



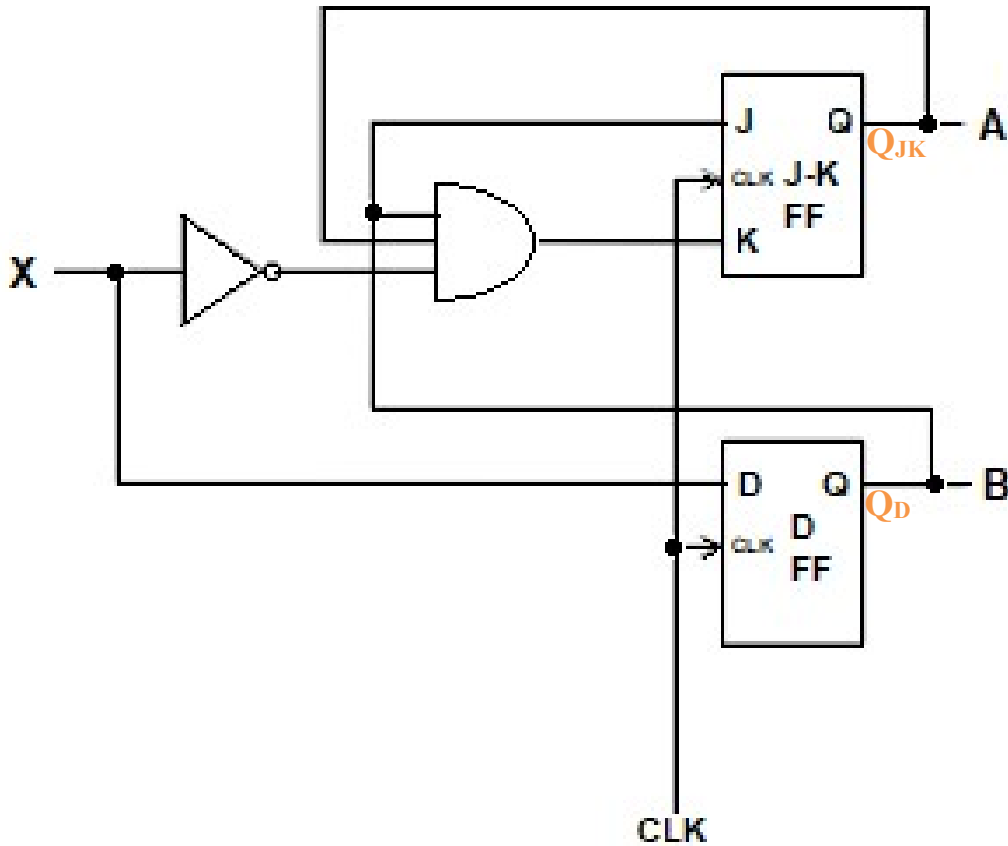
BLG 231E - Digital Circuits

Assignment 5

Student ID : 150200054

Full Name : Aslı Yel

Analyze the synchronous sequential circuit with a single input (X) and two outputs (A, B) shown in the figure below. (**Note:** One flip-flop is a J-K flip-flop, the other is a D flip-flop).



a) Write the next state equations, $S^+ = H(S, I)$.

$$S^+ = \{Q_{JK}^+, Q_D^+\}$$

$$\left. \begin{array}{l} J = Q_D \\ K = X' \cdot Q_D \cdot Q_{JK} \\ D = X \end{array} \right\} F(S, I)$$

$$Q_{JK}^+ = J \cdot Q_{JK}' + K' \cdot Q_{JK} \quad (\text{J-K flip-flop characteristic equation})$$

$$Q_{JK}^+ = Q_D \cdot Q_{JK}' + (X' \cdot Q_D \cdot Q_{JK})' \cdot Q_{JK}$$

$$Q_{JK}^+ = Q_D \cdot Q_{JK}' + (X + Q_D' + Q_{JK}') \cdot Q_{JK}$$

$$Q_{JK}^+ = Q_D \cdot Q_{JK}' + X \cdot Q_{JK} + Q_D' \cdot Q_{JK} + Q_{JK}' \cdot Q_{JK}$$

$$Q_{JK}^+ = Q_D \cdot Q_{JK}' + Q_D' \cdot Q_{JK} + X \cdot Q_{JK}$$

$$Q_{JK}^+ = Q_D \oplus Q_{JK} + X \cdot Q_{JK} \quad \leftarrow$$

minimization

$$Q_D^+ = D \quad (\text{D flip-flop characteristic equation})$$

$$Q_D^+ = X$$

$$\begin{array}{l} Q_{JK}^+ = Q_D \oplus Q_{JK} + X \cdot Q_{JK} \\ Q_D^+ = X \end{array} \quad S^+ = H(S, I)$$

b) Construct the state/output table.

$$S^+ = \{Q_{JK}^+, Q_D^+\}$$

$$\begin{array}{l} Q_{JK}^+ = Q_D \oplus Q_{JK} + X \cdot Q_{JK} \\ Q_D^+ = X \end{array} \quad S^+ = H(S, I)$$

Outputs A and B depend only on the state variables (Q_D , Q_{JK}).

The circuit is designed using the Moore model and output functions are in the form of $O = G(S)$

Output function for output A:

$$A = Q_{JK}$$

Output function for output B:

$$B = Q_D$$

		$Q_{JK}^+ Q_D^+$			
		X			
		0	1	A	B
$Q_{JK} Q_D$	00	00	01	0	0
	01	10	11	0	1
	10	10	11	1	0
	11	00	11	1	1

c) Draw the state diagram.

