Query Evaluation

EECS 339

Lecture 13

Overview of Query Evaluation

- Plan: Tree of R.A. ops, with choice of alg for each op.
 - Each operator typically implemented using a `pull' interface: when an operator is `pulled' for the next output tuples, it `pulls' on its inputs and computes them.
- Two main issues in query optimization:
 - For a given query, what plans are considered?
 - Algorithm to search plan space for cheapest (estimated) plan.
 - How is the cost of a plan estimated?
- Ideally: Want to find best plan. Practically: Avoid worst plans!
- We will study the System R approach.

Some Common Techniques

- Algorithms for evaluating relational operators use some simple ideas extensively:
 - Indexing: Can use WHERE conditions to retrieve small set of tuples (selections, joins)
 - Iteration: Sometimes, faster to scan all tuples even if there is an index. (And sometimes, we can scan the data entries in an index instead of the table itself.)
 - Partitioning: By using sorting or hashing, we can partition the input tuples and replace an expensive operation by similar operations on smaller inputs.

^{*} Watch for these techniques as we discuss query evaluation!

Statistics and Catalogs

- Need information about the relations and indexes involved. Catalogs typically contain at least:
 - # tuples (NTuples) and # pages (NPages) for each relation.
 - # distinct key values (NKeys) and NPages for each index.
 - Index height, low/high key values (Low/High) for each tree index.
- Catalogs updated periodically.
 - Updating whenever data changes is too expensive; lots of approximation anyway, so slight inconsistency ok.
- More detailed information (e.g., histograms of the values in some field) are sometimes stored.

Access Paths

- An <u>access path</u> is a method of retrieving tuples:
 - File scan, or index that matches a selection (in the query)
- * A tree index *matches* (a conjunction of) terms that involve only attributes in a *prefix* of the search key.
 - E.g., Tree index on $\langle a, b, c \rangle$ matches the selection a=5 AND b=3, and a=5 AND b>6, but not b=3.
- ❖ A hash index <u>matches</u> (a conjunction of) terms that has a term <u>attribute</u> = <u>value</u> for every attribute in the search key of the index.
 - E.g., Hash index on $\langle a, b, c \rangle$ matches a=5 AND b=3 AND c=5; but it does not match b=3, or a=5 AND b=3, or a>5 AND b=3 AND c=5.

A Note on Complex Selections

(day<8/9/94 AND rname= 'Paul') or bid=5 or sid=3

- Selection conditions are first converted to conjunctive normal form (CNF):
 (day<8/9/94 or bid=5 or sid=3) AND (rname= 'Paul' or bid=5 or sid=3)
- We only discuss case with no ORs; see text if you are curious about the general case.

One Approach to Selections

- Find the most selective access path, retrieve tuples using it, and apply any remaining terms that don't match the index:
 - Most selective access path: An index or file scan that we estimate will require the fewest page I/Os.
 - Terms that match this index reduce the number of tuples retrieved; other terms are used to discard some retrieved tuples, but do not affect number of tuples/pages fetched.
 - Consider day<8/9/94 AND bid=5 AND sid=3. A B+ tree index on day can be used; then, bid=5 and sid=3 must be checked for each retrieved tuple. Similarly, a hash index on <bid, sid> could be used; day<8/9/94 must then be checked.</p>

Using an Index for Selections

- Cost depends on #qualifying tuples, and clustering.
 - Cost of finding qualifying data entries (typically small) plus cost of retrieving records (could be large w/o clustering).
 - In example, assuming uniform distribution of names, about 10% of tuples qualify (100 pages, 10000 tuples). With a clustered index, cost is little more than 100 I/Os; if unclustered, up to 10000

SELECT *
FROM Reserves R
WHERE R.rname < 'C''

Projection

- The expensive part is removing duplicates.
 - SQL systems don't remove duplicates unless the keyword DISTINCT is specified in a query.
- Sorting Approach: Sort on <sid, bid> and remove duplicates. (Can optimize this by dropping unwanted information while sorting.)
- Hashing Approach: Hash on <sid, bid> to create partitions. Load partitions into memory one at a time, build in-memory hash structure, and eliminate duplicates.
- If there is an index with both R.sid and R.bid in the search key, may be cheaper to sort data entries!

