



## Department of Computer Science and Engineering

### Assignment

Course Title – Numerical Methods Lab  
Course Code- CSE314

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Submitted by:

Section- A1

Name- Md. Abdur Rashid

ID- 19101008

Submitted to:

Nadeem Ahmed,

Assistant Professor

University of Asia Pacific

## Question 1

Take a 2nd/3rd degree equation. To find the root, apply both Bisection and Newton Raphson Algorithm.

Now provide a comparative analysis of the above algorithms.

## Answer

Let's consider the 3<sup>rd</sup> degree equation is  $x^3 - 0.165x^2 + 3.993 \times 10^{-4}$  for both Bisection Method and Newton Raphson Method. Here I have perform 10 iteration for both Bisection Method and Newton Raphson Method.

### Code for Bisection Method:

```
clc
clear
nMax = 10; % total number of iteration
bisec = @(x) x.^3 - 0.165*x.^2 + 3.993*10.^-4;
x_l = 0;
x_u = 0.11;
arr = [];
if bisec(x_l)*bisec(x_u) < 0
    for i = 1:nMax
        x_m = (x_l+x_u)/2;
        arr(i) = double(x_m);
        if bisec(x_l)*bisec(x_m) < 0
            x_u = x_m;
        else
            x_l = x_m;
        endif
    endfor
else
    disp("no root");
end
disp("Value of x_m in every iteration are : ");
disp(arr);
```

## **Output:**

```
Command Window
Value of x_m in every iteration are :
0.055000 0.082500 0.068750 0.061875 0.065312 0.063594 0.062734 0.062305 0.062520 0.062412
>> |
```

On this problem we used Bisection Method on  $f(x) = x^3 - 0.165x^2 + 3.993 \cdot 10^{-4}$  on the interval  $0 \leq x \leq 2$  using octave. By using octave, it gives more accurate result than traditional manual method.

## **Code for Newton Raphson Method:**

```
clc
clear
nMax = 10; % total number of iteration
f = @(x) x.^3 - 0.165*x.^2 + 3.993*10.^-4;
dfdx = @(x) 3*x.^2 - 0.165*2*x;
arr = [];
arr(1) = 0.05; %initial guess
for i = 1 : nMax-1
    arr(i+1) = arr(i) - (f(arr(i))/dfdx(arr(i)));
end
disp("Value of x_m in every iteration are : ");
disp(arr);
```

## **Output:**

```
line: 13 col: 1 encoding: SYSTEM (CP1252) eol: CRLF
Command Window
Value of x_m in every iteration are :
0.050000 0.062422 0.062378 0.062378 0.062378 0.062378 0.062378 0.062378 0.062378 0.062378
>> |
```

**Comparative analysis:**

On previous problem we used bisection method for root-finding. but on this problem we have used Newton Raphson Method on  $f(x) = x^3 - 0.165x^2 + 3.993 \cdot 10^{-4}$  on the interval  $0 \leq x \leq 2$  using octave. Its shows the new estimate  $x_n$  and  $f(x_n)$  at each step.

And we can observe that Newton's method is the more accurate and effective than Bisection method.

## Question 2:

Find the below code:

---

```
function ball_function()
    % This is the main program
    time = 0.6;                % Just pick some time
    vertical_position = y(time);
    fprintf('%f \n',vertical_position)
    time = 0.9;                % Pick another time
    vertical_position = y(time);
    fprintf('%f \n',vertical_position)
end

% The function 'y' is a _local_ function in this file
function result = y(t)
    g = 9.81;                % Acceleration of gravity
    v0 = 5;                  % Initial velocity
    result = v0*t - 0.5*g*t^2;
end
```

---

a) Change the first line from function ball\_function () to ball\_function(), i.e. remove the word function.

```
Command Window
>> ans2

error: parse error near line 11 of file H:\CSE 314\ans2.m

    syntax error

>>> end
      ^
>>
```

---

Here, we can see that when we remove function word from 1st line. We get error. Because without function this code cannot run.

**b) Change the first line from function ball\_function () to function ball\_func (), i.e., change the name of the function.**

```
warning: function name 'ball_func' does not agree with function filename
1.234200
0.526950
>> |
```

---

If we change the line ball\_function to ball\_func (), we can be warning, this function name ball\_func does not acceptable in this program and the function in a file should have the same name as the name of the file.

**c) Change the line function result = y(t) to function y(t).**

```
warning: function name 'ball_func' does not agree with function filename
error: value on right hand side of assignment is undefined
error: called from
    ball_function at line 4 column 21
>> |
```

---

If we change the y(t) function, we cannot solve this code because y(t) function, there is an operator. the calculation (result = v0t - 0.5gt<sup>2</sup>) is assigned to the variable result. And this result will be returned through the function y(t) from which the function was called.

**d) Change the line function result = y(t) to function result = y (), i.e., remove the parameter t.**

```
warning: function name 'ball_func' does not agree with function filename
error: 't' undefined near line 14, column 14
error: called from
    ans2>y at line 14 column 10
    ans2 at line 4 column 21
>> |
```

---

Our equation is:  $(\text{result} = v_0t - 0.5gt^2)$ , where 't' is included, the error is showing because if we remove t parameter and y(t) to y (), then this code will give an error. But in this code, Variable 't' which is not defined. If the 't' variable is defined in the y (t) function, then the code will run perfectly. So there is no problem if there is no argument in the y (t) function.

**e) Change the first statement that calls y from vertical\_position = y(time); to vertical\_position = y ();**

```
warning: function name 'ball_func' does not agree with function filename
error: 't' undefined near line 14, column 14
error: called from
    ans2>y at line 14 column 10
    ans2 at line 4 column 21
>> |
```

---

Here we show the same error as the previous one because Octave does not know about the parameter unless it goes through the function. Since vertical\_position = y (time) was supposed to pass an argument to y (t), but could not. Could not find any parameter. Octave is looking for where the 't' is defined.