Gov 2018: Social Networks

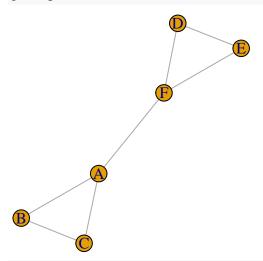
Your name:

Apr 12, 2022

There are a ton of R packages available for network analysis, however, here you're going to focus on using the igraph package throughout (Gabor & Nepusz 2006, http://igraph.org). It combines ease of use and high-level computation (it is also available for Python and C/C++). This package has proven to be very useful, and it covers a lot of basic network analysis methods as well as plotting capabilities. This exercise uses materials from Dai Shizuka and Pablo Barbera.

To see how to manually make a network and take a look at it before you dive in:

```
g=make_graph(~A-B-C-A, D-E-F-D, A-F)
plot(g)
```



```
#look at vertices
V(g)
```

+ 6/6 vertices, named, from 3e9b050: ## [1] A B C D E F

#look at edges
E(g)

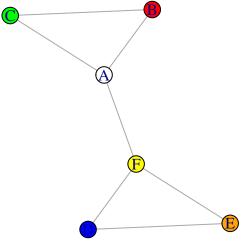
+ 7/7 edges from 3e9b050 (vertex names): ## [1] A--B A--C A--F B--C D--E D--F E--F

#look at vertex attributes (currently just name)
V(g)\$name

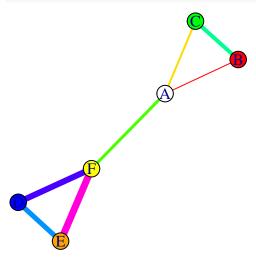
[1] "A" "B" "C" "D" "E" "F"

#Create new vertex attributes -- some can actually be directly interpreted by igraph, such as color V(g) color=c("white", "red", "green", "blue", "orange", "yellow") #a random set of colors

plot(g)



```
#Add edge attributes
E(g)$width=1:7
E(g)$color=rainbow(7) #rainbow() function chooses a specified number of colors
plot(g)
```



1 Exploring network data formats

1.1 Adjacency matrix, Edge list, Affiliation

Extract the adjacency matrix of g using $as_adjacency_matrix$. Then pull out the edgelist using $as_edgelist$.

```
# extract the adjacency matrix
as_adjacency_matrix(g)
```

```
## 6 x 6 sparse Matrix of class "dgCMatrix"
## A B C D E F
## A . 1 1 . . . 1
## B 1 . 1 . . . .
## C 1 1 . . . .
```

```
## D . . . 1 1
## E . . . 1 . 1
## F 1 . . 1 1 .
# pull out edge list
as edgelist(g)
##
         [,1] [,2]
## [1,]
        "A"
              "B"
              "C"
  [2,]
        " A "
              "F"
        "A"
   [3,]
              "C"
   [4,]
        "B"
              "E"
   [5,]
        "D"
## [6,]
        "D"
              "F"
## [7,] "E"
              "F"
```

1.2 Affiliation matrix

In many cases, we will construct social networks from co-membership in groups. For example, we would draw edges between individuals based on their patterns of co-occurrence in a flock. Similarly, we could construct networks of species co-occurrences in populations, etc.

To do this, we would first need data in a matrix in which rows represent individuals (or species) and columns represent groups (or populations). Note that you could flip the columns and rows–either way is fine. You just need to be aware of how you arranged it.

Below is a toy example in which individuals A through E occur in different combinations in 4 groups.

```
A=c(1,1,0,0)
B=c(1,0,1,0)
C=c(1,0,1,0)
D=c(0,1,0,1)
E=c(0,0,1,1)
aff=matrix(c(A,B,C,D,E),nrow=5,byrow=TRUE)
dimnames(aff)=list(c("A","B","C","D","E"),c("Group1","Group2","Group3","Group4"))
aff #The individual-by-group matrix
```

```
##
      Group1 Group2 Group3 Group4
## A
            1
                    1
                            0
                                     0
## B
            1
                    0
                            1
                                     0
                                     0
## C
            1
                    0
                            1
## D
            0
                    1
                            0
                                     1
## E
            0
                    0
                            1
                                     1
```

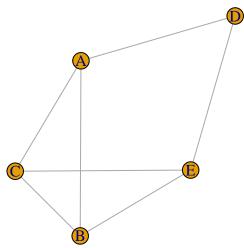
There are different ways to convert this data into a social network—i.e., a network that describes which individual co-occurs with which individual in groups. One simple way is to do what is called a one-mode projection of this data by multiplying this matrix with the transpose of itself. Do such a projection on aff and print it out. Then take the projection and plot the adjacency matrix from it where edges are weighted by the variable weight.

```
# one-mode projection of aff: multiply aff with the transpose of itself
# print it out
aff_t <- aff %*% t(aff)
aff_t</pre>
```

```
## ABCDE
```

```
## B 1 2 2 0 1
## C 1 2 2 0 1
## D 1 0 0 2 1
## E 0 1 1 1 2

# create igraph object using graph_from_adjacency_matrix() with mode = "undirected", weighted = T, diag
# plot the graph using the edge attribute named `weight` as your edge.width
igraph_obj <- graph_from_adjacency_matrix(aff_t, mode = "undirected", weighted = T, diag = F)
plot(igraph_obj)</pre>
```



2 Real data

A 2 1 1 1 0

Here you will be using a small network that indicates interactions in the movie Star Wars Episode IV. Each node is a character and each edge indicates whether they appeared together in a scene of the movie. Edges here are thus undirected and they also have weights attached, since they can appear in multiple scenes together.

The first step is to read the list of edges and nodes in this network:

```
edges <- read.csv("star-wars-network-edges.csv")
head(edges)</pre>
```

```
##
        source target weight
## 1
         C-3PO R2-D2
                          17
## 2
         LUKE R2-D2
                          13
## 3
       OBI-WAN
               R2-D2
                           6
## 4
         LEIA R2-D2
                           5
           HAN R2-D2
                           5
## 6 CHEWBACCA R2-D2
                           3
```

```
nodes <- read.csv("star-wars-network-nodes.csv")
head(nodes)</pre>
```

```
## name id
## 1 R2-D2 0
## 2 CHEWBACCA 1
## 3 C-3P0 2
## 4 LUKE 3
```

```
## 5 DARTH VADER 4
## 6 CAMIE 5
```

For example, we learn that C-3PO and R2-D2 appeared in 17 scenes together.

How do we convert these two datasets into a network object in R? There are multiple packages to work with networks, but the most popular is igraph because it's very flexible and easy to do. Other packages that you may want to explore are sna and networks.

