

**University of Stuttgart**  
IPVS

Analytic Computing



# Fachpraktikum Artificial Intelligence

**Billiard Motion Prediction**

# Motivation & Problem Statement

## Motivation

- Use Artificial Intelligence by learning from data
- Implement whole data mining cycle
- Application: Motion Prediction of multiple objects

## Problem Statement

- Billiard balls motion prediction
- Input: Short video starting with strike
- Output: Ball positions and velocities over time
- Regression Goal: Minimize difference between predicted and ground truth trajectory



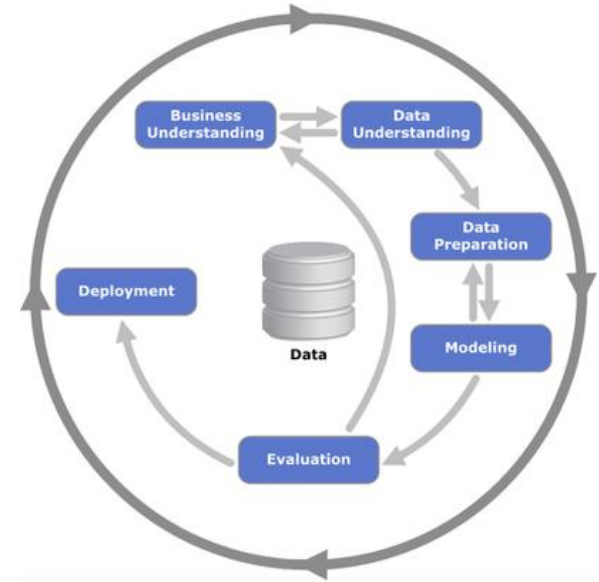
# Methodology & Setup

## Methodology

- CRISP-DM Model
- Requirements analysis

## Setup

- Tracking of tasks with Trello
- Communication via Discord
- Scrum with weekly sprint review
- Git as collaborative version control system
- Modular software architecture
- Formal documentation with UML



<https://statistik-dresden.de/archives/1128>

# Table of contents

- Data Preparation
- Modeling
- Evaluation
- Conclusion

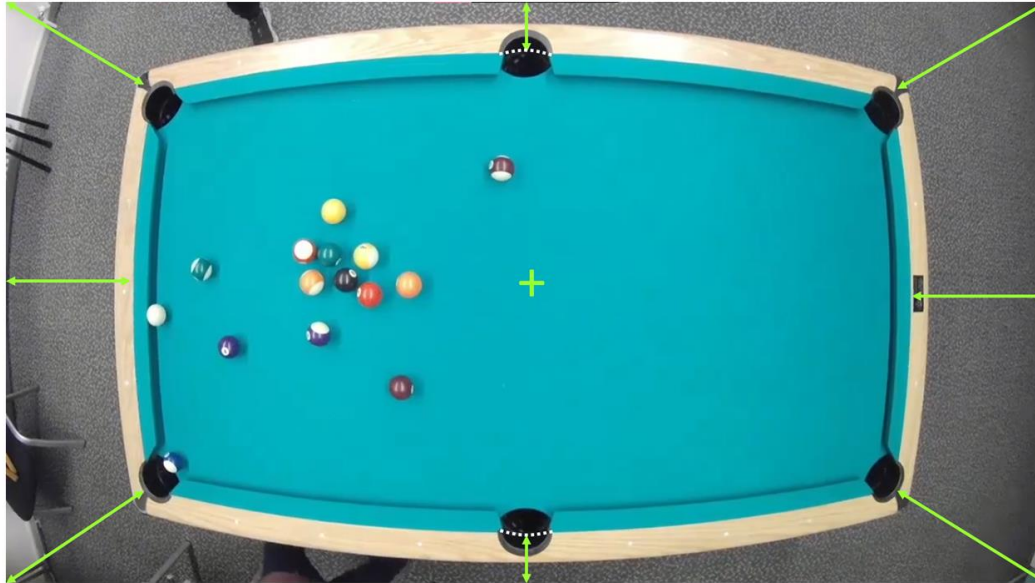
# **Data Preparation**

# Overview

1. Video Recording
2. Clips Generation
3. Camera Calibration
4. Distortion Correction
5. Data Augmentation
6. Alignment
7. Preprocessing
8. Dataset Cleaning

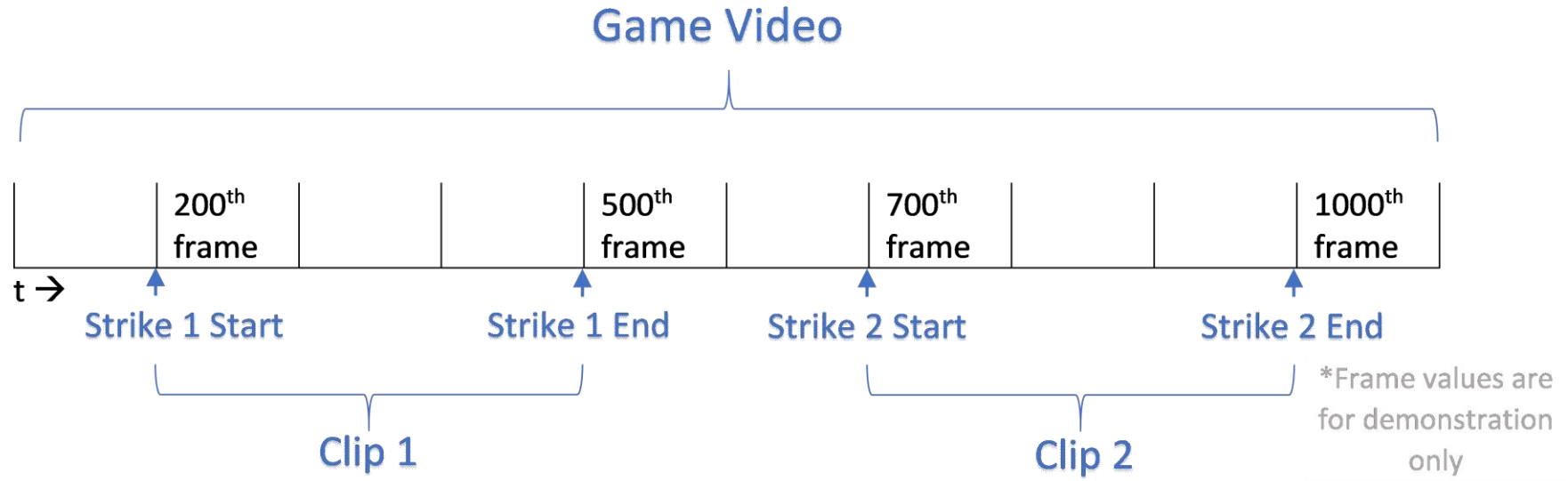
# Video Recording

- No occlusions
- Uniform lighting
- Table centered
  - borders equidistant from image edges
  - corners equidistant from image corners



# Clips Generation

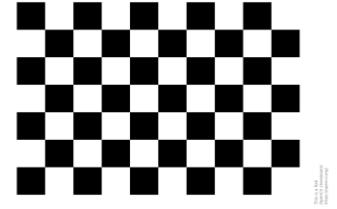
- Timestamps noted manually
- **Automated video clip generation** using **python script** that accepts timestamps



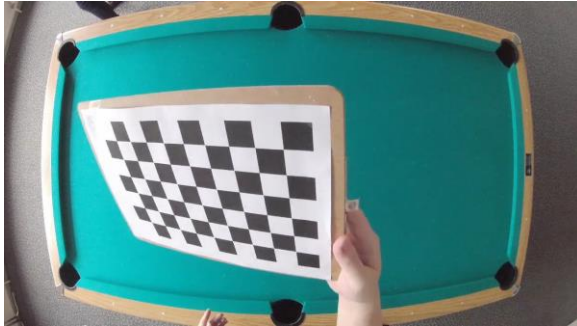


# Camera Calibration

- Moving chessboard pattern in different angles
- Snapshots (10-20) as source
- Finding the chessboard pattern positions
- Calculating intrinsic of camera: camera matrix & distortion matrix



