Mid Semester Examination: Summer Term **PHI455: Philosophical Logic** HSS, IIT Kanpur

General Instructions: Read carefully each question. Fill in your with a pen and circle the correct answer on paper as well. All your work must be done in these pages.

- You have up to 180 minutes.
- For each Wrong answer 0.25% marks will be deducted.
- Please ensure that you keep a copy of your rough work and save it somewhere for future reference. Save it with the course number and and your roll number.
- Every item on the test awards 2 points for each correct answer, for a maximum possible score of 60 points.
- Multiple choice questions may have more than one answer. Circle each of the correct answer.
- Each Question in part-B consists of 5 marks each. For each wrong answer (0.25%) 1.25 M will be deducted.

Part I. True or False Questions. 20M

	Fart 1. TRUE OR FALSE QUESTIONS. 20M
1.	The following argument is valid in K. 1. If Narendra Modi is the prime minister of India, then Narendra Modi is an Indian citizen. 2. Narendra Modi is possibly an Indian citizen. So, 3. Narendra Modi is necessarily an Indian citizen.
	A. True B. False
2.	The class of transitive frames is characterized by the formula $\Diamond \Diamond A \to \Diamond A$. A. True B. False
3.	$\Box(\Box A \to A) \to \Box A$ is a theorem in B modal logic system. A. True B. False

- 4. The statement Food and water are required for survival is translated into Modal logic as $\Box ((F \land W) \rightarrow S)$.
 - A. True B. False
- 5. The following argument is valid in S5. Necessarily, if snow is white (S), then snow is white or $Green(S \vee G)$. Snow is necessarily white. Therefore, necessarily grass is green(G).
 - A. True B. False
- 6. The statement If today is Friday, then it is impossible that today is not Friday is better translated as $(F \to \neg \lozenge F)$.
 - A. True B. False
- 7. A formula $\Diamond p \leftrightarrow \Box p$ is not valid in all Kripke models and hence it is not valid in K. A. True B. False
- 8. It is not possible that it is raining if and only if it is necessary that it is not raining, is translated as $\neg \lozenge p \leftrightarrow \Box \neg p$.
 - A. True B. False
- 9. God's being merciful(M) is inconsistent with your imperfection(I) being incompatible with your going to heaven(H) is translated in to modal logic as $\neg \lozenge (M \land \neg \lozenge (I \land H))$
 - A. True B. False
 - A. True B. False
- 10. The wff $\neg \Diamond (p \land (q \lor \Diamond r))$ and $\Box (\neg p \lor \neg q) \land (\Box \neg p \lor \Box \neg r)$ are logically equivalent to each other.
 - A. True B. False

- 1. Which of the following are well formed formulas in Modal Propositional Logic \mathcal{L} :
 - A. $\Box \Diamond \Box \Diamond \Diamond p \land \Diamond (p \rightarrow q)$
 - B. $(p \to \Diamond \Box \Diamond (r \lor \Box \top))$
 - C. $p \neg \Diamond \leftrightarrow \neg \Diamond p \lor q \land r$
 - D. $(\Box\Diamond\Box\Diamond\Diamond(p\rightarrow q)\leftrightarrow\neg\Box\Diamond\Box\Diamond\Diamond(p\lor q))\wedge\Box(p\rightarrow (q\rightarrow p))$
 - E. none of the above
- 2. Which of the following are true in minimal modal logic K:
 - 1. If P is necessary, then P is true.
 - 2. If P is possible then P is true.
 - 3. If P is true, then P is possible
 - 4. If P is not true, then P is not possible.
 - 5. If P is necessary, then it is impossible for P to be false
 - 6. If P is possible, then P is not a necessary falsehood.
 - A. 2
 - B. 1
 - C. 3
 - D. 4
 - E. 1,3,4,5,6
 - F. None of the above
 - G. All
- 3. Which of the following is false.
 - 1. $\vdash_K \Box (p \land q) \rightarrow (\Box p \land \Box q)$
 - $2. \vdash_K \Box (p \to q) \to (\Box p \to \Box q)$
 - $3. \vdash_K \Box (p \lor q) \to (\Box p \lor q)$
 - $4. \vdash_K \Diamond (p \land q) \rightarrow (\Diamond p \land \Diamond q)$
 - A. 1
 - B. 2
 - C. 3
 - D. 4
 - E. None of the above
 - F. All are false.
- 4. A formula ϕ is satisfiable if it is satisfiable in some model, and valid if it is globally true in every model(valid in K). Which of the following formulas are satisfiable? Which ones are valid? Write your answer below.
 - 1. $\Box \top \lor \Diamond \neg p$
 - 2. $\Diamond p \rightarrow \Diamond \Diamond p$
 - 3. $(\lozenge p \land \square q) \rightarrow \square (p \land q)$