Now, how do we create the igraph object? We can use the graph_from_data_frame function, which takes two arguments: d, the data frame with the edge list in the first two columns; and vertices, a data frame with node data with the node label in the first column. (Note that igraph calls the nodes vertices, but it's exactly the same thing.)

```
g <- graph_from_data_frame(d=edges, vertices=nodes, directed=FALSE)
g</pre>
```

```
## IGRAPH 0a0033b UNW- 22 60 --
## + attr: name (v/c), id (v/n), weight (e/n)
## + edges from 0a0033b (vertex names):
   [1] R2-D2
                   --C-3PO
                                  R2-D2
                                                            R2-D2
                                                                        --OBI-WAN
                                              --LUKE
##
   [4] R2-D2
                   --LEIA
                                  R2-D2
                                              --HAN
                                                            R2-D2
                                                                        --CHEWBACCA
   [7] R2-D2
                   --DODONNA
                                             --OBI-WAN
                                                                        --C-3P0
                                  CHEWBACCA
                                                            CHEWBACCA
##
                   --LUKE
                                                                        --LEIA
## [10] CHEWBACCA
                                  CHEWBACCA
                                             --HAN
                                                            CHEWBACCA
## [13] CHEWBACCA
                   --DARTH VADER CHEWBACCA
                                             --DODONNA
                                                            LUKE
                                                                        --CAMIE
## [16] CAMIE
                   --BIGGS
                                  LUKE
                                              --BIGGS
                                                            DARTH VADER--LEIA
## [19] LUKE
                   --BERU
                                  BERU
                                              --OWEN
                                                            C-3P0
                                                                        --BERU
## [22] LUKE
                   --OWEN
                                  C-3P0
                                              --LUKE
                                                            C-3P0
                                                                        --OWEN
## + ... omitted several edges
```

What does it mean? - U means undirected

- N means named graph
- W means weighted graph
- 22 is the number of nodes
- 60 is the number of edges
- name (v/c) means name is a node attribute and it's a character
- weight (e/n) means weight is an edge attribute and it's numeric

2.1 Practice accessing elements of the network

Practice accessing the following elements of the network: nodes, names of the nodes, attributes of the nodes, edges, weights for each edge, all attributes of the edges, the adjacency matrix, and just the first row of the adjacency matrix.

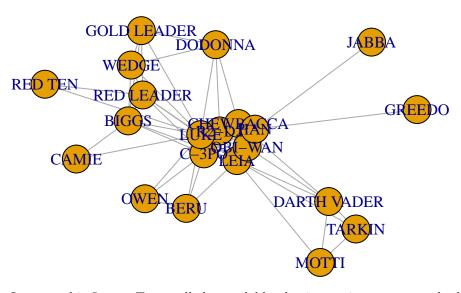
```
# nodes
# names of each node
# all attributes of the nodes
# edges
# weights for each edge
# all attributes of the edges
# adjacency matrix
# first row of adjacency matrix
```

2.2 Network visualization

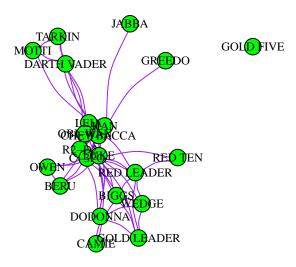
How can we visualize this network? The plot() function works out of the box, but the default options are often not ideal:

```
par(mar=c(0,0,0,0))
plot(g)
```





Improve this figure. To see all the available plotting options, you can check <code>?igraph.plotting</code>. Set the vertex color, label colors, the size of the labels, curvature to the edge and edge color to ones different from the default settings and in a way that is visually appealing to you.



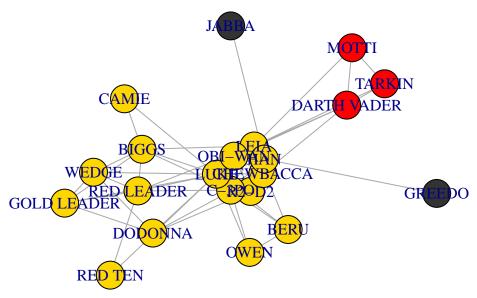
Now modify some of these plotting attributes so that they are function of network properties. For example, a common adjustment is to change the size of the nodes and node labels so that they match their importance.

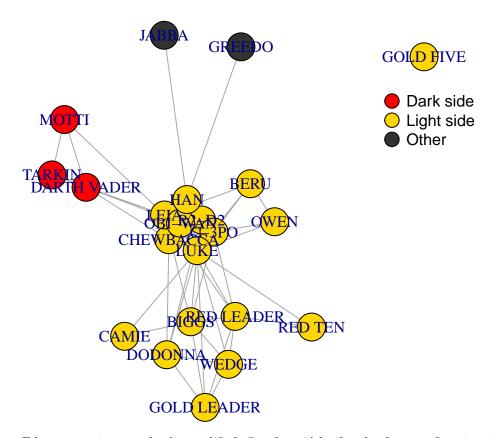
Here, strength will correspond to the number of scenes they appear in. Let the size of the node be determined by the strength, and only show the labels of character that appear in 10 or more scenes. Finally change the colors of the node based on what side they're in (dark side or light side) and add an informative legend.

```
# let the size of the node be determined by the `strength`:
# - you may need to take log to improve the visualization
# - only show the labels of character that appear in 10 or more scenes
# Change the colors of each node based on what side they're in (dark side or light side):
# - create vectors with characters in each side
dark_side <- c("DARTH VADER", "MOTTI", "TARKIN")</pre>
light_side <- c("R2-D2", "CHEWBACCA", "C-3P0", "LUKE", "CAMIE", "BIGGS",
                "LEIA", "BERU", "OWEN", "OBI-WAN", "HAN", "DODONNA",
                "GOLD LEADER", "WEDGE", "RED LEADER", "RED TEN", "GOLD FIVE")
other <- c("GREEDO", "JABBA")
# - create a new color variable as a node property
V(g)$color <- NA
V(g)$color[V(g)$name %in% dark_side] <- "red"</pre>
V(g)$color[V(g)$name %in% light_side] <- "gold"</pre>
V(g)$color[V(g)$name %in% other] <- "grey20"
vertex_attr(g)
## $name
    [1] "R2-D2"
                       "CHEWBACCA"
                                     "C-3P0"
                                                                   "DARTH VADER"
##
                                                    "LUKE"
    [6] "CAMIE"
                       "BIGGS"
                                     "LEIA"
                                                    "BERU"
                                                                   "OWEN"
## [11] "OBI-WAN"
                       "ITTOM"
                                     "TARKIN"
                                                    "HAN"
                                                                   "GREEDO"
                                     "GOLD LEADER" "WEDGE"
                                                                   "RED LEADER"
   [16] "JABBA"
                       "DODONNA"
   [21] "RED TEN"
                       "GOLD FIVE"
##
##
## $id
##
    [1]
           1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21
        0
##
## $color
    [1] "gold"
                  "gold"
                           "gold"
                                    "gold"
                                              "red"
                                                       "gold"
                                                                 "gold"
                                                                          "gold"
   [9] "gold"
                           "gold"
                                    "red"
                                              "red"
                                                       "gold"
                                                                 "grey20" "grey20"
##
                  "gold"
## [17] "gold"
                  "gold"
                           "gold"
                                    "gold"
                                              "gold"
                                                       "gold"
```

```
par(mar=c(0,0,0,0)); plot(g)
```