Chessboard pattern  
(via opencv.org)



- Chessboard patterns images (cut from video)

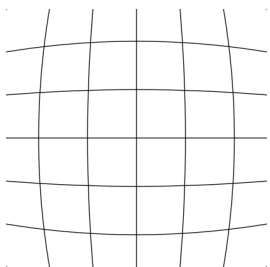
- Found corners

# Distortion Correction

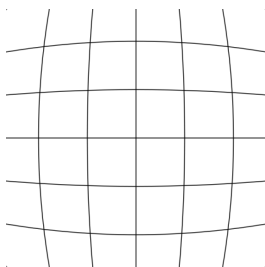
- Using these two matrices to un-distort the source images



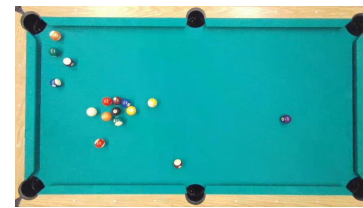
- original



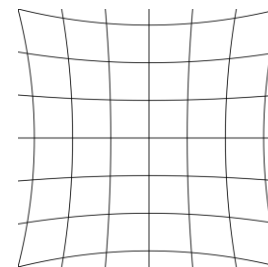
- Based on 7 images



- Based on 14 images



- Based on 21 images



→ Increasing number of images improves result

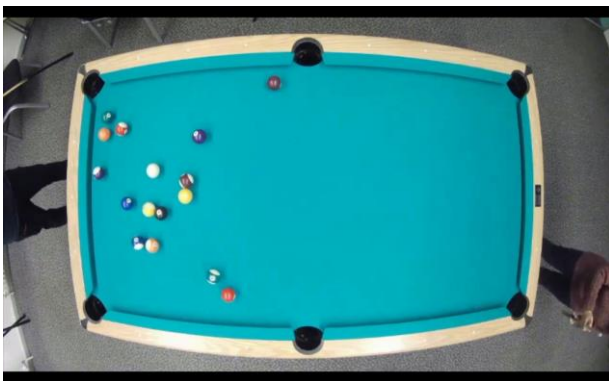
# Data Augmentation



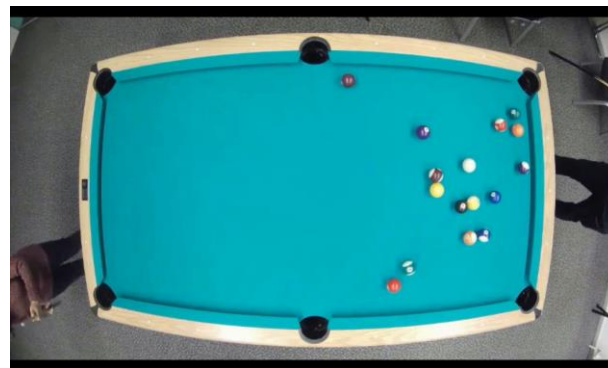
- original



- vertical

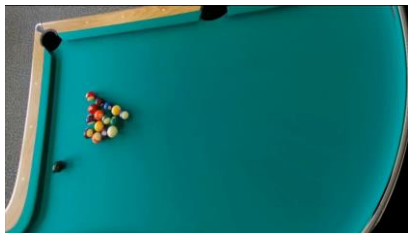


- horizontal



- vertical & horizontal

# Alignment



- Different size



- Different angle



- Test video



- Training video



- Alignment result



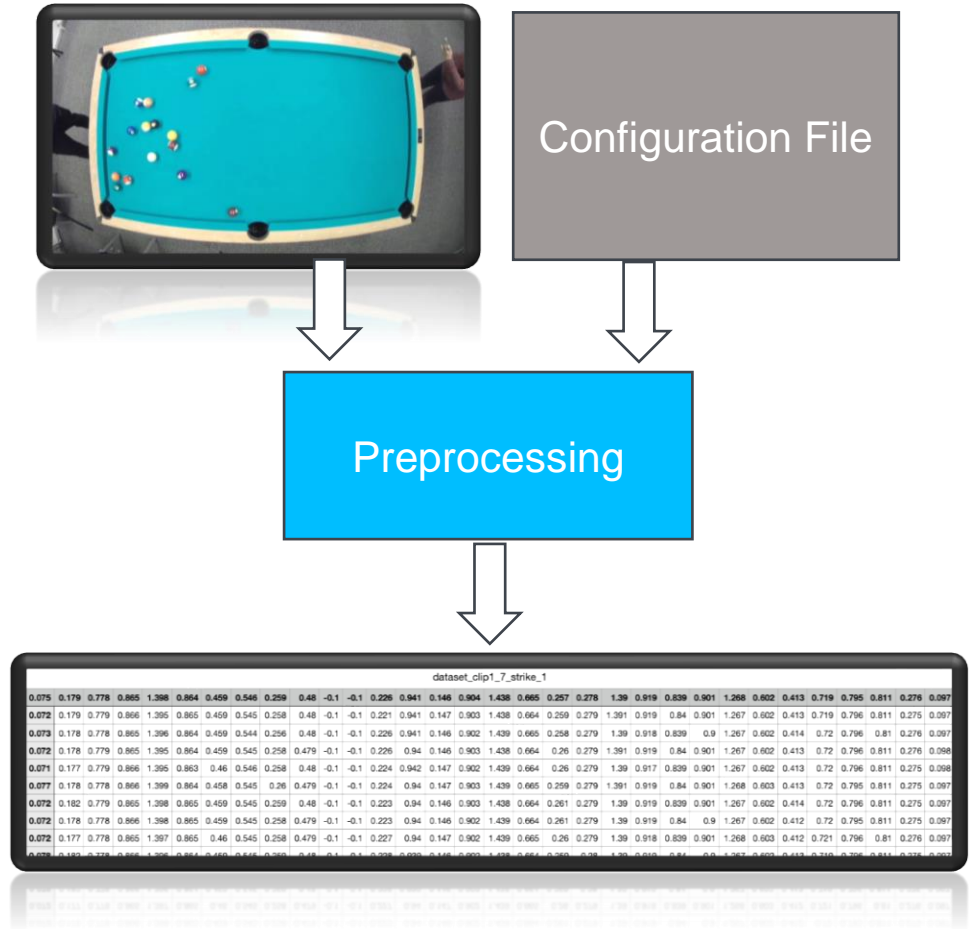
- Correction result

- Feature matching

- Calculating the homograph matrix
- Applying it on the source image

# Preprocessing – Overview

- Inputs : Clips, Configuration File
- Image Processing
  - Image preprocessing & transformation
  - Circle detection + Color classification
- Bidirectional temporal tracking
- Outputs : CSV Files