SELECT DISTINCT
R.sid, R.bid
FROM Reserves R

Join: Index Nested Loops

foreach tuple r in R do foreach tuple s in S where $r_i == s_j$ do add <r, s> to result

- If there is an index on the join column of one relation (say S), can make it the inner and exploit the index.
 - Cost: $M + ((M*p_R) * cost of finding matching S tuples)$
 - M=#pages of R, p_R =# R tuples per page
- For each R tuple, cost of probing S index is about 1.2 for hash index, 2-4 for B+ tree. Cost of then finding S tuples (assuming Alt. (2) or (3) for data entries) depends on clustering.
 - Clustered index: 1 I/O (typical), unclustered: upto 1 I/O per matching S tuple.

Examples of Index Nested Loops

- Hash-index (Alt. 2) on sid of Sailors (as inner):
 - Scan Reserves: 1000 page I/Os, 100*1000 tuples.
 - For each Reserves tuple: 1.2 I/Os to get data entry in index, plus 1 I/O to get (the exactly one) matching Sailors tuple.
 Total: 220,000 I/Os.
- Hash-index (Alt. 2) on sid of Reserves (as inner):
 - Scan Sailors: 500 page I/Os, 80*500 tuples.
 - For each Sailors tuple: 1.2 I/Os to find index page with data entries, plus cost of retrieving matching Reserves tuples.
 Assuming uniform distribution, 2.5 reservations per sailor (100,000 / 40,000). Cost of retrieving them is 1 or 2.5 I/Os depending on whether the index is clustered.

Sophisticated Joins

- Until now, we have used nested loops for joining data
 - This is slow, n^2 comparisons
- How can we do better?
 - Sorting
 - Divide & conquer
- Trade-off in I/O and CPU time for each algo

Sort Merge Join

```
Equi-join of two tables S & R
|S| = Pages in S; {S} = Tuples in S
|S| ≥ |R|
M pages of memory; M > sqrt(|S|)
```

Algorithm:

- Partition S and R into memory sized sorted runs, write out to disk
- Merge all runs simultaneously

Total I/O cost: Read |R| and |S| twice, write once

$$3(|R| + |S|) I/Os$$

R=1,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6

R1 = 1,3,4 R2 = 6,9,14 R3 = 1,7,11

S1 = 2,3,7 S2 = 8,9,12 S3 = 4,6,15

R1	R2	R3	S1	S2	S3
1 🛑	6	1	2	8	4
3	9	7	3	9	6
4	14	11	7	12	15

OUTPUT

Need enough memory to keep 1 page of each run in memory at a time

$$R1 = 1,3,4$$

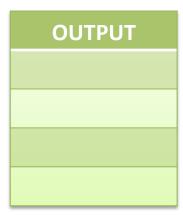
$$R2 = 6,9,14$$

$$S1 = 2,3,7$$

$$S2 = 8,9,12$$

$$S1 = 2,3,7$$
 $S2 = 8,9,12$ $S3 = 4,6,15$

R1	R2	R3	S1	S2	S3
1	6	1	2	8	4
3	9	7	3	9	6
4	14	11	7	12	15



$$R1 = 1,3,4$$

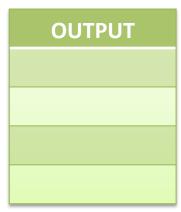
$$R2 = 6.9.14$$

$$S1 = 2,3,7$$

$$S2 = 8,9,12$$

$$S1 = 2,3,7$$
 $S2 = 8,9,12$ $S3 = 4,6,15$

R1	R2	R3	S1	S2	S3
1	6	1	2	8	4
3	9	7	3	9	6
4	14	11	7	12	15



$$R1 = 1,3,4$$

$$R3 = 1.7.11$$

$$S1 = 2,3,7$$

$$S3 = 4,6,15$$

R1	R2	R3	S1	S2	S3
1	6	1	2	8	4
3	9	7	3	9	6
4	14	11	7	12	15

OUTPUT
(3,3)

$$R1 = 1,3,4$$

$$R2 = 6.9.14$$

$$S1 = 2,3,7$$

$$S3 = 4,6,15$$

R1	R2	R3	S1	S2	S3
1	6	1	2	8	4
3	9	7	3	9	6
4	14	11	7	12	15

OUTPUT
(3,3)
(4,4)

