

Naïve Bayes Classifier

Naive Bayes

- Naive Bayes is a probabilistic technique for constructing classifiers.
- The characteristic assumption of the naive Bayes classifier is to consider that the value of a particular feature is independent of the value of any other feature, given the class variable.

Application – Naive Bayes

- To mark an email as **spam**, or **not spam** ?
- Classify a news article about **technology**, **politics**, or **sports** ?
- NLP(textual data analysis) kind of task.
- Check a piece of text expressing **positive** emotions, or **negative** motions?

Bayes theorem

- It works on conditional probability.
- Conditional probability is the probability that something will happen, given that something else has already occurred.
- Using the conditional probability, we can calculate the probability of an event using its prior knowledge.

conditional probability.

$$P(H | E) = \frac{P(E | H) * P(H)}{P(E)}$$

Bayes theorem

where

- $P(H)$ is the probability of hypothesis H being true. This is known as the prior probability.
- $P(E)$ is the probability of the evidence (regardless of the hypothesis).
- $P(E|H)$ is the probability of the evidence given that hypothesis is true.
- $P(H|E)$ is the probability of the hypothesis given that the evidence is there.

Example-

Problem

- A Lab is performing a Test of disease say “D” with two results “Positive” & “Negative.”
- They guarantee that their test result is 99% accurate: if you have the disease, they will give test positive 99% of the time.
- If you don’t have the disease, they will test negative 99% of the time. If 3% of all the people have this disease and test gives “positive” result, what is the probability that you actually have the disease?

Bayes theorem

- calculating the probability that the patient actually have the disease
i.e, $P(D | Pos)$ we will use Bayes theorem

$$P(D | Pos) = \frac{P(Pos | D) * P(D)}{P(Pos)}$$

Bayes theorem

- Probability of people suffering from Disease D, $P(D) = 0.03 = 3\%$
- Probability that test gives “positive” result and patient have the disease, $P(\text{Pos} \mid D) = 0.99 = 99\%$
- Probability of people not suffering from Disease D, $P(\sim D) = 0.97 = 97\%$
- Probability that test gives “positive” result and patient does have the disease, $P(\text{Pos} \mid \sim D) = 0.01 = 1\%$

Bayes theorem

We have all the values of numerator but we need to calculate $P(\text{Pos})$:

$$\begin{aligned} P(\text{Pos}) &= P(D, \text{pos}) + P(\sim D, \text{pos}) \\ &= P(\text{pos} | D) * P(D) + P(\text{pos} | \sim D) * P(\sim D) \\ &= 0.99 * 0.03 + 0.01 * 0.97 \\ &= 0.0297 + 0.0097 \\ &= 0.0394 \end{aligned}$$

$$\begin{aligned} \text{Let's calculate, } P(D | \text{Pos}) &= (P(\text{Pos} | D) * P(D)) / P(\text{Pos}) \\ &= (0.99 * 0.03) / 0.0394 \\ &= 0.753807107 \end{aligned}$$

So, Approximately 75% chances are there that the patient is actually suffering from disease.

Naïve Bayes Classifier

Naive Bayes is a kind of classifier which uses the Bayes Theorem. It predicts membership probabilities for each class such as the probability that given record or data point belongs to a particular class.

The class with the highest probability is considered as the most likely class. This is also known as **Maximum A Posteriori (MAP)**.

Naïve Bayes Classifier Algorithm

The MAP for a hypothesis is:

$$\text{MAP}(H)$$

$$= \max(P(H|E))$$

$$= \max((P(E|H)*P(H))/P(E))$$

$$= \max(P(E|H)*P(H))$$

$$\mathbf{P(H | Multiple Features)} = P(E_1 | H) * P(E_2 | H) \dots * P(E_n | H) * P(H) / P(\text{Multiple Features})$$

Advantages

- Naive Bayes Algorithm is a fast, highly scalable algorithm.
- Naive Bayes can be use for Binary and Multiclass classification. It provides different types of Naive Bayes Algorithms like Gaussian NB, Multinomial NB, Bernoulli NB.
- It is a simple algorithm that depends on doing a bunch of counts.
- Great choice for Text Classification problems. It's a popular choice for spam email classification.
- It can be easily train on small dataset

Disadvantages

- It considers all the features to be unrelated, so it cannot learn the relationship between features.
- E.g., Let's say Remo is going to a party. While cloth selection for the party, Remo is looking at his cupboard. Remo likes to wear a white color shirt. In Jeans, he likes to wear a brown Jeans, But Remo doesn't like wearing a white shirt with Brown Jeans.
- Naive Bayes can learn individual features importance but can't determine the relationship among features.