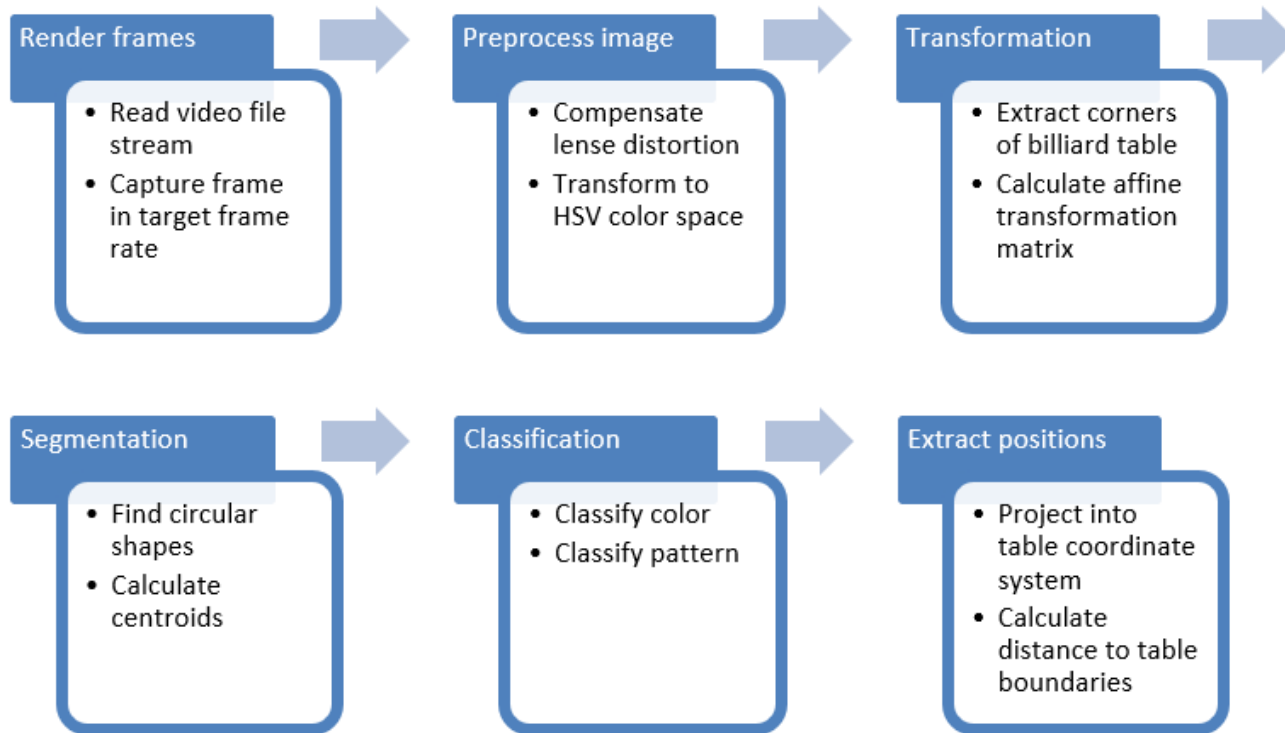
# Preprocessing – Inputs

## Configuration File Parsing

- YAML file containing clip names as entries
- Each entry is marked with at-least one:
  - Start frame
    - Frame where the strike/s occurs
  - Valid flag
    - True : Balls are tracked successfully during the corresponding strike duration, hence csv file can be generated
    - False : Unsuccessful tracking
- Parser extracts the clip name and its metadata
- Feeds it to image processing pipeline

```
1  randomly_clip_7.mp4:
2      1:
3          start_frame: 13
4          valid: False
5      2:
6          start_frame: 200
7          valid: True
```

# Preprocessing – Pipeline

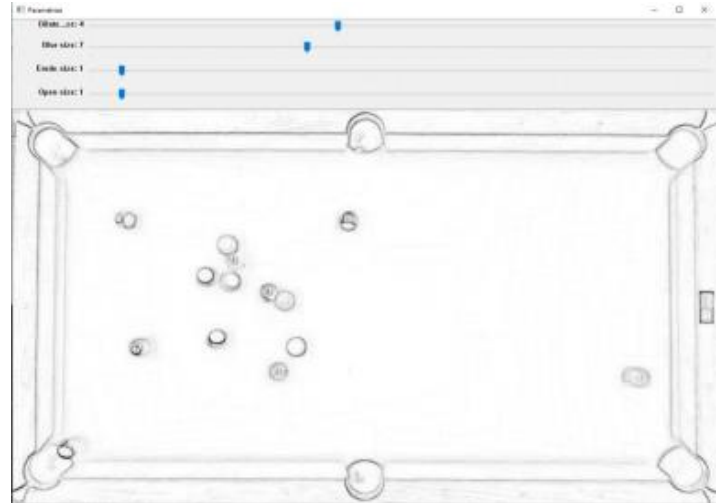
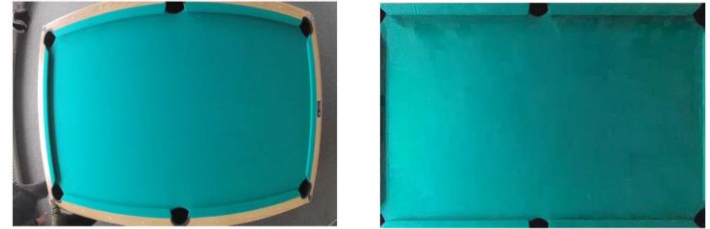


# Preprocessing – Image Processing

## Preprocess Image :

- Camera calibration and distortion correction
- Parameterization
  - Shadow removal
  - Morphological transformations
    - Dilation, Blurring, Erosion, Opening
    - Real time tracker for adjustment of values
- Gamma Correction
  - Adjustment of contrast in different lightning condition

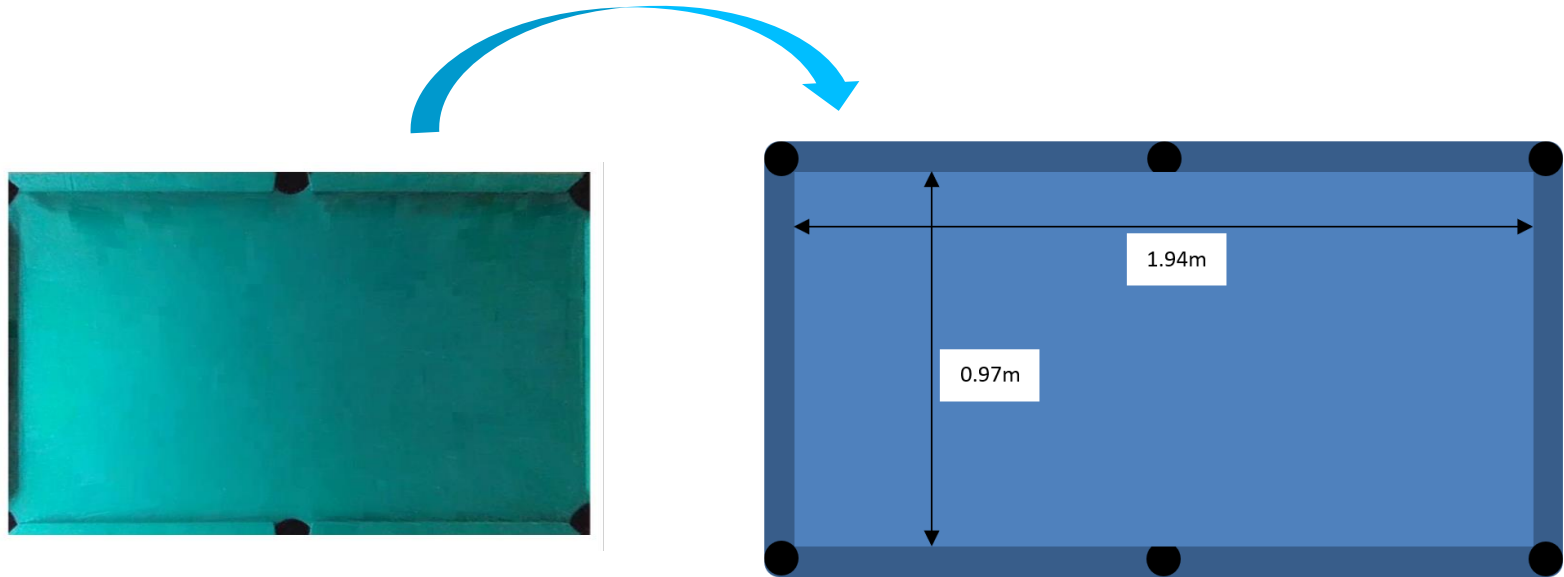
```
5 ##camera matrix
6 camtx = np.array([[661.36745612, 0, 626.09553138],[0, 663.35892418, 354.8585088 ],[0, 0, 1]])
7
8 ##distortion coefficient
9 distco = np.array([-3.52903264e-01, 1.65315869e-01, -3.39131620e-04, -1.64084879e-06, -4.30240406e-02])
```





