $\leftrightarrow$ table[i+(1<<(k-1))][j][k-1][0]); 44 nodes.push\_back(node); for(int 1 = 1; 1 <= log[m - j]; 1++) 25 return (int)nodes.size() - 1; 45 table[i][j][k][l] = choose(table[i][j][k][l-1], 46 table[i][j+(1<<(1-1))][k][1-1]); 47 27 int inner\_query(int id, const Rectangle &rec, int depth) { } 28 if (id == -1) return 0; 49 } 29 50 Rectangle rg = nodes[id].range; 30 51 if (rg.lx >= rec.lx && rg.rx <= rec.rx && rg.ly >= rec.ly && T query(int r1, int r2, int c1, int c2) { 31 rg.ry <= rec.ry) { </pre> assert(r1 >= 0 && r2 < n && r1 <= r2); 32 return nodes[id].num; 52 assert(c1 >= 0 && c2 < m && c1 <= c2); 33 } 53 int rl = log[r2 - r1 + 1], cl = log[c2 - c1 + 1]; 34 54 int ans = 0;T ca1 = choose(table[r1][c1][r1][c1], if (depth % 2) { // pruning 55 → table[r2-(1<<rl)+1][c1][r1][c1]);</pre> if (rec.lx <= nodes[id].point.x) ans +=</pre> 56 T ca2 = choose(table[r1][c2-(1<<c1)+1][r1][c1], inner\_query(nodes[id].lc, rec, depth + 1); table[r2-(1<<rl)+1][c2-(1<<cl)+1][r1][c1]); if (rec.rx >= nodes[id].point.x) ans += 57 return choose(ca1, ca2); 37 inner\_query(nodes[id].rc, rec, depth + 1); } 38 58 } else { }; 39 if (rec.ly <= nodes[id].point.y) ans += 59 → inner\_query(nodes[id].lc, rec, depth + 1); • USAGE if (rec.ry >= nodes[id].point.y) ans += 60 inner\_query(nodes[id].rc, rec, depth + 1); vector<vector<int>> test = { 61 {1, 2, 3, 4}, {2, 3, 4, 5}, {9, 9, 9, 9}, {-1, -1, -1, -1} if (is\_in(nodes[id].point, rec)) ans += 1; 62 }; return ans; 63 4 // Range min query <sup>64</sup> SparseTable2d<int> st(test); SparseTable2d<int,greater<int>> st2(test); // Range max query 65 int query(const Rectangle &rec) { return inner\_query(root,

```
y->access();
                                                                     70
                                                                     71
                                                                          void cut(Node *x, Node *y) {
                                                                     72
    Link/Cut Tree
                                                                            split(x, y);
                                                                     73
                                                                            x->p = y->ch[0] = nullptr;
                                                                     74
    struct Node {
                                                                            y->pull();
                                                                     75
      Node *ch[2], *p;
      int id;
                                                                          bool connected(Node *p, Node *q) {
                                                                     77
      bool rev;
                                                                     78
                                                                              p->access();
      Node(int id) : ch{nullptr, nullptr}, p(nullptr), id(id),
                                                                     79
                                                                              q->access();
      → rev(false) {}
                                                                              return p->p != nullptr;
                                                                     80
      friend void reverse(Node *p) {
        if (p != nullptr) {
          swap(p->ch[0], p->ch[1]);
          p->rev ^= 1;
9
                                                                          Geometry
11
12
      void push() {
                                                                          Basic stuff
        if (rev) {
13
          reverse(ch[0]);
14
                                                                          using ll = long long;
          reverse(ch[1]);
15
                                                                          using ld = long double;
          rev = false;
16
17
                                                                          constexpr auto eps = 1e-8;
      }
18
                                                                          const auto PI = acos(-1);
       void pull() {}
19
                                                                          int sgn(ld x) { return (abs(x) <= eps) ? 0 : (x < 0 ? -1 : 1); }</pre>
      bool is_root() { return p == nullptr || p->ch[0] != this &&

    p->ch[1] != this; }

                                                                          struct Point {
      bool pos() { return p->ch[1] == this; }
21
                                                                            ld x = 0, y = 0;
                                                                      9
      void rotate() {
22
                                                                     10
                                                                            Point() = default;
         Node *q = p;
                                                                     11
                                                                            Point(ld _x, ld _y) : x(_x), y(_y) {}
        bool x = !pos();
24
                                                                            bool operator<(const Point &p) const { return !sgn(p.x - x) ?</pre>
         q->ch[!x] = ch[x];
25
                                                                           \hookrightarrow sgn(y - p.y) < 0 : x < p.x; \}
         if (ch[x] != nullptr) ch[x]->p = q;
                                                                           bool operator == (const Point &p) const { return !sgn(p.x - x)
                                                                     13
27
        p = q->p;
                                                                           \leftrightarrow && !sgn(p.y - y); }
         if (!q->is\_root()) q->p->ch[q->pos()] = this;
                                                                           Point operator+(const Point &p) const { return {x + p.x, y +
29
         ch[x] = q;

    p.y}; }

         q->p = this;
30
                                                                           Point operator-(const Point &p) const { return {x - p.x, y -
                                                                     15
        pull();
31
                                                                           \rightarrow p.y}; }
        q->pull();
32
                                                                            Point operator*(ld a) const { return {x * a, y * a}; }
33
      }
                                                                            Point operator/(ld a) const { return \{x / a, y / a\}; }
                                                                     17
      void splay() {
34
                                                                            auto operator*(const Point &p) const { return x * p.x + y *
        vector<Node *> s;
35
                                                                           \rightarrow p.y; } // dot
         for (Node *i = this; !i->is_root(); i = i->p)
36
                                                                           auto operator^(const Point &p) const { return x * p.y - y *
                                                                     19

    s.push_back(i→>p);

    p.x; } // cross

         while (!s.empty()) s.back()->push(), s.pop_back();
37
                                                                           friend auto &operator>>(istream &i, Point &p) { return i >>
                                                                     20
        push():
38
                                                                           \rightarrow p.x >> p.y; }
         while (!is_root()) {
                                                                     21
                                                                           friend auto &operator << (ostream &o, Point p) { return o << p.x
40
          if (!p->is_root()) {
                                                                           if (pos() == p->pos()) {
41
                                                                     22
              p->rotate();
42
                                                                     23
            } else {
43
                                                                          struct Line {
              rotate();
                                                                            Point s = \{0, 0\}, e = \{0, 0\};
                                                                     25
45
                                                                            Line() = default;
                                                                     26
46
                                                                     27
                                                                            Line(Point _s, Point _e) : s(_s), e(_e) {}
47
          rotate();
                                                                            friend auto &operator>>(istream &i, Line &l) { return i >> l.s
                                                                     28
48
                                                                           \Rightarrow >> 1.e; } // ((x1, y1), (x2, y2)
49
        pull();
                                                                          ጉ:
                                                                     29
50
                                                                          struct Segment : Line {
        for (Node *i = this, *q = nullptr; i != nullptr; q = i, i
52
                                                                           using Line::Line;
                                                                     32
        i->p) {
                                                                          }:
          i->splay();
53
                                                                     34
          i->ch[1] = q;
54
                                                                          struct Circle {
           i->pull();
                                                                           Point o = {0, 0};
                                                                     36
56
                                                                     37
                                                                            ld r = 0;
57
        splay();
                                                                     38
                                                                            Circle() = default;
      }
58
                                                                            Circle(Point _o, ld _r) : o(_o), r(_r) {}
                                                                     39
      void makeroot() {
59
60
         access();
61
        reverse(this):
                                                                          auto dist2(const Point &a) { return a * a; }
62
                                                                          auto dist2(const Point &a, const Point &b) { return dist2(a -
63
    }:

→ b): }

64
    void link(Node *x, Node *y) {
                                                                          auto dist(const Point &a) { return sqrt(dist2(a)); }
65
      x->makeroot();
                                                                         auto dist(const Point &a, const Point &b) { return sqrt(dist2(a
      x->p = y;
66
                                                                          → - b)); }
                                                                          auto dist(const Point &a, const Line &1) { return abs((a - 1.s)
    void split(Node *x, Node *y) {
```

69

x->makeroot():

}:

```
auto dist(const Point &p, const Segment &1) {
  if (l.s == l.e) return dist(p, l.s);
  auto d = dist2(1.s, 1.e), t = min(d, max((1d)0, (p - 1.s) *)
 Relation
  return dist((p - l.s) * d, (l.e - l.s) * t) / d;
                                                                      enum class Relation { SEPARATE, EX_TOUCH, OVERLAP, IN_TOUCH,
/* Needs is_intersect

→ INSIDE }:

auto dist(const Segment &11, const Segment &12) {
                                                                       Relation get_relation(const Circle &a, const Circle &b) {
  if (is_intersect(l1, l2)) return (ld)0;
                                                                         auto c1c2 = dist(a.o, b.o);
  return min(\{dist(l1.s, l2), dist(l1.e, l2), dist(l2.s, l1), 
                                                                         auto r1r2 = a.r + b.r, diff = abs(a.r - b.r);
 \leftrightarrow dist(l2.e, l1)});
                                                                         if (sgn(c1c2 - r1r2) > 0) return Relation::SEPARATE;
                                                                         if (sgn(c1c2 - r1r2) == 0) return Relation::EX_TOUCH;
                                                                         if (sgn(c1c2 - diff) > 0) return Relation::OVERLAP;
Point perp(const Point &p) { return Point(-p.y, p.x); }
                                                                         if (sgn(c1c2 - diff) == 0) return Relation::IN_TOUCH;
                                                                        return Relation::INSIDE;
                                                                   9
auto rad(const Point &p) { return atan2(p.y, p.x); }
                                                                  10
                                                                  11
                                                                       auto get_cos_from_triangle(ld a, ld b, ld c) { return (a * a + b
Transformation
                                                                       + * b - c * c) / (2.0 * a * b); }
Point project(const Point &p, const Line &l) {
                                                                  13
  return 1.s + ((1.e - 1.s) * ((1.e - 1.s) * (p - 1.s))) /
                                                                       bool on_line(const Line &1, const Point &p) { return !sgn((1.s -

    dist2(1.e - 1.s);

                                                                       \hookrightarrow p) \hat{} (l.e - p)); }
                                                                       bool on_segment(const Segment &1, const Point &p) {
                                                                  16
Point reflect(const Point &p, const Line &l) {
                                                                  17
                                                                        return !sgn((l.s - p) ^ (l.e - p)) && sgn((l.s - p) * (l.e -
                                                                        \hookrightarrow p)) <= 0;
  return project(p, 1) * 2 - p;
Point dilate(const Point &p, ld scale_x = 1, ld scale_y = 1) { 20
                                                                       bool on_segment2(const Segment &1, const Point &p) { // assume p
 → return Point(p.x * scale_x, p.y * scale_y); }

→ on Line l

Line dilate(const Line &1, ld scale_x = 1, ld scale_y = 1) { 21
                                                                        if (1.s == p || 1.e == p) return true;

→ return Line(dilate(l.s, scale_x, scale_y), dilate(l.e,
                                                                         if (\min(l.s, l.e)  return true;
                                                                  22

    scale_x, scale_y)); }

                                                                         return false;
Segment dilate(const Segment &1, ld scale_x = 1, ld scale_y = 1)
 _{\hookrightarrow} { return Segment(dilate(1.s, scale_x, scale_y), dilate(1.e,25
                                                                       {\color{red}\textbf{bool}} \ {\color{blue}\textbf{is\_parallel(const}} \ {\color{blue}\textbf{Line}} \ {\color{blue}\&\textbf{a}}, \ {\color{blue}\textbf{const}} \ {\color{blue}\textbf{Line}} \ {\color{blue}\&\textbf{b}}) \ {\color{blue}\textbf{f}} \ {\color{blue}\textbf{return}}

    scale_x, scale_y)); }

vector<Point> dilate(const vector<Point> &p, ld scale_x = 1, ld
                                                                        \rightarrow !sgn((a.s - a.e) ^ (b.s - b.e)); }
 \Rightarrow scale_y = 1) {
                                                                       bool is_orthogonal(const Line &a, const Line &b) { return
  int n = p.size();
                                                                       \rightarrow !sgn((a.s - a.e) * (b.s - b.e)); }
  vector<Point> res(n);
  for (int i = 0; i < n; i++)
                                                                      int is_intersect(const Segment &a, const Segment &b) {
                                                                  29
    res[i] = dilate(p[i], scale_x, scale_y);
                                                                       auto d1 = sgn((a.e - a.s) \hat{ } (b.s - a.s)), d2 = sgn((a.e - a.s))
                                                                       \hookrightarrow ^ (b.e - a.s));
  return res;
                                                                        auto d3 = sgn((b.e - b.s) \hat{ } (a.s - b.s)), d4 = <math>sgn((b.e - b.s))
                                                                        Point rotate(const Point &p, ld a) { return Point(p.x * cos(a) 32
                                                                        if (d1 * d2 < 0 && d3 * d4 < 0) return 2; // intersect at
 \rightarrow p.y * sin(a), p.x * sin(a) + p.y * cos(a)); }

→ non-end point

Line rotate(const Line &1, ld a) { return Line(rotate(1.s, a), 33
                                                                        return (d1 == 0 && sgn((b.s - a.s) * (b.s - a.e)) <= 0) ||

→ rotate(l.e, a)); }
                                                                  34
Segment rotate(const Segment &1, 1d a) { return
                                                                  35
                                                                                (d4 == 0 \&\& sgn((a.e - b.s) * (a.e - b.e)) <= 0);
 ⇔ Segment(rotate(l.s, a), rotate(l.e, a)); }
                                                                  36
Circle rotate(const Circle &c, ld a) { return Circle(rotate(c.og
\rightarrow a), c.r); }
vector<Point> rotate(const vector<Point> &p, ld a) {
                                                                       int is_intersect(const Line &a, const Segment &b) {
                                                                  39
                                                                       auto d1 = sgn((a.e - a.s) \hat{ } (b.s - a.s)), d2 = sgn((a.e - a.s))
  int n = p.size();
                                                                  40
  vector<Point> res(n);
                                                                        \rightarrow ^ (b.e - a.s));
  for (int i = 0; i < n; i++)
                                                                        if (d1 * d2 < 0) return 2; // intersect at non-end point
    res[i] = rotate(p[i], a);
                                                                        return d1 == 0 || d2 == 0;
                                                                  42
  return res;
                                                                  43
                                                                  44
                                                                       Point intersect(const Line &a, const Line &b) {
                                                                  45
Point translate(const Point &p, 1d dx = 0, 1d dy = 0) { return 46
                                                                         auto u = a.e - a.s, v = b.e - b.s;
\rightarrow Point(p.x + dx, p.y + dy); }
                                                                         auto t = ((b.s - a.s) ^ v) / (u ^ v);
                                                                  47
Line translate(const Line &1, ld dx = 0, ld dy = 0) { return
                                                                         return a.s + u * t;
49
Segment translate(const Segment &1, ld dx = 0, ld dy = 0) {

→ return Segment(translate(l.s, dx, dy), translate(l.e, dx, 51)
                                                                       int is_intersect(const Circle &c, const Line &l) {
                                                                         auto d = dist(c.o, 1);
 \leftrightarrow dy)); }
                                                                  52
Circle translate(const Circle &c, ld dx = 0, ld dy = 0) { returns
                                                                         return sgn(d - c.r) < 0 ? 2 : !sgn(d - c.r);

    Gircle(translate(c.o, dx, dy), c.r); }

vector<Point> translate(const vector<Point> &p, ld dx = 0, ld dy
 \Rightarrow = 0) {
                                                                       vector<Point> intersect(const Circle &a, const Circle &b) {
  int n = p.size();
                                                                  57
                                                                         auto relation = get_relation(a, b);
  vector<Point> res(n);
                                                                        if (relation == Relation::INSIDE || relation ==
  for (int i = 0; i < n; i++)

→ Relation::SEPARATE) return {};
    res[i] = translate(p[i], dx, dy);
                                                                       auto vec = b.o - a.o;
                                                                        auto d2 = dist2(vec);
  return res:
```

