7 - intercations

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# Chapter 7 - interactions

Loading data

# Packages  
library(pacman)  
p\_load(rethinking, brms, tidyverse, patchwork)  
  
# Data  
data(rugged)  
d <- rugged  
  
detach(package:rethinking, unload = T)

Make data subsets

# make log version of outcome  
d <- d %>% mutate(  
 log\_gdp = log(rgdppc\_2000)  
)  
  
# extract countries with GDP data  
dd <- d %>% filter(complete.cases(rgdppc\_2000))  
  
# split countries into Africa and not-Africa  
d.A1 <- dd %>% filter(cont\_africa == 1) # Afrika  
d.A0 <- dd %>% filter(cont\_africa == 0) # not Afrika

Fit models to the two data subsets

b7.1 <-  
 brm(data = d.A1, family = gaussian, # Afrikan data  
 log\_gdp ~ 1 + rugged,  
 prior = c(prior(normal(8, 100), class = Intercept),  
 prior(normal(0, 1), class = b),  
 prior(uniform(0, 10), class = sigma)),  
 iter = 2000, warmup = 1000, chains = 4, cores = 4,  
 seed = 7)

## Compiling the C++ model

## Start sampling

## Warning: There were 1 transitions after warmup that exceeded the maximum treedepth. Increase max\_treedepth above 10. See  
## http://mc-stan.org/misc/warnings.html#maximum-treedepth-exceeded

## Warning: Examine the pairs() plot to diagnose sampling problems

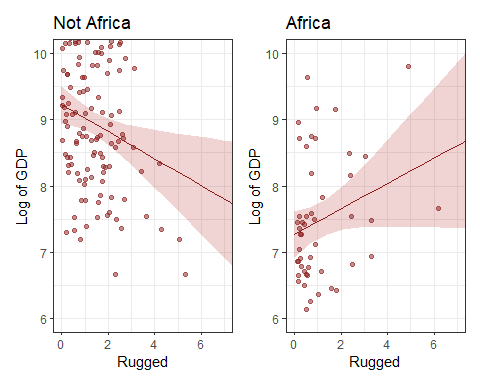
b7.2 <-  
 update(b7.1, # Not Afrikan data  
 newdata = d.A0)

## Start sampling

##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 1).  
## Chain 1:   
## Chain 1: Gradient evaluation took 0 seconds  
## Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 1: Adjust your expectations accordingly!  
## Chain 1:   
## Chain 1:   
## Chain 1: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 1: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 1: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 1: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 1: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 1: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 1: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 1: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 1: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 1: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 1: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 1: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 1:   
## Chain 1: Elapsed Time: 0.034 seconds (Warm-up)  
## Chain 1: 0.023 seconds (Sampling)  
## Chain 1: 0.057 seconds (Total)  
## Chain 1:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 2).  
## Chain 2:   
## Chain 2: Gradient evaluation took 0 seconds  
## Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 2: Adjust your expectations accordingly!  
## Chain 2:   
## Chain 2:   
## Chain 2: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 2: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 2: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 2: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 2: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 2: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 2: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 2: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 2: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 2: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 2: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 2: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 2:   
## Chain 2: Elapsed Time: 0.022 seconds (Warm-up)  
## Chain 2: 0.031 seconds (Sampling)  
## Chain 2: 0.053 seconds (Total)  
## Chain 2:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 3).  
## Chain 3:   
## Chain 3: Gradient evaluation took 0 seconds  
## Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 3: Adjust your expectations accordingly!  
## Chain 3:   
## Chain 3:   
## Chain 3: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 3: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 3: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 3: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 3: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 3: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 3: Iteration: 1001 / 2000 [ 50%] (Sampling)  
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## Chain 3: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 3: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 3: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 3: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 3:   
## Chain 3: Elapsed Time: 0.023 seconds (Warm-up)  
## Chain 3: 0.022 seconds (Sampling)  
## Chain 3: 0.045 seconds (Total)  
## Chain 3:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 4).  
## Chain 4:   
## Chain 4: Gradient evaluation took 0 seconds  
## Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 4: Adjust your expectations accordingly!  
## Chain 4:   
## Chain 4:   
## Chain 4: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 4: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 4: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 4: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 4: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 4: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 4: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 4: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 4: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 4: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 4: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 4: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 4:   
## Chain 4: Elapsed Time: 0.023 seconds (Warm-up)  
## Chain 4: 0.086 seconds (Sampling)  
## Chain 4: 0.109 seconds (Total)  
## Chain 4:

Plot posterior predictions

africa <- d.A1 %>%  
 ggplot(aes(x = rugged, y = log\_gdp)) +  
 stat\_smooth(method = "lm", fullrange = T, size = 1/2,  
 color = "firebrick4", fill = "firebrick", alpha = 1/5) +  
 geom\_point(size = 1.5, color = "firebrick4", alpha = 1/2) +  
 scale\_x\_continuous("Rugged", limits = c(0, 55)) +  
 coord\_cartesian(xlim = 0:7, ylim = 6:10) +  
 ylab("Log of GDP") +  
 theme\_bw() + ggtitle("Africa")   
   
not\_africa <- d.A0 %>%  
 ggplot(aes(x = rugged, y = log\_gdp)) +  
 stat\_smooth(method = "lm", fullrange = T, size = 1/2,  
 color = "firebrick4", fill = "firebrick", alpha = 1/5) +  
 geom\_point(size = 1.5, color = "firebrick4", alpha = 1/2) +  
 scale\_x\_continuous("Rugged", limits = c(0, 55)) +  
 coord\_cartesian(xlim = 0:7, ylim = 6:10) +  
 ylab("Log of GDP") +  
 theme\_bw() + ggtitle("Not Africa")  
   
  
not\_africa + africa



# slope is positive within africa but negative outside africa

It is better if we keep the data in the same data set. Multilevel models borrow data from the different categories in order to improve estimates in all categories - and many other reasons. But even if we added the dummy variable cont\_africa, this will not solve the problem - as a normal linear regression does not account for different slopes for the categories of the dummy.

# Comapre the models with/without the dummy cont\_africa as predictor ( but no interaction effect)

# Start with the model I made before (without the dummy cont\_africa) - just with all the data  
b7.3 <-  
 update(b7.1, newdata = dd) # all data

## Start sampling

##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 1).  
## Chain 1:   
## Chain 1: Gradient evaluation took 0 seconds  
## Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 1: Adjust your expectations accordingly!  
## Chain 1:   
## Chain 1:   
## Chain 1: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 1: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 1: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 1: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 1: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 1: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 1: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 1: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 1: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 1: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 1: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 1: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 1:   
## Chain 1: Elapsed Time: 0.025 seconds (Warm-up)  
## Chain 1: 0.063 seconds (Sampling)  
## Chain 1: 0.088 seconds (Total)  
## Chain 1:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 2).  
## Chain 2:   
## Chain 2: Gradient evaluation took 0 seconds  
## Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 2: Adjust your expectations accordingly!  
## Chain 2:   
## Chain 2:   
## Chain 2: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 2: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 2: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 2: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 2: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 2: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 2: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 2: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 2: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 2: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 2: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 2: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 2:   
## Chain 2: Elapsed Time: 0.025 seconds (Warm-up)  
## Chain 2: 0.025 seconds (Sampling)  
## Chain 2: 0.05 seconds (Total)  
## Chain 2:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 3).  
## Chain 3:   
## Chain 3: Gradient evaluation took 0.001 seconds  
## Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 10 seconds.  
## Chain 3: Adjust your expectations accordingly!  
## Chain 3:   
## Chain 3:   
## Chain 3: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 3: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 3: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 3: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 3: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 3: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 3: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 3: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 3: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 3: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 3: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 3: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 3:   
## Chain 3: Elapsed Time: 0.024 seconds (Warm-up)  
## Chain 3: 0.048 seconds (Sampling)  
## Chain 3: 0.072 seconds (Total)  
## Chain 3:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 4).  
## Chain 4:   
## Chain 4: Gradient evaluation took 0 seconds  
## Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 4: Adjust your expectations accordingly!  
## Chain 4:   
## Chain 4:   
## Chain 4: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 4: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 4: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 4: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 4: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 4: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 4: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 4: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 4: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 4: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 4: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 4: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 4:   
## Chain 4: Elapsed Time: 0.032 seconds (Warm-up)  
## Chain 4: 0.038 seconds (Sampling)  
## Chain 4: 0.07 seconds (Total)  
## Chain 4:

# Now the same but added is the dummy as a predictor (in the formula)  
b7.4 <-  
 update(b7.3,  
 newdata = dd,  
 formula = log\_gdp ~ 1 + rugged + cont\_africa)