# Preprocessing – Image Processing

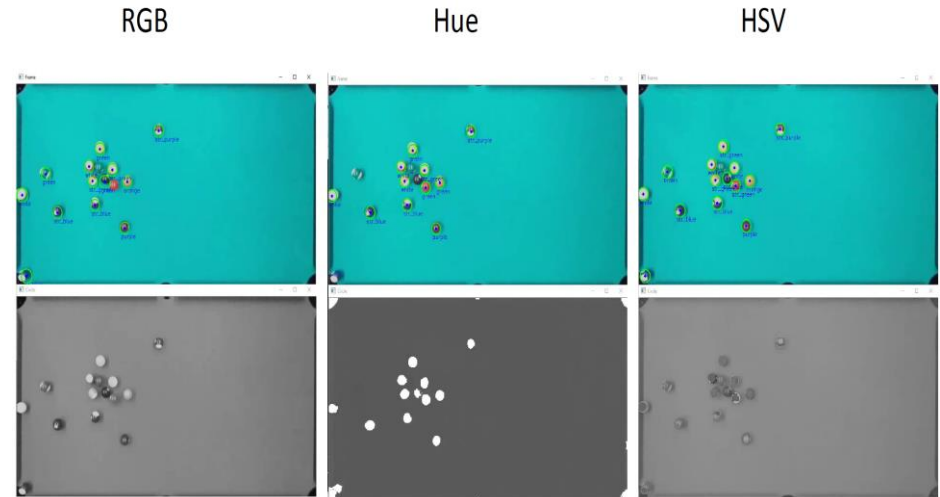
- Find affine transformation matrix to table dimension
- Project from image coordinate system to table coordinate system



# Preprocessing – Image Processing

Circle detection :

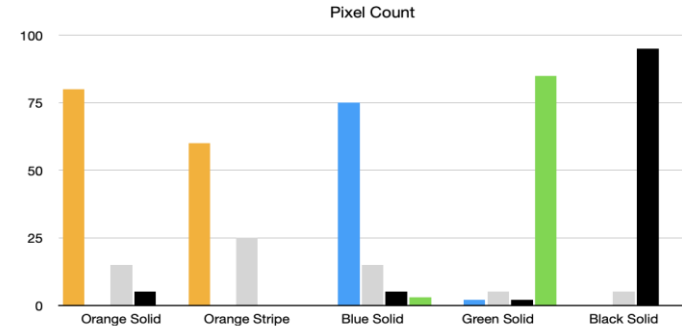
- Three strategies :
  1. Red-Green-Blue (RGB)
  2. Hue
  3. Hue-Saturation-Value (HSV)
    - Combine to get noise free frame
- Apply 3\*3 kernel for blurring
- Hough Circle transformation
  - Parameter tuning
- Detect circles
  - Return centroids and radii



# Preprocessing – Image Processing

Color classification :

- Mark detected circles as region of interests (ROI)
- For each ROI in a frame :
  1. Determine pixels per color using defined Hue, Saturation, Value (HSV) color ranges
  2. Find dominant color and compute color-to-white ratio
  3. Use (2) to classify ball as ball-type
- Store ball positions with corresponding ball-type for each frame in a sequence



Orange	Blue	White	Black	Green	Dominant color	Color to White ratio	Ball
80	0	15	5	0	Orange	5	Orange Solid
60	0	25	0	0	Orange	2	Orange Stripe
0	75	15	5	3	Blue	5	Blue Solid
0	2	5	2	85	Green	17	Green Solid
0	0	5	95	0	Black	19	Black Solid

# Preprocessing – Bidirectional Temporal Tracking

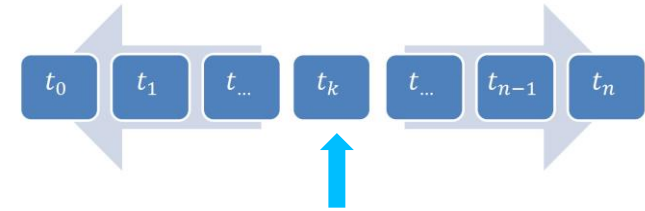
Need :

- To avoid color flickering due to non-robustness of color classification in some of the frames

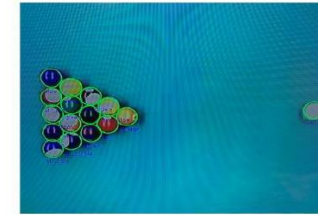
Steps :

1. Search across input sequence for **best detection frame  $t_k$**
2. Initiate backward tracking
  - Store sequence  $t_0$  to  $t_{k-1}$
3. Initiate forward tracking
  - Store sequence  $t_k$  to  $t_n$
4. Combine both sequences to form entire strike sequence

Tracker used : Channel and Spatial Reliability Tracking (CSRT)



All detected balls are uniquely color-classified



Perfectly detected frame



Tracking triggered



Tracking continues in subsequent frames

# Dataset Cleaning

Problems with the generated dataset :

**Hand occlusions** (resulting in false positives)

- **Workaround** : Avoid hand occlusions during data collection

**Lost trackers** (fast movement of balls)

- **Workaround** : Data collected at a higher frame rate

**No white ball** (White ball misclassified as yellow)

- **Workaround** : Python script which eliminates data with absent white ball

**Balls disappearing & reappearing** (coming out of holes)

- **Workaround** : Python script which eliminates such data

**No movement till 1 sec** (30 to 60 frames)

- **Workaround** : Python script which eliminates initial rows with no movement

# Modeling

# Overview

- BaseNet serves as template
- Baseline: Naive Model
- Baseline: Linear Model
- LSTM Recurrent Neural Network Model

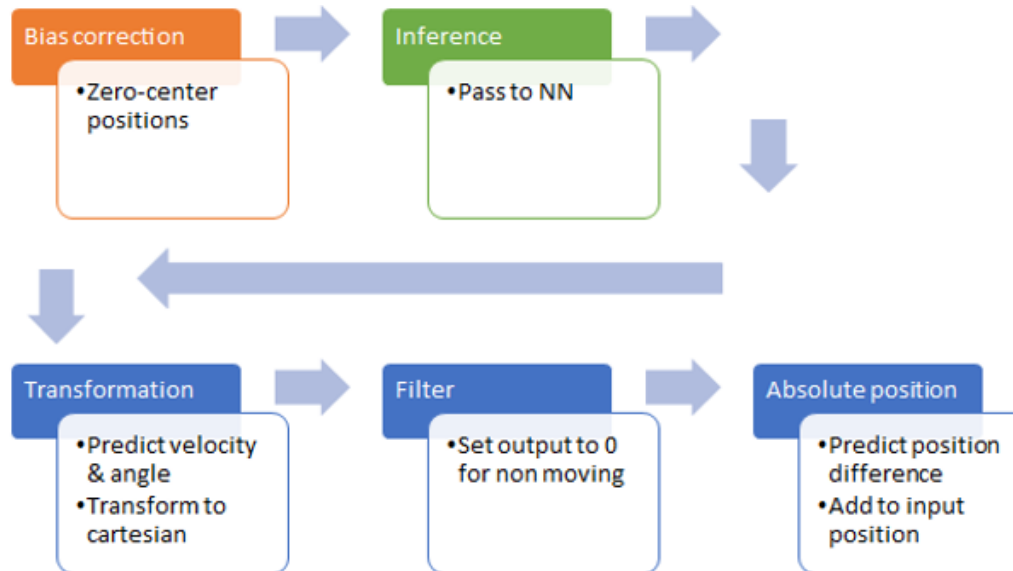
# Model Inputs & Outputs

- Inputs:
  - Position [5x32]: 5 timesteps, absolute position in x and y for 16 balls
- Outputs:
  - Position [1x32]: 1 timestep, difference in x and y for 16 balls
  - Is\_Moving [1x16]: 1 timestep, moving probability for 16 balls
- Prediction "in the loop" → Output used as new input