10

11

13

15

17

5

13 14

15

16

17

18

24

25

26

28

29

30

31

37

39

```
auto p = (d2 + a.r * a.r - b.r * b.r) / ((long double) 2 * d2) 39
      \rightarrow h2 = a.r * a.r - p * p * d2;
                                                                             return \{x / (3 * sum), y / (3 * sum)\};
       auto mid = a.o + vec * p, per = perp(vec) * sqrt(max((long 132

    double)0, h2) / d2);

       if (relation == Relation::OVERLAP)
63
         return {mid + per, mid - per};
64
       else
65
                                                                           auto area(const vector<Point> &p) {
         return {mid};
 66
                                                                             int n = (int)p.size();
     }
67
                                                                             long double area = 0;
68
                                                                             for (int i = 0; i < n; i++) area += p[i] ^ p[(i + 1) % n];
     vector<Point> intersect(const Circle &c, const Line &l) {
69
                                                                             return area / 2.0;
       if (!is_intersect(c, 1)) return {};
70
                                                                       6
       auto v = 1.e - 1.s, t = v / dist(v);
       Point a = 1.s + t * ((c.o - 1.s) * t);
72
                                                                           auto area(const Point &a, const Point &b, const Point &c) {
73
       auto d = sqrt(max((1d)0, c.r * c.r - dist2(c.o, a)));
                                                                             return ((long double)((b - a) ^ (c - a))) / 2.0;
                                                                       9
74
       if (!sgn(d)) return {a};
       return {a - t * d, a + t * d};
75
                                                                       11
76
                                                                           auto area2(const Point &a, const Point &b, const Point &c) {
77

→ return (b - a) ^ (c - a); }
78
     int in_poly(const vector<Point> &p, const Point &a) {
                                                                       13
       int cnt = 0, n = (int)p.size();
79
                                                                           auto area_intersect(const Circle &c, const vector<Point> &ps) {
 80
       for (int i = 0; i < n; i++) {
                                                                             int n = (int)ps.size();
                                                                       15
         auto q = p[(i + 1) \% n];
81
                                                                             auto arg = [%](const Point &p, const Point &q) { return
         if (on_segment(Segment(p[i], q), a)) return 1; // on the ^{16}
82
                                                                            \rightarrow atan2(p \hat{q}, p * q); };
         edge of the polygon
                                                                             auto tri = [&](const Point &p, const Point &q) {
         cnt \hat{} = ((a.y < p[i].y) - (a.y < q.y)) * ((p[i] - a) \hat{} (q - ^{17}
 83
                                                                               auto r2 = c.r * c.r / (long double)2;
      \rightarrow a)) > 0;
                                                                               auto d = q - p;
                                                                       19
       }
 84
                                                                               auto a = d * p / dist2(d), b = (dist2(p) - c.r * c.r) /
       return cnt ? 2 : 0;
85
                                                                            \rightarrow dist2(d):
86
                                                                       21
                                                                               long double det = a * a - b;
87
                                                                               if (sgn(det) \le 0) return arg(p, q) * r2;
                                                                       22
     int is_intersect(const vector<Point> &p, const Line &a) {
 88
                                                                               auto s = max((long double)0, -a - sqrt(det)), t = min((long
                                                                       23
       // 1: touching, >=2: intersect count
 89

    double)1, -a + sqrt(det));

       int cnt = 0, edge_cnt = 0, n = (int)p.size();
90
                                                                               if (sgn(t) < 0 \mid \mid sgn(1 - s) \le 0) return arg(p, q) * r2;
                                                                       24
       for (int i = 0; i < n; i++) {
91
                                                                               auto u = p + d * s, v = p + d * t;
                                                                       25
         auto q = p[(i + 1) \% n];
92
                                                                               return arg(p, u) * r2 + (u ^ v) / 2 + arg(v, q) * r2;
                                                                      26
         if (on_line(a, p[i]) \&\& on_line(a, q)) return -1; //
                                                                      27
                                                                             }:
        infinity
                                                                             long double sum = 0;
                                                                      28
         auto t = is_intersect(a, Segment(p[i], q));
94
                                                                             for (int i = 0; i < n; i++) sum += tri(ps[i] - c.o, ps[(i + 1)
                                                                      29
         (t == 1) && edge_cnt++, (t == 2) && cnt++;
95
                                                                            96
                                                                      30
                                                                             return sum:
97
       return cnt + edge_cnt / 2;
                                                                      31
98
                                                                       32
                                                                           auto adaptive_simpson(ld _1, ld _r, function<ld(ld)> f) {
                                                                      33
     vector<Point> tangent(const Circle &c, const Point &p) {
100
                                                                             auto simpson = [\&] (ld l, ld r) { return (r - 1) * (f(1) + 4 *
      auto d = dist(c.o, p), 1 = c.r * c.r / d, h = sqrt(c.r * c.r)^{34}
101
                                                                            \leftrightarrow f((1 + r) / 2) + f(r)) / 6; };
      \rightarrow 1 * 1);
                                                                             function<ld(ld, ld, ld)> asr = [\&](ld l, ld r, ld s) {
       auto v = (p - c.o) / d;
102
                                                                               auto mid = (1 + r) / 2;
       return {c.o + v * 1 + perp(v) * h, c.o + v * 1 - perp(v) * h};
103
                                                                               auto left = simpson(l, mid), right = simpson(mid, r);
104
                                                                               if (!sgn(left + right - s)) return left + right;
105
                                                                               return asr(l, mid, left) + asr(mid, r, right);
     Circle get_circumscribed(const Point &a, const Point &b, const ^{39}
106
                                                                             };
      → Point &c) {
                                                                       41
                                                                             return asr(_1, _r, simpson(_1, _r));
       Line u((a + b) / 2, ((a + b) / 2) + perp(b - a));
107
                                                                      42
       Line v((b + c) / 2, ((b + c) / 2) + perp(c - b));
108
                                                                      43
       auto o = intersect(u, v);
109
                                                                           vector<Point> half_plane_intersect(vector<Line> &L) {
                                                                      44
110
       return Circle(o, dist(o, a));
                                                                             int n = (int)L.size(), 1 = 0, r = 0; // [left, right]
111
                                                                             sort(L.begin(), L.end(),
                                                                       46
112
                                                                                   [](const Line &a, const Line &b) { return rad(a.s - a.e)
     Circle get_inscribed(const Point &a, const Point &b, const Point
113
                                                                              < rad(b.s - b.e); });
                                                                             vector<Point> p(n), res;
114
       auto 11 = dist(b - c), 12 = dist(c - a), 13 = dist(a - b);
                                                                             vector<Line> q(n);
       Point o = (a * 11 + b * 12 + c * 13) / (11 + 12 + 13);
115
                                                                             q[0] = L[0];
                                                                       50
       return Circle(o, dist(o, Line(a, b)));
116
                                                                             for (int i = 1; i < n; i++) {
117
                                                                               while (1 < r && sgn((L[i].e - L[i].s) ^ (p[r - 1] - L[i].s))
118
     pair<ld, ld> get_centroid(const vector<Point> &p) {
119
                                                                               while (1 < r \&\& sgn((L[i].e - L[i].s) ^ (p[1] - L[i].s)) <=
                                                                       53
120
       int n = (int)p.size();

→ 0) 1++;

       1d x = 0, y = 0, sum = 0;
121
                                                                               q[++r] = L[i];
                                                                       54
       auto a = p[0], b = p[1];
122
                                                                               if (sgn((q[r].e - q[r].s) ^ (q[r - 1].e - q[r - 1].s)) == 0)
                                                                      55
       for (int i = 2; i < n; i++) {
         auto c = p[i];
124
                                                                      56
         auto s = area({a, b, c});
                                                                                 if (sgn((q[r].e - q[r].s) ^ (L[i].s - q[r].s)) > 0) q[r] =
                                                                      57
126
         sum += s;
                                                                            x += s * (a.x + b.x + c.x);
127
                                                                      58
         y += s * (a.y + b.y + c.y);
128
                                                                                if (1 < r) p[r - 1] = intersect(q[r - 1], q[r]);
         swap(b, c);
129
                                                                       60
```

```
while (1 < r \&\& sgn((q[1].e - q[1].s) \hat{} (p[r - 1] - q[1].s))_{56} vector<Point> get_convex2_safe(vector<Point> points, bool
     ← <= 0) r--;</pre>

    allow_collinear = false) {
      if (r - 1 <= 1) return {};
                                                                             return get_convex2(points, allow_collinear);
62
      p[r] = intersect(q[r], q[1]);
63
                                                                       58
      return vector<Point>(p.begin() + 1, p.begin() + r + 1);
64
                                                                       59
                                                                           bool is_convex(const vector<Point> &p, bool allow_collinear =
65
                                                                       60

  false) {
                                                                             int n = p.size();
     Convex
                                                                             int lo = 1, hi = -1;
                                                                       62
                                                                             for (int i = 0; i < n; i++) {
                                                                       63
    vector<Point> get_convex(vector<Point> &points, bool
                                                                               int cur = sgn((p[(i + 2) \% n] - p[(i + 1) \% n]) ^ (p[(i + 1)
        allow_collinear = false) {
                                                                            // strict, no repeat, two pass
                                                                               lo = min(lo, cur); hi = max(hi, cur);
      sort(points.begin(), points.end());
                                                                       66
      points.erase(unique(points.begin(), points.end()),
                                                                       67
                                                                             return allow_collinear ? (hi - lo) < 2 : (lo == hi && lo);

→ points.end());
                                                                           }
                                                                       68
      vector<Point> L, U;
                                                                       69
      for (auto &t : points) {
                                                                           auto rotating_calipers(const vector<Point> &hull) {
         for (ll sz = L.size(); sz > 1 && (sgn((t - L[sz - 2]) ^
                                                                             // use get convex2
                                                                       71
     \leftrightarrow (L[sz - 1] - L[sz - 2])) >= 0);
                                                                             int n = (int)hull.size(); // return the square of longest
              L.pop_back(), sz = L.size()) {
                                                                            \hookrightarrow dist
                                                                             assert(n > 1);
        L.push_back(t);
10
                                                                             if (n <= 2) return dist2(hull[0], hull[1]);</pre>
                                                                       74
      }
11
                                                                             ld res = 0;
                                                                       75
12
      for (auto &t : points) {
                                                                             for (int i = 0, j = 2; i < n; i++) {
                                                                       76
         for (ll sz = U.size(); sz > 1 && (sgn((t - U[sz - 2]) ^
13
                                                                               auto d = hull[i], e = hull[(i + 1) % n];
                                                                       77
        (U[sz - 1] - U[sz - 2])) <= 0);
                                                                               while (area2(d, e, hull[j]) < area2(d, e, hull[(j + 1) \%
              U.pop_back(), sz = U.size()) {
14
                                                                            \rightarrow n])) j = (j + 1) \% n;
                                                                               res = max(res, max(dist2(d, hull[j]), dist2(e, hull[j])));
                                                                       79
         U.push_back(t);
16
                                                                             }
                                                                       80
17
                                                                       81
                                                                             return res;
      \begin{tabular}{ll} /\!/ contain\ repeats\ if\ all\ collinear,\ use\ a\ set\ to\ remove \end{tabular}
18
                                                                           }
                                                                       82
        repeats
                                                                       83
      if (allow_collinear) {
19
                                                                           // Find polygon cut to the left of l
                                                                       84
        for (int i = (int)U.size() - 2; i >= 1; i--)
20
                                                                      85
                                                                           vector<Point> convex_cut(const vector<Point> &p, const Line &l)

