

5. Binary Search Trees, BST Sort

Link: <https://www.youtube.com/watch?v=9Jry5-82I68>

Runway Reservation System

Airport with a single runway:

- Certain data structures are no good for accomplishing $O(\log n)$ time for reserving landing
 - Unsorted arrays require linear time to search, match, and insert landing time
 - No binary search since it's unsorted
 - Sorted array
 - $\log n$ to search
 - Constant for comparison (comparing $R[1]$ and $R[i-1]$)
 - Actual insertion requires shifting $O(n)$ time
 - Sorted list
 - You can't do binary search on a list
 - Heaps: min/max
 - Has a weak invariant
 - Will take $O(n)$ times
 - In a min/max heap, you have to check both sides
- Reservations for future landings
 - Reserve, request specifies landing time t
 - Add t to the set R if no other landings are scheduled within k minutes
- Remove from set R after plane lands

Binary Search Trees

- Unlike a heap, it requires pointers to parent, left child, and right child
- Invariant: for all nodes x , if y is in the left subtree of x ... $\text{key}(y) \leq \text{key}(x)$, y is the right..... $\text{key}(y) \geq \text{key}(x)$
- To find the lowest and highest numbers in BST, it will require $O(\text{height of tree})$

New Requirement (Rank)

- Rank(t): how many planes are scheduled to land at times $\leq t$?
- We will have to augment the BST structure
 - We can add a size number to each node stating how many children nodes in contains
- What lands before t ?
 - Walk down tree to find desired time
 - Add in the nodes that are smaller
 - Add in the subtree size to the left
-
- If we placed the array 43,46,48,50 into a BST, it will appear as a list. Searching will take $O(n)$ equivalent to a linked list which is no good. We need it to be balanced so searching will equal to $O(\log n)$