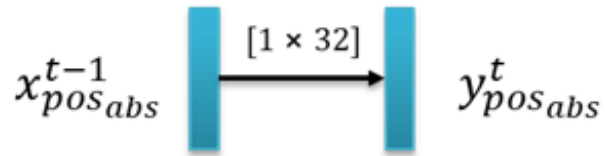
# BaseNet

- Template for NN implementation → shared across models
- Realize preparation of input
- Realize transformation of output



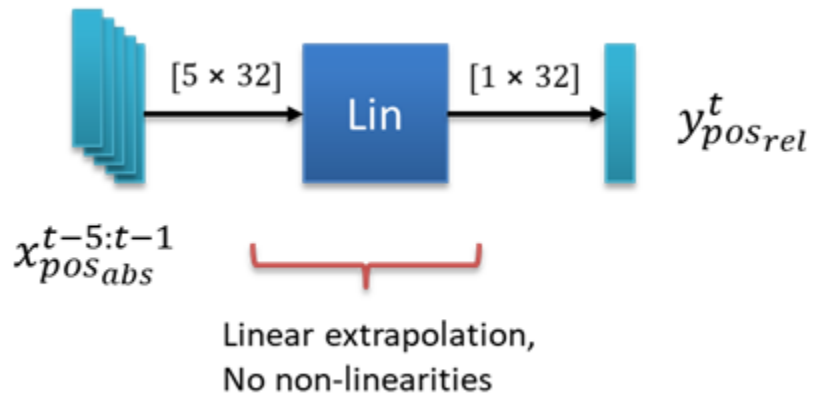
## Baseline: Naive Model

- In billiard most balls are steady during strike
- Constant position is good prior
- Naive model gives input as output
- Used as reference to quantify



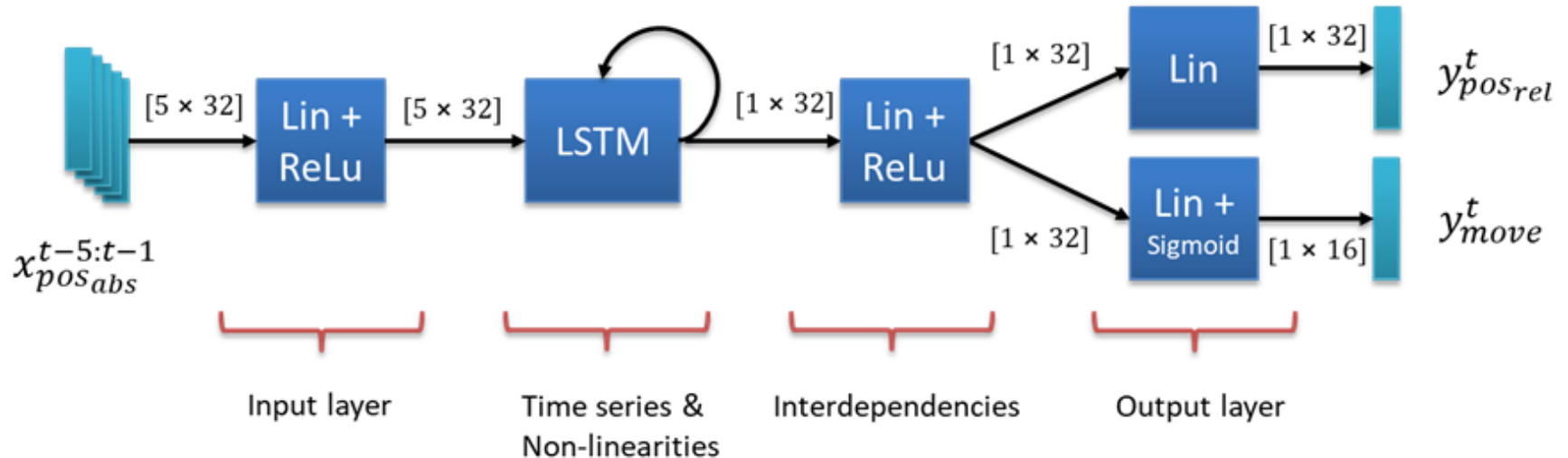
## Baseline: Linear Model

- Simple linear layer without activation function
- Learns extrapolation of position
- Underestimates position difference in linear motion case
- Disregards non-linearities (collisions, boundaries)



# LSTM Model

- Recurrent cell to capture non-linearities across time series
- Linear layers before and after LSTM to prepare and inter-combine features
- No activation function applied to position output to learn linear mapping
- Output includes is\_moving per ball as probabilistic estimate



# Loss Function

- Evaluation metric: Avg. Euclidean position error
  - Position: RMSE
- Training loss: Joint loss accumulated over **N training steps** and **K balls**
  - **Position: Mean Squared Error**
  - **Moving: Binary Cross Entropy**
  - **Physical constraints: Potential map**

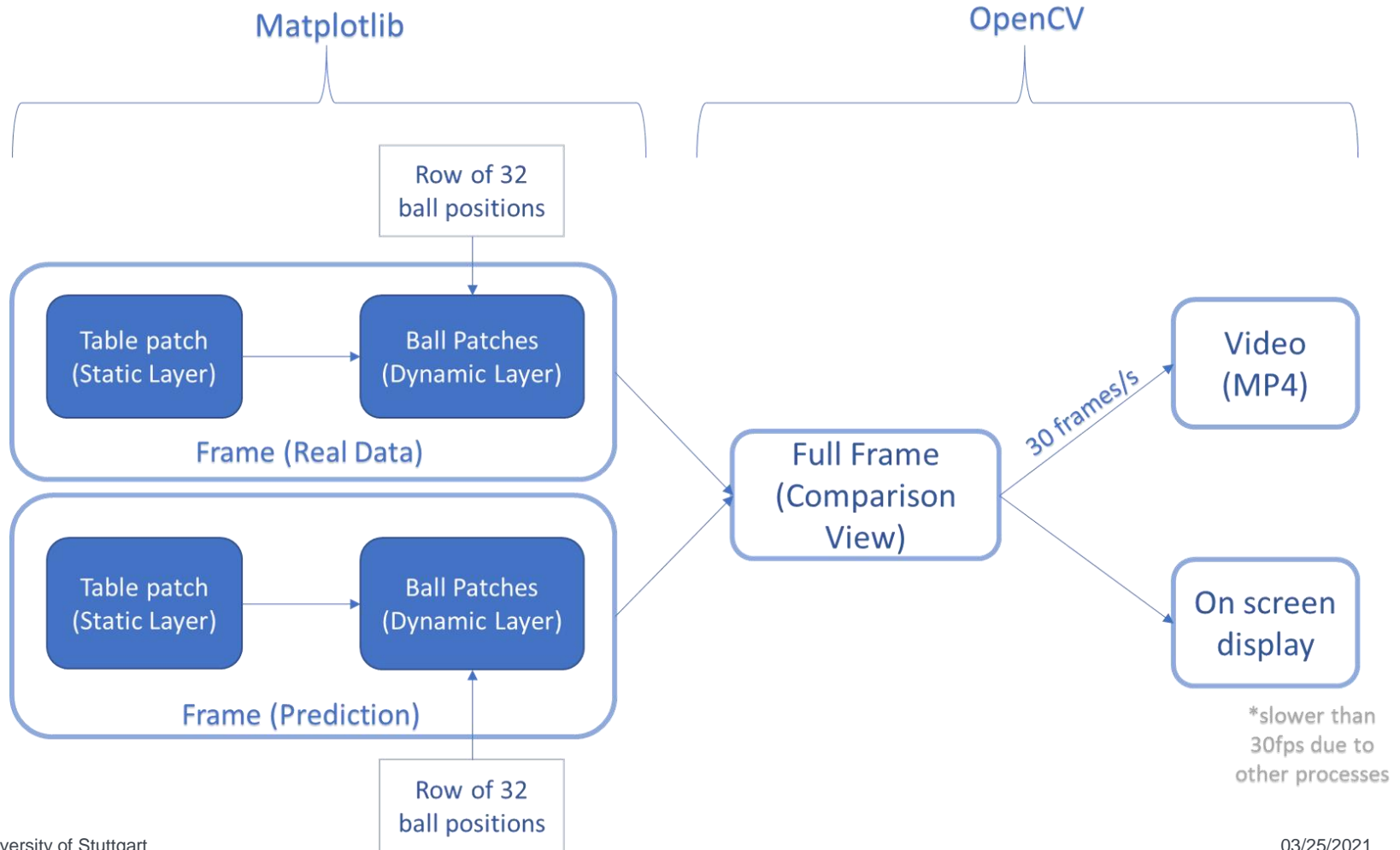
$$\begin{aligned} loss_{train} &= \sum_{n \in steps}^N \sum_{i \in balls}^K loss_{pos_{n,i}} + loss_{mov_{n,i}} + loss_{physic_{n,i}} \\ &= \sum_{n \in steps}^N \sum_{i \in balls}^K MSE(pos_{d_{n,i}}, pos_{p_{n,i}}) + BCE(mov_{d_{n,i}}, mov_{p_{n,i}}) + Potential(pos_{p_{n,i}}) \end{aligned}$$