    L.push_back(U[i]);
21
      } else {
                                                                             int n = p.size();
         set<Point> st(L.begin(), L.end());
22
                                                                             vector<Point> cut;
                                                                       87
         for (int i = (int)U.size() - 2; i >= 1; i--) {
23
                                                                             for (int i = 0; i < n; i++) {
                                                                       88
           if (st.count(U[i]) == 0) L.push_back(U[i]),
24
                                                                               auto a = p[i], b = p[(i + 1) \% n];
                                                                       89
         st.insert(U[i]);
                                                                                if (sgn((1.e - 1.s) ^ (a - 1.s)) >= 0)
                                                                       90
25
        }
                                                                                 cut.push_back(a);
                                                                       91
      }
26
                                                                                if (sgn((1.e - 1.s) ^ (a - 1.s)) * sgn((1.e - 1.s) ^ (b - 1.s)) 
                                                                       92
27
      return L;
                                                                               1.s)) == -1)
28
                                                                                  cut.push_back(intersect(Line(a, b), 1));
                                                                       93
                                                                             }
                                                                       94
    vector<Point> get_convex2(vector<Point> &points, bool
30
                                                                             return cut;
     \hookrightarrow allow_collinear = false) { // strict, no repeat, one pass
                                                                      96
31
      nth_element(points.begin(), points.begin(), points.end());
      sort(points.begin() + 1, points.end(), [&](const Point &a,
32
                                                                           // Sort by angle in range [0, 2pi)
                                                                      98
         const Point &b) {
                                                                           template <class RandomIt>
                                                                      99
         int rad_diff = sgn((a - points[0]) ^ (b - points[0]));
33
                                                                           void polar_sort(RandomIt first, RandomIt last, Point origin =
                                                                      100
         return !rad_diff ? (dist2(a - points[0]) < dist2(b -
                                                                            → Point(0, 0)) {
     o points[0])) : (rad_diff > 0);
                                                                             auto get_quad = [&](const Point& p) {
                                                                      101
35
      });
                                                                               Point diff = p - origin;
                                                                      102
36
      if (allow_collinear) {
                                                                                if (diff.x > 0 \&\& diff.y >= 0) return 1;
         int i = (int)points.size() - 1;
37
                                                                               if (diff.x \le 0 \&\& diff.y > 0) return 2;
         while (i >= 0 && !sgn((points[i] - points[0]) ^ (points[i]_{105}^{-1}
                                                                                if (diff.x < 0 && diff.y <= 0) return 3;
     → points.back()))) i--;
                                                                               return 4;
                                                                      106
39
        reverse(points.begin() + i + 1, points.end());
                                                                             };
                                                                      107
      }
40
                                                                             auto polar_cmp = [&](const Point& p1, const Point& p2) {
                                                                      108
      vector<Point> hull;
41
                                                                               int q1 = get_quad(p1), q2 = get_quad(p2);
                                                                      109
      for (auto &t : points) {
42
                                                                      110
                                                                                if (q1 != q2) return q1 < q2;
         for (ll sz = hull.size();
43
                                                                               return ((p1 - origin) ^ (p2 - origin)) > 0;
                                                                     111
              sz > 1 && (sgn((t - hull[sz - 2]) ^ (hull[sz - 1] -
                                                                             }:
                                                                     112
        hull[sz - 2])) >= allow_collinear);
                                                                             sort(first, last, polar_cmp);
              hull.pop_back(), sz = hull.size()) {
45
                                                                     114
46
        hull.push_back(t);
47
48
                                                                           Basic 3D
      return hull;
49
    }
                                                                           using ll = long long;
50
                                                                           using ld = long double;
51
                                                                       2
    vector<Point> get_convex_safe(vector<Point> points, bool
52
                                                                       3

    allow_collinear = false) {
                                                                           constexpr auto eps = 1e-8;
                                                                           const auto PI = acos(-1);
      return get_convex(points, allow_collinear);
53
    }
                                                                           int sgn(ld x) { return (abs(x) <= eps) ? 0 : (x < 0 ? -1 : 1); }</pre>
54
55
```

```
auto [ri, rj, rdist] = recurse(mid, r);
      1d x = 0, y = 0, z = 0;
      Point3D() = default;
                                                                                 if (ldist < rdist) { i = li; j = lj; d = ldist; }
10
      Point3D(ld _x, ld _y, ld _z) : x(_x), y(_y), z(_z) {}
                                                                                 else { i = ri; j = rj; d = rdist; }
11
      bool operator<(const Point3D &p) const { return !sgn(p.x - x)27
                                                                                 inplace_merge(pts.begin() + 1, pts.begin() + mid,
     \leftrightarrow ? (!sgn(p.y - y) ? sgn(p.z - z) < 0 : y < p.y) : x < p.x; }

→ pts.begin() + r, cmp_y);

      bool operator == (const Point3D &p) const { return !sgn(p.x - x)
                                                                                 buf.clear():
     \leftrightarrow && !sgn(p.y - y) && !sgn(p.z - z); }
                                                                                 for (int a = 1; a < r; a++) {
                                                                                   if (abs(x - pts[a].first.x) >= d) continue;
      Point3D operator+(const Point3D &p) const { return {x + p.x, 3p
                                                                                   for (int b = buf.size() - 1; b >= 0; b--) {
     \leftrightarrow + p.y, z + p.z}; }
      Point3D operator-(const Point3D &p) const { return {x - p.x, 3p
                                                                                     if (pts[a].first.y - buf[b].first.y >= d) break;
     \rightarrow - p.y, z - p.z}; }
                                                                                     ld cur = dist(pts[a].first, buf[b].first);
      Point3D operator*(ld a) const { return \{x * a, y * a, z * a\}_{34}
                                                                                     if (cur < d) { i = pts[a].second; j = buf[b].second; d</pre>
                                                                               = cur: }
      Point3D operator/(ld a) const { return \{x / a, y / a, z / a\}_{35}
                                                                                   buf.push_back(pts[a]);
      auto operator*(const Point3D &p) const { return x * p.x + y *37
                                                                              }
     \rightarrow p.y + z * p.z; } // dot
                                                                              return {i, j, d};
      Point3D operator (const Point3D &p) const { return {y * p.z -39}
19
     \rightarrow z * p.y, z * p.x - x * p.z, x * p.y - y * p.x}; } // crosao
      friend auto &operator>>(istream &i, Point3D &p) { return i >>41
                                                                            return recurse(0, n);

    p.x >> p.y >> p.z; }

    };
21
                                                                          Line abc_to_line(ld a, ld b, ld c) {
22
                                                                      44
    struct Line3D {
                                                                             assert(!sgn(a) || !sgn(b));
23
                                                                      45
      Point3D s = \{0, 0, 0\}, e = \{0, 0, 0\};
                                                                            if(a == 0) return Line(Point(0, -c/b), Point(1, -c/b));
24
                                                                      46
      Line3D() = default;
                                                                             if(b == 0) return Line(Point(-c/a, 0), Point(-c/a, 1));
      Line3D(Point3D _s, Point3D _e) : s(_s), e(_e) {}
26
                                                                      48
                                                                            Point s(0, -c/b), e(1, (-c - a)/b), diff = e - s;
                                                                            return Line(s, s + diff/dist(diff));
27
                                                                      49
28
                                                                      50
    struct Segment3D : Line3D {
29
                                                                      51
                                                                           tuple<ld,ld,ld> line_to_abc(const Line& 1) {
30
      using Line3D::Line3D;
                                                                      52
                                                                            Point diff = l.e - l.s:
31
                                                                      53
                                                                            return {-diff.y, diff.x, -(diff ^ 1.s)};
                                                                      54
32
    auto dist2(const Point3D &a) { return a * a; }
    auto dist2(const Point3D &a, const Point3D &b) { return dist2(a
    auto dist(const Point3D &a) { return sqrt(dist2(a)); }
                                                                           Graph Theory
35
    auto dist(const Point3D &a, const Point3D &b) { return

    sqrt(dist2(a - b)); }

                                                                          Max Flow
    auto dist(const Point3D &a, const Line3D &l) { return dist((a -
     \leftrightarrow l.s) ^ (l.e - l.s)) / dist(l.s, l.e); }
                                                                          struct Edge {
    auto dist(const Point3D &p, const Segment3D &l) {
38
                                                                            int from, to, cap, remain;
      if (1.s == 1.e) return dist(p, 1.s);
      auto d = dist2(1.s, 1.e), t = min(d, max((1d)0, (p - 1.s) *)
     \hookrightarrow (l.e - l.s)));
                                                                          struct Dinic {
      return dist((p - 1.s) * d, (1.e - 1.s) * t) / d;
41
                                                                            vector<Edge> e;
                                                                            vector<vector<int>> g;
                                                                             vector<int> d, cur;
    Miscellaneous
                                                                            Dinic(int _n) : n(_n), g(n), d(n), cur(n) {}
                                                                      10
    tuple<int,int,ld> closest_pair(vector<Point> &p) {
                                                                             void add_edge(int u, int v, int c) {
                                                                               g[u].push_back((int)e.size());
      using Pt = pair<Point,int>;
                                                                      12
      int n = p.size();
                                                                      13
                                                                               e.push_back({u, v, c, c});
      assert(n > 1);
                                                                      14
                                                                               g[v].push_back((int)e.size());
      vector<Pt> pts(n), buf;
                                                                               e.push_back({v, u, 0, 0});
                                                                      15
      for (int i = 0; i < n; i++) pts[i] = {p[i], i};
      sort(pts.begin(), pts.end());
                                                                            11 max_flow(int s, int t) {
                                                                      17
      buf.reserve(n);
                                                                      18
                                                                               int inf = 1e9;
      auto cmp_y = [](const Pt& p1, const Pt& p2) { return
                                                                               auto bfs = [&]() {
                                                                      19

   p1.first.y < p2.first.y; };</pre>
                                                                                fill(d.begin(), d.end(), inf), fill(cur.begin(),
                                                                      20
      function<tuple<int,int,ld>(int, int)> recurse = [&](int 1, int

    cur.end(), 0);

    r) → tuple<int,int,ld> {
                                                                                 d[s] = 0;
                                                                      21
         int i = pts[1].second, j = pts[1 + 1].second;
                                                                                 vector<int> q{s}, nq;
                                                                      22
         ld d = dist(pts[1].first, pts[1 + 1].first);
                                                                                 for (int step = 1; q.size(); swap(q, nq), nq.clear(),
12
         if (r - 1 < 5) {

    step++) {
13
          for (int a = 1; a < r; a++) for (int b = a + 1; b < r;
                                                                                   for (auto& node : q) {
                                                                                    for (auto& edge : g[node]) {

→ b++) {

                                                                      25
             ld cur = dist(pts[a].first, pts[b].first);
                                                                                       int ne = e[edge].to;
15
            if (cur < d) { i = pts[a].second; j = pts[b].second; d _{27}
                                                                                       if (!e[edge].remain || d[ne] <= step) continue;</pre>
16
                                                                                       d[ne] = step, nq.push_back(ne);
       cur; }
                                                                                       if (ne == t) return true;
17
          sort(pts.begin() + 1, pts.begin() + r, cmp_y);
                                                                      30
18
                                                                      31
                                                                                   }
         else {
20
                                                                      32
           int mid = (1 + r)/2;
                                                                                 return false;
```