R=1,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6

R1 = 1,3,4 R2 = 6,9,14 R3 = 1,7,11

S1 = 2,3,7 S2 = 8,9,12 S3 = 4,6,15

R1	R2	R3	S1	S2	S3
1	6	1	2	8	4
3	9	7	3	9	6
4	14	11	7	12	15

OUTPUT
(3,3)
(4,4)

$$R1 = 1,3,4$$

$$R2 = 6.9.14$$

$$S1 = 2,3,7$$

$$S3 = 4,6,15$$

R1	R2	R3	S1	S2	S3
1	6	1	2	8	4
3	9	7	3	9	6
4	14	11	7	12	15

OUTPUT
(3,3)
(4,4)
(6,6)

R=1,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6

$$R1 = 1.3.4$$

$$R2 = 6,9,14$$

$$S1 = 2,3,7$$

$$S3 = 4,6,15$$

R1	R2	R3	S1	S2	S3
1	6	1	2	8	4
3	9	7	3	9	6
4	14	11	7	12	15

OUTPUT
(3,3)
(4,4)
(6,6)
(7,7)

Output in sorted order!

Study Break: Sort-Merge Join

Say we are joining tables:

A=8,20,19,20,3,13,20,18,6,5,4,5

B=15,1,3,13,13,10,19,6,8,15,16,2

If our in-memory runs are of length 4, what will the sorted runs be for A and B?

What is the join output? Walk through the steps of the merge.

Study Break Solution

- A: (8,19,20,20) (3,13,18,20)(4,5,5,6)
- B: (1,3,13,15)(6,10,13,19)(2,8,15,16)

Output: (3,3)(6,6) (8,8)(13,13)(13,13)(19,19) (output in sorted order)

Simple Hash

```
Algorithm:
   Given hash function H(x) \rightarrow [0,...,P-1]
       where P is number of partitions
   for i in [0,...,P-1]:
       for each r in R:
           if H(r)=i, add r to in-memory hash
           otherwise, write r back to disk in R'
       for each s in S:
           if H(s)=i, lookup s in hash, output matches
           otherwise, write s back to disk in S'
       replace R with R', S with S'
```

Simple Hash I/O Analysis

```
Suppose P=2, and hash uniformly maps tuples to partitions
    Read
           |R| + |S|
   Write 1/2(|R| + |S|)
    Read 1/2(|R| + |S|) = 2(|R| + |S|)
P=3
    Read |R| + |S|
    Write
          2/3 (|R| + |S|)
    Read 2/3(|R| + |S|)
    Write 1/3(|R| + |S|)
    Read 1/3(|R| + |S|) = 3(|R| + |S|)
P=4
    |R| + |S| + 2 * (3/4 (|R| + |S|)) + 2 * (2/4 (|R| + |S|)) + 2 * (1/4 (|R| + |S|))
    = 4(|R| + |S|)
```

 \rightarrow P = n; n * (|R| + |S|) I/Os

Grace Hash

```
Algorithm:
Partition:
     Suppose we have P partitions, and H(x) \rightarrow [0...P-1]
     Choose P = |S| / M \rightarrow P \le sqrt(|S|) //may need to leave a little slop for imperfect hashing
     Allocate P 1-page output buffers, and P output files for R
     For each r in R:
           Write r into buffer H(r)
           If buffer full, append to file H(r)
     Allocate P output files for S
     For each s in S:
           Write s into buffer H(s)
           if buffer full, append to file H(s)
Join:
     For i in [0,...,P-1]
           Read file i of R, build hash table
           Scan file i of S, probing into hash table and outputting matches
```

