

# QAD-Package

Medicus, Oberreiter, Hilgart

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## 1 Introduction

The "*Quantification of Asymmetric Dependence*" package introduces a copula-based dependency measure capable of detecting and depicting asymmetry.

It does so, by constructing the empirical copula from a given bivariate sample and aggregating it to the smooth empirical checkerboard copula, which is used as a strongly consistent estimate for the dependency measure used.

## 2 qad

### 2.1 Description

Quantifies the (asymmetric) dependence structure between two random variables  $X$  and  $Y$ .

### 2.2 Arguments

`qad(x,...)`

- *x*: either a data.frame containing columns of observations of two random variables or a vector containing the observations of one.
- *y*: if *x* is not a data.frame of two columns, a vector containing the observations of the second random variable.
- *resolution*: an integer indicating the number of strips for the checkerboard aggregation. Default = NULL uses the optimal resolution.
- *permutation*: a logical indicating whether a permuted p-value is computed.
- *nperm*: an integer indicating the number of permutation runs.

### 2.3 Value

`qad` returns an object of class `qad` containing the following components:

- *data*: a data.frame containing the input data.
- *results*: a data.frame containing the results of the dependence measures.
- *mass\_matrix*: a matrix containing the mass distribution of the empirical checkerboard copula.
- *resolution*: an integer containing the used resolution of the checkerboard aggregation.

### 2.4 Examples

```
## Warning: package 'qad' was built under R version 3.5.3
```

```
n = 200
x = runif(n,-2,4)
y = sin(x^2)
df = data.frame(x,y)
model = qad(df, print = FALSE, permutation = TRUE)
model$results
```

##		coef	p.values
## 1	q(x1,x2)	0.7090350	0
## 2	q(x2,x1)	0.4169353	0
## 3	mean.dependence	0.5629851	0
## 4	asymmetry	0.2920997	0

### 3 pairwise.qad

Computes the function `qad()` for each pair of columns in the given data frame and returns a list of corresponding `qad` objects.

### 4 heatmap.qad

The pairwise computed dependency measure as output from the `pairwise.qad()` function, are illustrated by a heatmap.

#### 4.1 Arguments

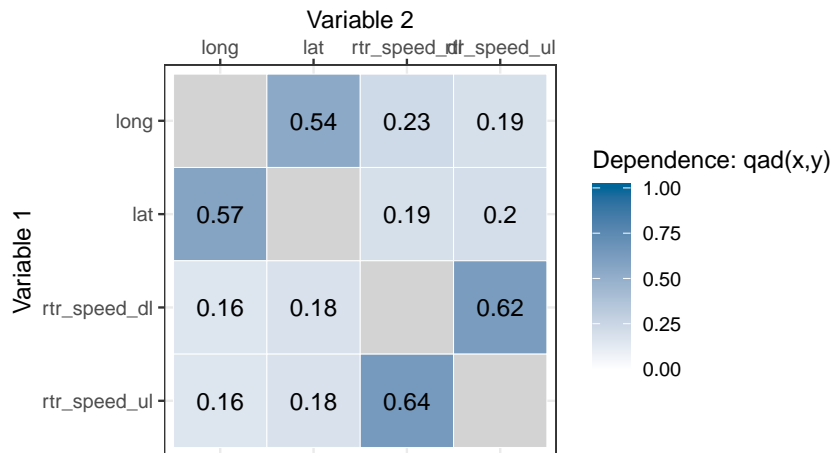
- *pw\_qad*: output of the function `pairwise.qad()`.
- *select*: a character indicating which dependence value is plotted. Options are `c("dependence", "mean.dependence", "asymmetry")`.
- *fontsize*: a numeric specifying the font size of the values.
- *significance*: a logical indicating whether significant values - with respect to the `permutatedp.values` - are marked with a star.
- *sign.level*: numeric value indicating the significance level.
- *scale*: character indicating whether the heatmap uses a relative or absolute scale. Options are `"rel"` or `"abs"` (default).

#### 4.2 Example

```
load(url("http://www.trutschnig.net/RTR.RData"))
df = RTR[sample(nrow(RTR), 1000),
          c('long', 'lat', 'rtr_speed_dl', 'rtr_speed_ul')]
model = pairwise.qad(df)

## [1] "Process..."
## [1] "Process: 1 / 4"
## [1] "Process: 2 / 4"
## [1] "Process: 3 / 4"
```

```
heatmap.qad(model)
```



## 5 cci

An approximated confidence interval for the dependence measure  $qad(x,y)$  for independent random variables. `cci()` can thus be used to test for independence

### 5.1 Arguments

- *n*: and integer indicating the sample size
- *alternative*: character string, whether a "one.sided" (default), or "two.sided" confidence interval is constructed.

### 5.2 Example

```
c = cci(n, alternative = "one.sided")

x = runif(n, -2, 4)
y = sin(x^2)
df = data.frame(x, y)
model = qad(df, print=FALSE)

if(coef(model, select = 'q(x1,x2)') %in% c){
  print('Accept H0')
}else{
  print('Reject H0')
}

## [1] "Reject H0"
```