auto [li, lj, ldist] = recurse(l, mid);

struct Point3D {

ld x = pts[mid].first.x;

34

}:

```
function<int(int, int)> find = [&](int node, int limit) { 37
                                                                             11 calc(int s, int t) {
           if (node == t || !limit) return limit;
                                                                               int v = sz(g);
36
                                                                      38
           int flow = 0;
                                                                               H[s] = v;
           for (int i = cur[node]; i < g[node].size(); i++) {</pre>
                                                                               ec[t] = 1;
38
                                                                      40
             cur[node] = i;
                                                                      41
                                                                               vi co(2 * v);
39
             int edge = g[node][i], oe = edge ^ 1, ne = e[edge].to; 42
                                                                               co[0] = v - 1;
40
             if (!e[edge].remain || d[ne] != d[node] + 1) continue; 43
                                                                               rep(i, 0, v) cur[i] = g[i].data();
41
             if (int temp = find(ne, min(limit - flow,
                                                                               for (Edge& e : g[s]) addFlow(e, e.c);
        e[edge].remain))) {
                                                                      45
               e[edge].remain -= temp, e[oe].remain += temp, flow +=46
                                                                               for (int hi = 0;;) {
43
                                                                                 while (hs[hi].empty())
        temp;
                                                                      47
                                                                                   if (!hi--) return -ec[s];
44
             } else {
                                                                      48
               d[ne] = -1;
                                                                                 int u = hs[hi].back();
                                                                                 hs[hi].pop_back();
46
                                                                      50
47
             if (flow == limit) break;
                                                                      51
                                                                                 while (ec[u] > 0) // discharge u
           }
                                                                                   if (cur[u] == g[u].data() + sz(g[u])) {
48
                                                                      52
          return flow;
                                                                                     H[u] = 1e9;
49
                                                                      53
50
        };
                                                                      54
                                                                                     for (Edge& e : g[u])
         11 \text{ res} = 0;
                                                                                        if (e.c && H[u] > H[e.dest] + 1) H[u] = H[e.dest] +
51
                                                                      55
         while (bfs())
                                                                            \rightarrow 1, cur[u] = &e;
                                                                                     if (++co[H[u]], !--co[hi] && hi < v)
           while (int flow = find(s, inf)) res += flow;
53
                                                                      56
54
                                                                      57
                                                                                       rep(i, 0, v) if (hi < H[i] && H[i] < v)-- co[H[i]],
                                                                            \hookrightarrow H[i] = v + 1;
      }
55
    };
                                                                                     hi = H[u];
56
                                                                      58
                                                                                   } else if (cur[u]->c \&\& H[u] == H[cur[u]->dest] + 1)

    USAGE

                                                                                     addFlow(*cur[u], min(ec[u], cur[u]->c));
                                                                      60
    int main() {
                                                                                     ++cur[u];
                                                                      62
      int n, m, s, t;
                                                                      63
      cin >> n >> m >> s >> t;
                                                                      64
      Dinic dinic(n);
                                                                             bool leftOfMinCut(int a) { return H[a] >= sz(g); }
                                                                      65
      for (int i = 0, u, v, c; i < m; i++) {
        cin >> u >> v >> c;
         dinic.add_edge(u - 1, v - 1, c);
8
                                                                           Min-Cost Max-Flow
      cout << dinic.max_flow(s - 1, t - 1) << '\n';</pre>
9
                                                                           struct MinCostFlow {
                                                                             static constexpr int INF = 1e9;
                                                                       2
                                                                             const int n;
                                                                       3
    PushRelabel Max-Flow (faster)
                                                                             vector<tuple<int, int, int>> e;
                                                                       4
                                                                             vector<vector<int>> g;
                                                                             vector<int> h, dis, pre;
        https://github.com/kth-competitive-programming/kactl/blob/main/coibborlt/Agirjkst/Pa/sinite ksubeiinth t) {
    #define rep(i, a, b) for (int i = a; i < (b); ++i)
                                                                               dis.assign(n, INF);
    #define all(x) begin(x), end(x)
                                                                               pre.assign(n. -1):
                                                                       9
                                                                               priority_queue<pair<int, int>, vector<pair<int, int>>,
     #define sz(x) (int)(x).size()
    typedef long long 11;

    greater<>> que;

    typedef pair<int, int> pii;
                                                                               dis[s] = 0;
    typedef vector<int> vi;
                                                                      12
                                                                               que.emplace(0, s);
                                                                               while (!que.empty()) {
8
                                                                      13
    struct PushRelabel {
                                                                                 auto [d, u] = que.top();
                                                                      14
      struct Edge {
                                                                                 que.pop();
10
                                                                      15
         int dest, back;
                                                                                 if (dis[u] != d) continue;
                                                                                 for (int i : g[u]) {
12
        11 f, c;
                                                                      17
                                                                      18
                                                                                   auto [v, f, c] = e[i];
13
                                                                                   if (c > 0 \&\& dis[v] > d + h[u] - h[v] + f) {
14
      vector<vector<Edge>> g;
                                                                      19
      vector<11> ec;
                                                                                     dis[v] = d + h[u] - h[v] + f;
15
                                                                      20
      vector<Edge*> cur;
                                                                                     pre[v] = i;
                                                                                     que.emplace(dis[v], v);
      vector<vi> hs;
17
                                                                      22
18
      PushRelabel(int n) : g(n), ec(n), cur(n), hs(2 * n), H(n) \{\} 24
                                                                                 }
19
                                                                               }
20
                                                                      25
      void addEdge(int s, int t, ll cap, ll rcap = 0) {
                                                                               return dis[t] != INF;
21
         if (s == t) return;
22
                                                                      27
         g[s].push_back({t, sz(g[t]), 0, cap});
                                                                             MinCostFlow(int _n) : n(_n), g(n) {}
23
                                                                      28
        g[t].push_back({s, sz(g[s]) - 1, 0, rcap});
                                                                             void addEdge(int u, int v, int f, int c) {
24
                                                                      29
25
                                                                      30
                                                                               g[u].push_back((int)e.size());
                                                                               e.emplace_back(v, f, c);
26
                                                                      31
                                                                               g[v].push_back((int)e.size());
      void addFlow(Edge& e, ll f) {
27
                                                                      32
         Edge& back = g[e.dest][e.back];
28
                                                                      33
                                                                               e.emplace_back(u, -f, 0);
         if (!ec[e.dest] && f) hs[H[e.dest]].push_back(e.dest);
29
                                                                      34
                                                                             pair<int, int> minCostMaxFlow(const int s, const int t) {
         e.f += f;
30
                                                                      35
         e.c -= f;
                                                                               int flow = 0, cost = 0;
31
                                                                      36
32
         ec[e.dest] += f;
                                                                      37
                                                                               h.assign(n, 0);
33
         back.f -= f;
                                                                      38
                                                                               while (dijkstra(s, t)) {
        back.c += f;
                                                                                 for (int i = 0; i < n; ++i) h[i] += dis[i];</pre>
34
                                                                      39
         ec[back.dest] -= f;
                                                                                 for (int i = t; i != s; i = get<0>(e[pre[i] ^ 1])) {
                                                                      40
                                                                                   --get<2>(e[pre[i]]);
      }
36
                                                                      41
```

```
\leftrightarrow exist)
43
44
          ++flow;
                                                                            auto augment = [&](int node) {
          cost += h[t];
                                                                              while (!que.empty()) que.pop();
45
                                                                   27
46
                                                                              iota(f.begin(), f.end(), 0);
                                                                   28
        return {flow, cost};
47
                                                                   29
                                                                              // vis = 0 corresponds to inner vertices, vis = 1
                                                                         48
    };
                                                                              fill(vis.begin(), vis.end(), -1);
                                                                              que.push(node);
                                                                   31
                                                                              vis[node] = 1, dep[node] = 0;
                                                                   32
    Heavy-Light Decomposition
                                                                   33
                                                                              while (!que.empty()) {
                                                                                int u = que.front();
                                                                   34
    int root = 0, cur = 0;
                                                                                que.pop();
    vector<int> parent(n), deep(n), hson(n, -1), top(n), sz(n),
                                                                                for (auto v : e[u]) {
                                                                   36
     \rightarrow dfn(n, -1);
                                                                   37
                                                                                  if (vis[v] == -1) {
    function<int(int, int, int)> dfs = [&](int node, int fa, int
                                                                                    vis[v] = 0, link[v] = u, dep[v] = dep[u] + 1;
                                                                   38
     → dep) {
                                                                                    // found an augmenting path
                                                                   39
      deep[node] = dep, sz[node] = 1, parent[node] = fa;
                                                                   40
                                                                                    if (match[v] == -1) {
      for (auto &ne : g[node]) {
                                                                                      for (int x = v, y = u, temp; y != -1; x = temp, y
                                                                   41
        if (ne == fa) continue;
                                                                            = x == -1 ? -1 : link[x]) {
        sz[node] += dfs(ne, node, dep + 1);
                                                                                        temp = match[y], match[x] = y, match[y] = x;
        if (hson[node] == -1|| sz[ne] > sz[hson[node]]) hson[node]
                                                                                      }
     → ne:
                                                                   44
                                                                                      return;
      }
                                                                   45
      return sz[node];
10
                                                                                    vis[match[v]] = 1, dep[match[v]] = dep[u] + 2;
                                                                   46
11
                                                                                    que.push(match[v]);
                                                                   47
    function<void(int, int)> dfs2 = [&](int node, int t) {
12
                                                                                  } else if (vis[v] == 1 && find(v) != find(u)) {
      top[node] = t, dfn[node] = cur++;
13
                                                                   49
                                                                                    // found a blossom
      if (hson[node] == -1) return;
                                                                                    int p = lca(u, v);
                                                                   50
      dfs2(hson[node], t);
15
                                                                   51
                                                                                    blossom(u, v, p), blossom(v, u, p);
      for (auto &ne : g[node]) {
                                                                   52
        if (ne == parent[node] || ne == hson[node]) continue;
17
                                                                                }
        dfs2(ne, ne);
18
                                                                              }
                                                                   54
19
      }
                                                                            };
                                                                   55
    };
20
                                                                            // find a maximal matching greedily (decrease constant)
                                                                   56
    // read in graph as vector<vector<int>> g(n)
                                                                            auto greedy = [\&]() {
                                                                   57
    dfs(root, -1, 0), dfs2(root, root);
                                                                              for (int u = 0; u < n; ++u) {
                                                                                if (match[u] != -1) continue;
                                                                   59
       • USAGE: get LCA
                                                                                for (auto v : e[u]) {
                                                                   60
                                                                                  if (match[v] == -1) {
    function<int(int, int)> lca = [&](int x, int y) {
                                                                   61
                                                                                    match[u] = v, match[v] = u;
      while (top[x] != top[y]) {
                                                                   62
        if (deep[top[x]] < deep[top[y]]) swap(x, y);</pre>
                                                                                    break;
                                                                   64
        x = parent[top[x]];
                                                                   65
                                                                                }
                                                                              }
      return deep[x] < deep[y] ? x : y;</pre>
                                                                   66
                                                                            };
                                                                   67
                                                                            greedy();
                                                                   68
                                                                            for (int u = 0; u < n; ++u)
                                                                   69
    General Unweight Graph Matching
                                                                              if (match[u] == -1) augment(u);
                                                                   71
                                                                            return match;
       • Complexity: O(n^3) (?)
                                                                   73
                                                                        };
    struct BlossomMatch {
2
      int n;
3
      vector<vector<int>> e;
                                                                        Maximum Bipartite Matching
      BlossomMatch(int _n) : n(_n), e(_n) {}
      void add_edge(int u, int v) { e[u].push_back(v),
                                                                          • Needs dinic, complexity \approx O(n + m\sqrt{n})

    e[v].push_back(u); }

      vector<int> find_matching() {
                                                                        struct BipartiteMatch {
        vector<int> match(n, -1), vis(n), link(n), f(n), dep(n);
                                                                          int 1, r;
        function < int(int) > find = [\&](int x) { return f[x] == x ? x_3}
                                                                          Dinic dinic = Dinic(0);
        : (f[x] = find(f[x])); };
                                                                          BipartiteMatch(int _1, int _r) : 1(_1), r(_r) {
        auto lca = [&](int u, int v) {
9
                                                                            dinic = Dinic(1 + r + 2);
                                                                    5
          u = find(u), v = find(v);
10
                                                                            for (int i = 1; i <= 1; i++) dinic.add_edge(0, i, 1);
          while (u != v) {
                                                                            for (int i = 1; i <= r; i++) dinic.add_edge(1 + i, 1 + r +
            if (dep[u] < dep[v]) swap(u, v);
12
                                                                            1, 1);
            u = find(link[match[u]]);
13
                                                                          7
          }
                                                                          void add_edge(int u, int v) { dinic.add_edge(u + 1, 1 + v + 1,
                                                                    9
          return u;
15
                                                                         16
                                                                          ll max_matching() { return dinic.max_flow(0, 1 + r + 1); }
                                                                   10
17
        queue<int> que;
                                                                   11
        auto blossom = [&](int u, int v, int p) {
18
          while (find(u) != p) {
19
20
            link[u] = v, v = match[u];
                                                                        2-SAT and Strongly Connected Components
21
            if (vis[v] == 0) vis[v] = 1, que.push(v);
            f[u] = f[v] = p, u = link[v];
                                                                        void scc(vector<vector<int>>& g, int* idx) {
22
          }
                                                                          int n = g.size(), ct = 0;
```