Total I/O cost: Read |R| and |S| twice, write once

3(|R| + |S|) I/Os

$$P = 3$$
; $H(x) = x \mod P$



R=5,4,3,6,9,14,1,7,11

S=2,3,7,12,9,8,4,15,6

R0	R1	R2

P output buffers

F0	F1	F2

P output files

 $P = 3; H(x) = x \mod P$



R=5,4,3,6,9,14,1,7,11

S=2,3,7,12,9,8,4,15,6

R0	R1	R2
		5

F0	F1	F2

 $P = 3; H(x) = x \mod P$



R=5,4,3,6,9,14,1,7,11

S=2,3,7,12,9,8,4,15,6

R0	R1	R2
	4	5

F0	F1	F2

 $P = 3; H(x) = x \mod P$



R0	R1	R2
3	4	5

F0	F1	F2

 $P = 3; H(x) = x \mod P$



R0	R1	R2
3	4	5
6		

F0	F1	F2

P = 3; $H(x) = x \mod P$



R=5,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6

R0	R1	R2
3	4	5
6		

Need to flush R0 to F0!

F0	F1	F2

 $P = 3; H(x) = x \mod P$



R0	R1	R2
	4	5

F0	F1	F2
3		
6		

 $P = 3; H(x) = x \mod P$



R0	R1	R2
9	4	5

F0	F1	F2
3		
6		

 $P = 3; H(x) = x \mod P$



R0	R1	R2
9	4	5
		14

F0	F1	F2
3		
6		

 $P = 3; H(x) = x \mod P$



R0	R1	R2
9	4	5
	1	14

F0	F1	F2
3		
6		

 $P = 3; H(x) = x \mod P$



R0	R1	R2
9	4	5
	1	14

F0	F1	F2
3		
6		

 $P = 3; H(x) = x \mod P$



R0	R1	R2
9		5
		14

F0	F1	F2
3	4	
6	1	

 $P = 3; H(x) = x \mod P$



R0	R1	R2
9	7	5
		14

F0	F1	F2
3	4	
6	1	

 $P = 3; H(x) = x \mod P$



R0	R1	R2
9	7	5
		14

F0	F1	F2
3	4	
6	1	

 $P = 3; H(x) = x \mod P$



R0	R1	R2
9	7	

F0	F1	F2
3	4	5
6	1	14

 $P = 3; H(x) = x \mod P$



R0	R1	R2
9	7	11

F0	F1	F2
3	4	5
6	1	14

 $P = 3; H(x) = x \mod P$



R0	R1	R2

F0	F1	F2
3	4	5
6	1	14
9	7	11

 $P = 3; H(x) = x \mod P$

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

S Files

F0	F1	F2
3	7	2
12	4	8
9		
15		
6		

$$P = 3$$
; $H(x) = x \mod P$

Matches:

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

Load F0 from R into memory

S Files

F0	F1	F2
3	7	2
12	4	8
9		
15		
6		

P = 3; $H(x) = x \mod P$

Matches:

R=5,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

Load F0 from R into memory

S Files

	F0	F1	F2
\Rightarrow	3	7	2
	12	4	8
	9		
	15		
	6		

$$P = 3$$
; $H(x) = x \mod P$

Matches: 3,3

R=5,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

Load F0 from R into memory

S Files

	F0	F1	F2
\Rightarrow	3	7	2
	12	4	8
	9		
	15		
	6		

$$P = 3$$
; $H(x) = x \mod P$

Matches: 3,3

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

Load F0 from R into memory

S Files

	F0	F1	F2
	3	7	2
\Rightarrow	12	4	8
	9		
	15		
	6		

P = 3; $H(x) = x \mod P$

R=5,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6 Matches:

3,3

9,9

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

Load F0 from R into memory

S Files

	F0	F1	F2
	3	7	2
	12	4	8
\Rightarrow	9		
	15		
	6		

P = 3; $H(x) = x \mod P$

R=5,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6 Matches:

3,3

9,9

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

Load F0 from R into memory

S Files

F0	F1	F2
3	7	2
12	4	8
9		
15		
6		

P = 3; $H(x) = x \mod P$

R=5,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6 Matches:

3,3

9,9

6,6

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

Load F0 from R into memory

S Files

FO	F1	F2
3	7	2
12	4	8
9		
15		
6		

P = 3; $H(x) = x \mod P$

R=5,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6 Matches:

3,3

9,9

6,6

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

S Files

F0	F1	F2
3	7	2
12	4	8
9		
15		
6		

 $P = 3; H(x) = x \mod P$

R=5,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

Matches:

3,3

9,9

6,6

7,7

4,4

S Files

F0	F1	F2
3	7	2
12	4	8
9		
15		
6		

 $P = 3; H(x) = x \mod P$

R=5,4,3,6,9,14,1,7,11 S=2,3,7,12,9,8,4,15,6

R Files

F0	F1	F2
3	4	5
6	1	14
9	7	11

Matches:

3,3

9,9

6,6

7,7

4,4

S Files

F0	F1	F2
3	7	2
12	4	8
9		
15		
6		

Execution Costs

Notation: P partitions / passes over data; assuming hash is O(1)

Sort-Merge	Simple Hash	Grace Hash
I/O: 3 (R + S) CPU: O(P x {S}/P log {S}/P)	I/O: P(R + S) CPU: O({R} + {S})	I/O: 3 (R + S) CPU: O({R} + {S})

Grace hash is generally a safe bet, unless memory is close to size of tables, in which case simple can be preferable

Extra cost of sorting makes sort merge unattractive unless there is a way to access tables in sorted order (e.g., a clustered index), or a need to output data in sorted order (e.g., for a subsequent ORDER BY)

Study Break: Grace Hash Join

Say we are joining tables:

A=8,20,19,20,3,13,20,18,6,5,4,5

B=15,1,3,13,13,10,19,6,8,15,16,2

If we have four partitions, what will the hash partitions be for A and B?

Walk through the steps for producing this join's output.

Study Break Solution

Partitions:

```
- A0: (8,20,20,20,4) A1: (13,5,5) A2: (18,6) A3: (19,3)
```

```
- B0: (8,16) B1: (1,13,13) B2: (2, 6, 10) B3: (15,3,19,15)
```

• Execution:

- Join A0 w/B0 (produces (8,8))
- Join A1 w/B1 (produces (13,13), (13,13))

– ...

Highlights of System R Optimizer

- Impact:
 - Most widely used currently; works well for < 10 joins.
- Cost estimation: Approximate art at best.
 - Statistics, maintained in system catalogs, used to estimate cost of operations and result sizes.
 - Considers combination of CPU and I/O costs.
- Plan Space: Too large, must be pruned.
 - Only the space of *left-deep plans* is considered.
 - Left-deep plans allow output of each operator to be <u>pipelined</u> into the next operator without storing it in a temporary relation.
 - Cartesian products avoided.

Cost Estimation

- For each plan considered, must estimate cost:
 - Must estimate cost of each operation in plan tree.
 - Depends on input cardinalities.
 - We've already discussed how to estimate the cost of operations (sequential scan, index scan, joins, etc.)
 - Must also estimate size of result for each operation in tree!
 - Use information about the input relations.
 - For selections and joins, assume independence of predicates.

Size Estimation and Reduction Factors

SELECT attribute list FROM relation list WHERE term1 AND ... AND termk

- Consider a query block:
- Maximum # tuples in result is the product of the cardinalities of relations in the FROM clause.
- Reduction factor (RF) associated with each term
 reflects the impact of the term in reducing result size.
 Result cardinality = Max # tuples * product of all
 RF's.
 - Implicit assumption that terms are independent!
 - Term col=value has RF 1/NKeys(I), given index I on col
 - Term col1=col2 has RF 1/MAX(NKeys(I1), NKeys(I2))
 - Term col>value has RF (High(I)-value)/(High(I)-Low(I))

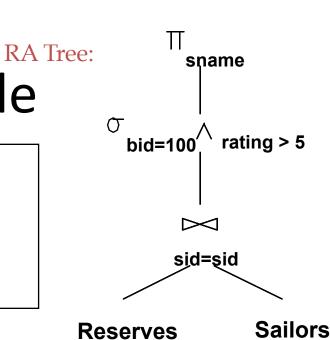
Schema for Examples

Sailors (<u>sid</u>: integer, sname: string, rating: integer, age: real) Reserves (<u>sid</u>: integer, <u>bid</u>: integer, <u>day</u>: dates, rname: string)

- Similar to old schema; rname added for variations.
- Reserves:
 - Each tuple is 40 bytes long, 100 tuples per page, 1000 pages.
- Sailors:
 - Each tuple is 50 bytes long, 80 tuples per page, 500 pages.