## Start sampling

##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 1).  
## Chain 1:   
## Chain 1: Gradient evaluation took 0 seconds  
## Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 1: Adjust your expectations accordingly!  
## Chain 1:   
## Chain 1:   
## Chain 1: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 1: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 1: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 1: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 1: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 1: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 1: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 1: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 1: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 1: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 1: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 1: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 1:   
## Chain 1: Elapsed Time: 0.027 seconds (Warm-up)  
## Chain 1: 0.041 seconds (Sampling)  
## Chain 1: 0.068 seconds (Total)  
## Chain 1:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 2).  
## Chain 2:   
## Chain 2: Gradient evaluation took 0 seconds  
## Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 2: Adjust your expectations accordingly!  
## Chain 2:   
## Chain 2:   
## Chain 2: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 2: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 2: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 2: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 2: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 2: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 2: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 2: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 2: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 2: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 2: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 2: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 2:   
## Chain 2: Elapsed Time: 0.05 seconds (Warm-up)  
## Chain 2: 0.029 seconds (Sampling)  
## Chain 2: 0.079 seconds (Total)  
## Chain 2:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 3).  
## Chain 3:   
## Chain 3: Gradient evaluation took 0 seconds  
## Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 3: Adjust your expectations accordingly!  
## Chain 3:   
## Chain 3:   
## Chain 3: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 3: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 3: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 3: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 3: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 3: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 3: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 3: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 3: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 3: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 3: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 3: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 3:   
## Chain 3: Elapsed Time: 0.032 seconds (Warm-up)  
## Chain 3: 0.031 seconds (Sampling)  
## Chain 3: 0.063 seconds (Total)  
## Chain 3:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 4).  
## Chain 4:   
## Chain 4: Gradient evaluation took 0 seconds  
## Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 4: Adjust your expectations accordingly!  
## Chain 4:   
## Chain 4:   
## Chain 4: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 4: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 4: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 4: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 4: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 4: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 4: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 4: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 4: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 4: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 4: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 4: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 4:   
## Chain 4: Elapsed Time: 0.032 seconds (Warm-up)  
## Chain 4: 0.031 seconds (Sampling)  
## Chain 4: 0.063 seconds (Total)  
## Chain 4:

# compute information criteria for both  
b7.3 <- add\_criterion(b7.3, c("loo", "waic"))  
b7.4 <- add\_criterion(b7.4, c("loo", "waic"))  
  
  
# compare IC  
loo\_compare(b7.3, b7.4,  
 criterion = "waic")

## elpd\_diff se\_diff  
## b7.4 0.0 0.0   
## b7.3 -31.7 7.3

loo\_compare(b7.3, b7.4,  
 criterion = "loo")

## elpd\_diff se\_diff  
## b7.4 0.0 0.0   
## b7.3 -31.7 7.3

# loo and waic agree - the model with the dummy fits teh data way better  
  
# compute weight  
model\_weights(b7.3, b7.4,  
 weights = "waic") %>%   
 round(digits = 3)

## b7.3 b7.4   
## 0 1

# The model with the dummy has all the weight :)

# adding a linear interaction

We want the realtionship between Y (GDP) and R (rugged) to vary as a function of A (dummy varible)

(the model comparisons do not work) add\_criterion() and model\_weigths() when using brms.

# Define new model with interaction effect   
b7.5 <-  
 update(b7.4,  
 newdata = dd,  
 formula = log\_gdp ~ 1 + rugged\*cont\_africa) # syntax as lmer()

## Start sampling

##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 1).  
## Chain 1:   
## Chain 1: Gradient evaluation took 0 seconds  
## Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 1: Adjust your expectations accordingly!  
## Chain 1:   
## Chain 1:   
## Chain 1: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 1: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 1: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 1: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 1: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 1: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 1: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 1: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 1: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 1: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 1: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 1: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 1:   
## Chain 1: Elapsed Time: 0.043 seconds (Warm-up)  
## Chain 1: 0.052 seconds (Sampling)  
## Chain 1: 0.095 seconds (Total)  
## Chain 1:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 2).  
## Chain 2:   
## Chain 2: Gradient evaluation took 0 seconds  
## Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 2: Adjust your expectations accordingly!  
## Chain 2:   
## Chain 2:   
## Chain 2: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 2: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 2: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 2: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 2: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 2: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 2: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 2: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 2: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 2: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 2: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 2: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 2:   
## Chain 2: Elapsed Time: 0.056 seconds (Warm-up)  
## Chain 2: 0.039 seconds (Sampling)  
## Chain 2: 0.095 seconds (Total)  
## Chain 2:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 3).  
## Chain 3:   
## Chain 3: Gradient evaluation took 0 seconds  
## Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 3: Adjust your expectations accordingly!  
## Chain 3:   
## Chain 3:   
## Chain 3: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 3: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 3: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 3: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 3: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 3: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 3: Iteration: 1001 / 2000 [ 50%] (Sampling)  
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## Chain 3: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 3: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 3: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 3: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 3:   
## Chain 3: Elapsed Time: 0.049 seconds (Warm-up)  
## Chain 3: 0.038 seconds (Sampling)  
## Chain 3: 0.087 seconds (Total)  
## Chain 3:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 4).  
## Chain 4:   
## Chain 4: Gradient evaluation took 0 seconds  
## Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 4: Adjust your expectations accordingly!  
## Chain 4:   
## Chain 4:   
## Chain 4: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 4: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 4: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 4: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 4: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 4: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 4: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 4: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 4: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 4: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 4: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 4: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 4:   
## Chain 4: Elapsed Time: 0.043 seconds (Warm-up)  
## Chain 4: 0.042 seconds (Sampling)  
## Chain 4: 0.085 seconds (Total)  
## Chain 4:

b7.5b <-  
 update(b7.4,  
 newdata = dd,  
 formula = log\_gdp ~ 1 + rugged + cont\_africa + rugged:cont\_africa)