// find an augmenting path starting from u and augment (if

42

};

24

++get<2>(e[pre[i] ^ 1]);

int out[n]:

```
vector<int> ginv[n];
                                                                     12
                                                                              if(deg[u] > deg[v] \mid \mid (deg[u] == deg[v] \&\& u > v))
      memset(out, -1, sizeof out);
                                                                                swap(u, v);
                                                                     13
      memset(idx, -1, n * sizeof(int));
                                                                              g[u].push_back(v);
      function<void(int)> dfs = [&](int cur) {
                                                                     15
         out[cur] = INT_MAX;
                                                                            vector<int> flag(n);
                                                                     16
        for(int v : g[cur]) {
                                                                           for(int i = 0; i < n; i++) {</pre>
9
                                                                     17
           ginv[v].push_back(cur);
                                                                             for(int v : g[i]) flag[v] = 1;
10
                                                                     18
                                                                              for(int v : g[i]) for(int u : g[v]) {
11
           if(out[v] == -1) dfs(v);
                                                                                if(flag[u]) f(i, v, u);
12
                                                                     20
13
        ct++; out[cur] = ct;
                                                                     21
14
      };
                                                                     22
                                                                              for(int v : g[i]) flag[v] = 0;
      vector<int> order;
15
                                                                     23
                                                                         }
      for(int i = 0; i < n; i++) {
        order.push_back(i);
17
18
         if(out[i] == -1) dfs(i);
                                                                         Tarjan
      }
19
      sort(order.begin(), order.end(), [&](int& u, int& v) {
20
                                                                            • shrink all circles into points (2-edge-connected-component)
21
        return out[u] > out[v];
22
      }):
                                                                         int cnt = 0, now = 0;
23
      ct = 0;
                                                                         vector<ll> dfn(n, -1), low(n), belong(n, -1), stk;
      stack<int> s;
24
                                                                         function \langle void(11, 11) \rangle tarjan = [&](11 node, 11 fa) {
      auto dfs2 = [&](int start) {
                                                                            dfn[node] = low[node] = now++, stk.push_back(node);
26
        s.push(start);
                                                                           for (auto& ne : g[node]) {
        while(!s.empty()) {
27
                                                                              if (ne == fa) continue;
          int cur = s.top();
28
                                                                              if (dfn[ne] == -1) {
          s.pop();
29
                                                                               tarjan(ne, node);
                                                                      8
          idx[cur] = ct;
                                                                      9
                                                                                low[node] = min(low[node], low[ne]);
          for(int v : ginv[cur])
31
                                                                             } else if (belong[ne] == -1) {
                                                                     10
             if(idx[v] == -1) s.push(v);
32
                                                                     11
                                                                                low[node] = min(low[node], dfn[ne]);
        }
33
                                                                     12
      };
34
                                                                     13
      for(int v : order) {
                                                                     14
                                                                           if (dfn[node] == low[node]) {
        if(idx[v] == -1) {
36
                                                                             while (true) {
                                                                     15
37
          dfs2(v);
                                                                                auto v = stk.back();
                                                                     16
38
           ct++;
                                                                               belong[v] = cnt;
                                                                     17
39
                                                                                stk.pop_back();
40
                                                                     19
                                                                                if (v == node) break;
41
                                                                     20
42
                                                                     21
                                                                              ++cnt;
    // 0 => impossible, 1 => possible
43
                                                                           }
                                                                     22
    pair<int, vector<int>> sat2(int n, vector<pair<int,int>>&
                                                                         };
     vector<int> ans(n);
45
                                                                            • 2-vertex-connected-component / Block forest
46
      vector<vector<int>> g(2*n + 1);
      for(auto [x, y] : clauses) {
                                                                         int cnt = 0, now = 0;
47
        x = x < 0 ? -x + n : x;
                                                                         vector<vector<1l>> e1(n);
48
        y = y < 0 ? -y + n : y;
                                                                         vector<ll> dfn(n, -1), low(n), stk;
49
         int nx = x \le n ? x + n : x - n;
                                                                         function<void(11)> tarjan = [&](11 node) {
50
         int ny = y <= n ? y + n : y - n;</pre>
                                                                            dfn[node] = low[node] = now++, stk.push_back(node);
         g[nx].push_back(y);
                                                                           for (auto& ne : g[node]) {
52
53
        g[ny].push_back(x);
                                                                             if (dfn[ne] == -1) {
      }
54
                                                                               tarjan(ne);
      int idx[2*n + 1];
                                                                                low[node] = min(low[node], low[ne]);
55
                                                                     9
      scc(g, idx);
                                                                                if (low[ne] == dfn[node]) {
56
                                                                     10
      for(int i = 1; i <= n; i++) {
                                                                                 e1.push_back({});
57
                                                                     11
         if(idx[i] == idx[i + n]) return {0, {}};
                                                                     12
                                                                                  while (true) {
         ans[i - 1] = idx[i + n] < idx[i];
                                                                                   auto x = stk.back();
59
                                                                     13
60
                                                                     14
                                                                                    stk.pop_back();
61
      return {1, ans};
                                                                                    e1[n + cnt].push_back(x);
                                                                     15
                                                                                    // e1[x].push_back(n + cnt); // undirected
62
                                                                     16
                                                                                    if (x == ne) break;
                                                                     18
    Enumerating Triangles
                                                                                  e1[node].push_back(n + cnt);
                                                                     19
                                                                                  // e1[n + cnt].push_back(node); // undirected
                                                                     20
       • Complexity: O(n + m\sqrt{m})
                                                                     21
                                                                                  cnt++:
                                                                                }
    void enumerate_triangles(vector<pair<int,int>>& edges,
                                                                             } else {
                                                                     23

  function < void(int, int, int) > f) {
                                                                     24
                                                                                low[node] = min(low[node], dfn[ne]);
      int n = 0;
                                                                     25
      for(auto [u, v] : edges) n = max({n, u + 1, v + 1});
                                                                           }
                                                                     26
      vector<int> deg(n);
                                                                         };
      vector<int> g[n];
      for(auto [u, v] : edges) {
        deg[u]++;
                                                                         Kruskal reconstruct tree
         deg[v]++;
                                                                      1 int n. m:
```

