

HW #4

1.

$$a. \frac{1 \text{ KB}}{\text{sector}} \times \frac{500 \text{ sectors}}{\text{track}} \times \frac{6 \text{ tracks}}{\text{cylinder}} \times \frac{10^4 \text{ cyl}}{\text{disk}} = 3.00 \times 10^7 \text{ KB} / 2^{20} \frac{\text{KB}}{\text{GB}} = \boxed{28.61 \text{ GB}}$$

$$b. \frac{6000 \text{ rot}}{\text{min}} \cdot \frac{1 \text{ min}}{60 \text{ s}} \cdot \frac{1 \text{ s}}{10^3 \text{ ms}} = 10^{-1} \frac{\text{rot}}{\text{ms}} = \frac{10 \text{ ms}}{\text{rot}} \text{ at worst}$$

$$\text{On avg, } \frac{5 \text{ ms}}{\text{rot}} \cdot \frac{1 \text{ rot}}{\text{read}} + \frac{10 \text{ ms}}{\text{read}} = \boxed{15 \text{ ms on avg.}}$$

$$c. \frac{1 \text{ tuple}}{72 \text{ bytes}} \cdot \frac{1024 \text{ bytes}}{\text{block}} = \frac{14 \text{ tuples}}{\text{block}} \cdot \frac{1000 \text{ tup}}{14 \text{ tup/block}} = \boxed{71 \text{ blocks.}}$$

$$d. 15 \text{ ms for first read, then } 0.02 \text{ ms/block.}$$

$$15 \text{ ms} + (0.02 \cdot 71) \text{ ms} = 16.42 \text{ ms.}$$

$$e. 15 \text{ ms for track change + random block access, on avg.}$$

$$0.06 \text{ ms to read 3 sequential blocks.}$$

$$\left(\frac{15 \text{ ms} + 0.02 \text{ ms} \cdot 3 \text{ blocks}}{\text{cluster block cluster}} \right) 24 \text{ clusters} = 361.44 \text{ ms to read 24 clusters}$$

$$f. n = \frac{1024 \text{ bytes}}{4 \text{ bytes/key}} \Rightarrow 256 \frac{\text{keys}}{\text{node}}$$

$$\log_{128} (10^3) = 1.42 \text{ blocks to read} \Rightarrow \text{at most 2 blocks.}$$

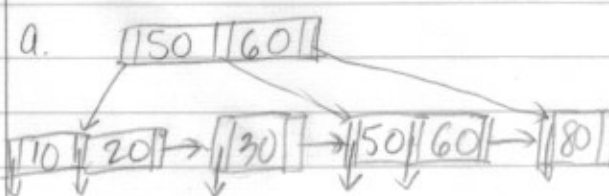
In this case, using a B+ slows down exec.

$$\text{So, at most } 15 \text{ ms} + 0.04 \text{ ms} = 15.04 \text{ ms.}$$

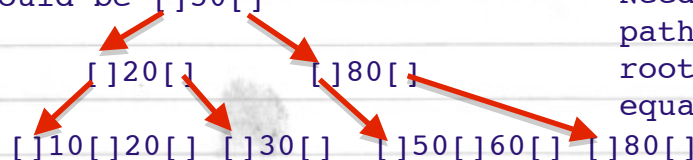
The B+ tree is helpful.

Need to do 10 random I/Os to retrieve all 2005 tuples (since there are 10 classes per year).

2.



2a is wrong. Should be [50[]]



Need to make sure path length from root to leaf is equal for all leaves.

3. max fanout = 5, max order = 2. max keys = 300 min -

max height: $2^h = 300 \rightarrow h = 9$

min height: $5^h = 300 \rightarrow h = 4$