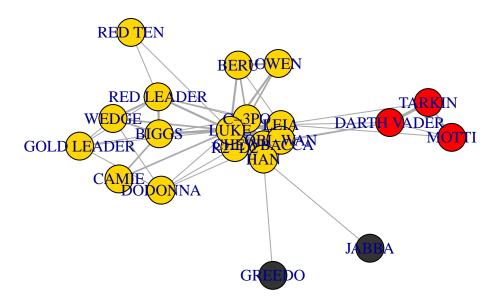




Edge properties can also be modified. Set the width of each edge as a function of the log number of scenes two characters appear together. Plot it.

```
# Hint: Use E(g)$width
E(g)$width <- log(E(g)$weight) + 1
edge_attr(g)
## $weight
   [1] 17 13 6
                                5 16 19 11 1
                 5
                    5
                       3
                         1
                             7
                                               1
                                                  2
                                                     2
                                                                       3 18
                 6
                       2
                             7
                                 9 26
                                      1
                                         1
                                            6
                                               1
                                                   1 13
## [51]
        3
           3 1
                 1 3 1
                          2 1
                                1
##
## $width
   [1] 3.833213 3.564949 2.791759 2.609438 2.609438 2.098612 1.000000 2.945910
   [9] 2.609438 3.772589 3.944439 3.397895 1.000000 1.000000 1.693147 1.693147
## [17] 2.386294 1.000000 2.098612 2.098612 1.693147 2.098612 3.890372 1.693147
## [25] 2.791759 3.833213 1.000000 3.944439 2.791759 1.000000 1.693147 1.000000
## [33] 2.945910 3.197225 4.258097 1.000000 1.000000 2.791759 1.000000 1.000000
## [41] 3.564949 1.000000 1.000000 1.000000 1.000000 1.000000 1.000000 1.693147
## [49] 1.000000 1.000000 2.098612 2.098612 1.000000 1.000000 2.098612 1.000000
## [57] 1.693147 1.000000 1.000000 1.000000
par(mar=c(0,0,0,0)); plot(g)
```



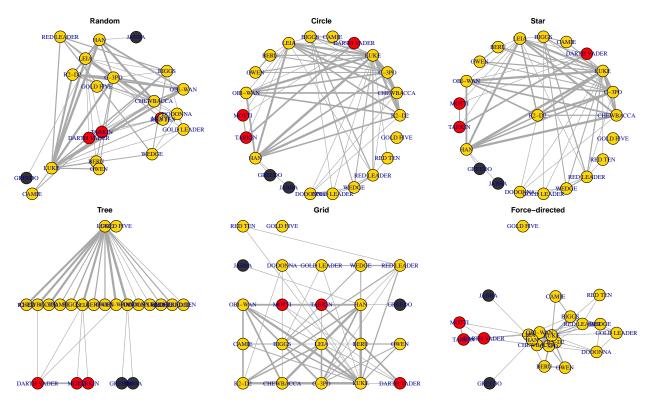


Extra: layouts

Up to now, each time we run the plot function, the nodes appear to be in a different location. Why? Because it's running a probabilistic function trying to locate them in the optimal way possible.

However, we can also specify the **layout** for the plot; that is, the (x,y) coordinates where each node will be placed. **igraph** has a few different layouts built-in, that will use different algorithms to find an **optimal** distribution of nodes. The following code illustrates some of these:

```
par(mfrow=c(2, 3), mar=c(0,0,1,0))
plot(g, layout=layout_randomly, main="Random")
plot(g, layout=layout_in_circle, main="Circle")
plot(g, layout=layout_as_star, main="Star")
plot(g, layout=layout_as_tree, main="Tree")
plot(g, layout=layout_on_grid, main="Grid")
plot(g, layout=layout_with_fr, main="Force-directed")
```



Note that each of these is actually just a matrix of (x,y) locations for each node.

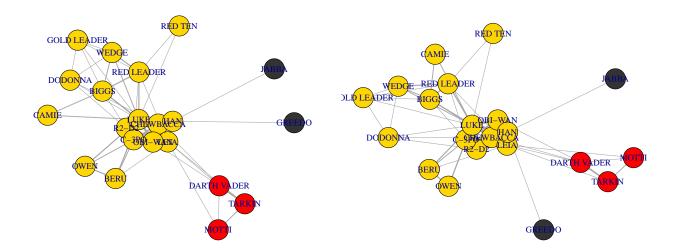
```
1 <- layout_randomly(g)
str(1)</pre>
```

```
## num [1:22, 1:2] -0.1635 0.4798 0.5684 -0.0622 -0.6679 ...
```

The most popular layouts are force-directed. These algorithms, such as Fruchterman-Reingold, try to position the nodes so that the edges have similar length and there are as few crossing edges as possible. The idea is to generate "clean" layouts, where nodes that are closer to each other share more connections in common that those that are located further apart. Note that this is a non-deterministic algorithm: choosing a different seed will generate different layouts.

```
par(mfrow=c(1,2))
set.seed(777)
fr <- layout_with_fr(g, niter=1000)
par(mar=c(0,0,0,0)); plot(g, layout=fr)
set.seed(666)
fr <- layout_with_fr(g, niter=1000)
par(mar=c(0,0,0,0)); plot(g, layout=fr)</pre>
```





3 Node properties

Let's look at descriptive statistics at the node level. All of these are in some way measures of importance or **centrality**.

The most basic measure is **degree**, the number of adjacent edges to each node. It is often considered a measure of direct influence. In the Star Wars network, it will be the unique number of characters that each character is interacting with. Sort the **degree** of the network and print it out.

```
# sort the `degree` of the network and print it out
sort(degree(g))
     GOLD FIVE
                      GREEDO
                                     JABBA
                                                                              OWEN
##
                                                  CAMIE
                                                             RED TEN
##
                            1
                                         1
                                                                    2
                                                                                 3
          MOTTI
                                      BERU DARTH VADER
##
                      TARKIN
                                                             DODONNA GOLD LEADER
##
              3
                           3
                                         4
                                                      5
                                                                    5
          WEDGE
                                     BIGGS
                                                          RED LEADER
##
                       R2-D2
                                                OBI-WAN
                                                                        CHEWBACCA
                                                                    7
                                                                                 8
##
              5
                                         7
                                                      7
##
            HAN
                       C-3P0
                                      LEIA
                                                   LUKE
##
                          10
                                        12
                                                     15
```

In directed graphs, there are three types of degree: indegree (incoming edges), outdegree (outgoing edges), and total degree. You can find these using mode="in" or mode="out" or mode="total".