cin >> \_n >> m; // \_n: # of node, m: # of edge

3 int n = 2 \* \_n - 1; // root: n-1

9

for(auto [u, v] : edges) {

if(u == v) continue;

```
vector<array<int, 3>> edges(m);
                                                                     26 }:
    for (auto& [w, u, v] : edges) {
      cin >> u >> v >> w, u--, v--;
                                                                             • large mod (for NTT to do FFT in ll range without modulo)
    sort(edges.begin(), edges.end());
8
                                                                          using ll = long long;
    vector<int> p(n);
9
                                                                          using i128 = __int128;
    iota(p.begin(), p.end(), 0);
10
                                                                          constexpr i128 MOD = 9223372036737335297;
    function \langle int(int) \rangle find = [&](int x) { return p[x] == x ? x :
     \hookrightarrow (p[x] = find(p[x])); };
                                                                          constexpr i128 norm(i128 x) { return x < 0 ? (x + MOD) \% MOD : x
    auto merge = [\&] (int x, int y) { p[find(x)] = find(y); };

→ % MOD: }

    vector<vector<int>> g(n);
13
                                                                          {\tt template} \ {\tt <typename} \ {\tt T>}
    vector<int> val(m);
14
                                                                          constexpr T power(T a, i128 b, T res = 1) {
    val.reserve(n);
                                                                            for (; b; b /= 2, (a *= a) \%= MOD)
    for (auto [w, u, v] : edges) {
16
                                                                              if (b & 1) (res *= a) %= MOD;
                                                                      9
      u = find(u), v = find(v);
                                                                            return res;
                                                                      10
      if (u == v) continue;
18
                                                                      11
      val.push_back(w);
19
                                                                     12
                                                                          struct Z {
      int node = (int)val.size() - 1;
20
                                                                            i128 x;
                                                                      13
      g[node].push_back(u), g[node].push_back(v);
21
                                                                            constexpr Z(i128 _x = 0) : x(norm(_x)) {}
                                                                     14
22
      merge(u, node), merge(v, node);
                                                                            Z operator-() const { return Z(norm(MOD - x)); }
                                                                            Z inv() const { return power(*this, MOD - 2); }
                                                                     16
                                                                             // auto operator<=>(const Z&) const = default;
                                                                      17
                                                                            Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
                                                                      18
    Math

    *this; }

                                                                            Z \& operator += (const Z \& rhs) \{ return x = norm(x + rhs.x), \}

→ *this: }

    Inverse
                                                                            Z &operator==(const Z &rhs) { return x = norm(x - rhs.x),
                                                                      20
    ll inv(ll a, ll m) { return a == 1 ? 1 : ((m - m / a) * inv(m \% _{21}

    *this; }

                                                                            Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
     \rightarrow a, m) % m); }
                                                                            Z &operator%=(const i128 &rhs) { return x %= rhs, *this; }
    // or
                                                                            friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs; }
                                                                      23
    power(a, MOD - 2)
                                                                      24
                                                                            friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs; }
                                                                            friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs; }

    USAGE: get factorial

                                                                            friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs; }
                                                                      26
    vector<ll> f(MAX_N, 1), rf(MAX_N, 1);
                                                                            friend Z operator%(Z lhs, const i128 &rhs) { return lhs %=
    for (int i = 1; i < MAX_N; i++) f[i] = (f[i - 1] * i) % MOD;
    for (int i = 1; i < MAX_N; i++) rf[i] = (rf[i - 1] * inv(i,
                                                                          };
     \hookrightarrow MOD)) % MOD;
    // or (the later one should be preferred
                                                                             • fastest mod class! be careful with overflow, only use when
    vector<ll> f(MAX_N, 1), rf(MAX_N, 1);
                                                                               the time limit is tight
    for (int i = 2; i < MAX_N; i++) f[i] = f[i - 1] * i % MOD;
    rf[MAX_N - 1] = power(f[MAX_N - 1], MOD - 2);
                                                                          constexpr int MOD = 998244353;
    for (int i = MAX_N - 2; i > 1; i--) rf[i] = rf[i + 1] * (i + 1)\frac{1}{2}

→ % MOD;

                                                                          constexpr int norm(int x) {
                                                                            if (x < 0) x += MOD;
    Mod Class
                                                                            if (x >= MOD) x -= MOD;
                                                                            return x;
    constexpr 11 norm(11 x) { return (x % MOD + MOD) % MOD; }
    template <typename T>
                                                                          template <typename T>
    constexpr T power(T a, ll b, T res = 1) \{
                                                                      9
                                                                          constexpr T power(T a, int b, T res = 1) {
       for (; b; b /= 2, (a *= a) %= MOD)
                                                                            for (; b; b /= 2, (a *= a) \%= MOD)
                                                                      10
         if (b & 1) (res *= a) %= MOD;
                                                                              if (b & 1) (res *= a) %= MOD;
                                                                      11
      return res;
                                                                            return res;
6
                                                                      12
    }
                                                                          }
    struct Z {
                                                                          struct Z {
                                                                      14
                                                                      15
       constexpr Z(11 _x = 0) : x(norm(_x)) \{ \}
                                                                            constexpr Z(int _x = 0) : x(norm(_x)) {}
                                                                      16
       // auto operator <=> (const Z &) const = default; // cpp20 only17
                                                                            // constexpr auto operator <=> (const Z &) const = default; //
11
      Z operator-() const { return Z(norm(MOD - x)); }

→ cpp20 only

                                                                            constexpr Z operator-() const { return Z(norm(MOD - x)); }
      Z inv() const { return power(*this, MOD - 2); }
13
                                                                      18
      Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
                                                                            constexpr Z inv() const { return power(*this, MOD - 2); }
                                                                      19

    *this; }

                                                                            constexpr Z &operator*=(const Z &rhs) { return x = ll(x) *
                                                                      20
      Z \& perator = (const Z \& rhs) \{ return x = norm(x + rhs.x),

    rhs.x % MOD, *this; }

15
                                                                           constexpr Z &operator+=(const Z &rhs) { return x = norm(x +

    *this; }

                                                                      21
      Z &operator-=(const Z &rhs) { return x = norm(x - rhs.x),

    rhs.x), *this; }

16
                                                                            constexpr Z &operator==(const Z &rhs) { return x = norm(x -
      Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }

    rhs.x), *this: }

17
      Z &operator%=(const ll &rhs) { return x %= rhs, *this; }
                                                                            constexpr Z &operator/=(const Z &rhs) { return *this *=
      friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs; }
19
                                                                           → rhs.inv(): }
      friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs; 24
                                                                            constexpr Z &operator %= (const ll &rhs) { return x %= rhs,
20
      friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs; }

    *this; }

      friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs; 2/s
                                                                            constexpr friend Z operator*(Z lhs, const Z &rhs) { return lhs
22
      friend Z operator%(Z lhs, const ll &rhs) { return lhs %= rhs;
                                                                            constexpr friend Z operator+(Z lhs, const Z &rhs) { return lhs
      friend auto &operator>>(istream &i, Z &z) { return i >> z.x; }
                                                                           24
                                                                            constexpr friend Z operator-(Z lhs, const Z &rhs) { return lhs
      friend auto &operator<<(ostream &o, const Z &z) { return o <∞7
     \hookrightarrow z.x; }
                                                                           → -= rhs; }
```

```
constexpr friend Z operator/(Z lhs, const Z &rhs) { return lhs
                                                                                   auto x = p[i + j], y = wk * p[i + j + mid];
                                                                                   p[i + j] = x + y, p[i + j + mid] = x - y;
     constexpr friend Z operator%(Z lhs, const ll &rhs) { return 21
     → lhs %= rhs: }
      friend auto &operator>>(istream &i, Z &z) { return i >> z.x; 2/3
                                                                             }
30
      friend auto &operator<<(ostream &o, const Z &z) { return o <0.4
                                                                             if (inv == 1) {
                                                                               for (int i = 0; i < len; i++) p[i].real(p[i].real() /</pre>
                                                                             len);
                                                                             }
                                                                    26
                                                                           };
                                                                    27
    NTT, FFT, FWT
                                                                           fft(a, 0), fft(b, 0);
                                                                    28
                                                                           for (int i = 0; i < len; i++) a[i] = a[i] * b[i];
                                                                    29
                                                                           fft(a, 1);
       ntt
                                                                    30
                                                                           a.resize(n + m - 1);
                                                                    31
    void ntt(vector<Z>& a, int f) {
                                                                           vector<double> res(n + m - 1);
      int n = int(a.size());
                                                                           for (int i = 0; i < n + m - 1; i++) res[i] = a[i].real();
                                                                    33
      vector<Z> w(n);
                                                                           return res;
      vector<int> rev(n);
                                                                         };
      for (int i = 0; i < n; i++) rev[i] = (rev[i / 2] / 2) | ((i &
     \leftrightarrow 1) * (n / 2));
                                                                         Polynomial Class
      for (int i = 0; i < n; i++) {
        if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
                                                                         using ll = long long;
                                                                         constexpr 11 MOD = 998244353;
      Z wn = power(f ? (MOD + 1) / 3 : 3, (MOD - 1) / n);
      w[0] = 1:
10
                                                                         11 norm(11 x) { return (x % MOD + MOD) % MOD; }
      for (int i = 1; i < n; i++) w[i] = w[i - 1] * wn;
11
                                                                         template <class T>
      for (int mid = 1; mid < n; mid *= 2) {
12
                                                                         T power(T a, 11 b, T res = 1) {
        for (int i = 0; i < n; i += 2 * mid) {
13
                                                                           for (; b; b /= 2, (a *= a) \%= MOD)
          for (int j = 0; j < mid; j++) {
14
                                                                             if (b & 1) (res \ast= a) \%= MOD;
            Z x = a[i + j], y = a[i + j + mid] * w[n / (2 * mid) *
15
                                                                     9
                                                                           return res:
                                                                     10
            a[i + j] = x + y, a[i + j + mid] = x - y;
16
                                                                    11
17
                                                                         struct Z {
        }
18
                                                                    13
                                                                           11 x;
      }
19
                                                                           Z(11 _x = 0) : x(norm(_x)) {}
                                                                     14
20
      if (f) {
                                                                           // auto operator<=>(const Z &) const = default;
                                                                    15
        Z iv = power(Z(n), MOD - 2);
21
                                                                    16
                                                                           Z operator-() const { return Z(norm(MOD - x)); }
22
        for (auto\& x : a) x *= iv;
                                                                    17
                                                                           Z inv() const { return power(*this, MOD - 2); }
23
                                                                           Z &operator*=(const Z &rhs) { return x = x * rhs.x % MOD,
                                                                    18
    }
24
                                                                            *this; }
       • USAGE: Polynomial multiplication
                                                                    19
                                                                          Z \& perator += (const Z \& rhs) \{ return x = norm(x + rhs.x) \}

    *this; }

    vector<Z> mul(vector<Z> a, vector<Z> b) {
                                                                           Z &operator-=(const Z &rhs) { return x = norm(x - rhs.x),
                                                                    20
      int n = 1, m = (int)a.size() + (int)b.size() - 1;
                                                                          → *this: }
2
      while (n < m) n *= 2;
                                                                           Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
                                                                     ^{21}
                                                                           Z &operator%=(const ll &rhs) { return x %= rhs, *this; }
      a.resize(n), b.resize(n);
                                                                    22
                                                                           friend Z operator*(Z lhs, const Z &rhs) { return lhs *= rhs; }
      ntt(a, 0), ntt(b, 0);
      for (int i = 0; i < n; i++) a[i] *= b[i];
                                                                           friend Z operator+(Z lhs, const Z &rhs) { return lhs += rhs; }
                                                                    24
      ntt(a, 1);
                                                                    25
                                                                           friend Z operator-(Z lhs, const Z &rhs) { return lhs -= rhs; }
                                                                           friend Z operator/(Z lhs, const Z &rhs) { return lhs /= rhs; }
      a.resize(m);
                                                                     26
      return a:
                                                                           friend Z operator%(Z lhs, const ll &rhs) { return lhs %= rhs;
                                                                    27
                                                                           friend auto &operator>>(istream &i, Z &z) { return i >> z.x; }
       • FFT (should prefer NTT, only use this when input is not
                                                                           friend auto &operator << (ostream &o, const Z &z) { return o <<
         integer)
                                                                          \hookrightarrow z.x; }
    const double PI = acos(-1);
    auto mul = [&](const vector<double>& aa, const vector<double>& 32
                                                                         void ntt(vector<Z> &a, int f) {
     → bb) {
                                                                    33
                                                                           int n = (int)a.size();
      int n = (int)aa.size(), m = (int)bb.size(), bit = 1;
                                                                           vector<Z> w(n);
                                                                    34
      while ((1 << bit) < n + m - 1) bit++;
                                                                           vector<int> rev(n);
                                                                    35
      int len = 1 << bit;</pre>
                                                                           for (int i = 0; i < n; i++) rev[i] = (rev[i / 2] / 2) | ((i &
      vector<complex<double>> a(len), b(len);
                                                                          \leftrightarrow 1) * (n / 2));
      vector<int> rev(len);
                                                                           for (int i = 0; i < n; i++)
      for (int i = 0; i < n; i++) a[i].real(aa[i]);</pre>
                                                                           if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
                                                                    38
      for (int i = 0; i < m; i++) b[i].real(bb[i]);</pre>
                                                                           Z wn = power(f ? (MOD + 1) / 3 : 3, (MOD - 1) / n);
                                                                    39
                                                                           w[0] = 1;
      for (int i = 0; i < len; i++) rev[i] = (rev[i >> 1] >> 1) | 40
     for (int i = 1; i < n; i++) w[i] = w[i - 1] * wn;
                                                                    41
      auto fft = [&](vector<complex<double>>& p, int inv) {
                                                                           for (int mid = 1; mid < n; mid *= 2) {</pre>
11
        for (int i = 0; i < len; i++)
                                                                             for (int i = 0; i < n; i += 2 * mid) {
12
                                                                    43
          if (i < rev[i]) swap(p[i], p[rev[i]]);</pre>
                                                                               for (int j = 0; j < mid; j++) {
13
                                                                    44
                                                                                 Z x = a[i + j], y = a[i + j + mid] * w[n / (2 * mid) *
        for (int mid = 1; mid < len; mid *= 2) {
14
          auto w1 = complex<double>(cos(PI / mid), (inv ? -1 : 1) *
15

    sin(PI / mid));
                                                                                 a[i + j] = x + y, a[i + j + mid] = x - y;
          for (int i = 0; i < len; i += mid * 2) {
                                                                    47
16
            auto wk = complex<double>(1, 0);
                                                                             }
17
            for (int j = 0; j < mid; j++, wk = wk * w1) {
                                                                           }
18
                                                                    49
```

```
50
       if (f) {
                                                                      122
                                                                                int k = 1;
         Z iv = power(Z(n), MOD - 2);
                                                                                while (k < m) {
51
                                                                      123
                                                                                  k *= 2;
         for (int i = 0; i < n; i++) a[i] *= iv;
52
       }
                                                                                  x = (x * (Poly({2}) - modxk(k) * x)).modxk(k);
53
                                                                      125
     }
                                                                      126
54
55
                                                                      127
                                                                                return x.modxk(m);
     struct Poly {
56
                                                                      128
                                                                              Poly log(int m) const { return (deriv() *
       vector<Z> a;

    inv(m)).integr().modxk(m); }

       Poly() {}
58
       Poly(const vector\langle Z \rangle \&_a) : a(_a) {}
                                                                              Poly exp(int m) const {
59
                                                                      130
       int size() const { return (int)a.size(); }
                                                                                Poly x(\{1\});
60
                                                                      131
       void resize(int n) { a.resize(n); }
                                                                                int k = 1;
61
                                                                      132
       Z operator[](int idx) const {
                                                                                while (k < m) {
                                                                      133
         if (idx < 0 || idx >= size()) return 0;
                                                                                  k *= 2:
63
                                                                      134
 64
         return a[idx];
                                                                      135
                                                                                  x = (x * (Poly(\{1\}) - x.log(k) + modxk(k))).modxk(k);
65
                                                                      136
       Z &operator[](int idx) { return a[idx]; }
                                                                                return x.modxk(m);
66
                                                                      137
67
       Poly mulxk(int k) const {
                                                                      138
         auto b = a;
                                                                              Poly pow(int k, int m) const {
68
                                                                      139
69
         b.insert(b.begin(), k, 0);
                                                                       140
                                                                                int i = 0;
                                                                                while (i < size() && a[i].x == 0) i++;
70
         return Poly(b);
                                                                      141
71
                                                                                if (i == size() || 1LL * i * k >= m) {
                                                                                  return Poly(vector<Z>(m));
       Poly modxk(int k) const { return Poly(vector<Z>(a.begin(), 143
72

    a.begin() + min(k, size()))); }

                                                                       144
       Poly divxk(int k) const {
                                                                                Z v = a[i];
 73
                                                                       145
                                                                                auto f = divxk(i) * v.inv();
         if (size() <= k) return Poly();</pre>
74
                                                                      146
         return Poly(vector<Z>(a.begin() + k, a.end()));
                                                                                return (f.log(m - i * k) * k).exp(m - i * k).mulxk(i * k) *
 75
76
                                                                                power(v, k);
       friend Poly operator+(const Poly &a, const Poly &b) {
77
                                                                      148
78
         vector<Z> res(max(a.size(), b.size()));
                                                                       149
                                                                              Poly sqrt(int m) const {
         for (int i = 0; i < (int)res.size(); i++) res[i] = a[i] + 150
                                                                                Poly x(\{1\});
79
                                                                                 int k = 1;
         return Polv(res):
                                                                                while (k < m) {
 80
                                                                       152
                                                                       153
                                                                                  k *= 2;
81
       friend Poly operator-(const Poly &a, const Poly &b) {
                                                                                  x = (x + (modxk(k) * x.inv(k)).modxk(k)) * ((MOD + 1) /
82
                                                                      154
         vector<Z> res(max(a.size(), b.size()));
                                                                                2);
83
         for (int i = 0; i < (int)res.size(); i++) res[i] = a[i] - 155
                                                                                }
         b[i]:
                                                                                return x.modxk(m);
                                                                       156
         return Poly(res);
 85
                                                                       157
                                                                              Poly mulT(Poly b) const {
 86
                                                                      158
       friend Poly operator*(Poly a, Poly b) {
                                                                                if (b.size() == 0) return Poly();
87
                                                                      159
         if (a.size() == 0 || b.size() == 0) return Poly();
