

Philosophical Logic: PHI455

Week1: Basics

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About the Course ✓

Basic Concepts of Logic: Propositional Logic

Tree Method as a decision procedure method ✓

Puzzles

Knaves / Knights

References

'Raymond Smullyan'

11 What is the name of the book?

About the Course

- See FCH ✓
- Syllabus: Propositional Logic, possibility and Paradox ✓]
- Midsem+EndSem+Term Paper ✓
- True/False questions and Multiple choice questions ✓]
- 7 Weeks: 7 Assignments ✓ →

What is Logic?

Handwritten notes and diagrams illustrating logic concepts:

Logical Symbols and Rules:

- \neg negation
- \wedge conjunction
- \vee disjunction
- \Rightarrow implication

Logical Rules and Diagrams:

- Soundness Proof:** A diagram showing the derivation of $A \Rightarrow B$ from $A \wedge B$ and A .
- Modus Ponens (MP):** A diagram showing the derivation of B from $A \Rightarrow B$ and A .
- De Morgan's Law:** A diagram showing the derivation of $\neg(A \wedge \neg A)$ from $A \wedge \neg A$.
- Deviant and Many-valued Logics:** A diagram showing the derivation of $A \Rightarrow B$ from B and A , labeled as a fallacy.

Definition of Logic:

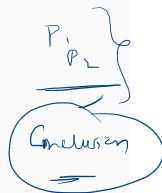
- It is the process of developing **valid argument**. It involves **inferring** new information from known **facts**.
- Logic is a formal system of rational thought that is useful for problem solving, decision making, and strategy formation.

Handwritten Examples:

- $A \equiv A$
- $A \vee \neg A$
- $\neg(A \wedge \neg A)$

How this term is used:

- Not everything follows the rules of logic.
- The logic behind this statement is faulty.
- There's no logic in his argument.
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Patrick Hurley
→ Concise Introduction
to Logic

Reasoning:

- Process of thinking about things in logical and rational way.
- Innate human ability- formalized by 'Logic, Mathematics, AI. ✓
- Formal, Informal, top-down, bottom-up
- It's a stupid decision that completely defies logic.
- I can't fault you on your logic. ✓
- What's the logic of your argument? ↵
- I don't follow the logic of your argument. =
- The logic behind this statement is faulty.

Thinking and
reasoning

- Should Reason
→ actually, reason ✓

$$\begin{array}{l} P_1 \\ P_2 \end{array} \left\{ \begin{array}{l} A \Rightarrow B \\ A \end{array} \right\}$$

$$\left(\frac{B}{A} \right)$$

Types of reasoning:

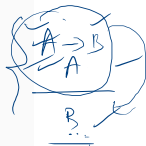
- **Deductive:** General to particular- it produces logically certain results.
- **Inductive reasoning:** It seeks theories to explain observations (bottom=up)- uncertain but likely results.
- **Abduction:** it allows for "best guesses". Used in diagnosis, troubleshooting.
- **Backward Induction:** It starts with theories or end states and works backwards to explain them. Example: Working backward to evaluate moves.
- **Critical Thinking:** Process of rational thought that seeks to draw conclusions in an objective, thorough and informed manner. Influenced by context, culture, based on natural language.

Thinking

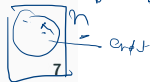
blood drain
ink



Inference
for the best
solution



Row 1 b1
Row 2 -
n+1
moving the
circle and
blank



Other kinds of Reasoning:

- Counterfactual thinking: Considering things that are known to be contrary-to-fact (impossible). How past actions influence present and future actions.
- Intuition: Judgements that are made by the mind that are perceived by the unconscious. Process by which they are generated is not well-understood. It played a significant role in the scientific discovery.

Intelligence, Rationality

- Intelligence: It is an **ability** of depth and variation that includes creativity, **reasoning**, understanding, abstraction, conceptual thinking, systems thinking, emotional intelligence, **logic**.
- Rationality: Rational thought is a state of being reasonable that can be judged by other humans. Human beings are **rational animals**.
- Rational thought is often somewhat logical, but it also includes factors such as, emotions, culture, language, and social conventions.

$A \rightarrow B$
 A
✓
D
P₁
P₂
C
✓

Qualia
↓
Consciousness
↑

Classical Logic:

- Allows for only two truth values: 0, 1
- Ex: it is false that Glass is full and false that glass is empty.
- Classical logic is widely used in proving theorems, Solve problems, and taking decisions.
- Strength: Correctness (Soundness / Complete)
- Fuzzy logic: Allows partial truths: 0.3 full and 0.7 empty.
- It allows infinite degrees of truth.

W | B
✓ Gray ✓

30% - full



30%

Possible - True
True → Possible

Partial truths

Glass full - F
Glass empty - T
V R G Y O R

Reductio ad absurdum:

- RAA states that something is true because something absurd can be implied from its denial.
- Something must be false if it were true something absurd would also be true.
- Examples: Gravity must exist or we would all float off into space.
- There earth can't be flat because that would make it impossible to sail around it.

x

$(x \rightarrow \perp) \rightarrow \neg x$

\perp $\neg x$

\vdots

\perp

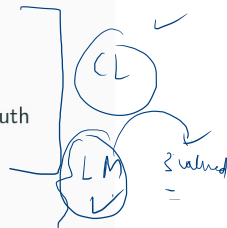
$\neg \neg x = x$

Law of Excluded Middle, Principle of bivalence

7 ass.

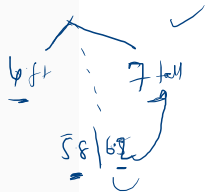
Philosophy

- Aristotle: Any proposition is true or its negation is true.
- It cannot handle degrees of truth.
- Principle of bivalence: Every proposition has **exact one** truth value, either true or false.



4 limits of Classical logic:

- Partial truths ✓
fails
- Language: fails ✓ in case of Vagueness, fail to capture the subtleties of natural language.
- Uncertainty: Real world decision making is dependent on reasoning with uncertainty and incomplete information. Commonsense reasoning is **non-monotonic**
- Perceptions: Aesthetics, metaphors, emotions and cultural concepts. Ex: Write a movie review using formal logic.



Basic Concepts of Logic:

Propositional Logic

Tree Method as a decision procedure method

Puzzles

References

- Key terms: <https://simplicable.com/>
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