Strength is a weighted measure of degree that takes into account the number of edges that go from one node to another. In this network, it will be the total number of interactions of each character with anybody else. Sort the **strength** of the network and print it out.

```
# sort the `strength` of the network and print it out
sort(strength(g))
##
     GOLD FIVE
                     GREEDO
                                    JABBA
                                               RED TEN
                                                              CAMIE
                                                                            MOTTI
##
                                                      2
                                                                   4
                                                                                4
                                        1
##
       DODONNA GOLD LEADER
                                     OWEN
                                                  BERU
                                                              WEDGE
                                                                           TARKIN
                                        8
                                                      9
                                                                   9
                                                                               10
##
              5
                           5
```

```
## DARTH VADER
                 RED LEADER
                                     BIGGS
                                                 OBI-WAN
                                                                 R2-D2
                                                                                LEIA
##
                                         14
                                                                    50
                                                                                  59
             11
                           13
                                                      49
     CHEWBACCA
##
                        C-3P0
                                       HAN
                                                    LUKE
##
             63
                           64
                                         80
                                                     129
```

Closeness measures how many steps are required to access every other node from a given node. It's a measure of how long information takes to arrive (who hears news first?). Higher values mean less centrality. Sort the closeness of the network (normalize it) and print it out.

```
# sort the `closeness` of the network and print it out
sort(closeness(g, normalized=TRUE))
## Warning in closeness(g, normalized = TRUE): At centrality.c:2617 :closeness
  centrality is not well-defined for disconnected graphs
                                  JABBA
##
     GOLD FIVE
                    GREEDO
                                                 HAN
                                                            OWEN
                                                                       CAMIE
    0.04545455
##
                0.11666667
                             0.11666667
                                         0.13043478
                                                     0.17647059
                                                                  0.18584071
                                OBI-WAN
                                                                         BERU
##
        TARKIN
                     R2-D2
                                              MOTTI DARTH VADER
##
    0.20000000
                0.20388350
                             0.20792079
                                         0.21000000
                                                      0.21649485
                                                                  0.21649485
##
     CHEWBACCA
                      WEDGE
                                RED TEN
                                              C-3P0
                                                            LUKE
                                                                         LEIA
##
    0.21875000
                0.21875000
                             0.22105263
                                         0.23595506
                                                      0.23863636
                                                                  0.24418605
## GOLD LEADER
                RED LEADER
                                DODONNA
                                              BIGGS
    0.24418605
                0.25000000 0.25301205
                                         0.25925926
```

Betweenness measures brokerage or gatekeeping potential. It is (approximately) the number of shortest paths between nodes that pass through a particular node. Sort the betweenness of the network and print it out.

```
# sort the `betweenness` of the network and print it out
sort(betweenness(g))
```

```
##
         CAMIE
                        OWEN
                                  OBI-WAN
                                                 MOTTI
                                                             TARKIN
                                                                          GREEDO
##
      0.000000
                   0.000000
                                0.000000
                                              0.000000
                                                           0.000000
                                                                        0.000000
##
          JABBA
                       WEDGE
                               GOLD FIVE
                                                  BERU
                                                            RED TEN DARTH VADER
##
      0.000000
                   0.000000
                                0.000000
                                              1.666667
                                                           2.200000
                                                                       15.583333
##
                                                        RED LEADER
     CHEWBACCA
                        LUKE
                                    R2-D2 GOLD LEADER
                                                                           BIGGS
##
     15.916667
                  18.333333
                               22.750000
                                            23.800000
                                                          31.416667
                                                                       31.916667
##
         C-3P0
                                 DODONNA
                         HAN
                                                  LEIA
##
     32.783333
                  37.000000
                               47.533333
                                            59.950000
```

Eigenvector centrality is a measure of being well-connected connected to the well-connected. First eigenvector of the graph adjacency matrix. Only works with undirected networks. Sort the returned *vector* from the eigen_centrality of the network and print it out.

```
# sort the `vector` from the `eigen_centrality` of the network and print it out
sort(eigen_centrality(g)$vector)
```

```
GREEDO
                                                         RED TEN GOLD LEADER
##
         ITTOM
                    TARKIN
                                  JABBA
## 0.009298153 0.011493184 0.011602602 0.011602604 0.015241796 0.017475057
## DARTH VADER
                     CAMIE
                                DODONNA
                                              WEDGE
                                                            OWEN
                                                                 RED LEADER
## 0.027009389 0.030744983 0.031723524 0.034374377 0.062695673 0.065141246
##
          BERU
                     BIGGS
                              GOLD FIVE
                                              R2-D2
                                                         OBI-WAN
  0.070824006 0.078921422 0.121485774 0.503053912 0.541729368 0.592624857
##
         C-3P0
                 CHEWBACCA
                                    HAN
                                               LUKE
## 0.595864470 0.657663375 0.812242325 1.000000000
```

Page rank approximates probability that any message will arrive to a particular node. This algorithm was developed by Google founders, and originally applied to website links. Sort the returned *vector* from the page_rank of the network and print it out.

```
# sort the `vector` from the `page_rank` of the network and print it out
sort(page_rank(g)$vector)
     GOLD FIVE
                                 GREEDO
                                            RED TEN
                                                           CAMIE
                                                                     DODONNA
##
                     JABBA
## 0.007092199 0.008310156 0.008310156 0.010573836 0.013792262 0.016185680
##
         MOTTI GOLD LEADER
                                                                      TARKIN
                                   OWEN
                                               BERU
                                                           WEDGE
## 0.016813964 0.017945853 0.018881975 0.020368818 0.026377242 0.034180007
## DARTH VADER RED LEADER
                                  BIGGS
                                            OBI-WAN
                                                           R2-D2
                                                                        I.F.T A
## 0.034576040 0.034578060 0.035070288 0.067378471 0.068538690 0.086027500
     CHEWBACCA
                     C-3P0
                                               LUKE
##
                                    HAN
## 0.086390090 0.088708430 0.114631333 0.185268949
```

Authority score is another measure of centrality initially applied to the Web. A node has high authority when it is linked by many other nodes that are linking many other nodes. Sort the returned *vector* from the authority_score of the network and print it out.

```
# sort the `vector` from the `authority_score` of the network and print it out
sort(authority_score(g)$vector)
      GOLD FIVE
                       ITTOM
                                    TARKIN
                                                 GREEDO
                                                                JABBA
                                                                           RED TEN
##
## 1.273708e-17 9.118469e-03 1.133319e-02 1.154515e-02 1.154515e-02 1.512880e-02
    GOLD LEADER DARTH VADER
                                                DODONNA
                                                                WEDGE
                                     CAMIE
                                                                               OWEN
  1.717615e-02 2.671707e-02 3.064953e-02 3.143121e-02 3.410098e-02 6.256707e-02
##
     RED LEADER
                         BERU
                                     BIGGS
                                                  R2-D2
                                                              OBI-WAN
                                                                               I.F.T A
## 6.476889e-02 7.063977e-02 7.856101e-02 5.030995e-01 5.417666e-01 5.923767e-01
##
          C-3P0
                   CHEWBACCA
                                       HAN
                                                   LUKE
## 5.957835e-01 6.577603e-01 8.125507e-01 1.000000e+00
```

Finally, not exactly a measure of centrality, but we can learn more about who each node is connected to by using the following functions: neighbors (for direct neighbors) and ego (for neighbors up to n neighbors away). Find the neighbors of "DARTH VADER". Find his neighbors up to order 2 away.

```
# find the neighbors of "DARTH VADER" using `neighbors` (for direct neighbors)
neighbors(g, v=which(V(g)$name=="DARTH VADER"))
## + 5/22 vertices, named, from 0a0033b:
## [1] CHEWBACCA LEIA
                           OBI-WAN
                                                TARKIN
# find his neighbors up to order 2 away using `ego`
ego(g, order=2, nodes=which(V(g)$name=="DARTH VADER"))
## [[1]]
## + 14/22 vertices, named, from 0a0033b:
                                                                      TARKIN
    [1] DARTH VADER CHEWBACCA
                                 LEIA
                                             OBI-WAN
                                                          ITTOM
    [7] R2-D2
                    C-3P0
                                 LUKE
                                                          DODONNA
                                                                      BIGGS
                                             HAN
## [13] BERU
                    RED LEADER
```