                                                                                int n = b.size();
                                                                       160
         int n = 1, m = (int)a.size() + (int)b.size() - 1;
                                                                                reverse(b.a.begin(), b.a.end());
                                                                      161
 89
         while (n < m) n *= 2;
                                                                       162
                                                                                return ((*this) * b).divxk(n - 1);
         a.resize(n), b.resize(n);
91
                                                                      163
                                                                              Poly divmod(Poly b) const {
         ntt(a.a, 0), ntt(b.a, 0);
92
                                                                      164
         for (int i = 0; i < n; i++) a[i] *= b[i];
                                                                      165
                                                                                auto n = size(), m = b.size();
93
                                                                                auto t = *this;
         ntt(a.a, 1);
94
                                                                      166
         a.resize(m);
                                                                                reverse(t.a.begin(), t.a.end());
95
                                                                       167
                                                                                reverse(b.a.begin(), b.a.end());
96
         return a;
                                                                      168
97
                                                                                Poly res = (t * b.inv(n)).modxk(n - m + 1);
       friend Poly operator*(Z a, Poly b) \{
98
                                                                      170
                                                                                reverse(res.a.begin(), res.a.end());
         for (int i = 0; i < (int)b.size(); i++) b[i] *= a;
                                                                                return res;
99
                                                                      171
         return b:
100
                                                                       172
                                                                              vector<Z> eval(vector<Z> x) const {
101
                                                                      173
       friend Poly operator*(Poly a, Z b) {
                                                                                if (size() == 0) return vector<Z>(x.size(), 0);
102
         for (int i = 0; i < (int)a.size(); i++) a[i] *= b;
103
                                                                      175
                                                                                const int n = max(int(x.size()), size());
                                                                                vector<Poly> q(4 * n);
104
                                                                       176
105
                                                                                vector<Z> ans(x.size());
                                                                       177
       Poly & operator += (Poly b) { return (*this) = (*this) + b; } 178
                                                                                x.resize(n);
106
       Poly &operator = (Poly b) { return (*this) = (*this) - b; } 179
                                                                                function<void(int, int, int)> build = [&](int p, int 1, int
107
108
       Poly &operator*=(Poly b) { return (*this) = (*this) * b; }
                                                                             Poly deriv() const {
                                                                                  if (r - 1 == 1) {
109
                                                                      180
                                                                                    q[p] = Poly(\{1, -x[1]\});
110
         if (a.empty()) return Poly();
                                                                      181
         vector<Z> res(size() - 1);
                                                                                  } else {
111
                                                                      182
         for (int i = 0; i < size() - 1; ++i) res[i] = (i + 1) * a[is3
                                                                                     int m = (1 + r) / 2;
                                                                                     build(2 * p, 1, m), build(2 * p + 1, m, r);
         + 1]:
                                                                      184
113
         return Poly(res);
                                                                                     q[p] = q[2 * p] * q[2 * p + 1];
114
                                                                      186
       Poly integr() const {
                                                                                };
                                                                      187
115
         vector<Z> res(size() + 1);
                                                                                build(1, 0, n);
116
         for (int i = 0; i < size(); ++i) res[i + 1] = a[i] / (i + 189
                                                                                auto work = [&] (auto self, int p, int l, int r, const Poly
117
                                                                                %num) -> void {
         1);
                                                                                  if (r - 1 == 1) {
118
         return Poly(res);
                                                                      190
                                                                                    if (1 < int(ans.size())) ans[1] = num[0];</pre>
119
                                                                      191
       Poly inv(int m) const {
                                                                      192
                                                                                  } else {
120
         Poly x({a[0].inv()});
                                                                                     int m = (1 + r) / 2;
121
```

```
194
             self(self, 2 * p, 1, m, num.mulT(q[2 * p + 1]).modxk(m 7
                                                                           int gaussian_elimination(vector<vector<T>> &a, int limit) {
      → 1));
                                                                                if (a.empty() || a[0].empty()) return -1;
             self(self, 2 * p + 1, m, r, num.mulT(q[2 * p]).modxk(r 9
                                                                              int h = (int)a.size(), w = (int)a[0].size(), r = 0;
195
                                                                              for (int c = 0; c < limit; c++) {</pre>
        m)):
           }
                                                                                int id = -1;
196
                                                                       11
         };
                                                                                for (int i = r; i < h; i++) {
197
                                                                       12
         work(work, 1, 0, n, mulT(q[1].inv(n)));
                                                                                  if (!is_0(a[i][c]) && (id == -1 || abs(a[id][c]) <
198
                                                                       13
                                                                                abs(a[i][c]))) {
       }
200
                                                                       14
                                                                                   id = i:
201
     };
                                                                       15
                                                                                7
                                                                       16
                                                                                if (id == -1) continue;
                                                                       17
     Sieve
                                                                                if (id > r) {
                                                                                  swap(a[r], a[id]);
                                                                       19
        • linear sieve
                                                                       20
                                                                                  for (int j = c; j < w; j++) a[id][j] = -a[id][j];
                                                                       21
     vector<int> min_primes(MAX_N), primes;
                                                                                vector<int> nonzero;
                                                                       22
     primes.reserve(1e5);
                                                                       23
                                                                                for (int j = c; j < w; j++) {
     for (int i = 2; i < MAX_N; i++) {</pre>
                                                                                  if (!is_0(a[r][j])) nonzero.push_back(j);
       if (!min_primes[i]) min_primes[i] = i, primes.push_back(i); _{25}
       for (auto& p : primes) {
                                                                                T inv_a = 1 / a[r][c];
         if (p * i >= MAX_N) break;
                                                                                for (int i = r + 1; i < h; i++) {
         min_primes[p * i] = p;
                                                                                 if (is_0(a[i][c])) continue;
                                                                       28
         if (i % p == 0) break;
                                                                                  T coeff = -a[i][c] * inv a;
                                                                       29
 9
       }
                                                                                  for (int j : nonzero) a[i][j] += coeff * a[r][j];
                                                                       30
 10
                                                                                }
                                                                       31
                                                                                ++r;

    mobius function

                                                                              }
                                                                       33
                                                                              for (int row = h - 1; row >= 0; row--) {
                                                                       34
     vector<int> min_p(MAX_N), mu(MAX_N), primes;
                                                                                for (int c = 0; c < limit; c++) {
                                                                       35
     mu[1] = 1, primes.reserve(1e5);
                                                                                  if (!is_0(a[row][c])) {
                                                                       36
     for (int i = 2; I < MAX_N; i++) {
 3
                                                                                    T inv_a = 1 / a[row][c];
       if (min_p[i] == 0) {
                                                                                    for (int i = row - 1; i >= 0; i--) {
                                                                       38
         min_p[i] = i;
                                                                                      if (is_0(a[i][c])) continue;
                                                                       39
         primes.push_back(i);
                                                                       40
                                                                                      T coeff = -a[i][c] * inv_a;
         mu[i] = -1:
 7
                                                                                      for (int j = c; j < w; j++) a[i][j] += coeff *
                                                                       41
 8
                                                                                a[row][j];
       for (auto p : primes) {
 9
                                                                       42
                                                                                    }
         if (i * p >= MAX_N) break;
 10
                                                                       43
                                                                                    break;
         min_p[i * p] = p;
                                                                                  }
                                                                       44
         if (i % p == 0) {
12
                                                                               }
                                                                       45
           mu[i * p] = 0;
13
                                                                              } // not-free variables: only it on its line
                                                                       46
           break;
14
                                                                              for(int i = r; i < h; i++) if(!is_0(a[i][limit])) return 0;</pre>
                                                                       47
15
                                                                       48
                                                                              return (r == limit) ? 1 : -1;
16
         mu[i * p] = -mu[i];
                                                                       49
       }
17
                                                                       50
     }
18
                                                                           template <typename T>
                                                                       51
                                                                           pair<int, vector<T>> solve_linear(vector<vector<T>> a, const
        • Euler's totient function
                                                                       52
                                                                             \hookrightarrow vector<T> &b, int w) {
     vector<int> min_p(MAX_N), phi(MAX_N), primes;
                                                                             int h = (int)a.size();
                                                                       53
     phi[1] = 1, primes.reserve(1e5);
                                                                              for (int i = 0; i < h; i++) a[i].push_back(b[i]);</pre>
     for (int i = 2; i < MAX_N; i++) {</pre>
 3
                                                                       55
                                                                             int sol = gaussian_elimination(a, w);
       if (\min_p[i] == 0) {
                                                                              if(!sol) return {0, vector<T>()};
                                                                       56
         min_p[i] = i;
                                                                              vector<T> x(w, 0);
                                                                       57
         primes.push_back(i);
                                                                              for (int i = 0; i < h; i++) {
 6
                                                                       58
         phi[i] = i - 1;
                                                                                for (int j = 0; j < w; j++) {
 8
                                                                       60
                                                                                  if (!is_0(a[i][j])) {
 9
       for (auto p : primes) {
                                                                                    x[j] = a[i][w] / a[i][j];
                                                                       61
         if (i * p >= MAX_N) break;
 10
                                                                       62
                                                                                    break;
         min_p[i * p] = p;
 11
                                                                       63
         if (i \% p == 0) {
12
                                                                                }
                                                                       64
13
           phi[i * p] = phi[i] * p;
                                                                       65
14
           break;
                                                                       66
                                                                             return {sol, x};
15
                                                                       67
16
         phi[i * p] = phi[i] * phi[p];
17
                                                                           is_prime
                                                                              • (Miller–Rabin primality test)
     Gaussian Elimination
                                                                           i128 power(i128 a, i128 b, i128 MOD = 1, i128 res = 1) {
     bool is_0(Z v) { return v.x == 0; }
                                                                              for (; b; b /= 2, (a *= a) \%= MOD)
     Z abs(Z v) { return v; }
                                                                                if (b & 1) (res *= a) \%= MOD;
                                                                        3
 3
     bool is_0(double v) { return abs(v) < 1e-9; }</pre>
                                                                        4
                                                                             return res;
     // 1 => unique solution, 0 => no solution, -1 => multiple
      \hookrightarrow solutions
                                                                           bool is_prime(ll n) {
     template <typename T>
                                                                             if (n < 2) return false;
```

```
static constexpr int A[] = {2, 3, 5, 7, 11, 13, 17, 19, 23}; 18
                                                                              using T_key = decltype(extract_key(data.front()));
       int s = __builtin_ctzll(n - 1);
                                                                              T_key minimum = numeric_limits<T_key>::max();
10
11
       11 d = (n - 1) >> s;
      for (auto a : A) {
                                                                              for (T &x : data)
12
                                                                      21
         if (a == n) return true;
                                                                      22
                                                                                   minimum = min(minimum, extract_key(x));
13
        11 x = (11)power(a, d, n);
                                                                      23
14
         if (x == 1 | | x == n - 1) continue;
                                                                              int max_bits = 0;
15
                                                                      24
         bool ok = false;
         for (int i = 0; i < s - 1; ++i) {
                                                                              for (T &x : data) {
17
                                                                      26
           x = 11((i128)x * x % n); // potential overflow!
18
                                                                      27
                                                                                   T_key key = extract_key(x);
          if (x == n - 1) {
                                                                                   max_bits = max(max_bits, key == minimum ? 0 : 64 -
19
                                                                      28
             ok = true;
                                                                               __builtin_clzll(key - minimum));
20
21
             break;
                                                                      29
22
                                                                      30
23
                                                                      31
                                                                               int passes = max((max_bits + bits_per_pass / 2) /
24
        if (!ok) return false;

→ bits_per_pass, 1);

25
                                                                      32
                                                                               if (64 - __builtin_clzll(data.size()) <= 1.5 * passes) {</pre>
26
      return true;
                                                                      33
                                                                                   stable_sort(data.begin(), data.end(), [&](const T &a,
27
                                                                      34
                                                                              const T &b) {
    11 pollard_rho(11 x) {
1
                                                                                       return extract_key(a) < extract_key(b);</pre>
                                                                      35
      ll s = 0, t = 0, c = rng() \% (x - 1) + 1;
2
                                                                      36
                                                                                  });
      ll stp = 0, goal = 1, val = 1;
                                                                      37
                                                                                   return;
      for (goal = 1;; goal *= 2, s = t, val = 1) {
                                                                              }
                                                                      38
         for (stp = 1; stp <= goal; ++stp) {
                                                                      39
          t = 11(((i128)t * t + c) \% x);
                                                                              vector<T> buffer(data.size());
                                                                      40
           val = 11((i128)val * abs(t - s) % x);
                                                                              vector<int> counts;
                                                                      41
          if ((stp \% 127) == 0) {
                                                                              int bits_so_far = 0;
                                                                      42
             11 d = gcd(val, x);
                                                                      43
             if (d > 1) return d;
10
                                                                      44
                                                                              for (int p = 0; p < passes; p++) {</pre>
11
                                                                                   int bits = (max_bits + p) / passes;
                                                                      45
12
                                                                                   counts.assign(1 << bits, 0);</pre>
                                                                      46
        11 d = gcd(val, x);
13
                                                                      47
         if (d > 1) return d;
14
                                                                                   for (T &x : data) {
                                                                      48
      }
15
                                                                                       T_key key = T_key(extract_key(x) - minimum);
                                                                      49
    }
16
                                                                                       counts[(key >> bits_so_far) & ((1 << bits) - 1)]++;</pre>
                                                                      50
17
                                                                                   }
    11 get_max_factor(11 _x) {
18
                                                                      52
      11 max_factor = 0;
19
                                                                                   int count_sum = 0;
                                                                      53
      function < void(11) > fac = [\&](11 x) {
20
                                                                      54
         if (x \le max_factor | | x < 2) return;
21
                                                                                   for (int &count : counts) {
                                                                      55
         if (is_prime(x)) {
22
                                                                                       int current = count;
          max_factor = max_factor > x ? max_factor : x;
23
                                                                                       count = count_sum;
                                                                      57
24
          return;
                                                                                       count_sum += current;
        }
25
                                                                                   }
                                                                      59
26
         11 p = x;
                                                                      60
         while (p >= x) p = pollard_rho(x);
27
                                                                                   for (T &x : data) {
                                                                      61
         while ((x \% p) == 0) x /= p;
28
                                                                                       T_key key = T_key(extract_key(x) - minimum);
                                                                      62
         fac(x), fac(p);
                                                                                       int key_section = int((key >> bits_so_far) & ((1 <<</pre>
      }:
30
                                                                              bits) - 1)):
31
      fac(_x);
                                                                                       buffer[counts[key_section]++] = x;
      return max_factor;
32
                                                                                   }
                                                                      65
33
                                                                      66
                                                                                   swap(data, buffer);
                                                                      67
                                                                                   bits_so_far += bits;
                                                                      68
    Radix Sort
                                                                          }
                                                                      70
    struct identity {
         template<typename T>

    USAGE

         T operator()(const T &x) const {
             return x;
                                                                          radix_sort(edges, 10, [&](const edge &e) -> int { return
5
                                                                           \rightarrow abs(e.weight - x); });
    };
    // A stable sort that sorts in passes of 'bits_per_pass' bits at
                                                                          String
    template<typename T, typename T_extract_key = identity>
                                                                          AC Automaton
    void radix_sort(vector<T> &data, int bits_per_pass = 10, const

    T_extract_key &extract_key = identity()) {

         if (int64_t(data.size()) * (64 -
                                                                          struct AC_automaton {
11
        __builtin_clzll(data.size())) < 2 * (1 << bits_per_pass)) {2
                                                                            int sz = 26;
             stable_sort(data.begin(), data.end(), [&](const T &a,
                                                                            vector<vector<int>>> e = {vector<int>(sz)}; // vector is
12

→ const T &b) {
                                                                           return extract_key(a) < extract_key(b);
                                                                            vector<int> fail = {0};
13
14
             });
                                                                            vector<int> end = {0};
             return;
15
                                                                      6
        }
                                                                            void insert(string& s) {
16
                                                                              int p = 0;
17
```

