

6. AVL Trees, AVL Sort

Link: <https://www.youtube.com/watch?v=FNEL18KsWPc>

Balanced Search Tree

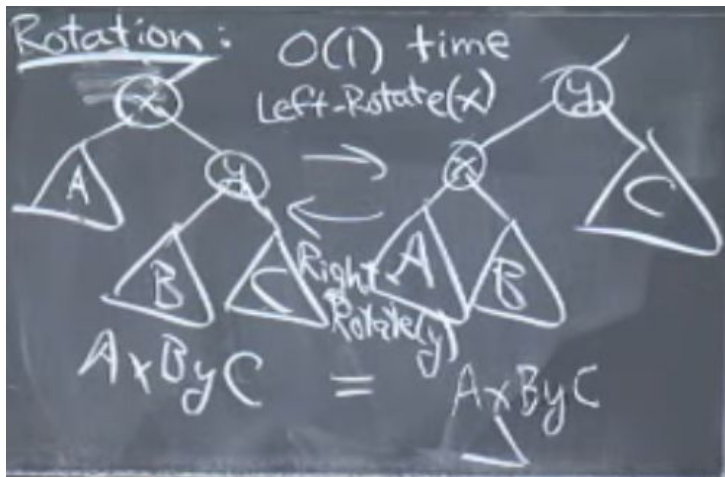
- Height - length of the longest path going from the root down to the leaf
- A tree is balanced if $h = O(\lg n)$
- Height of a node
 - Length of longest path from it down to a leaf
 - $\max(\text{height}(\text{left child}), \text{height}(\text{right child})) + 1$
- Rebalancing should occur when the height gets too large

AVL Trees

- Require heights of left and right children of every node to differ by at most ± 1
- The reason why it's not 0 is because it's difficult to accomplish a perfectly balanced BST
 - It's impossible in trees with even amount of nodes
- AVL trees are balanced:
 - Worst case is when right subtree has height 1 more than the left for every node
 - $N; h = \min \# \text{ nodes in an AVL tree of height } h$

AVL Insert

- 1) Simple BST insert
- 2) Fix AVL property
 - a) From changed node up, suppose x is lowest node violates AVL
 - b) Assume $\text{right}(x)$ higher aka $x.\text{right}$



- 3)
- 4) If x 's right child is right-heavy or balanced

AVL Sort

- Insert n items $O(n \lg n)$
- In-order transversal - $O(n)$
- AVL allows you to find successor and predecessor

- Heap allows you to find min and max

Abstract Data Type

- Insert and delete
- Min
- successor/pred