- $4. \, \Diamond \Box \Diamond \, p \to \, \Box \Diamond \, \Box \, p$
- 5. $\Diamond \Box p \to \Box \Diamond p$
- 6. $\Box p \leftrightarrow \Diamond \neg p$
 - A. Satisfiability:
 - B. validity:
 - C. Unsatisfiable:
- 5. The following formulae are S4-theorems:
 - 1. $\Box\Box p \leftrightarrow p$
 - $2. \, \Diamond \Diamond \, p \, \leftrightarrow \to \Diamond p$
 - 3. $\Box \Diamond \Box \Diamond p \leftrightarrow \Box \Diamond p$
 - $4. \ \Diamond \Box \Diamond \Box p \leftrightarrow \Diamond \Box p$
 - 5. $\Box \Diamond \Box p \leftrightarrow p$
 - 6. $\Diamond \Box p \rightarrow \Box \Diamond p$
 - A. 5
 - B. 6
 - C. 1, 2, 3, 4
 - D. None of the above
 - E. All
- 6. Four friends have been identified as suspects for an unauthorized access into a computer system. They have made statements to the investigating authorities. Ajay said *Chetan did it*. Jayanth said *I did not do it*. Chetan said *Digvijay* did it. Digvijay said *Chetan lied when he said that I did it*.
 - 1. If the authorities also know that exactly one of the four suspects is telling the *truth*, who did it?
 - A. Jayanth
 - B. Digvijay
 - C. Chetan, Jayanth
 - D. Chetan
 - E. None of them
 - F. It cannot be determined
 - G. All
 - 2. If the authorities also know that exactly one is *lying*, who did it?
 - A. Jayanth
 - B. Digvijay
 - C. Chetan, Jayanth
 - D. Chetan
 - E. None of them
 - F. It cannot be determined
 - G. All

- 7. There once was a king in a far off island who read, in which a prisoner must choose between two rooms, one containing a lady and the other a tiger. If he chooses the former, the prisoner marries the lady; while if he chooses the latter, he (probably) gets eaten by the tiger. The following signs placed on the two doors. There could be ladies in both rooms, tigers in both rooms, or a lady in one room and a tiger in the other. Additionally, At most only one statement is true. Where's the Lady?
 - **D1** A Tiger is in this room
 - **D2** A Lady is in this room
 - **D3** A Tiger is in room two
 - A. Door 1
 - B. both doors $D1 \wedge D2$
 - C. Door 2
 - D. Cant determine, Prisoner needs more information.
 - E. None of the above
- 8. In the Kripke model $\{W, R, V\}$, Let $W = \{i, j, k, l\}$, $R = \{(i, j), (j, k), (k, l), (l, i), (l, j), (k, k), (l, j)\}$ and V is a valuation function defined as follows: $M, i \models \neg p, q, r$ and $M, j \models p, q, \neg r$ $M, k \models p, q, r$, $M, l \models \neg p, \neg q, \neg r$. Which of the following formulas are valid in the model (You need to check the truth of the formula under all worlds (i, j, k, l)).
 - 1. $\Diamond (p \land q) \rightarrow \Diamond p \land \Diamond q$.
 - $2. \square\square\square\Diamond r$
 - 3. $\Diamond \Box p \lor \Diamond \Diamond \Box p$
 - 4. $\Box\Box\Diamond q$
 - A. 1,2,3
 - B. 1,3
 - C. 2,3
 - D. 3
 - E. none of the above

Part III. ROUGH WORK

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Part I11. ROUGH WORK