# Evaluation

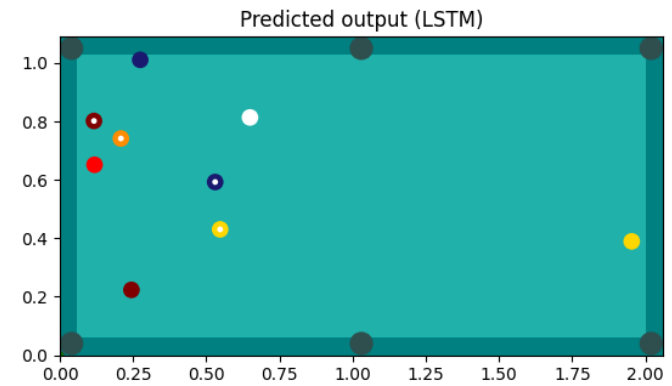
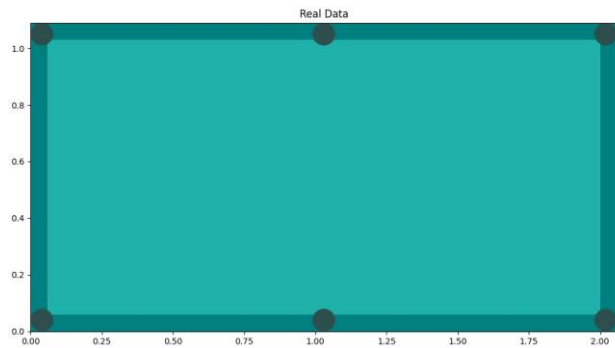
# Overview

- Model performance is evaluated:
  - Quantitatively: Compare evaluation metric to baselines
  - Qualitatively: Subjective plausibility of predicted videos
- Predicted videos instrumental to figure out current state and weaknesses of the model
  - Rendering toolbox developed to compare model to ground truth
  - Easily visible:
    - Linear movement
    - Collisions with boundaries/balls
    - Stationary balls
  - Prediction flaws in video guide adjustments of training

# Rendering

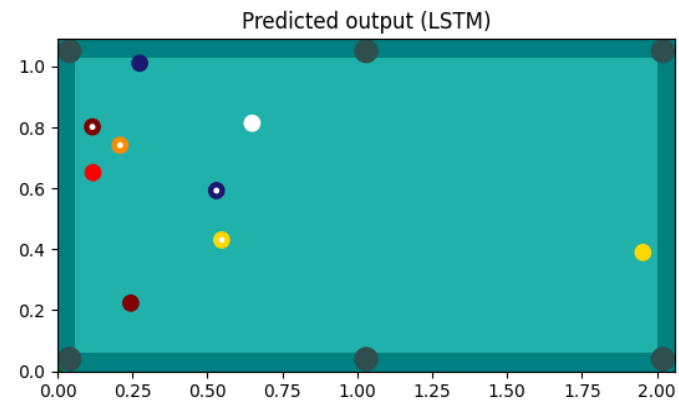
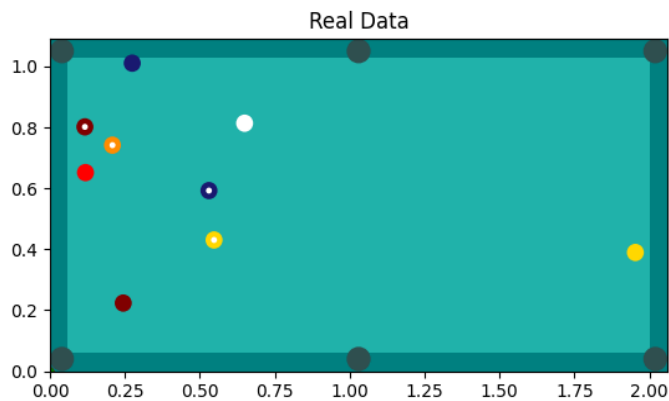