### General Suffix Automaton for (auto c : s) { c -= 'a'; 10 if (!e[p][c]) { constexpr int SZ = 26; 11 e.emplace\_back(sz); 12 2 fail.emplace\_back(); struct GSAM { 13 3 vector<vector<int>>> e = {vector<int>(SZ)}; // the labeled end.emplace\_back(); 14 e[p][c] = e.size() - 1; $\rightarrow$ edges from node i 15 vector<int> parent = {-1}; // the parent of i vector<int> length = {0}; = e[p][c]; // the length of 17 6 18 $\hookrightarrow$ the longest string 19 end[p] += 1; GSAM(int n) { e.reserve(2 \* n), parent.reserve(2 \* n), 20 → length.reserve(2 \* n); }; 21 void build() { int extend(int c, int p) { // character, last 22 9 bool f = true; 23 queue<int> q; 10 // if already exist for (int i = 0; i < sz; i++) int r = 0;// potential new node 24 11 if (e[0][i]) q.push(e[0][i]); // only extend when not exist if (!e[p][c]) { 25 12 26 while (!q.empty()) { f = false; int p = q.front(); 27 e.push\_back(vector<int>(SZ)); 14 q.pop(); parent.push\_back(0); for (int i = 0; i < sz; i++) { length.push\_back(length[p] + 1); 29 16 if (e[p][i]) { 17 r = (int)e.size() - 1;for (; $\neg p \&\& !e[p][c]; p = parent[p]) e[p][c] = r; //$ fail[e[p][i]] = e[fail[p]][i]; 31 q.push(e[p][i]); update parents 32 } else { 33 19 e[p][i] = e[fail[p]][i]; if (f || ~p) { 34 20 int q = e[p][c]; 21 } if $(length[q] == length[p] + 1) {$ 36 22 37 if (f) return q; 23 } 38 24 parent[r] = q; }; } else { 39 25 e.push\_back(e[q]); parent.push\_back(parent[q]); 27 length.push\_back(length[p] + 1); 28 **KMP** int qq = parent[q] = (int)e.size() - 1; for (; p & e[p][c] == q; p = parent[p]) e[p][c] = qq;• nex[i]: length of longest common prefix & suffix for pat[0.31]if (f) return qq; parent[r] = qq; vector<int> get\_next(vector<int> &pat) { 33 int m = (int)pat.size(); 7 34 vector<int> nex(m); return r; 35 for (int i = 1, j = 0; i < m; i++) { } 36 while (j && pat[j] != pat[i]) j = nex[j - 1]; }; 37 if (pat[j] == pat[i]) j++; nex[i] = j;• Topo sort on GSAM return nex; } 1 11 sz = gsam.e.size(); vector<int> c(sz + 1); 2 • kmp match for txt and pat 3 vector<int> order(sz); for (int i = 1; i < sz; i++) c[gsam.length[i]]++;</pre> auto nex = get\_next(pat); 5 for (int i = 1; i < sz; i++) c[i] += c[i - 1];</pre> for (int i = 0, j = 0; i < n; i++) { 6 for (int i = 1; i < sz; i++) order[c[gsam.length[i]]--] = i;</pre> while (j && pat[j] != txt[i]) j = nex[j-1];7 reverse(order.begin(), order.end()); // reverse so that large if (pat[j] == txt[i]) j++; $\hookrightarrow$ len to small if (j == m) { // do what you want with the match • can be used as an ordinary SAM // start index is `i - m + 1` j = nex[j - 1];• USAGE (the number of distinct substring) } 9 int main() { 1 int n, last = 0; 2 string s; Z function cin >> n; auto a = GSAM(); • z[i]: length of longest common prefix of s and s[i:] for (int i = 0; i < n; i++) { cin >> s; vector<int> z\_function(string s) { 8 last = 0; // reset last int n = (int)s.size(); for (auto&& c : s) last = a.extend(c, last); 3 vector<int> z(n): 10 for (int i = 1, l = 0, r = 0; i < n; ++i) { 11 11 ans = 0;if (i <= r) z[i] = min(r - i + 1, z[i - 1]);for (int i = 1; i < a.e.size(); i++) {</pre> 12 while (i + z[i] < n && s[z[i]] == s[i + z[i]]) ++z[i];ans += a.length[i] - a.length[a.parent[i]]; 13 if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;14 cout << ans << endl;</pre> 15 return z; 16 return 0;

17

}

```
Manacher
    string longest_palindrome(string& s) {
     // init "abc" -> "^$a#b#c$"
vector<char> t{'^', '#'};
      for (char c : s) t.push_back(c), t.push_back('#');
      t.push_back('$');
      // manacher
      int n = t.size(), r = 0, c = 0;
      vector<int> p(n, 0);
      for (int i = 1; i < n - 1; i++) {
9
        if (i < r + c) p[i] = min(p[2 * c - i], r + c - i);
10
        while (t[i + p[i] + 1] == t[i - p[i] - 1]) p[i]++;
11
        if (i + p[i] > r + c) r = p[i], c = i;
12
13
        // s[i] \rightarrow p[2 * i + 2] (even), p[2 * i + 2] (odd)
14
15
      // output answer
      int index = 0;
16
      for (int i = 0; i < n; i++)
17
18
        if (p[index] < p[i]) index = i;</pre>
      return s.substr((index - p[index]) / 2, p[index]);
19
    Lyndon
      • def: suf(s) > s
    void duval(const string &s) {
      int n = (int)s.size();
      for (int i = 0; i < n;) {
```