## Start sampling

##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 1).  
## Chain 1:   
## Chain 1: Gradient evaluation took 0.001 seconds  
## Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 10 seconds.  
## Chain 1: Adjust your expectations accordingly!  
## Chain 1:   
## Chain 1:   
## Chain 1: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 1: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 1: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 1: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 1: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 1: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 1: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 1: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 1: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 1: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 1: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 1: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 1:   
## Chain 1: Elapsed Time: 0.067 seconds (Warm-up)  
## Chain 1: 0.05 seconds (Sampling)  
## Chain 1: 0.117 seconds (Total)  
## Chain 1:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 2).  
## Chain 2:   
## Chain 2: Gradient evaluation took 0 seconds  
## Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 2: Adjust your expectations accordingly!  
## Chain 2:   
## Chain 2:   
## Chain 2: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 2: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 2: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 2: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 2: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 2: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 2: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 2: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 2: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 2: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 2: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 2: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 2:   
## Chain 2: Elapsed Time: 0.042 seconds (Warm-up)  
## Chain 2: 0.04 seconds (Sampling)  
## Chain 2: 0.082 seconds (Total)  
## Chain 2:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 3).  
## Chain 3:   
## Chain 3: Gradient evaluation took 0 seconds  
## Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 3: Adjust your expectations accordingly!  
## Chain 3:   
## Chain 3:   
## Chain 3: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 3: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 3: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 3: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 3: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 3: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 3: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 3: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 3: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 3: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 3: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 3: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 3:   
## Chain 3: Elapsed Time: 0.043 seconds (Warm-up)  
## Chain 3: 0.045 seconds (Sampling)  
## Chain 3: 0.088 seconds (Total)  
## Chain 3:   
##   
## SAMPLING FOR MODEL 'd17ad44a3d728c149e5d93af8572a666' NOW (CHAIN 4).  
## Chain 4:   
## Chain 4: Gradient evaluation took 0 seconds  
## Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0 seconds.  
## Chain 4: Adjust your expectations accordingly!  
## Chain 4:   
## Chain 4:   
## Chain 4: Iteration: 1 / 2000 [ 0%] (Warmup)  
## Chain 4: Iteration: 200 / 2000 [ 10%] (Warmup)  
## Chain 4: Iteration: 400 / 2000 [ 20%] (Warmup)  
## Chain 4: Iteration: 600 / 2000 [ 30%] (Warmup)  
## Chain 4: Iteration: 800 / 2000 [ 40%] (Warmup)  
## Chain 4: Iteration: 1000 / 2000 [ 50%] (Warmup)  
## Chain 4: Iteration: 1001 / 2000 [ 50%] (Sampling)  
## Chain 4: Iteration: 1200 / 2000 [ 60%] (Sampling)  
## Chain 4: Iteration: 1400 / 2000 [ 70%] (Sampling)  
## Chain 4: Iteration: 1600 / 2000 [ 80%] (Sampling)  
## Chain 4: Iteration: 1800 / 2000 [ 90%] (Sampling)  
## Chain 4: Iteration: 2000 / 2000 [100%] (Sampling)  
## Chain 4:   
## Chain 4: Elapsed Time: 0.041 seconds (Warm-up)  
## Chain 4: 0.035 seconds (Sampling)  
## Chain 4: 0.076 seconds (Total)  
## Chain 4:

# add IC   
b7.5 <- add\_criterion(b7.5,c("loo","waic"))  
  
# compare all 3 models  
l <- loo\_compare(b7.3, b7.4, b7.5, criterion = "waic")  
  
print(l, simplify = F)

## elpd\_diff se\_diff elpd\_waic se\_elpd\_waic p\_waic se\_p\_waic waic   
## b7.4 0.0 0.0 -238.0 7.4 4.1 0.8 476.0  
## b7.5 0.0 0.0 -238.0 7.4 4.1 0.8 476.0  
## b7.3 -31.7 7.3 -269.7 6.5 2.5 0.3 539.3  
## se\_waic  
## b7.4 14.8   
## b7.5 14.8   
## b7.3 13.0

# weight  
model\_weights(b7.3, b7.4, b7.5,  
 weights = "loo") %>%   
 round(digits = 3)

## b7.3 b7.4 b7.5   
## 0.0 0.5 0.5

b7.5$loo # This is not working!

## NULL