Static Layer

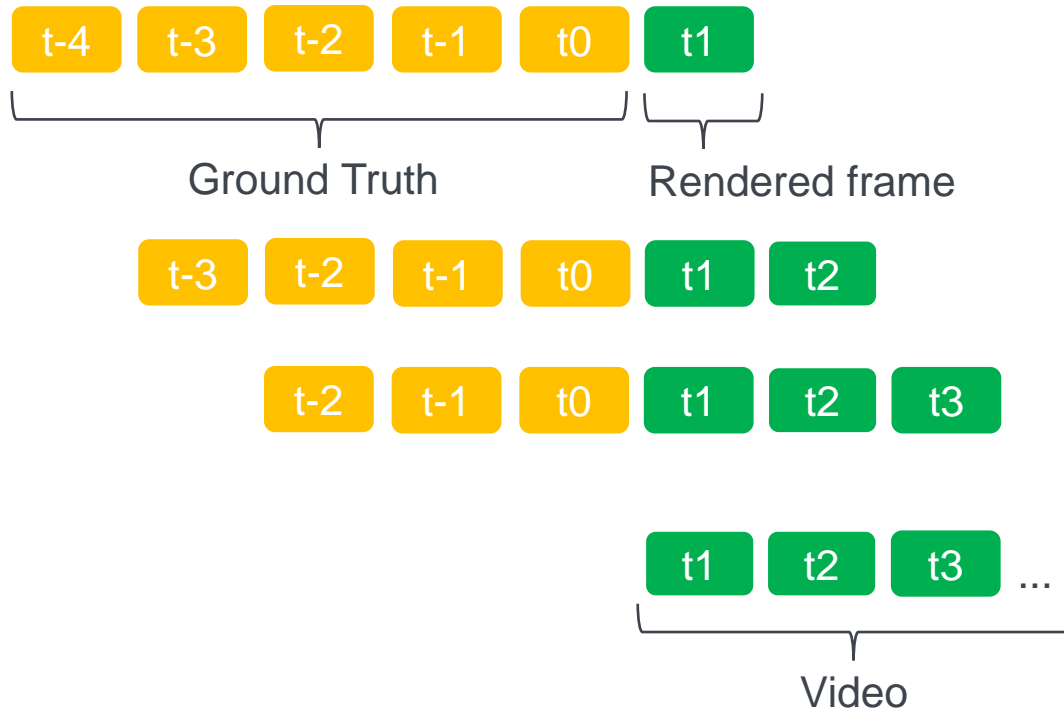
Dynamic Layer



Comparison View

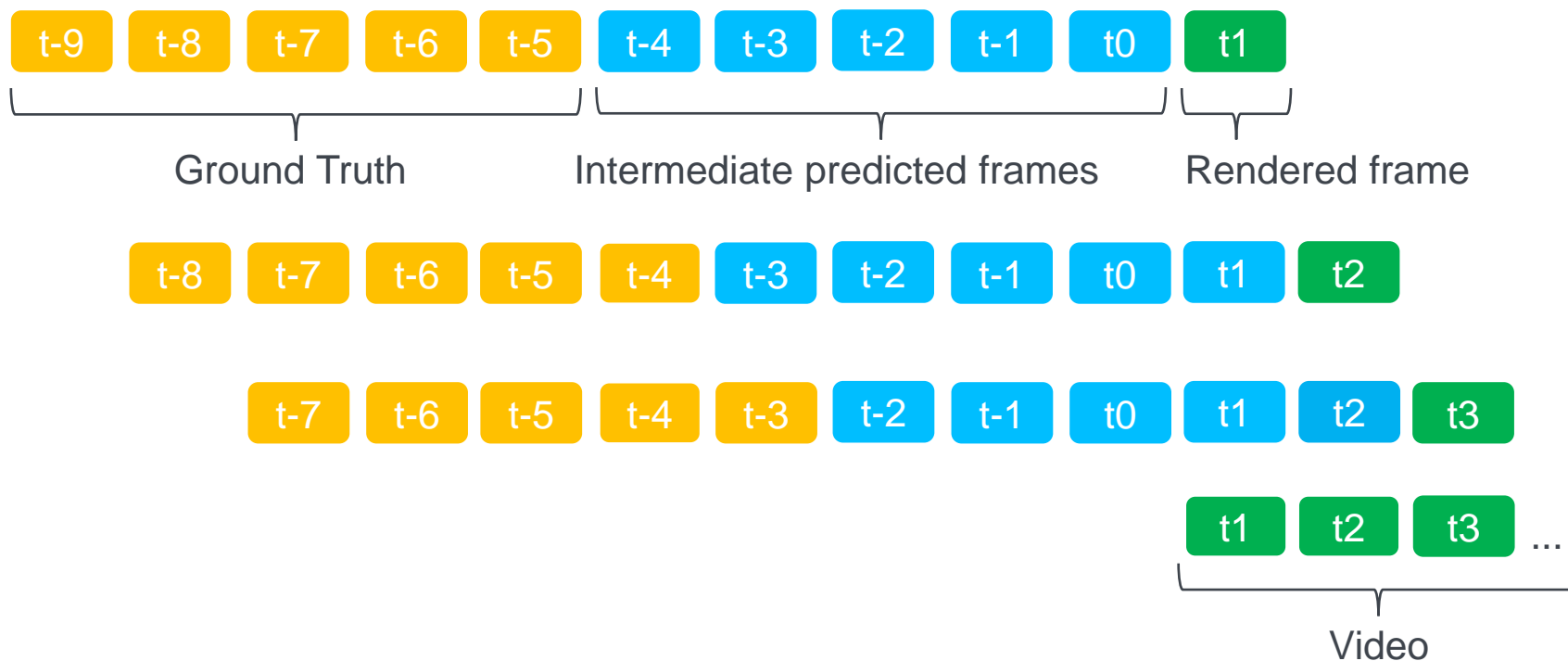
# Multi-step prediction

- Two prediction modes for evaluation:
  - "In-the-loop" prediction of entire strike after initializing with the first 5 frames:



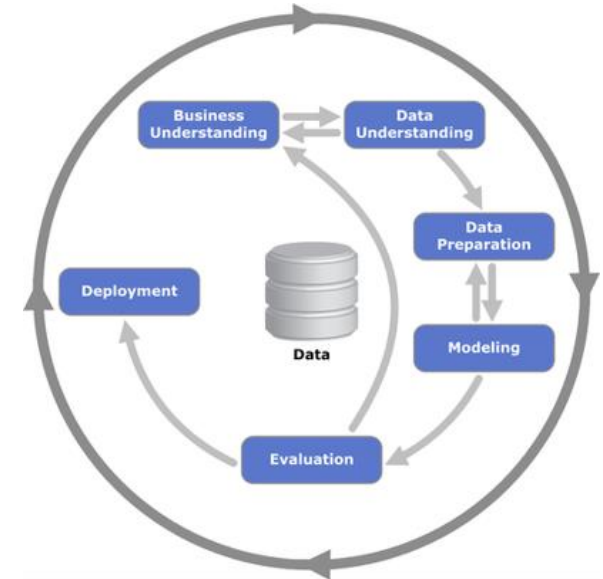
# Multi-step prediction

- Two prediction modes for evaluation:
  - N-step prediction with ground truth as initialization for each predicted frame:



# Modeling-Validation Cycle

- Multiple cycles in CRISP-DM model:
  - Initially not enough data
  - Modeling of non-existing balls with large position  
→ set very small position
  - Inconsistencies in data found  
→ clean data with scripts
  - Insufficient performance of tracker  
→ use higher recording framerate
  - Model instable  
→ predict relative instead of absolute positions
  - Disregards non-linearities  
→ extend loss function with physical regularization



<https://statistik-dresden.de/archives/1128>

# Comparison to Baseline

- Baseline naive → steady state, actually good
- Baseline linear → learns linear motion
- LSTM recurrent → learns non-linear collisions
- No detailed quantitative analysis available yet due to:
  - Delayed/restricted data collection (COVID)
  - Complex data preparation
  - Build generic model pipeline
  - Limited dataset size→ We created starting point for future work

# Conclusion

# Conclusion

## Lessons learned

- Pandemic adds difficulty (delayed data collection, pure virtual collaboration)
- Data creation and preparation takes time
- Lack of data is limitation for sophisticated NN architectures

## Future work

- Incorporate more physical constraints (e.g., conservation of momentum)
- Further DL architectures: Transformer, Graph Neural Network

**Thank you!**

**Demo**



**Backup**

# Demo

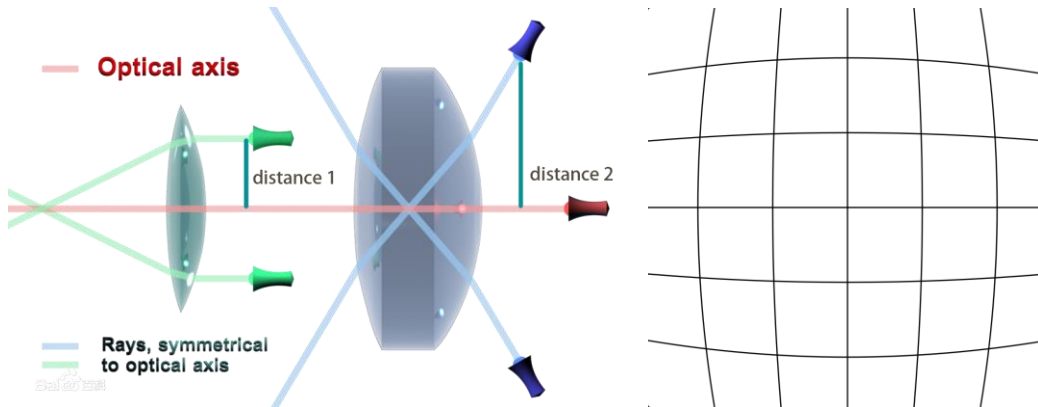
- Show data preparation pipeline
  - Code walkthrough
  - Recorded videos
  - Preprocessing -> Ashish to prepare
- Show Rendering
- Show video of early model
- Show LSTM with nonlinearity
- Show constant baseline
- Show Linear baseline

## Data Preparation - Video Recording

- **Camera Device:** GoXtreme Black Hawk 4k+
- **Software:** OBS Studio
- **Table measurements:** 194cm x 97cm
- **Ball diameter:** 5.7 cm
- Several games were played with 600+ strikes
- **Camera orientation:** Points that were considered while video recording:
  - Table should be free of occlusions
  - Uniform lighting conditions all over the table
  - Table placed at the center of the field of camera vision
  - All 4 table borders should be equidistant from 4 edges of the camera field of vision.
- **Frame rate:** Initially videos were recorded at 30fps, which wasn't suitable for preprocessing so later videos were recorded in 60 fps
- **Video Resolution:** 1280 x 720

# Data Preparation – Lens Distortion

- Distortion is one of the 5 basic optical aberrations.
- Distortion  $\propto d^3$
- The camera we used causes Barrel Distortion.