4 Network properties

Let's now try to describe what a network looks like as a whole. We can start with measures of the **size** of a network. diameter is the length of the longest path (in number of edges) between two nodes. We can use

get_diameter to identify this path. mean_distance is the average number of edges between any two nodes in the network. We can find each of these paths between pairs of edges with distances. Find the diameter and mean distances of the network.

```
# find the length of the longest path (`diameter`)
diameter(g, directed=FALSE, weights=NA)
## [1] 3
get_diameter(g, directed=FALSE, weights=NA)
## + 4/22 vertices, named, from 0a0033b:
## [1] DARTH VADER CHEWBACCA
                                 C-3P0
                                              OWEN
# find the mean distances of the network (`mean_distance`)
mean distance(g, directed=FALSE)
## [1] 1.909524
dist <- distances(g, weights=NA)</pre>
dist[1:5, 1:5]
##
                R2-D2 CHEWBACCA C-3PO LUKE DARTH VADER
## R2-D2
                    0
                               1
                                      1
                                           1
## CHEWBACCA
                    1
                               0
                                           1
                                      1
## C-3PO
                                                        2
                               1
                                      0
                    1
                                           1
## LUKE
                    1
                               1
                                           0
                                      1
                                           2
## DARTH VADER
                    2
                               1
                                      2
                                                        0
edge_density is the proportion of edges in the network over all possible edges that could exist. Find the
edge_density of the network.
# find the `edge_density`
edge_density(g)
## [1] 0.2597403
# (How can we calculate this manually?)
60/((22*21)/2)
## [1] 0.2597403
reciprocity measures the propensity of each edge to be a mutual edge; that is, the probability that if i is
connected to j, j is also connected to i. Find the reciprocity of the network – you should find that it is 1.
Explain why you think reciprocity=1 in this case.
# find the reciprocity of the network
reciprocity(g)
## [1] 1
# Why is it 1?
# because there is one person at the center of the whole network - it all revolves around Luke.
```

transitivity, also known as clustering coefficient, measures that probability that adjacent nodes of a network are connected. In other words, if i is connected to j, and j is connected to k, what is the probability that i is also connected to k? Find the transitivity of the network.

```
# find the transitivity of the network
transitivity(g)
```

[1] 0.5375303

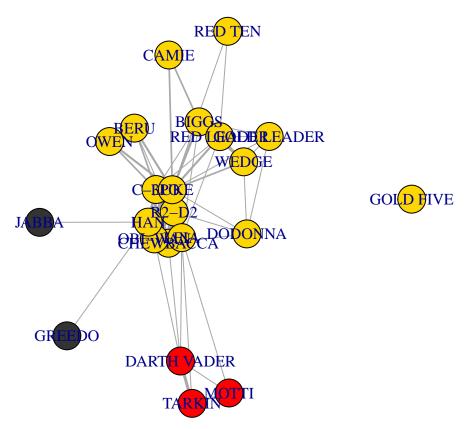
Extra: Network communities

par(mar=c(0,0,0,0)); plot(g)

Networks often have different clusters or communities of nodes that are more densely connected to each other than to the rest of the network. Let's cover some of the different existing methods to identify these communities.

The most straightforward way to partition a network is into **connected components**. Each component is a group of nodes that are connected to each other, but *not* to the rest of the nodes. For example, this network has two components.

```
components(g)
##
   $membership
                   CHEWBACCA
                                     C-3P0
                                                   LUKE DARTH VADER
                                                                             CAMIE
##
          R2-D2
##
              1
                                         1
                                                       1
                                                                                  1
##
          BIGGS
                        LEIA
                                      BERU
                                                   OWEN
                                                             OBI-WAN
                                                                             MOTTI
##
                            1
                                                                    1
              1
                                         1
                                                       1
                                                                                  1
                                                             DODONNA GOLD LEADER
##
         TARKIN
                         HAN
                                    GREEDO
                                                  JABBA
                                                                    1
##
                                                                                  1
              1
                            1
                                         1
                                                       1
##
          WEDGE
                 RED LEADER
                                  RED TEN
                                              GOLD FIVE
##
              1
                            1
                                         1
                                                       2
##
## $csize
   [1] 21 1
##
##
## $no
## [1] 2
```



Most networks have a single **giant connected component** that includes most nodes. Most studies of networks actually focus on the giant component (e.g. the shortest path between nodes in a network with two or more component is Inf!).

giant <- decompose(g)[[1]]</pre>

Components can be **weakly connected** (in undirected networks) or ___strongly connected (in directed networks, where there is an edge that ends in every single node of that component).

Even within a giant component, there can be different subsets of the network that are more connected to each other than to the rest of the network. The goal of **community detection algorithms** is to identify these subsets.

There are a few different algorithms, each following a different logic.

The walktrap algorithm finds communities through a series of short random walks. The idea is that these random walks tend to stay within the same community. The length of these random walks is 4 edges by default, but you may want to experiment with different values. The goal of this algorithm is to identify the partition that maximizes a modularity score.

cluster_walktrap(giant)

```
## IGRAPH clustering walktrap, groups: 6, mod: 0.16
##
   + groups:
     $`1`
##
##
     [1] "CAMIE"
                         "BIGGS"
                                        "DODONNA"
                                                       "GOLD LEADER" "WEDGE"
##
     [6] "RED LEADER"
                        "RED TEN"
##
##
     $`2`
     [1] "DARTH VADER" "MOTTI"
                                        "TARKIN"
##
##
```

```
##
     $`3`
##
     [1] "R2-D2"
                       "CHEWBACCA" "C-3PO"
                                                  "I.UKE."
                                                               "T.F.T A "
                                                                            "OBI-WAN"
##
     [7] "HAN"
     + ... omitted several groups/vertices
##
cluster_walktrap(giant, steps=10)
## IGRAPH clustering walktrap, groups: 3, mod: 0.15
##
   + groups:
     $`1`
##
##
     [1] "DARTH VADER" "MOTTI"
                                         "TARKIN"
##
##
     $`2`
                                                                             "BERU"
##
      [1] "R2-D2"
                        "CHEWBACCA" "C-3PO"
                                                   "LUKE"
                                                                "I.F.T A "
##
      [7] "OWEN"
                        "OBI-WAN"
                                     "HAN"
                                                   "GREEDO"
                                                                "JABBA"
##
##
     $`3`
##
     [1] "CAMIE"
                         "BIGGS"
                                         "DODONNA"
                                                        "GOLD LEADER" "WEDGE"
     [6] "RED LEADER"
##
                         "RED TEN"
##
     + ... omitted several groups/vertices
```

Other methods are:

- The **fast and greedy** method tries to directly optimize this modularity score.
- The **infomap** method attempts to map the flow of information in a network, and the different clusters in which information may get remain for longer periods. Similar to walktrap, but not necessarily maximizing modularity, but rather the so-called "map equation".
- The **edge-betweenness** method iteratively removes edges with high betweenness, with the idea that they are likely to connect different parts of the network. Here betweenness (gatekeeping potential) applies to edges, but the intuition is the same.
- The label propagation method labels each node with unique labels, and then updates these labels by choosing the label assigned to the majority of their neighbors, and repeat this iteratively until each node has the most common labels among its neighbors.

```
cluster_fast_greedy(giant)
```

```
## IGRAPH clustering fast greedy, groups: 4, mod: 0.17
##
  + groups:
     $`1`
##
##
     [1] "CHEWBACCA" "LUKE"
                                  "LEIA"
                                               "OBI-WAN"
                                                           "HAN"
                                                                        "GREEDO"
     [7] "JABBA"
##
##
##
     $`2`
     [1] "R2-D2" "C-3P0" "BERU"
##
                                  "OWEN"
##
##
     $`3`
##
     [1] "CAMIE"
                        "BIGGS"
                                      "DODONNA"
                                                     "GOLD LEADER" "WEDGE"
##
     [6] "RED LEADER"
                       "RED TEN"
     + ... omitted several groups/vertices
cluster_edge_betweenness(giant)
## Warning in cluster edge betweenness(giant): At community.c:460 :Membership
## vector will be selected based on the lowest modularity score.
## Warning in cluster_edge_betweenness(giant): At community.c:467 : Modularity
## calculation with weighted edge betweenness community detection might not make
## sense -- modularity treats edge weights as similarities while edge betwenness
```

```
## treats them as distances
## IGRAPH clustering edge betweenness, groups: 2, mod: 0.033
## + groups:
     $`1`
##
      [1] "R2-D2"
                                        "DARTH VADER" "LEIA"
##
                         "CHEWBACCA"
                                                                      "OBI-WAN"
      [6] "MOTTI"
                         "TARKIN"
                                        "HAN"
                                                       "GREEDO"
                                                                      "JABBA"
##
##
##
     $`2`
##
      [1] "C-3PO"
                         "LUKE"
                                        "CAMIE"
                                                       "BIGGS"
                                                                      "BERU"
                         "DODONNA"
      [6] "OWEN"
                                        "GOLD LEADER" "WEDGE"
                                                                      "RED LEADER"
##
##
     [11] "RED TEN"
##
cluster infomap(giant)
## IGRAPH clustering infomap, groups: 2, mod: 0.064
## + groups:
     $`1`
##
                                        "C-3P0"
                                                                      "CAMIE"
##
      [1] "R2-D2"
                         "CHEWBACCA"
                                                       "LUKE"
                         "LEIA"
##
      [6] "BIGGS"
                                        "BERU"
                                                       "OWEN"
                                                                      "OBI-WAN"
##
     [11] "HAN"
                         "GREEDO"
                                        "JABBA"
                                                       "DODONNA"
                                                                      "GOLD LEADER"
     [16] "WEDGE"
##
                         "RED LEADER"
                                        "RED TEN"
##
##
     $`2`
##
     [1] "DARTH VADER" "MOTTI"
                                       "TARKIN"
cluster_label_prop(giant)
## IGRAPH clustering label propagation, groups: 2, mod: 0.064
## + groups:
##
     $`1`
##
      [1] "R2-D2"
                         "CHEWBACCA"
                                        "C-3P0"
                                                       "LUKE"
                                                                      "CAMIE"
##
      [6] "BIGGS"
                         "LEIA"
                                        "BERU"
                                                       "OWEN"
                                                                      "OBI-WAN"
     [11] "HAN"
                         "GREEDO"
                                        "JABBA"
                                                       "DODONNA"
                                                                      "GOLD LEADER"
##
     [16] "WEDGE"
##
                         "RED LEADER"
                                        "RED TEN"
##
##
     $`2`
##
     [1] "DARTH VADER" "MOTTI"
                                       "TARKIN"
```

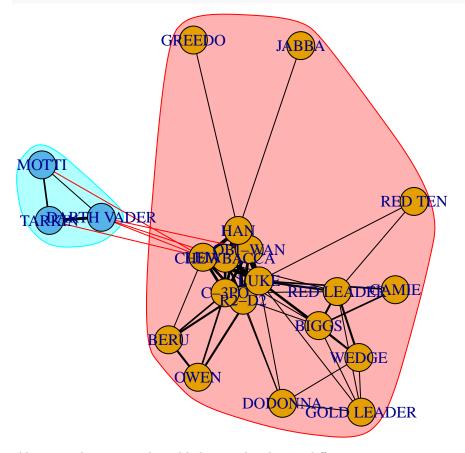
Infomap tends to work better in most social science examples (websites, social media, classrooms, etc), but fastgreedy is faster.

igraph also makes it very easy to plot the resulting communities:

```
comm <- cluster_infomap(giant)
modularity(comm) # modularity score</pre>
```

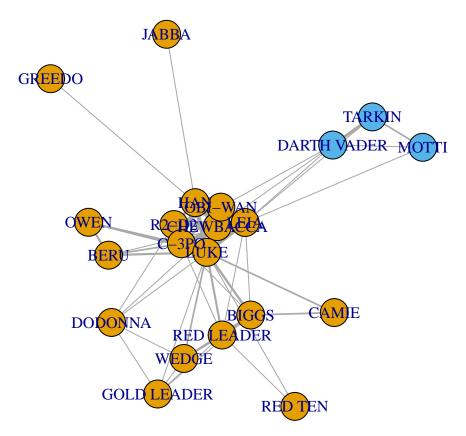
[1] 0.06420569

par(mar=c(0,0,0,0)); plot(comm, giant)



Alternatively, we can also add the membership to different communities as a color parameter in the <code>igraph</code> object.

```
V(giant)$color <- membership(comm)
par(mar=c(0,0,0,0)); plot(giant)</pre>
```

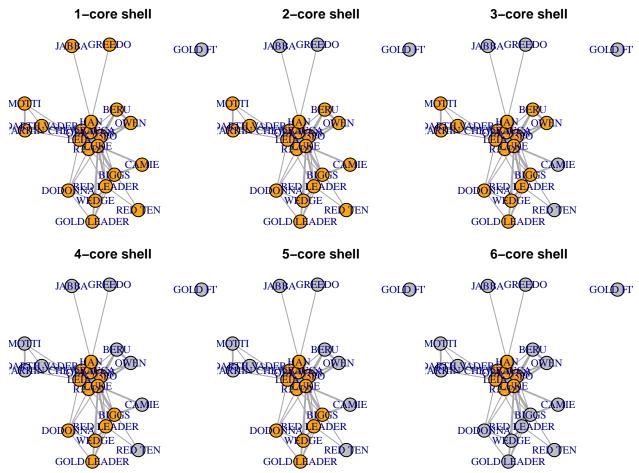


The final way in which we can think about network communities is in terms of hierarchy or structure. We'll discuss one of these methods.