Motivating Example

SELECT S.sname FROM Reserves R, Sailors S WHERE R.sid=S.sid AND R.bid=100 AND S.rating>5



Cost: 500+500*1000 I/Os

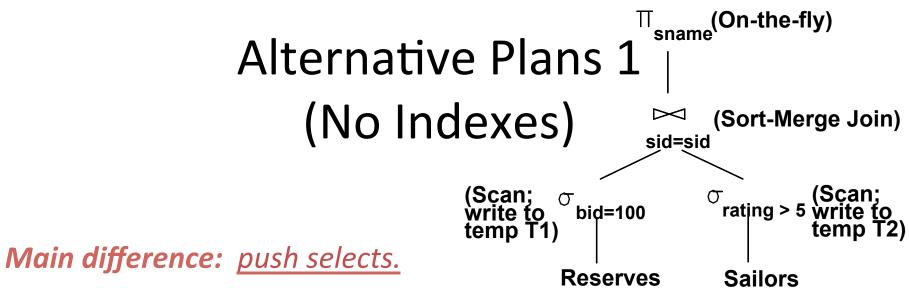
By no means the worst plan!

Misses several opportunities: selections could have been `pushed' or earlier, no use is made of any available indexes, etc.

Goal of optimization: To find more efficient plans that compute the same answer.

(On-the-fly) Plan: sname bid=100 \tag{ rating > 5 (On-the-flv) (Simple Nested Loops) sid=sid Sailors

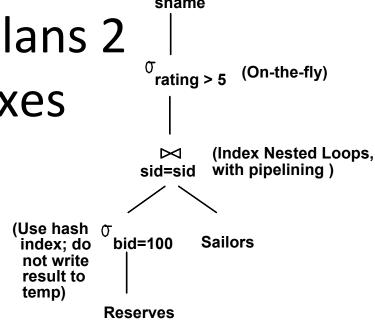
Reserves



- With 5 buffers, cost of plan:
 - Scan Reserves (1000) + write temp T1 (10 pages, if we have 100 boats, uniform distribution).
 - Scan Sailors (500) + write temp T2 (250 pages, if we have 10 ratings).
 - Sort T1 (2*2*10), sort T2 (2*3*250), merge (10+250)
 - Total: 3560 page I/Os.
- If we used BNL join, join cost = 10+4*250, total cost = 2770.
- If we `push' projections, T1 has only sid, T2 only sid and sname:
 - T1 fits in 3 pages, cost of BNL drops to under 250 pages, total < 2000.

Alternative Plans 2 With Indexes

- With clustered index on bid of Reserves, we get 100,000/100 = 1000 tuples on 1000/100 = 10 pages.
- INL with <u>pipelining</u> (outer is not materialized).
 - -Projecting out unnecessary fields from outer doesn't help.
- Join column *sid* is a key for Sailors.
 - -At most one matching tuple, unclustered index on *sid* OK.
- * Decision not to push *rating*>5 before the join is based on availability of *sid* index on Sailors.
- Cost: Selection of Reserves tuples (10 I/Os); for each,
 must get matching Sailors tuple (1000*1.2); total 1210 I/Os.



(On-the-fly)

Summary

- There are several alternative evaluation algorithms for each relational operator.
 - Especially for joins!
- A query is evaluated by converting it to a tree of operators and evaluating the operators in the tree.
- Must understand query optimization in order to fully understand the performance impact of a given database design (relations, indexes) on a workload (set of queries).
- Two parts to optimizing a query:
 - Consider a set of alternative plans.
 - Must prune search space; typically, left-deep plans only.
 - Must estimate cost of each plan that is considered.
 - Must estimate size of result and cost for each plan node.
 - Key issues: Statistics, indexes, operator implementations.