- Optical axis
- Barrel distortion(source:wiki)

dataset\_clip1\_7\_strike\_1

0.075	0.179	0.778	0.865	1.398	0.864	0.459	0.546	0.259	0.48	-0.1	-0.1	0.226	0.941	0.146	0.904	1.438	0.665	0.257	0.278	1.39	0.919	0.839	0.901	1.268	0.602	0.413	0.719	0.795	0.811	0.276	0.097
0.072	0.179	0.779	0.866	1.395	0.865	0.459	0.545	0.258	0.48	-0.1	-0.1	0.221	0.941	0.147	0.903	1.438	0.664	0.259	0.279	1.391	0.919	0.84	0.901	1.267	0.602	0.413	0.719	0.796	0.811	0.275	0.097
0.073	0.178	0.778	0.865	1.396	0.864	0.459	0.544	0.256	0.48	-0.1	-0.1	0.226	0.941	0.146	0.902	1.439	0.665	0.258	0.279	1.39	0.918	0.839	0.9	1.267	0.602	0.414	0.72	0.796	0.81	0.276	0.097
0.072	0.178	0.779	0.865	1.395	0.864	0.459	0.545	0.258	0.479	-0.1	-0.1	0.226	0.94	0.146	0.903	1.438	0.664	0.26	0.279	1.391	0.919	0.84	0.901	1.267	0.602	0.413	0.72	0.796	0.811	0.276	0.098
0.071	0.177	0.779	0.866	1.395	0.863	0.46	0.546	0.258	0.48	-0.1	-0.1	0.224	0.942	0.147	0.902	1.439	0.664	0.26	0.279	1.39	0.917	0.839	0.901	1.267	0.602	0.413	0.72	0.796	0.811	0.275	0.098
0.077	0.178	0.778	0.866	1.399	0.864	0.458	0.545	0.26	0.479	-0.1	-0.1	0.224	0.94	0.147	0.903	1.439	0.665	0.259	0.279	1.391	0.919	0.84	0.901	1.268	0.603	0.413	0.72	0.795	0.811	0.275	0.097
0.072	0.182	0.779	0.865	1.398	0.865	0.459	0.545	0.259	0.48	-0.1	-0.1	0.223	0.94	0.146	0.903	1.438	0.664	0.261	0.279	1.39	0.919	0.839	0.901	1.267	0.602	0.414	0.72	0.796	0.811	0.275	0.097
0.072	0.178	0.778	0.866	1.398	0.865	0.459	0.545	0.258	0.479	-0.1	-0.1	0.223	0.94	0.146	0.902	1.439	0.664	0.261	0.279	1.39	0.919	0.84	0.9	1.267	0.602	0.412	0.72	0.795	0.811	0.275	0.097
0.072	0.177	0.778	0.865	1.397	0.865	0.46	0.545	0.258	0.479	-0.1	-0.1	0.227	0.94	0.147	0.902	1.439	0.665	0.26	0.279	1.39	0.918	0.839	0.901	1.268	0.603	0.412	0.721	0.796	0.81	0.276	0.097
0.078	0.182	0.778	0.866	1.396	0.864	0.459	0.545	0.259	0.48	-0.1	-0.1	0.228	0.939	0.146	0.902	1.438	0.664	0.259	0.28	1.39	0.919	0.84	0.9	1.267	0.602	0.413	0.719	0.796	0.811	0.275	0.097

## CSV Generation

- Traverse through entire strike sequence obtained from tracking
- Each csv row corresponds to a point/frame in the strike sequence
- Row consists of 16\*2 coordinates of balls ordered in a predefined way
- Mirror/Augment data (see next slides)

# Modeling

## Synthetic Dataset

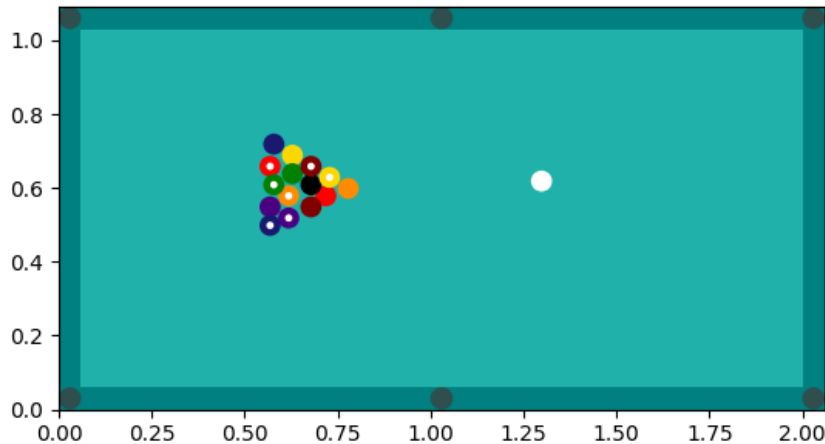
- Obvious bottleneck for model early into development: training data
- Create intermediary synthetic dataset:
  - Balls at random positions on table
  - Random linear motion direction of balls
  - No collisions, but learn linear motion
  - Keep improving the model until more real data is available
- Later in development switch back to real (and augmented) data

# Evaluation

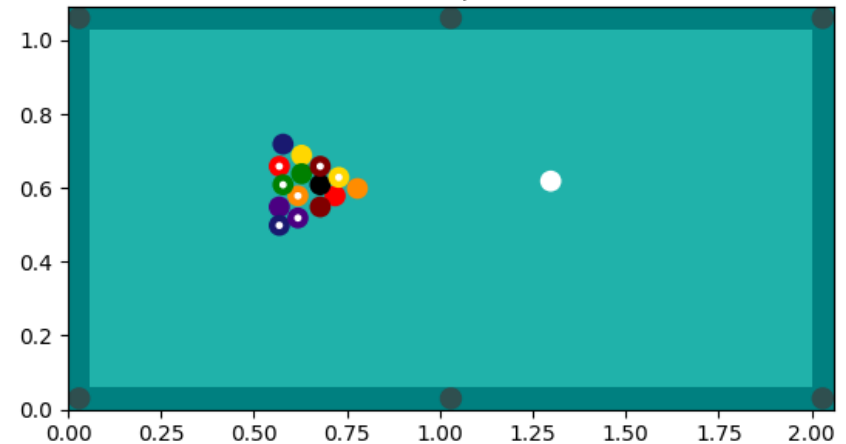
## Rendering

- Object plotting on layers using Matplotlib
- Frame Generation
- Video generation using OpenCV
- Comparison view

Real Data



Predicted output (Linear)



# Rendering

## Features

- Dimensions are an exact scaled version of the original. Colours are as close as possible to the original table.
- Solid balls represented as solid circles and striped balls are represented as a solid circle with a white inner circle.
- **Comparison view** of real data and predicted output
- Option for **video generation** as well as **on screen display**
- Support for different representation of different model outputs
- Video generation at the rate of 30 frames/s



# Rendering

## Idea

- Prediction output of the model is in the form of a row of 32 float values corresponding to the (x,y) coordinate of each ball with respect to the table.
- Difficult to have a cohesive and coherent understanding of the model behavior through plain numeric values.
- To get a better idea of the behaviour of the model, with respect to real life ball movement on a billiards table, a visual representation of the numeric values was needed which was close to the original imagery.
- **Matplotlib** library was used for **frame** generation and **OpenCV** was used for **video** generation.

# Evaluation

## Multi-step prediction

- N-step prediction easier than full prediction
  - Can be as simple as singlestep prediction with  $n=1$
  - Shows short-term mistakes, but no cumulative long-term inaccuracies
  - Useful to spot mistakes in earlier models
- Later switch to full prediction for more advanced models