K-core decomposition allows us to identify the core and the periphery of the network. A k-core is a maximal subnet of a network such that all nodes have at least degree K.

```
coreness(g)
                                                  LUKE DARTH VADER
                                                                            CAMIE
##
         R2-D2
                  CHEWBACCA
                                    C-3P0
##
              6
                           6
                                        6
                                                      6
                                                                   3
                                                                                2
##
         BIGGS
                        LEIA
                                     BERU
                                                  OWEN
                                                            OBI-WAN
                                                                            MOTTI
##
              5
                           6
                                        3
                                                      3
                                                                   6
##
        TARKIN
                         HAN
                                   GREEDO
                                                 JABBA
                                                            DODONNA GOLD LEADER
##
                                                                   5
                                                                                5
              3
                                        1
                                                      1
##
         WEDGE
                 RED LEADER
                                  RED TEN
                                             GOLD FIVE
                           5
##
              5
which(coreness(g)==6) # what is the core of the network?
##
       R2-D2 CHEWBACCA
                             C-3P0
                                          LUKE
                                                    LEIA
                                                            OBI-WAN
                                                                            HAN
##
                                  3
                                                                             14
which(coreness(g)==1) # what is the periphery of the network?
## GREEDO
            JABBA
##
       15
               16
# Visualizing network structure
V(g)$coreness <- coreness(g)</pre>
par(mfrow=c(2, 3), mar=c(0.1, 0.1, 1, 0.1))
set.seed(777); fr <- layout_with_fr(g)</pre>
```

```
for (k in 1:6){
   V(g)$color <- ifelse(V(g)$coreness>=k, "orange", "grey")
   plot(g, main=pasteO(k, '-core shell'), layout=fr)
}
```



5 Social network analysis with vosonSML

The vosonSML R package is a suite of easy to use functions for collecting and generating different types of networks from social media data. The package supports the collection of data from twitter, youtube and reddit, as well as hyperlinks from web sites. Networks in the form of node and edge lists can be generated from collected data, supplemented with additional metadata and used to create graphs for Social Network Analysis.

Install and load the latest release of the package:

```
library(magrittr) # %>%
## Warning: package 'magrittr' was built under R version 4.1.2
library(vosonSML)
```

The following Reddit example will provide a quick start to using vosonSML functions. Additionally there is an Introduction to vosonSML vignette that is a practical and explanatory guide to collecting data and creating networks.

Collecting Data from Reddit

The vosonSML does not require Reddit API credentials to be provided when collecting the data, unlike twitter and youtube.

To collect Reddit comment data, first construct a character vector containing the post URL(s). In the example below, a post relating to the politics around the Australian bushfires was used: https://www.reddit.com/r/worldnews/comments/elcb9b/australias_leaders_deny_link_between_climate/.

```
myThreadUrls <- c("https://www.reddit.com/r/worldnews/comments/elcb9b/australias_leaders_deny_link_betw
```

This post was created on 7th January 2020 and it had attracted over 4000 comments. According to the vignettes of the package, the reddit web endpoint used for collection has maximum limit of 500 comments per thread url, but this limit might have been updated since then.

Collect and explore the data using the codes below.

redditData <- Authenticate("reddit") %>%

```
Collect(threadUrls = myThreadUrls,
                    writeToFile = FALSE) # whether to write the returned dataframe to file as an .rds
## Collecting comment threads for reddit urls...
## Waiting between 3 and 10 seconds per thread request.
## Request thread: r/worldnews (elcb9b)
## Continue thread: r/worldnews (elcb9b) - fdhvspn
## Continue thread: r/worldnews (elcb9b) - fdhqght
## Continue thread: r/worldnews (elcb9b) - fdhy26s
## Continue thread: r/worldnews (elcb9b) - fdhtd7v
## Continue thread: r/worldnews (elcb9b) - fdhvm74
## Continue thread: r/worldnews (elcb9b) - fdhgyqk
## Continue thread: r/worldnews (elcb9b) - fdho9wa
## Continue thread: r/worldnews (elcb9b) - fdhs3qw
## Continue thread: r/worldnews (elcb9b) - fdhvi6h
## Continue thread: r/worldnews (elcb9b) - fdi0u9c
## HTML decoding comments.
## thread_id | title
                                                        | subreddit | count
            | Australia's leaders deny link between clim... | worldnews | 761
## Collected 761 total comments.
## Done.
str(redditData)
## tibble[,23] (S3: tbl_df/tbl/data.frame/datasource/reddit)
##
   $ id
                    : int [1:761] 1 2 3 4 5 6 7 8 9 10 ...
                    : chr [1:761] "1" "4_1_1_1_1_1_1_1" "4_1_1_4_2_1_1_1_1" "4_1_1_4_3_1_1_1_3_
##
  $ structure
                   : chr [1:761] "2020-01-07 14:34:58" "2020-01-07 14:34:58" "2020-01-07 14:34:58" "
## $ post_date
## $ post date unix : num [1:761] 1.58e+09 1.58e+09 1.58e+09 1.58e+09 1.58e+09 ...
## $ comm id
                    : chr [1:761] "fdhjzyd" "fdhvspn" "fdhqght" "fdhy26s" ...
## $ comm date
                    : chr [1:761] "2020-01-07 19:11:10" "2020-01-07 21:04:05" "2020-01-07 20:15:49" "
  $ comm_date_unix : num [1:761] 1.58e+09 1.58e+09 1.58e+09 1.58e+09 1.58e+09 ...
##
   $ num_comments
                    ##
                    : chr [1:761] "worldnews" "worldnews" "worldnews" ...
## $ subreddit
##
  $ upvote_prop
                    : int [1:761] 45731 45727 45729 45725 45731 45730 45728 45728 45736 45728 ...
##
  $ post_score
                    : chr [1:761] "Gboard2" "Gboard2" "Gboard2" "...
##
   $ author
                    : chr [1:761] "sandwooder" "[deleted]" "smackofham" "LazerSturgeon" ...
## $ user
```

```
: int [1:761] 1901 140 16 13 7 9 125 4 5 10 ...
   $ comment score
##
   $ controversiality: int [1:761] 0 0 0 0 0 0 0 0 0 0 ...
##
                     : chr [1:761] "[And now a report from 2006 predicting it](https://www.tai.org.au/
                      : chr [1:761] "Australia's leaders deny link between climate change and the count
##
  $ title
                     : chr [1:761] "" "" "" ...
##
   $ post_text
                      : chr [1:761] "https://www.theglobeandmail.com/world/article-australias-leaders-u
##
   $ link
                      : chr [1:761] "theglobeandmail.com" "theglobeandmail.com" "theglobeandmail.com" "
##
   $ domain
                      : chr [1:761] "https://www.reddit.com/r/worldnews/comments/elcb9b/australias_lead
##
   $ url
##
   $ rm
                      : logi [1:761] FALSE FALSE FALSE FALSE FALSE ...
                      : chr [1:761] "elcb9b" "elcb9b" "elcb9b" "elcb9b" ...
   $ thread_id
```

Creating Reddit Networks

It is currently possible to create two types of networks using Reddit data: (1) actor network and (2) activity network.

Actor Network In the Reddit actor network, nodes represent users who have posted original posts and comments and the edges are the interactions between users in the comments i.e. where there is an edge from user i to user j if i writes a comment that replies to user j's comment (or the original post).

Create a Reddit actor network with comment text as an edge attribute by the following steps:

- Run Create(data = redditData,type = "actor") which returns a named list containing two dataframes named "nodes" and "edges".
- Pass the list to AddText(), which adds the comment text data to the network dataframe, stored as an edge attribute.
- Pass the list to Graph(), which returns an igraph graph object.

```
actorNetwork <- Create(data = redditData, type = "actor") %>% AddText(redditData)
\hbox{\tt\#\#} \ {\tt Adding} \ {\tt text} \ {\tt to} \ {\tt network}... \\ {\tt Generating} \ {\tt reddit} \ {\tt actor} \ {\tt network}... \\ {\tt Done}.
## Done.
actorGraph <- actorNetwork %>% Graph(writeToFile = F)
## Creating igraph network graph...Done.
actorGraph
## IGRAPH 8d7cd0f DN-- 385 762 --
## + attr: type (g/c), name (v/c), user (v/c), label (v/c), subreddit
## | (e/c), thread_id (e/c), comment_id (e/n), comm_id (e/c),
## | vosonTxt_comment (e/c), title (e/c)
## + edges from 8d7cd0f (vertex names):
## [1] 1 ->385 2 ->2
                          3 ->99 4 ->105 5 ->105 6 ->2
                                                              2 ->172 7 ->16 8 ->16
## [10] 9 ->2
                 2 ->2
                                   11->2
                                            12->3
                          10->1
                                                      13->4
                                                                       2 -> 2
                                                                                15 -> 7
## [19] 16->8
                 17->9
                           2 ->2
                                   18->10
                                            2 ->11
                                                     2 ->3
                                                              2 ->2
                                                                       19->18
                                                                                20 -> 2
## [28] 3 ->2
                 21->2
                          22->1
                                   23->2
                                             2 ->21
                                                     1 ->22
                                                              24->2
                                                                       25->2
                                                                                 19->1
                                                     19->28
## [37] 26->2
                 27->25 28->1
                                   2 ->26
                                            29->2
                                                              30->2
                                                                       2 ->29
                                                                                31->1
## [46] 32->2
                 33->2
                          34->1
                                   35->2
                                             36->2
                                                      37->1
                                                               2 ->35
                                                                       38->2
                                                                                19->1
## + ... omitted several edges
```

The Reddit actor network contains a graph attribute type (set to "reddit").

The node attributes are: - name (sequential ID number for actor, generated by vosonSML), - user (Reddit handle or screen name)) and - label (a concatenation of the ID and screen name).

The edge attributes are: - subreddit (the subreddit from which the post is collected), - thread_id (the 6 character ID of the thread or post), - comment_id (sequential ID number for comment, generated by vosonSML). - There is also an edge attribute title, which is set to NA for all comments except the comment representing the original post. Further note that the original post is represented as a self-loop edge from the user who authored the post (and this is how the post text can be accessed, as an edge attribute). - Finally, because we used AddText() in the above example, there is also an edge attribute vosonTxt_comment which is the text associated with the comment, or original post.

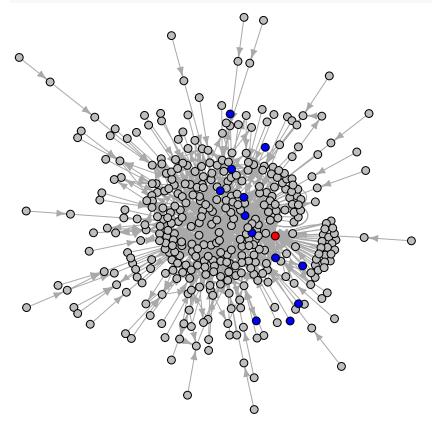
How many nodes and edges are there in the example Reddit actor network?

Use the following codes for a visualization of the actor network. Note that the author of the post is indicated by a red node, and blue nodes indicate those people who mentioned "arson" or "starting fires" in at least one of their comments.

```
# set node color of original post to red based on presence of title edge attribute
# set other node colors to grey
V(actorGraph)$color <- "grey"
V(actorGraph)$color[tail_of(actorGraph, which(!is.na(E(actorGraph)$title)))] <- "red"

# get node indexes for the tails of edges that have comments containing words of interest: e.g., "arson # set their node colors to blue
ind <- tail_of(actorGraph, grep("arson|starting fires", tolower(E(actorGraph)$vosonTxt_comment)))
V(actorGraph)$color[ind] <- "blue"

par(mfrow=c(1,1), mar=c(0,0,0,0))
plot(actorGraph, vertex.label = "", vertex.size = 4, edge.arrow.size = 0.5)</pre>
```



Activity Network In the Reddit activity network, nodes are either comments and/or initial thread posts and the edges represent replies to the original post, or replies to comments. Create a Reddit activity network

```
as before with type = "activity".
activityNetwork <- Create(data = redditData, type = "activity") %>% AddText(redditData)
## Adding text to network...Generating reddit activity network...
## -----
## collected reddit comments | 761
## threads
## comments
                            | 761
                            | 762
## nodes
## edges
                             l 761
## Done.
## Done.
activityGraph <- activityNetwork %>% Graph(writeToFile = F)
## Creating igraph network graph...Done.
activityGraph
## IGRAPH 980f432 DN-- 762 761 --
## + attr: type (g/c), name (v/c), thread_id (v/c), comm_id (v/c),
## | datetime (v/c), ts (v/n), subreddit (v/c), user (v/c), node_type
## | (v/c), vosonTxt_comment (v/c), title (v/c), label (v/c), edge_type
## | (e/c)
## + edges from 980f432 (vertex names):
## [1] elcb9b.1
                                 ->elcb9b.0
## [2] elcb9b.4_1_1_1_1_1_1_1_1->elcb9b.4_1_1_1_1_1_1_1
## [3] elcb9b.4 1 1 4 2 1 1 1 1 1->elcb9b.4 1 1 4 2 1 1 1 1
## [4] elcb9b.4_1_1_4_3_1_1_1_3_1->elcb9b.4_1_1_4_3_1_1_1_3
## [5] elcb9b.4_1_1_4_3_1_1_1_3_2->elcb9b.4_1_1_4_3_1_1_1_3
## + ... omitted several edges
```

The Reddit activity network contains a graph attribute type (set to "reddit").

The node attributes are: - name (string showing position of the comment in the thread), - date (date when the comment was authored, in DD-MM-YY format), - subreddit (the subreddit from which the post is collected), - user (Reddit handle or screen name of the user who authored the comment or post), - node_type ('comment' or 'thread'), - title (NA for all nodes except that representing the original post), - label (a concatenation of name and user). - Because we used AddText() in the above example, there is also a node attribute vosonTxt_comment which is the text from the comment, or original post.

The edge attribute contains edge_type which is 'comment' for all edges.

How many nodes and edges are there in the example Reddit activity network?

Use the following codes for a visualization of the actor network.

```
# set original post node colors to red based on a node type of thread
# set other node colors to grey
V(activityGraph)$color <- "grey"
V(activityGraph)$color[which(V(activityGraph)$node_type == "thread")] <- "red"

# get node indexes for nodes that have comment attributes containing words of interest
# set their node colors to blue
ind <- grep("arson|starting fires", tolower(V(activityGraph)$vosonTxt_comment))
V(activityGraph)$color[ind] <- "blue"</pre>
```

